

## Sorting Assignment

### Problem Statement 1:

Given an Integer  $N$  and a list `arr`. Sort the array using bubble sort algorithm.

Example 1:

Input:

$N = 5$

`arr[] = {4, 1, 3, 9, 7}`

Output:

1 3 4 7 9

Example 2:

Input:

$N = 10$

`arr[] = {10, 9, 8, 7, 6, 5, 4, 3, 2, 1}`

Output:

1 2 3 4 5 6 7 8 9 10

Expected Time Complexity:  $O(N^2)$ .

Expected Auxiliary Space:  $O(1)$ .

Constraints:

$1 \leq N \leq 10^3$

$1 \leq arr[i] \leq 10^3$

### Problem Statement 2:

Given an array of size  $N$  containing only 0s, 1s, and 2s; sort the array in ascending order.

Example 1:

Input:

$N = 5$

`arr[] = {0 2 1 2 0}`

Output:

0 0 1 2 2

Explanation:

0s 1s and 2s are segregated  
into ascending order.

Example 2:

Input:

N = 3

arr[] = {0 1 0}

Output:

0 0 1

Explanation:

0s 1s and 2s are segregated  
into ascending order.

Expected Time Complexity:  $O(N)$

Expected Auxiliary Space:  $O(1)$

Constraints:

$1 \leq N \leq 10^6$

$0 \leq A[i] \leq 2$

### Problem Statement 3:

Given two sorted arrays arr1[] and arr2[] of sizes n and m in non-decreasing order. Merge them in sorted order without using any extra space. Modify arr1 so that it contains the first N elements and modify arr2 so that it contains the last M elements.

Example 1:

Input:

n = 4, arr1[] = [1 3 5 7]

$m = 5$ ,  $arr2[] = [0\ 2\ 6\ 8\ 9]$

Output:

$arr1[] = [0\ 1\ 2\ 3]$

$arr2[] = [5\ 6\ 7\ 8\ 9]$

Explanation:

After merging the two non-decreasing arrays, we get,  $0\ 1\ 2\ 3\ 5\ 6\ 7\ 8\ 9$ .

Example 2:

Input:

$n = 2$ ,  $arr1[] = [10\ 12]$

$m = 3$ ,  $arr2[] = [5\ 18\ 20]$

Output:

$arr1[] = [5\ 10]$

$arr2[] = [12\ 18\ 20]$

Explanation:

After merging two sorted arrays we get  $5\ 10\ 12\ 18\ 20$ .

Expected Time Complexity:  $O((n+m) \log(n+m))$

Expected Auxiliary Space:  $O(1)$

Constraints:

$1 \leq n, m \leq 10^5$

$0 \leq arr1_i, arr2_i \leq 10^7$

#### **Problem Statement 4:**

Given an array  $arr[]$  of size  $N$ , check if it is sorted in non-decreasing order or not.

Example 1:

Input:

$N = 5$

$arr[] = \{10, 20, 30, 40, 50\}$

Output: 1

Explanation: The given array is sorted.

Example 2:

Input:

$N = 6$

$\text{arr[]} = \{90, 80, 100, 70, 40, 30\}$

Output: 0

Explanation: The given array is not sorted.

Expected Time Complexity:  $O(N)$

Expected Auxiliary Space:  $O(1)$

Constraints:

$1 \leq N \leq 10^5$

$1 \leq \text{Arr}[i] \leq 10^6$

### **Problem Statement 5:**

Given an array  $\text{arr}[]$ , its starting position  $l$  and its ending position  $r$ . Sort the array using the Merge Sort algorithm.

Example 1:

Input:

$N = 5$

$\text{arr[]} = \{4\ 1\ 3\ 9\ 7\}$

Output:

1 3 4 7 9

Example 2:

Input:

$N = 10$

$\text{arr[]} = \{10\ 9\ 8\ 7\ 6\ 5\ 4\ 3\ 2\ 1\}$

Output:

1 2 3 4 5 6 7 8 9 10

Expected Time Complexity:  $O(n \log n)$

Expected Auxiliary Space:  $O(n)$

Constraints:

$1 \leq N \leq 10^5$

$1 \leq \text{arr}[i] \leq 10^5$

Example 1:

Input:

$N = 5$

$\text{arr}[] = \{ 4, 1, 3, 9, 7 \}$

Output:

1 3 4 7 9

Example 2:

Input:

$N = 10$

$\text{arr}[] = \{10, 9, 8, 7, 6, 5, 4, 3, 2, 1\}$

Output:

1 2 3 4 5 6 7 8 9 10

Expected Time Complexity:  $O(N*N)$ .

Expected Auxiliary Space:  $O(1)$ .

