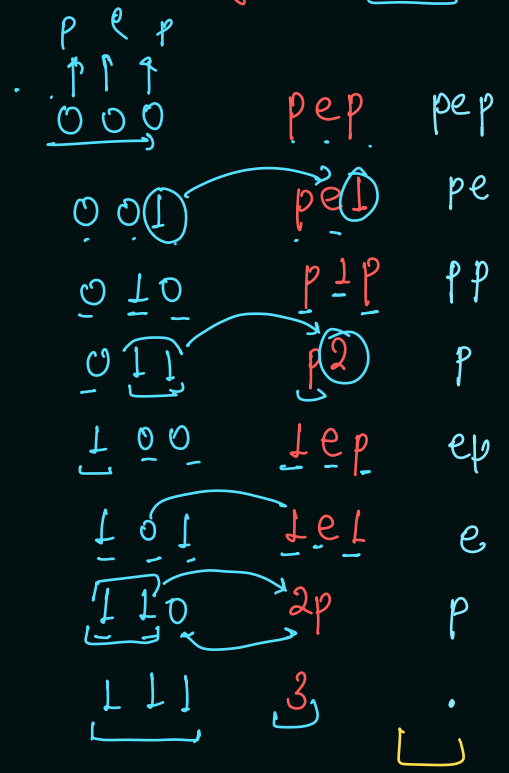
Abbreviation using backtracking:

String ⇒ pep

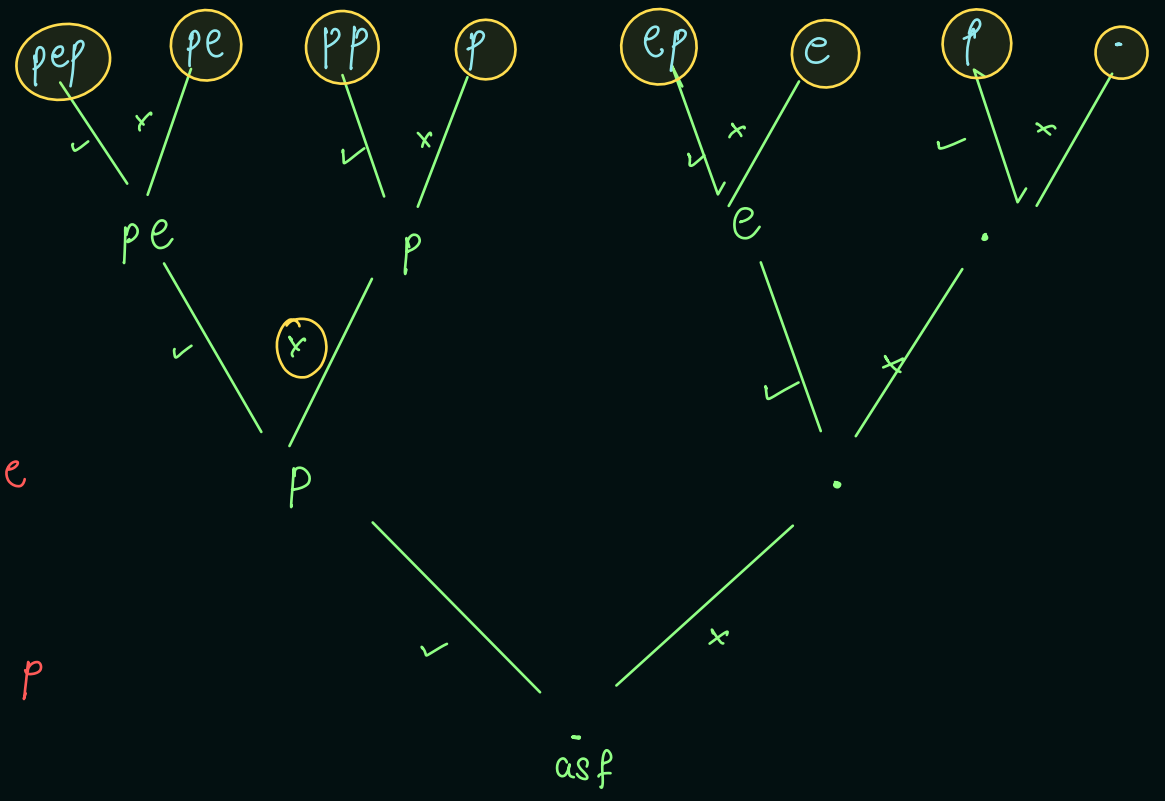
Base Idea of problem is → Subsequence.

