Time Complexity

What is efficiency in a program ?

In a program efficiency can be considered in 2 ways -

- Time Complexity:
 - There are trillions of data need to be searched and sort as per user search, so if time complexity will not considered then it might takes hours to fetch the results. Google Search: use to pagerank algorithm for searching millions of info in less than 1 sec.
- Space Complexity:
 - There are lot of space constrain in real world, so to maintain such constraint we should use space complexity concept. Game Space: Reducing a game storage from gb to mb for lite version of it so than it can be a part of user who have less storage phones.

```
In [3]: number = int(input('enter the number'))

digits = '0123456789'
    result = ''
    while number != 0:
        result = digits[number % 10] + result
        number = number//10

print(result)

# Log(n)
```

```
In [4]: L = [1,2,3,4]

sum = 0
for i in L:
    sum = sum + i

product = 1
```

```
for i in L:
          product = product*i
        print(sum, product)
        \# O(n)+O(n)=O(2n)==O(n)
       10 24
In [6]: A = [1,2,3,4]
        B = [5,6,7,8]
        for i in A:
         for j in B:
            print(i,j)
        # O(len(A)*len(B))
       1 5
       1 6
      1 7
      1 8
      2 5
      2 6
       2 7
      2 8
       3 5
       3 6
       3 7
      3 8
      4 5
      4 6
       4 7
       4 8
In [8]: A = [1,2,3,4]
        B = [5,6,7,8]
        for i in A:
          for j in B:
           for k in range(100):
              print(i,j)
```

O(len(A)*len(B))

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In [10]: L = [1,2,3,4,5]
         for i in range(0,len(L)//2):
           other = len(L) - i - 1
           temp = L[i]
           L[i] = L[other]
           L[other] = temp
         print(L)
         \# O(n/2) == O(n)
        [5, 4, 3, 2, 1]
In [11]: n = 10
         k = 0
         for i in range(n//2,n):
           for j in range(2,n,pow(2,j)):
                 k = k + n / 2;
         print(k)
         # O(nLogn)
        35.0
In [13]: a = 10
         b = 3
         if b <= 0:
           print(-1)
         div = a//b
         print(a-div-b)
         # 0(1)
```

localhost:8888/lab/tree/Time Complexity.ipynb?

```
In [14]: n = 345
         sum = 0
         while n>0:
           sum = sum + n%10
           n = n // 10
         print(sum)
         # O(Logn)
        12
In [15]: def fib(n):
           if n == 1 or n == 0:
              return 1
            else:
              return fib(n-1) + fib(n-2)
         # O(2^n)
 In [ ]: # Subset Algo
                     {3T(n-1) if n>0
             T(n) = \{1, otherwise\}
In [16]: # 0(3<sup>n</sup>)
                     {2T(n-1)-1 if n>0
             T(n) = \{1, otherwise\}
In [17]: # 0(1)
         End
```

localhost:8888/lab/tree/Time Complexity.ipynb?