Priority Queue :

Usage → questions

Complexity

class + pq + comparable interface with oops.

pq. function →

add / push	→	O(log n)
remove / pop	→	O(log n)
top / peek	→	O(1)
size	→	O(1)
isEmpty	→	true / false — O(1)

removal is done on priority Element

why it is log(n) ? → Creation

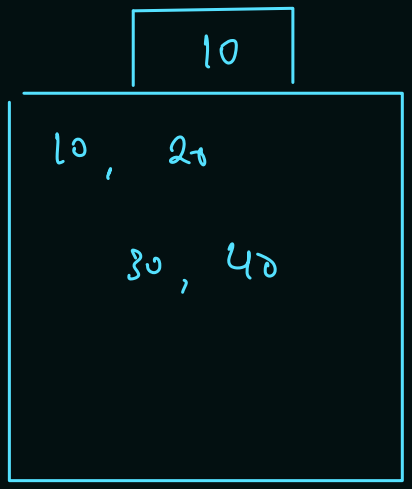
→ priority → min

pq.add(10);

20;

30;

40;



K Largest Elements: k = 3

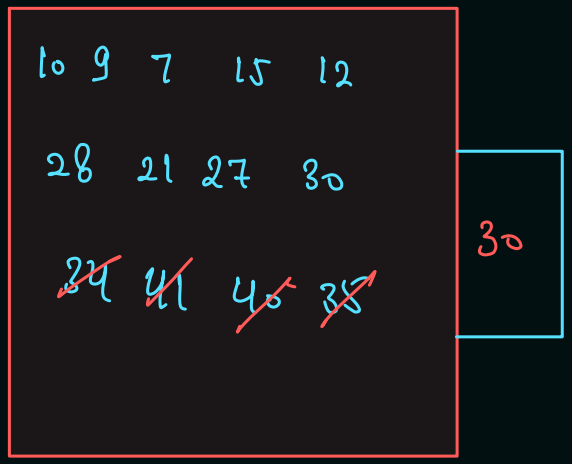
array → 10 9 7 15 12 28 21 27 30 34 41 40 35

Approach-1

① Add all Element in pq.

② print top k Elements.

Time Complexity → nlogn



41, 40, 35, 34 — k largest

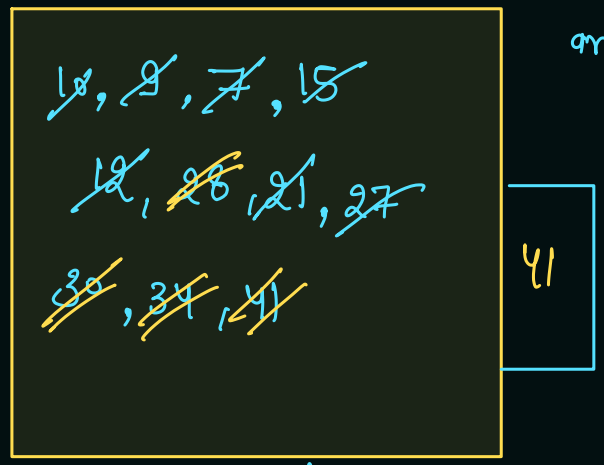
Approach-2

① Add k Elements in min priority ques.

② Add next Elem in priority queue if it is greater than peek Elem & remove peek Elem.

T → nlogk

k = 4



array → 10 9 7 15 12 28 21 27 30 34 41 4 23

klogk — 4 stay — 23 stays.