level → character

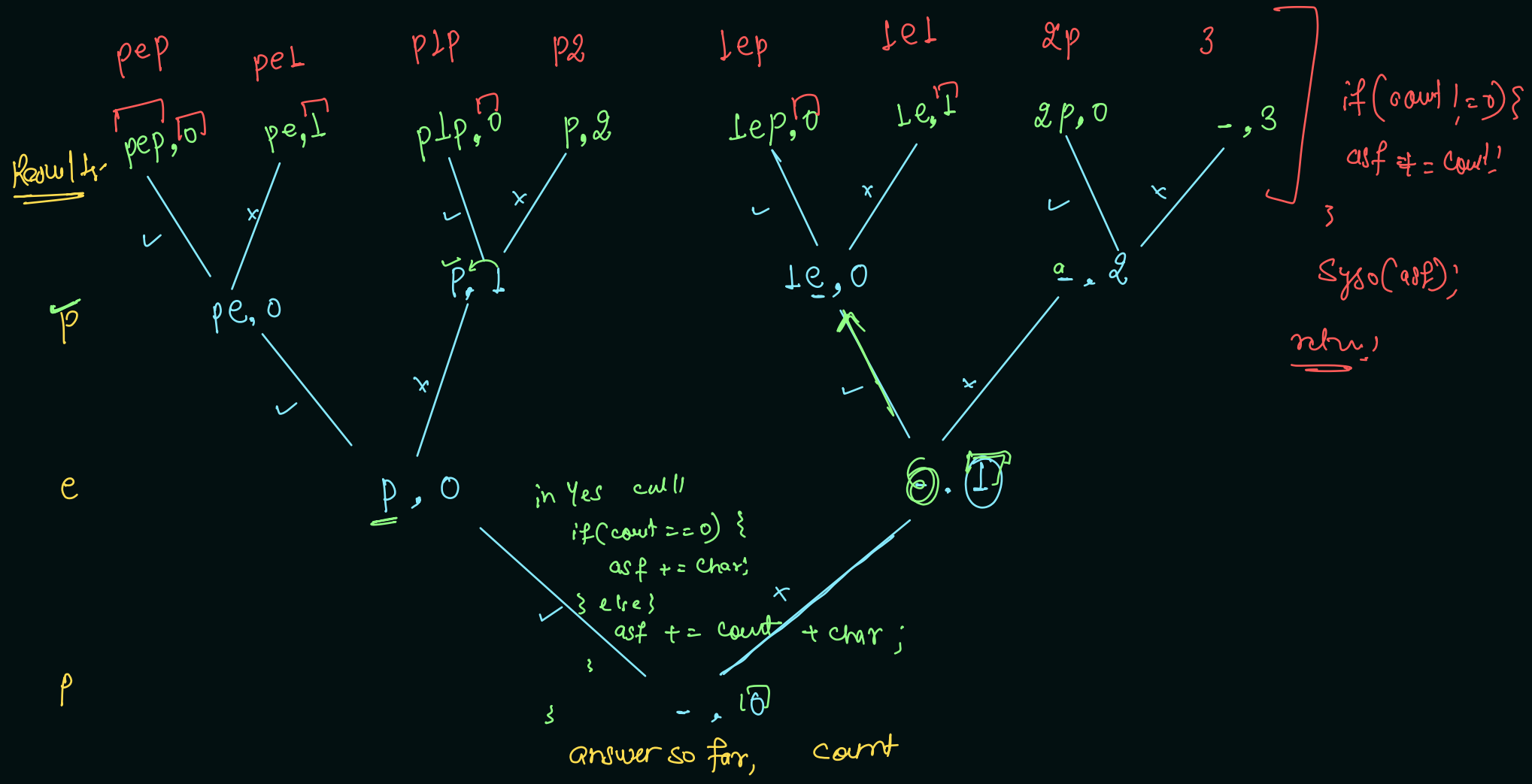
option → Yes and No of character



Results

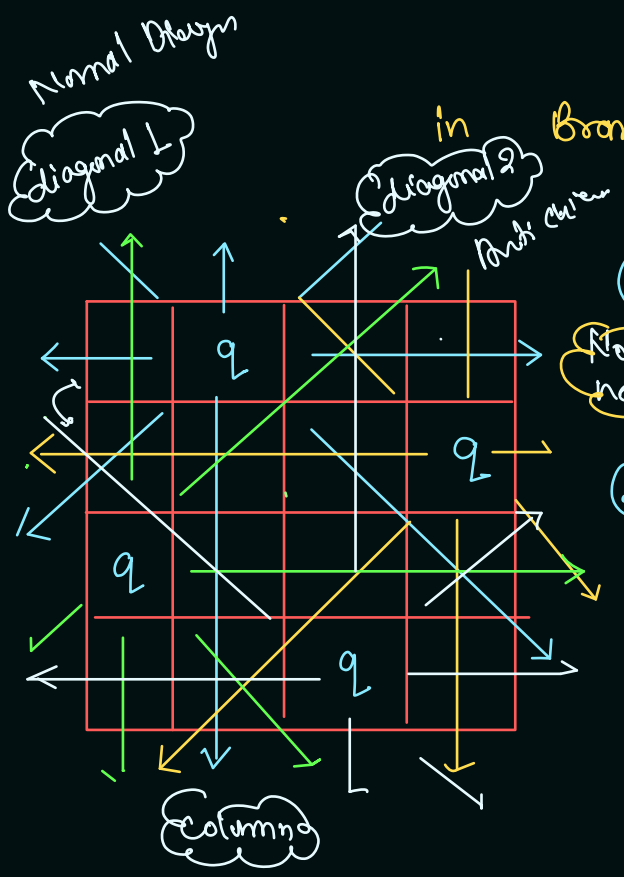


How we can print numerical value.