Constraints:

$1 \leq N \leq 1000$

$1 \leq \text{arr}[i] \leq 1000$

### **Problem Statement 6:**

Given a random set of numbers, Print them in sorted order.

Example 1:

Input:

$N = 4$

`arr[] = {1, 5, 3, 2}`

Output: `{1, 2, 3, 5}`

Explanation: After sorting array will be like `{1, 2, 3, 5}`.

Example 2:

Input:

`N = 2`

`arr[] = {3, 1}`

Output: `{1, 3}`

Explanation: After sorting array will be like `{1, 3}`.

Expected Time Complexity:  $O(N * \log N)$

Expected Auxiliary Space:  $O(1)$

Constraints:

$1 \leq N, A[i] \leq 105$

### **Problem Statement 7:**

You are given two integer arrays `nums1` and `nums2`, sorted in non-decreasing order, and two integers `m` and `n`, representing the number of elements in `nums1` and `nums2` respectively.

Merge `nums1` and `nums2` into a single array sorted in non-decreasing order.

The final sorted array should not be returned by the function, but instead be stored inside the array `nums1`. To accommodate this, `nums1` has a length of `m + n`, where the first `m` elements denote the elements that should be merged, and the last `n` elements are set to 0 and should be ignored. `nums2` has a length of `n`.

Example 1:

Input: `nums1 = [1,2,3,0,0,0]`, `m = 3`, `nums2 = [2,5,6]`, `n = 3`

Output: [1,2,2,3,5,6]

Explanation: The arrays we are merging are [1,2,3] and [2,5,6].

The result of the merge is [1,2,2,3,5,6] with the underlined elements coming from nums1.

Example 2:

Input: nums1 = [1], m = 1, nums2 = [], n = 0

Output: [1]

Explanation: The arrays we are merging are [1] and [].

The result of the merge is [1].

Example 3:

Input: nums1 = [0], m = 0, nums2 = [1], n = 1

Output: [1]

Explanation: The arrays we are merging are [] and [1].

The result of the merge is [1].

Note that because m = 0, there are no elements in nums1. The 0 is only there to ensure the merge result can fit in nums1.

Constraints:

`nums1.length == m + n`

`nums2.length == n`

`0 <= m, n <= 200`

`1 <= m + n <= 200`

`-109 <= nums1[i], nums2[j] <= 10^9`

### **Problem Statement 8:**

Given an array of integers nums, sort the array in ascending order and return it.

You must solve the problem without using any built-in functions in  $O(n\log(n))$  time complexity and with the smallest space complexity possible.

Example 1:

Input: `nums = [5,2,3,1]`

Output: `[1,2,3,5]`

Explanation: After sorting the array, the positions of some numbers are not changed (for example, 2 and 3), while the positions of other numbers are changed (for example, 1 and 5).

Example 2:

Input: `nums = [5,1,1,2,0,0]`

Output: `[0,0,1,1,2,5]`

Explanation: Note that the values of `nums` are not necessarily unique.

Constraints:

$1 \leq \text{nums.length} \leq 5 * 10^4$

$-5 * 10^4 \leq \text{nums}[i] \leq 5 * 10^4$

### **Problem Statement 9:**

You are given a 0-indexed integer array `nums` and a target element `target`.

A target index is an index `i` such that `nums[i] == target`.

Return a list of the target indices of `nums` after sorting `nums` in non-decreasing order. If there are no target indices, return an empty list. The returned list must be sorted in increasing order.

Example 1:

Input: `nums = [1,2,5,2,3]`, `target = 2`

Output: `[1,2]`

Explanation: After sorting, `nums` is `[1,2,2,3,5]`.

The indices where `nums[i] == 2` are 1 and 2.



Example 2:

Input: `nums = [1,2,5,2,3]`, `target = 3`

Output: `[3]`

Explanation: After sorting, `nums` is `[1,2,2,3,5]`.

The index where `nums[i] == 3` is 3.

Example 3:

Input: `nums = [1,2,5,2,3]`, `target = 5`

Output: `[4]`

Explanation: After sorting, `nums` is `[1,2,2,3,5]`.

The index where `nums[i] == 5` is 4.

Constraints:

$1 \leq \text{nums.length} \leq 100$

$1 \leq \text{nums}[i], \text{target} \leq 100$

**Problem Statement 10:**

Given an array `nums`, return `true` if the array was originally sorted in non-decreasing order, then rotated some number of positions (including zero). Otherwise, return `false`.

There may be duplicates in the original array.

Note: An array `A` rotated by `x` positions results in an array `B` of the same length such that  $A[i] == B[(i+x) \% A.length]$ , where `%` is the modulo operation.

Example 1:

Input: `nums = [3,4,5,1,2]`

Output: `true`

Explanation: `[1,2,3,4,5]` is the original sorted array.

