# ACADOS / ACADO 2.0 / ???? Reference

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## Chapter 1

## Interfaces

### 1.1 OCP QP Interface

The interface describes an Optimal Control Problem (OPC) Quadratic Programming (QP) problem in the form

$$\min_{x,u} \quad \sum_{n=0}^{N-1} \frac{1}{2} \begin{bmatrix} u_n \\ x_n \\ 1 \end{bmatrix}^T \begin{bmatrix} R_n & S_n & r_n \\ S_n^T & Q_n & q_n \\ r_n^T & q_n^T \end{bmatrix} \begin{bmatrix} u_n \\ x_n \\ 1 \end{bmatrix} + \frac{1}{2} \begin{bmatrix} x_N \\ 1 \end{bmatrix}^T \begin{bmatrix} Q_N & q_N \\ q_N^T \end{bmatrix} \begin{bmatrix} x_N \\ 1 \end{bmatrix} \quad (1.1)$$

s.t. 
$$x_{n+1} = A_n x_n + B_n u_n + b_n$$
 ,  $n = 0, ..., N-1$  (1.2)

$$\underline{u}_n \le u_n \le \overline{u}_n \quad , \quad n = 0, \dots, N - 1$$
 (1.3)

$$\underline{x}_n \le x_n \le \overline{x}_n \quad , \quad n = 0, \dots, N$$
 (1.4)

$$\underline{d}_n \le C_n x_n + D_n u_n \le \overline{d}_n \quad , \quad n = 0, \dots, N - 1$$
(1.5)

$$\underline{d}_N \le C_N x_N \le \overline{d}_N \tag{1.6}$$

The C code interface looks like

```
int ocp_qp_solver(
   int N, int *nx, int *nu, int *nb, int *ng,
   double **A, double **B, double **b,
   double **Q, double **S, double **R, double **q, double **r,
   int **idxb, double **lb, double **ub,
   double **C, double **D, double **ld, double **ud,
   double **x, double **u,
   struct ocp_qp_solver_args *args, double *work);
```

where

N [input] is the horizon length.

nx [input] is the vector of the state sizes  $n_u$  at the different stages, such that nx [n] is the state size at stage n.

- nu [input] is the vector of the input sizes  $n_x$  at the different stages, such that nu[n] is the input size at stage n.
- nb [input] is the vector of the bound sizes  $n_b$  at the different stages, such that nb[n] is the bound size at stage n. The value of nb[n] is smaller or equal to nx[n]+nu[n].
- ng [input] is the vector of the general polytopic constraint sizes  $n_g$  at the different stages, such that ng[n] is the general polytopic constraint size at stage n.
- A [input] is the vector of size N of the pointers to the first element of the matrices  $A_n$ , such that A[n] is the pointer to the first element of the matrix  $A_n$ , and A[n][0] is the first element of the matrix  $A_n$ . The matrix referenced by the pointer A[n] is stored in column-major (or Fortranlike) order, in a vector of  $nx[n+1] \times nx[n]$  double-precision floating-point numbers.
- **B** [input] is the vector of size N of the pointers to the first element of the matrices  $B_n$ , such that B[n] is the pointer to the first element of the matrix  $B_n$ , and B[n][0] is the first element of the matrix  $B_n$ . The matrix referenced by the pointer B[n] is stored in column-major (or Fortranlike) order, in a vector of  $nx[n+1] \times nu[n]$  double-precision floating-point numbers.
- **b** [input] is the vector of size N of the pointers to the first element of the vectors  $b_n$ , such that b[n] is the pointer to the first element of the vector  $b_n$ , and b[n][0] is the first element of the vector  $b_n$ . The vector referenced by the pointer b[n] is stored in a vector of  $nx[n+1] \times 1$  double-precision floating-point numbers.
- **Q** [input] is the vector of size N+1 of the pointers to the first element of the matrices  $Q_n$ , such that Q[n] is the pointer to the first element of the matrix  $Q_n$ , and Q[n][0] is the first element of the matrix  $Q_n$ . The matrix referenced by the pointer Q[n] is stored in column-major (or Fortranlike) order, in a vector of  $nx[n] \times nx[n]$  double-precision floating-point numbers.
- **S** [input] is the vector of size N of the pointers to the first element of the matrices  $S_n$ , such that S[n] is the pointer to the first element of the matrix  $S_n$ , and S[n][0] is the first element of the matrix  $S_n$ . The matrix referenced by the pointer S[n] is stored in column-major (or Fortranlike) order, in a vector of  $nu[n] \times nx[n]$  double-precision floating-point numbers.
- **R** [input] is the vector of size N of the pointers to the first element of the matrices  $R_n$ , such that R[n] is the pointer to the first element of the matrix  $R_n$ , and R[n][0] is the first element of the matrix  $R_n$ . The matrix