N - Queen Branch and Bound:

Complexity of "IsSafetoplace Queen" in previous question ? nearly = $4n \equiv O(n)$



in Branch & Bound, we will reduce complexity from $O(n)$ to $O(1)$

① In a row, we have to place Exactly one queen for sure. we can't place more than one queen in a row

② In next row, we have to check if position is safe or not.

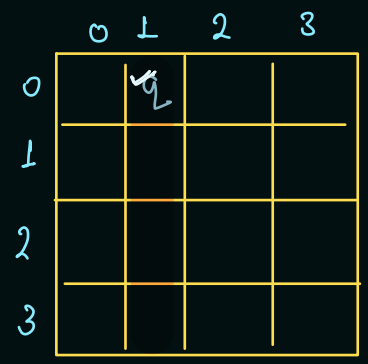
Rows are at level, & Row will change at every level, Place queen 'q' and stop column & diagonals for future queen, this whole logic is called "Branch & bound" method.

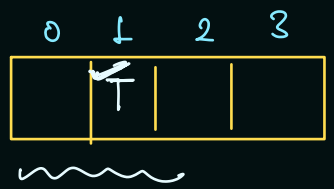
How to check isSafe in $O(1)$

diagonal 2 → normal diagonal [from top-right to bottom left]

diagonal → Reverse diagonal [from top-left to bottom-right]

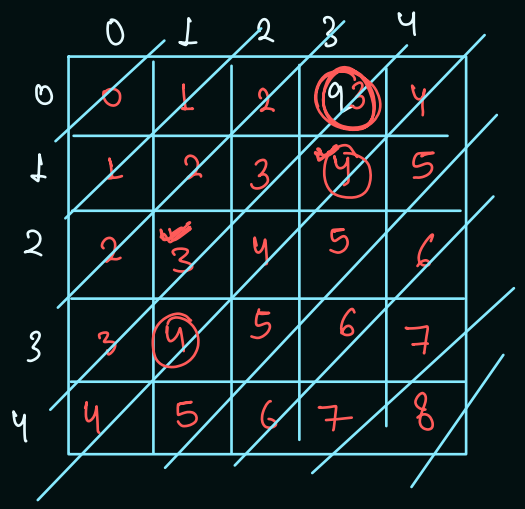
① How to Ensure Safety of Column;





boolean[] col = new boolean[column.length];

② How to Ensure Safety of Normal diagonal [from top-right to bottom left]

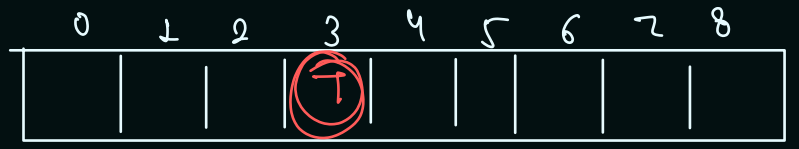


→ direction

no. of diagonal : row + col

length of diagonal array to check saffety is

2 * length − 1 = 2 × 5 − 1 = 9



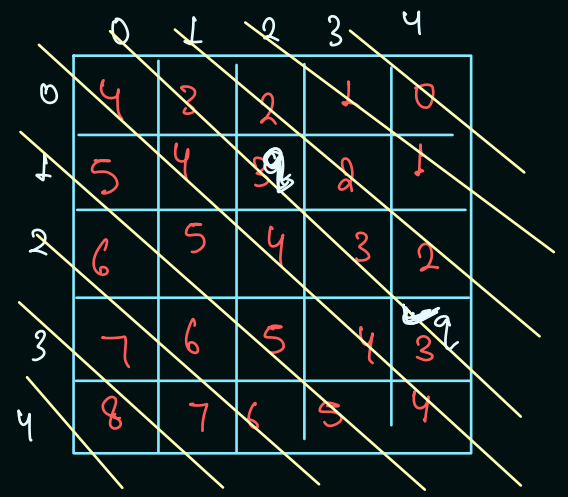
③ How to Ensure Safety in Reverse diagonal [from top-left to Bottom-Right]