decreasing order →

Time → nlogk

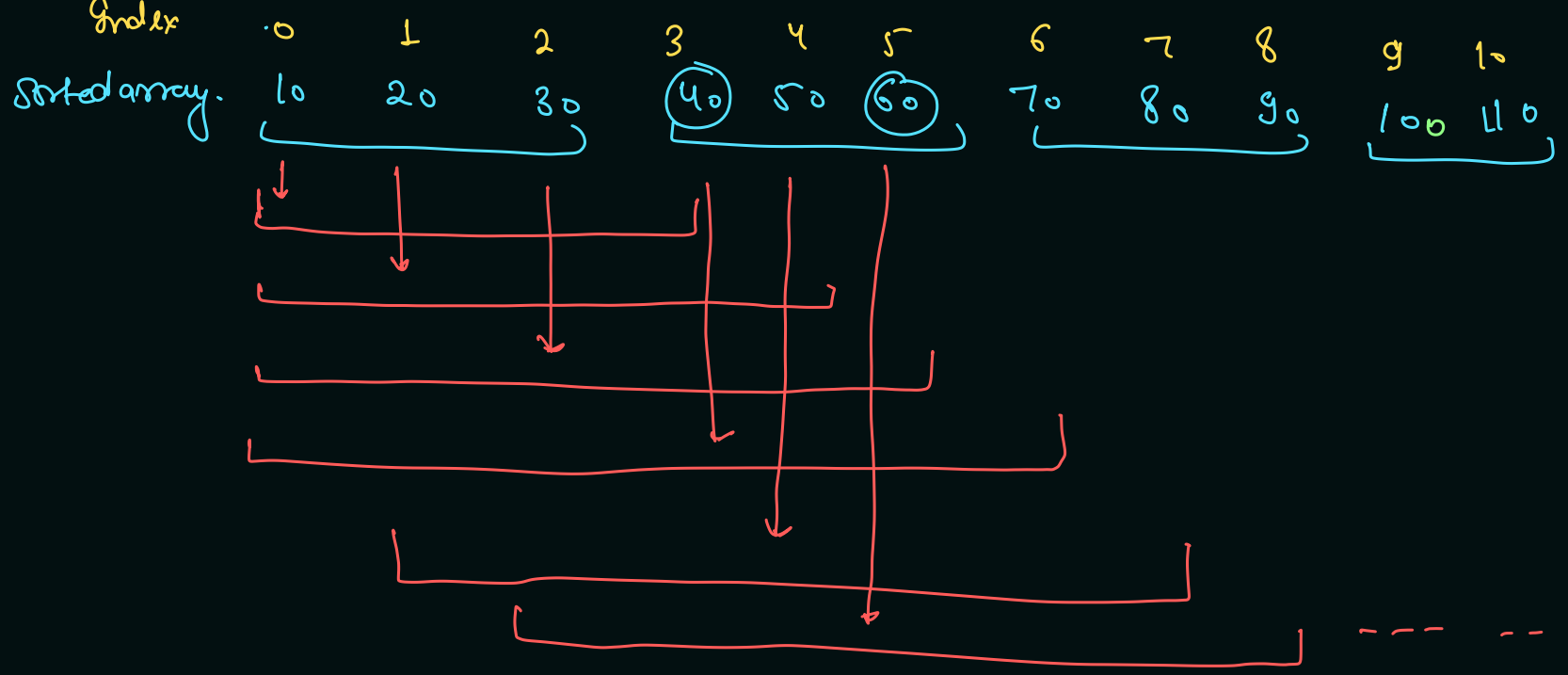
28 30 34 41 — k Largest Elem — Increasing order

using Stack

↳ order → Decreasing

Sort k-Sorted array: k=3

Elemt is spot k-distance either left or either right from its actuall position



↓

these type of array is known as k-sorted arr.

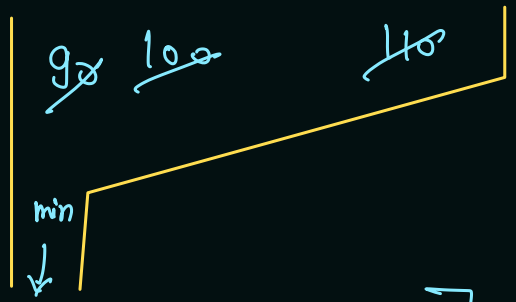
k=3

0	1	2	3	4	5	6	7	8	9
30	40	20	10	80	60	70	100	110	90

Time Complexity

↳ nlogk

min-pq.



✓10 ✓20 ✓30 40 60 70 80 90 100 110 ← sort

Median Priority Queue:

no. of Elements ⟶ odd → middle value is median

Even → first mid is median.

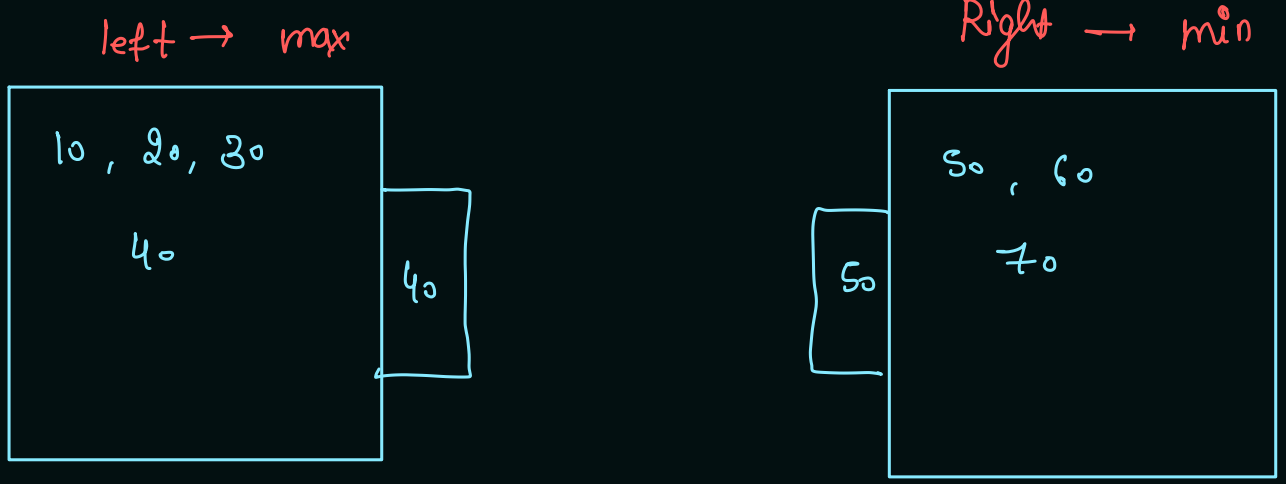
Ex 1 → 10 20 30 40 50 60 ⟶ Even → 30 median.