- referenced by the pointer R[n] is stored in column-major (or Fortran-like) order, in a vector of  $nu[n] \times nu[n]$  double-precision floating-point numbers.
- $\mathbf{q}$  [input] is the vector of size N+1 of the pointers to the first element of the vectors  $q_n$ , such that  $\mathbf{q}[\mathbf{n}]$  is the pointer to the first element of the vector  $q_n$ , and  $\mathbf{q}[\mathbf{n}][\mathbf{0}]$  is the first element of the vector  $q_n$ . The vector referenced by the pointer  $\mathbf{q}[\mathbf{n}]$  is stored in a vector of  $\mathbf{n}\mathbf{x}[\mathbf{n}] \times \mathbf{1}$  double-precision floating-point numbers.
- $\mathbf{r}$  [input] is the vector of size N of the pointers to the first element of the vectors  $r_n$ , such that  $\mathbf{r}[\mathbf{n}]$  is the pointer to the first element of the vector  $r_n$ , and  $\mathbf{r}[\mathbf{n}]$  [0] is the first element of the vector  $r_n$ . The vector referenced by the pointer  $\mathbf{r}[\mathbf{n}]$  is stored in a vector of  $\mathbf{nu}[\mathbf{n}] \times \mathbf{1}$  double-precision floating-point numbers.
- idxb [input] is the vector of size N+1 of the pointers to the first element of the integer vectors  $idxb_n$  describing the indexes of the corresponding upper and lower bounds in 1b and ub, such that idxb[n] is the pointer to the index of the first bound at stage n, and idxb[n][0] is index of the first bound at stage n. The indexes in idxb[n] correspond to the position of the constrained components in the variables vector  $\begin{bmatrix} u_n \\ x_n \end{bmatrix}$ : therefore a bound on the first input component has index 0, a bound on the last input component has index nu[n]-1, a bound on the first state component has index nu[n]+nx[n]-1. The vector referenced by the pointer idxb[n] is stored in a vector of  $nb[n] \times 1$  integer numbers.
- lb [input] is the vector of size N+1 of the pointers to the first element of the vectors  $\begin{bmatrix} \underline{u}_n \\ \underline{x}_n \end{bmatrix}$ , such that lb[n] is the pointer to the first element of the vector  $\begin{bmatrix} \underline{u}_n \\ \underline{x}_n \end{bmatrix}$ , and lb[n][0] is the first element of the vector  $\begin{bmatrix} \underline{u}_n \\ \underline{x}_n \end{bmatrix}$ . The vector referenced by the pointer lb[n] is stored in a vector of nb[n]×1 double-precision floating-point numbers.
- $\begin{array}{lll} \textbf{ub} & [\text{input}] \text{ is the vector of size } N+1 \text{ of the pointers to the first element of the} \\ & \text{vectors } \begin{bmatrix} \overline{u}_n \\ \overline{x}_n \end{bmatrix}, \text{ such that } \textbf{ub} [\textbf{n}] \text{ is the pointer to the first element of the} \\ & \text{vector } \begin{bmatrix} \overline{u}_n \\ \overline{x}_n \end{bmatrix}, \text{ and } \textbf{ub} [\textbf{n}] [\textbf{0}] \text{ is the first element of the vector } \begin{bmatrix} \overline{u}_n \\ \overline{x}_n \end{bmatrix}. \text{ The} \\ & \text{vector referenced by the pointer } \textbf{ub} [\textbf{n}] \text{ is stored in a vector of } \textbf{nb} [\textbf{n}] \times 1 \\ & \text{double-precision floating-point numbers.} \end{array}$
- C [input] is the vector of size N+1 of the pointers to the first element of the matrices  $C_n$ , such that C[n] is the pointer to the first element of the matrix  $C_n$ , and C[n] [0] is the first element of the matrix  $C_n$ . The matrix