	0	1	2	3	4
0	0	-1	-2	-3	-4
1	1	0	-1	-2	-3
2	2	1	0	-1	-2
3	3	2	1	0	-1
4	4	3	2	1	0

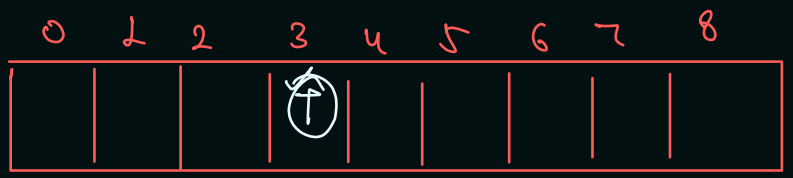
row - col → direction of diagonal

How to find proper index

$\Rightarrow$ (row - col) + (length - 1)



length of diagonal = $2 * length - 1 = 2 \times 5 - 1 = 9$



(1, 2)

Rev. diag ind = (row - col) + (length - 1)

$= (1-2) + (5-1)$

$= 3$

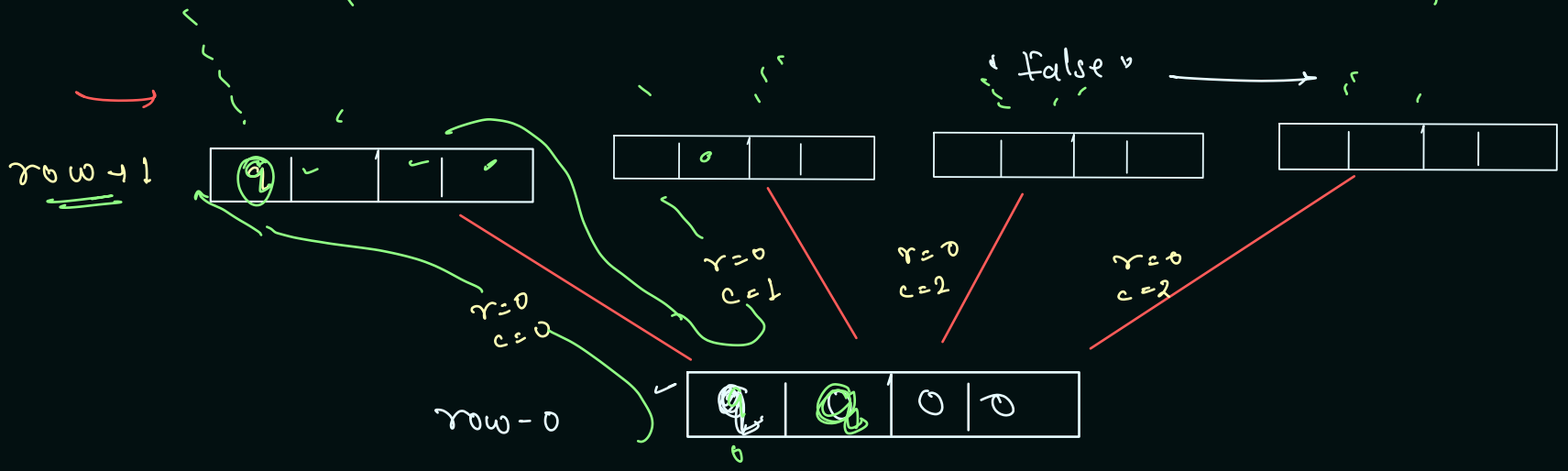
to place a queen at i,j indexs

↳ pass three check →
1. check of colums
2. check of diagonal
3. check of rev. diagonal

→ if check is pass
↳ then make a mark on
1. colum → col[j] = true
2. Diagonal → dia1[i+j] = true
3. Reverse diag → dia2[i-j+length-1] = true

make call

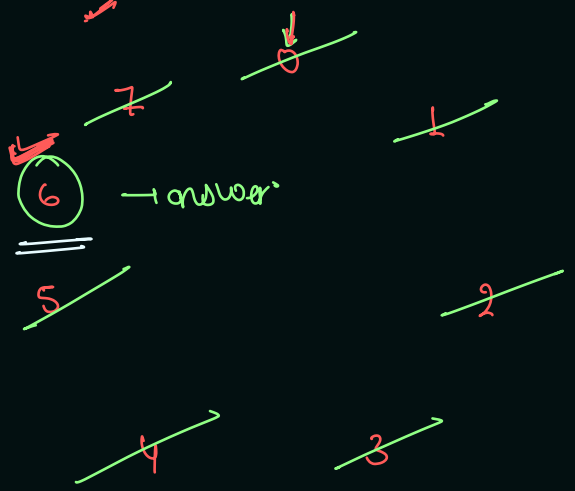
→ recursive → 1. colum 2. Diagonal & 3. Rever. diagon