first mid

Second Mid

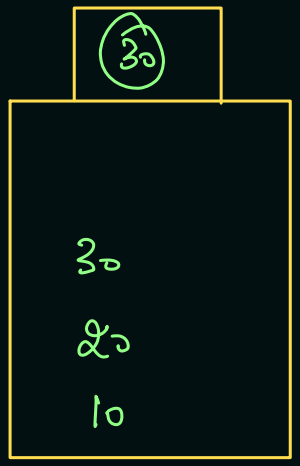
Ex 2 - 10 20 30 [40] 50 60 70 ⟶ odd → 40 median

mid

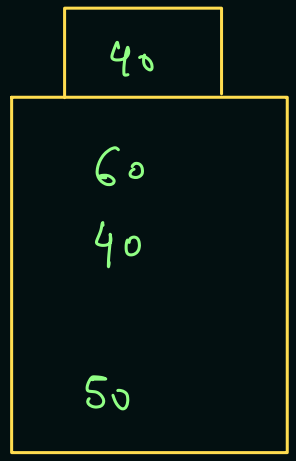


add
remove
peek
size

10 ✓
20 ✓
30 ✓
40 ✓
50 ✓
60 ✓
70



left → max



Right - min.

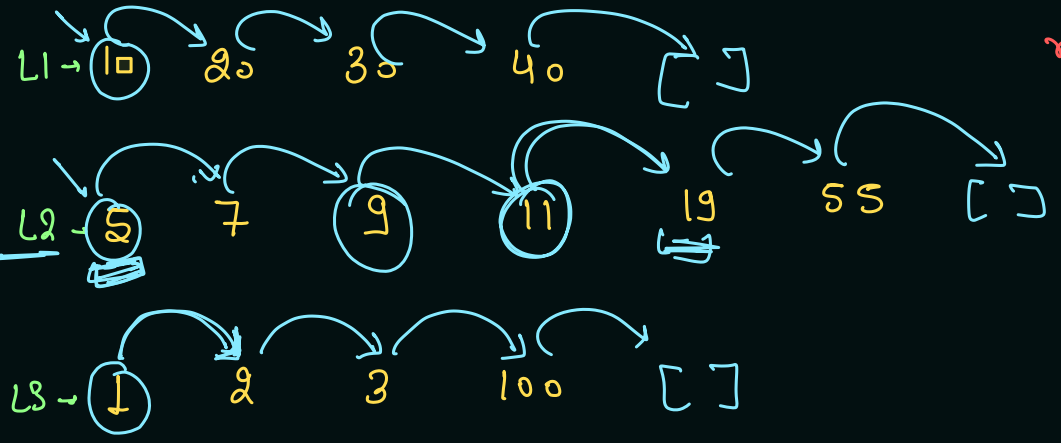
⟶ size diff. b/w left & Right ≤ 1.

Size → $\frac{\text{left size}}{z} = \frac{\text{right size}}{z}$

✓ $y+1 > y$

✓ $x < x+1$

Merge K- Sorted List:

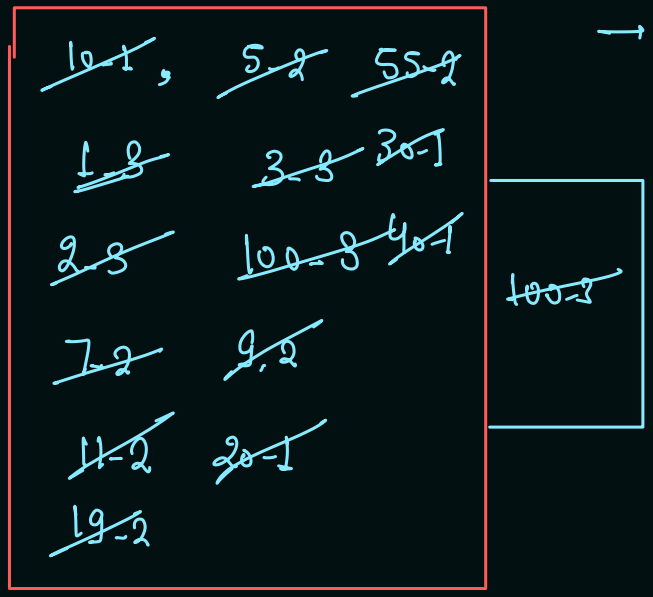


method 1 → add all element in pq. then one by one remove min. $n \log(n)$

using pointer → $n \times k$

method 2 (using PQ)

$n \log k$



→ 1, 2, 3, 5, 7, 9, 10, 11, 19, 20, 30

40, 55, 100.

Pq:

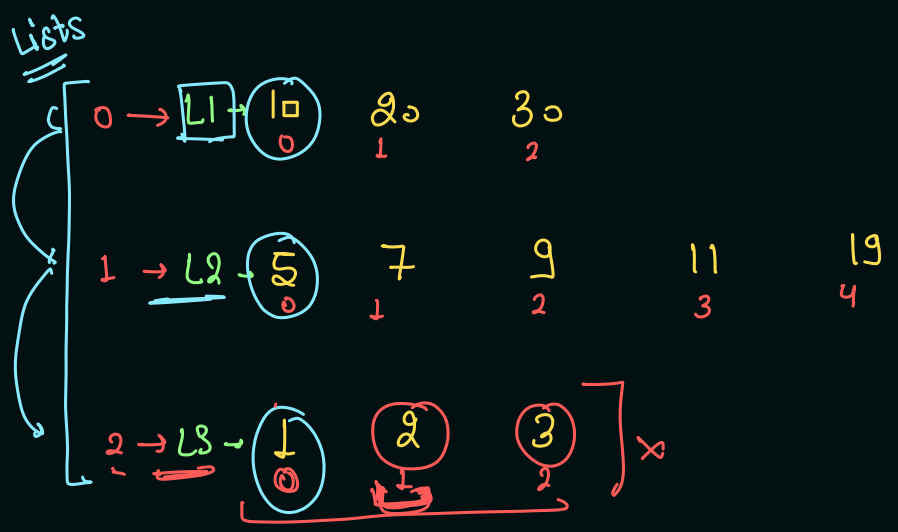
data

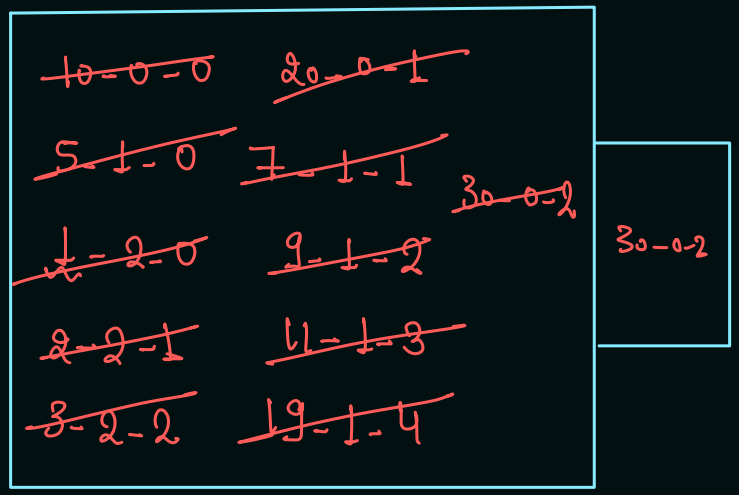
List index

priority on data.

[data
List index
data index]

→ first data ↑ single remove in A_L $O(1)$






```java
public static ArrayList<Integer> mergeKSortedLists(ArrayList<ArrayList<Integer>> list
    ArrayList<Integer> res = new ArrayList<>();
    PriorityQueue<Pair> pq = new PriorityQueue<>();
    for(int r = 0; r < lists.size(); r++) {
        pq.add(new Pair(lists.get(r).get( index: 0), r, di: 0));
    }
    while(pq.size() > 0) {
        Pair rem = pq.remove();
        res.add(rem.data);
        if(lists.get(rem.li).size() > rem.di + 1) {
            pq.add(new Pair(lists.get(rem.li).get(rem.di + 1), rem.li, rem.di + 1));
        }
    }
    return res;
}
```

result →

1 2 3 5 7 9 10

11 19 20 80