You can rotate the array by  $x = 3$  positions to begin on the element of value 3:  
[3,4,5,1,2].

Example 2:

Input: `nums = [2,1,3,4]`

Output: `false`

Explanation: There is no sorted array once rotated that can make `nums`.

Example 3:

Input: `nums = [1,2,3]`

Output: `true`

Explanation: [1,2,3] is the original sorted array.

You can rotate the array by  $x = 0$  positions (i.e. no rotation) to make `nums`.

Constraints:

$1 \leq \text{nums.length} \leq 100$

$1 \leq \text{nums}[i] \leq 100$

### **Problem statement 11:**

Given an array `arr[]`, its starting position `l` and its ending position `r`. Sort the array using the Merge Sort algorithm and also solve using the Quick Sort algorithm.

Example 1:

Input:

`N = 5`

`arr[] = {4 1 3 9 7}`

Output:

`1 3 4 7 9`

Example 2:

Input:

`N = 10`

`arr[] = {10 9 8 7 6 5 4 3 2 1}`

Output:

1 2 3 4 5 6 7 8 9 10

Expected Time Complexity:  $O(n \log n)$

Expected Auxiliary Space:  $O(n)$

Constraints:

$1 \leq N \leq 10^5$

$1 \leq \text{arr}[i] \leq 10^5$

Example 1:

Input:

$N = 5$

$\text{arr}[] = \{4, 1, 3, 9, 7\}$

Output:

1 3 4 7 9

Example 2:

Input:

$N = 10$

$\text{arr}[] = \{10, 9, 8, 7, 6, 5, 4, 3, 2, 1\}$

Output:

1 2 3 4 5 6 7 8 9 10

Expected Time Complexity:  $O(N^2)$ .

Expected Auxiliary Space:  $O(1)$ .

Constraints:

$1 \leq N \leq 1000$

$1 \leq \text{arr}[i] \leq 1000$

### Problem Statement 12:

Given an array  $\text{arr}[]$  of size  $N$ , check if it is sorted in non-decreasing order or not.

Use quick sort

Example 1:

Input:

$N = 5$

$\text{arr}[] = \{10, 20, 30, 40, 50\}$

Output: 1

Explanation: The given array is sorted.

Example 2:

Input:

$N = 6$

$\text{arr}[] = \{90, 80, 100, 70, 40, 30\}$

Output: 0

Explanation: The given array is not sorted.

Expected Time Complexity:  $O(N)$

Expected Auxiliary Space:  $O(1)$

Constraints:

$1 \leq N \leq 10^5$

$1 \leq \text{Arr}[i] \leq 10^6$

### **Problem Statement 13:**

Given an array of integers `nums`, sort the array in ascending order and return it.

You must solve the problem without using any built-in functions in  $O(n \log(n))$  time complexity and with the smallest space complexity possible.

(Solve using merge sort)

Example 1:

Input: `nums = [5,2,3,1]`

Output: `[1,2,3,5]`

Explanation: After sorting the array, the positions of some numbers are not changed (for example, 2 and 3), while the positions of other numbers are changed (for example, 1 and 5).

Example 2:

Input: nums = [5,1,1,2,0,0]

Output: [0,0,1,1,2,5]

Explanation: Note that the values of nums are not necessarily unique.

Constraints:

$1 \leq \text{nums.length} \leq 5 * 10^4$

$-5 * 10^4 \leq \text{nums}[i] \leq 5 * 10^4$

**Problem Statement 14:**

Given an array of size N containing only 0s, 1s, and 2s; sort the array in ascending order. (sort using : Quicksort algorithm)

Example 1:

Input:

N = 5

arr[] = {0 2 1 2 0}

Output:

0 0 1 2 2

Explanation:

0s 1s and 2s are segregated into ascending order.

Example 2:

Input:

N = 3

arr[] = {0 1 0}

Output:

0 0 1

Explanation:

0s 1s and 2s are segregated

into ascending order.

Expected Time Complexity:  $O(N)$

Expected Auxiliary Space:  $O(1)$

Constraints:

$1 \leq N \leq 10^6$

$0 \leq A[i] \leq 2$

### **Problem Statement 15:**

Given a random set of numbers, Print them in sorted order.

Use : merge and quicksort

Example 1:

Input:

$N = 4$

$arr[] = \{1, 5, 3, 2\}$

Output:  $\{1, 2, 3, 5\}$

Explanation: After sorting array will be like  $\{1, 2, 3, 5\}$ .

Example 2:

Input:

$N = 2$

$arr[] = \{3, 1\}$

Output:  $\{1, 3\}$

Explanation: After sorting array will be like  $\{1, 3\}$ .

Expected Time Complexity:  $O(N * \log N)$

Expected Auxiliary Space:  $O(1)$

Constraints:

$1 \leq N, A[i] \leq 105$