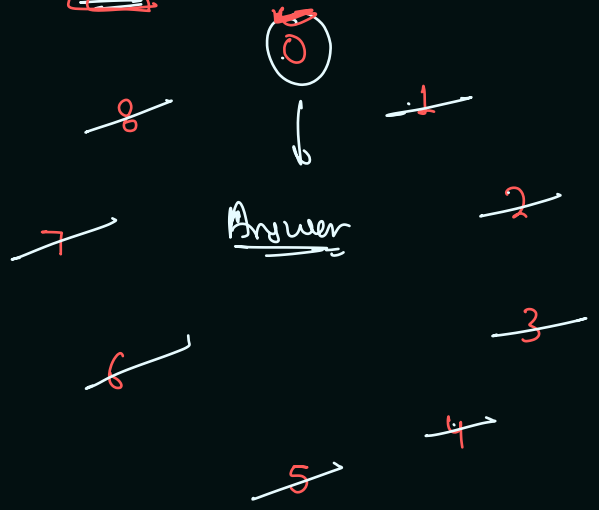
Josephus Problem:

n = no. of people in circle , k → number.

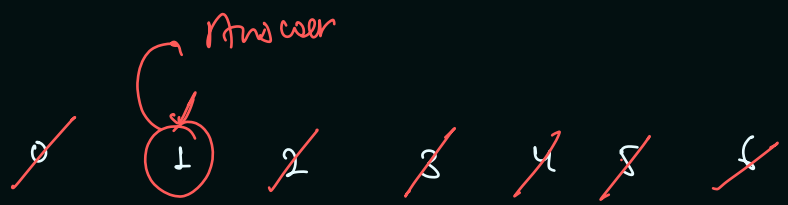
n=8, k=3



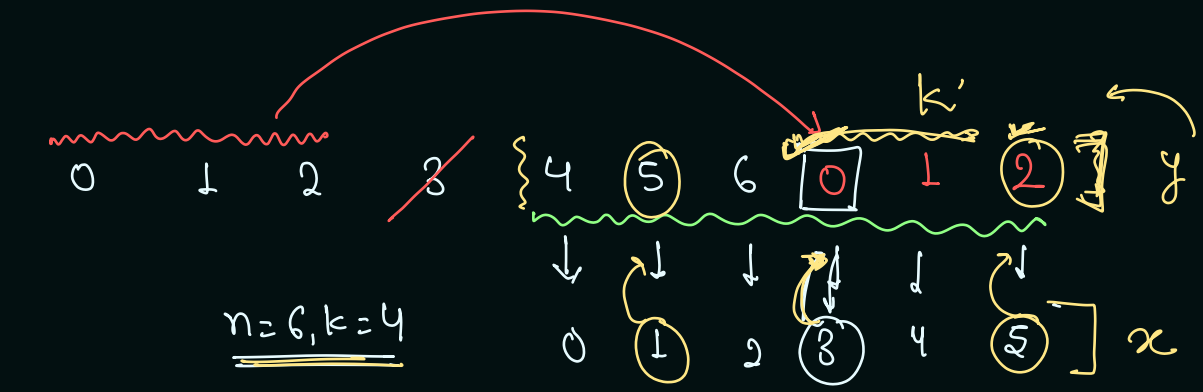
n=9, k=4



n=7, k=4



n=7, k=4.



$y = (x + k) \% n$ incurrent level :

x=3

$y = (3+4) \% 7 = 7 \% 7 = 0$

$y = (1+4) \% 7 = 5 \% 7 = 5$

$y = (5+4) \% 7 = 9 \% 7 = 2$

Expectation → f(n, k) → find remain person.