- referenced by the pointer C[n] is stored in column-major (or Fortran-like) order, in a vector of  $ng[n] \times nx[n]$  double-precision floating-point numbers.
- **D** [input] is the vector of size N of the pointers to the first element of the matrices  $D_n$ , such that D[n] is the pointer to the first element of the matrix  $D_n$ , and D[n][0] is the first element of the matrix  $D_n$ . The matrix referenced by the pointer D[n] is stored in column-major (or Fortranlike) order, in a vector of  $ng[n] \times nu[n]$  double-precision floating-point numbers.
- Id [input] is the vector of size N+1 of the pointers to the first element of the vectors  $\underline{d}_n$ , such that  $\mathtt{ld}[n]$  is the pointer to the first element of the vector  $\underline{d}_n$ , and  $\mathtt{ld}[n][0]$  is the first element of the vector  $\underline{d}_n$ . The vector referenced by the pointer  $\mathtt{ld}[n]$  is stored in a vector of  $\mathtt{ng}[n] \times 1$  double-precision floating-point numbers.
- ud [input] is the vector of size N+1 of the pointers to the first element of the vectors  $\overline{d}_n$ , such that ud[n] is the pointer to the first element of the vector  $\overline{d}_n$ , and ud[n][0] is the first element of the vector  $\overline{d}_n$ . The vector referenced by the pointer ud[n] is stored in a vector of ng[n]×1 double-precision floating-point numbers.
- $\mathbf{x}$  [output] is the vector of size N+1 of the pointers to the first element of the vectors  $x_n$ , such that  $\mathbf{x}[\mathbf{n}]$  is the pointer to the first element of the vector  $x_n$ , and  $\mathbf{x}[\mathbf{n}][0]$  is the first element of the vector  $x_n$ . The vector referenced by the pointer  $\mathbf{x}[\mathbf{n}]$  is stored in a vector of  $\mathbf{n}\mathbf{x}[\mathbf{n}] \times 1$  double-precision floating-point numbers.
- ${\bf u}$  [output] is the vector of size N+1 of the pointers to the first element of the vectors  $u_n$ , such that  ${\bf u}[{\bf n}]$  is the pointer to the first element of the vector  $u_n$ , and  ${\bf u}[{\bf n}]$  [0] is the first element of the vector  $u_n$ . The vector referenced by the pointer  ${\bf u}[{\bf n}]$  is stored in a vector of  ${\bf nu}[{\bf n}] \times 1$  double-precision floating-point numbers.
- args [input] is the pointer to a structure of type ocp\_qp\_solver\_args that defines the arguments (as e.g. maximum number of iterations, minimum step size, ...) passed to the specific solver.
- work [workspace] is the pointer to the working space used by the specific solver. The working space size (in doubles) is returned by a call to the function ocp\_qp\_SOLVERNAME\_workspace\_double(int N, int \*nx, int \*nu, int \*nb, int \*ng, struct ocp\_qp\_solver\_args \*args), where SOLVERNAME is the name of the specific solver.

Furthermore, the function returns an int, that is defined in the following enum (TODO change the names to something better!!!):

ACADOS\_SUCCESS Solution successfully found.

ACADOS\_MAXITER Maximum number of iterations reached.

**ACADOS\_MINSTEP** Minumum step size reached (in IPs, probably unfeasible problem).

### 1.1.1 Examples

#### MPC problem

In the MPC problem, the initial state is fixed. This is modelled by choosinig nx[0]=0, i.e. not considering the initial state as an optimization variable. As a consequence, e.g. the matrix A[0] has size  $nx[1]\times 0$ , the matrix Q[0] has size  $0\times 0$ , and the vector q[0] has size  $0\times 1$ . The information about the known value of  $x_0$  and the matrix  $A_0$  are used to compute the value of the vector b[0], that is initialized to  $b_0 + A_0 \cdot x_0$ .