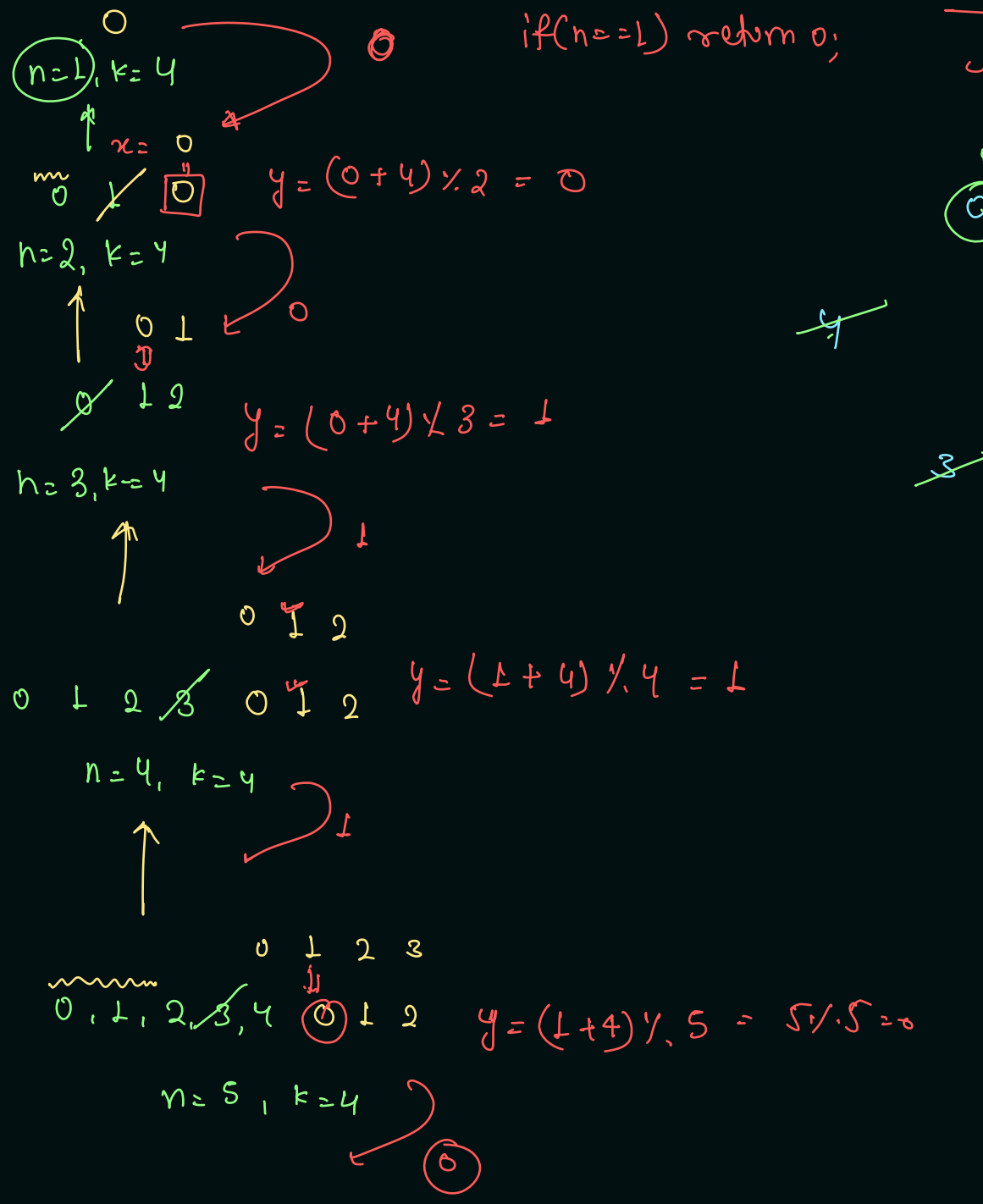
faith → x = (n-1, k) → send you no. of remaining sure.

Merging → find 'y' & return to next level

return = (x+k) % n;

n=5, k=4

```
p. int fun(int n, int k) {
    if(n == 1)
        return 0;
    int x = fun(n-1, k);
    return (x+k) % n;
}
```



lexicographical printing : n = 1000 [1 to 1000] print no. in lexicographical order

order of dictionary

dictionary order.

a →

b →

c →

d →

- da
- ab
- dc
  - dca ..
  - dcb
  - dcc ..

Set

1 → Set

2 → Set

3 → Set

4 → Set

4

41

42

43

n = 1000

1

10

100

1000

101

102

103

104

105

106

107

108

109

11

110

111

112

113

119

12 ....

120

121

122

123

129

13 -----

130

131

132

133

139

19

190

191

199

2 ....

20 ---

200 ---

201 --

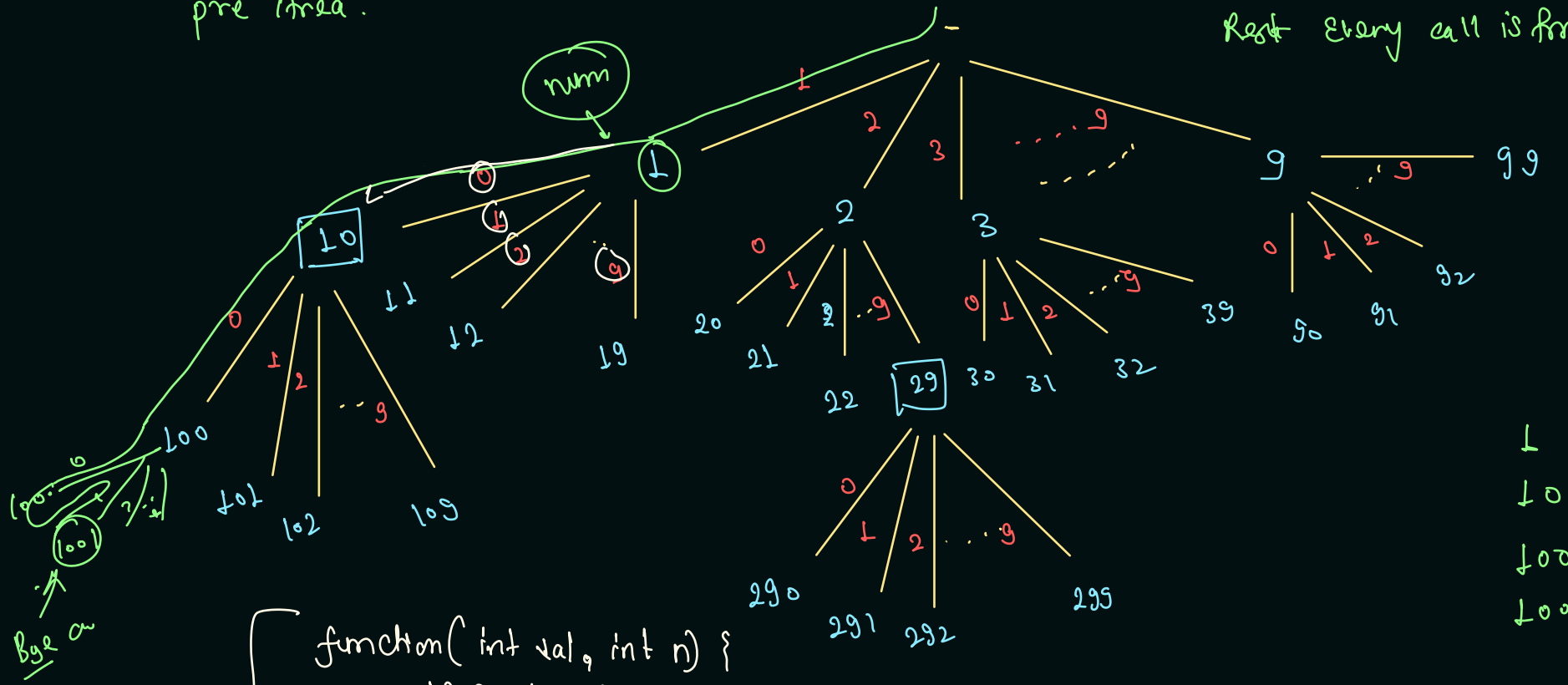
202 --

205 ..

Note → answer will print in pre Area.

n = 1000

first level call from main function → from 1 to 9.
Rest Every call is from 0 to 9



1
10
100
1000

Solution

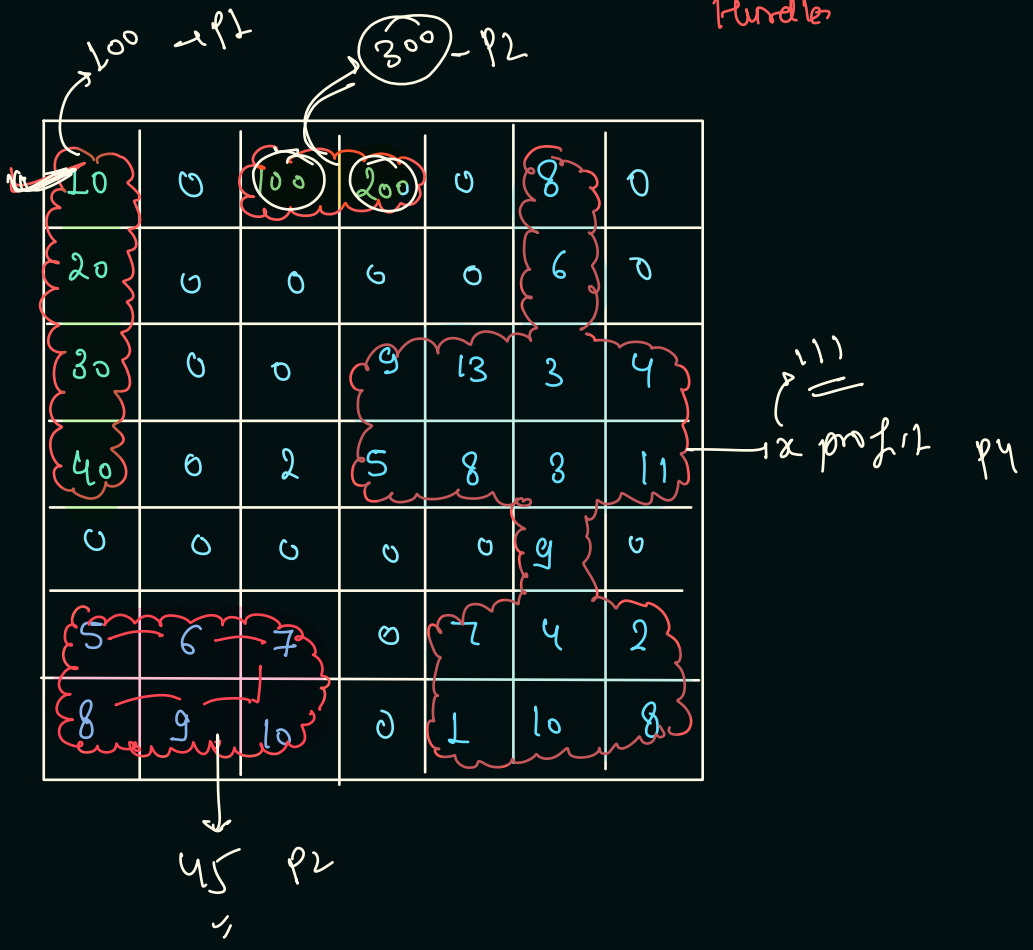
```
function( int val, int n) {
    if (val > n) return;

    sysO( val);
    for(int i=0; i<=9; i++){
        function( 10 * val + i, n);
    }
}
```

Goldmine 2:

if (mine[i][j] == 0) → Barrier / Hurdle

connected from top-left - down-right

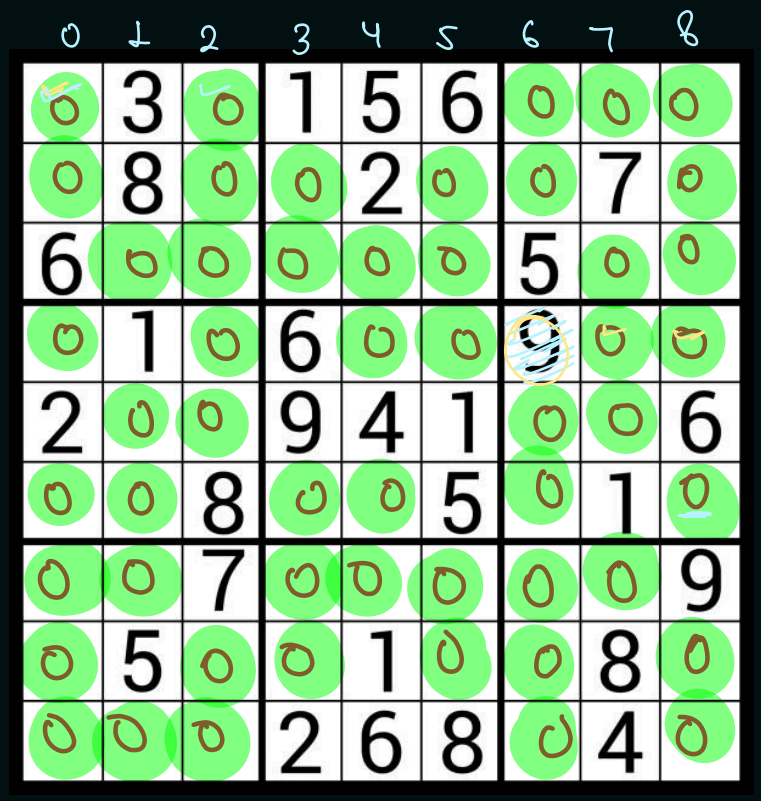


max profit = ?

Result = max (P1, P2, P3, P4)

Solve Sudoku:

number will no Repeat in
1. same Row
2. same col
3. same sub matrix



Safety: →
1. same Row
2. same col
3. same sub matrix

Starting of Submatrix →

rr = r - r%3

cc = c - c%3

Eg ⇒ 5, 8

5 - 5%3 = 5-2 = 3

8 - 8%3 = 8-2 = 6

```
isSafe to place( int i, int j, int num, int[][] board){
  // same col ⟶ loop in Row
  // same Row ⟶ loop in col,
  // for sub matrix
     int rr = i - i%3;
     int cc = j - j%3;
}
```

```
for(int r=0; r<3; r++){
   for(int c=0; c<3; c++){
      int ii = r+rr;
      int jj = c+cc;
      if(bd[ii][jj] == num) return false
}
```

After all check → return 0;

2D in 1D.

Array list of cell number →

	0	1	2	3	4	5	6	7	8
0	0	3	0	1	5	6	0	0	0
1	0	8	0	0	2	0	0	7	0
2	6	0	0	0	0	0	5	0	0
3	0	1	0	6	0	0	0	0	0
4	2	0	0	9	4	1	0	0	6
5	0	0	8	0	0	5	0	1	0
6	0	0	7	0	0	0	0	0	9
7	0	5	0	0	1	0	0	8	0
8	0	0	0	2	6	8	0	4	0

Recursion on list → 0 → cell no.

find r, c Total

r = cell / col

c = cell % col

How to find cell no.:

cell no = n * r + c

r=0 c=5 → 9*0+5 = 5

r=1 c=3 → 9*1+3 = 12

if cell no = 7

r = 7/9 = 0

c = 7 % 9 = 7

```
for(int num = 1 to 9; num++)
    Check safety;
    bd[r][c] = num;
    cell++
    bd[r][c] = 0;
}
```