

Data Structures I: Vectors, Matrices, and Arrays



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BSDS 100 - Intro to Data Science with \mathbb{R}



- Vectors
- Matrices



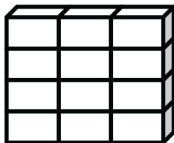
- A **data structure** is a format or organization of data in software that enables efficient use.
- Every programming language has its own types of data structures
- In \mathbb{R} , you can create your own type of data structure; however, there are some that are automatically recognized by the software.
- **Examples:** list, array, data.frame, vector, matrix, string



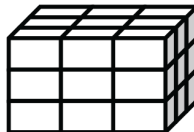
(a) Vector



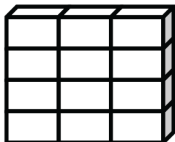
(b) Matrix



(c) Array

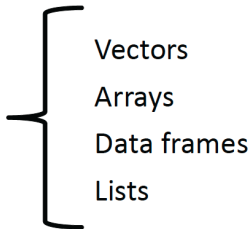


(d) Data frame



Columns can be different modes

(e) List



Vectors

Arrays

Data frames

Lists



Dimension	Homogeneous	Heterogeneous
1	Atomic Vector	List
2	Matrix	Data Frame
n	Array	

Homogeneous: All contents must be of the same type

Heterogeneous: Contents can be of different types

Note: There are no 0-dimensional (scalar) types in R, only vectors of length one

Part I: Vectors



- The basic data structure in R is the vector
- There two types of vectors: atomic vectors and lists

Properties of Vectors

- Type (`typeof()`)
- Length (`length()`)
- Attributes (`attributes()`)

Use `is.atomic()` or `is.list()` to determine if an object is a vector, **not** `is.vector()`



Four Common Types of Vectors

- Logical
- Integer
- Double (numeric)
- Character

```
> doubleAtomicVector <- c(1, 3.14, 99.999)
```

```
# use L suffix to get integers instead of doubles
```

```
> integerAtomicVector <- c(1L, 3L, 19L)
```

```
> logicalAtomicVector <- c(TRUE, FALSE, T, F)
```

```
> characterAtomicVector <- c("this", "is a", "string")
```


Example: Try This



- 1 Create the vector `myFavNum` of you favorite fractional number
- 2 Create the vector `myNums` of your seven favorite numbers
- 3 Create the vector `firstNames` of the first names of two people next to you
- 4 Create the vector `myVec` of the last name and age of someone you know

Example: Answer these



- 1 Guess and then check what types your vectors are.
- 2 Check the length of each vector.
- 3 Did you write the code in the console window or the editor?
- 4 How do you execute a line of code in the editor?
- 5 How do you execute multiple lines of code simultaneously in the editor?
- 6 Did you use the `TAB` button for auto-completion?

Accessing Elements of a Vector



- To access the individual elements of a vector

```
> (myAtomicVector <- c(1, 2, 3, 4, -99, 5, NA, 4, 22.223))  
[1] 1.000 2.000 3.000 4.000 -99.000 5.000 NA  
[8] 4.000 22.223
```

#look at fifth element of the vector

```
> myAtomicVector[5]  
[1] -99
```

```
> myAtomicVector[c(1, 2, 5, 9)]  
[1] 1.000 2.000 -99.000 22.223
```

```
> myAtomicVector[10]  
[1] NA
```

#look at the third through eighth elements of the vector

```
> myAtomicVector[3:8]  
[1] 3 4 -99 5 NA 4
```



- To look at the first and last 6 elements of a vector

```
> (myAtomicVector <- c(1, 2, 3, 4, -99, 5, NA, 4, 22.223))  
[1] 1.000 2.000 3.000 4.000 -99.000 5.000 NA  
[8] 4.000 22.223
```

#look at the first and last six elements of the vector

```
> head(myAtomicVector)  
[1] 1.000 2.000 3.000 4.000 -99.000 5.000
```

```
> tail(myAtomicVector)  
[1] 4.000 -99.000 5.000 NA 4.000 22.223
```

Example, continued



- ➊ Add `myFavNum` to the seventh entry of `myNums` and store the result in a variable named `myFirstAddition`
- ➋ Add `myFavNum` to each of the seven entries of `myNums` and store the result in a variable named `mySecondAddition`
- ➌ Add `myFavNum` to **all** of the values in `myNums` and store the result in a variable named `myFirstSum`
- ➍ Add `myFavNum` to the smallest number in `myNums` and store the result in a variable named `thisIsGettingMoreComplex`
- ➎ Add the second entry of `myNums` to the age of the person you select for `myVec` and store the result in a variable named `whatTypeOfVectorIsThis`
 - Does what we did make sense? Did it work? Why?



```
# preamble
myFavNum <- 3.1415
myNums <- c(1, 3, 55, 33, 86, -sqrt(2), -110)
# also works myNums <- 1:7
firstNames <- c("Sarah", "Terence", "Habibi")
myVec <- c("Parr", 99)
```

- ❶ myFirstAddition <- myFavNum + myNums[7]
- ❷ mySecondAddition <- myFavNum + myNums
- ❸ myFirstSum <- myFavNum + sum(myNums)
- ❹ thisIsGettingMoreComplex <- myFavNum + min(myNums)
- ❺ whatTypeOfVectorIsThis <- sum(c(myNums[2], myVec[2]))
Error in sum(c(myNums[2], myVec[2])) :
invalid 'type' (character) of argument



Why did (2) `myFavNum + myNums` work?

R "recycles" the shorter vector to get the length of the longer vector

Try this:

```
my_n1_vector <- 5
my_n3_vector <- 1:3
my_n7_vector <- c(3, 7, 28, 43, 1, 5.5, 19)
my_n9_vector <- sample(1:100, 9)
```

- 1 What happens if you add `my_n1_vector` to `my_n3_vector`?
- 2 What happens if you add `my_n3_vector` to `my_n9_vector`?
- 3 What happens if you add `my_n7_vector` to `my_n9_vector`?



```
# What happens when you add a vector of length 1 to  
# a vector of length 3?
```

```
> my_n1_vector + my_n3_vector  
[1] 6 7 8
```

```
# The single item is added to each of the three  
# elements of the vector of length 3.
```




```
# What happens when you add a vector of length 3 to  
# a vector of length 9?
```

```
> my_n3_vector + my_n9_vector  
[1] 62  4 50 27 17 47 87 43 99
```

```
# The three elements are added (in order) to the first  
# three, second three, and third three elements of the  
# length nine vector
```



```
# What happens when you add a vector of length 7 to a vector of  
# length 9?
```

```
> my_n7_vector + my_n9_vector  
[1] 64.0 9.0 75.0 69.0 16.0 49.5 105.0 44.0 103.0
```

Warning message:

```
In my_n7_vector + my_n9_vector :  
  longer object length is not a multiple of shorter object length
```

```
# The first two elements of the length-7 vector will be recycled,  
# the last five will be used once
```



Missing values are specified with `NA`, a logical vector of length one.

- `NA` will always be coerced to the correct type if used inside `c()`

```
> c(1, 2, 3, NA)
[1] 1 2 3 NA
```

```
> x[1]
[1] 1
```

```
> x <- c(1, 2, 3, NA)
```

```
> x[4]
[1] NA
```

```
> typeof(x)
[1] "double"
```

```
> typeof(x[4])
[1] "double"
```



- Certain functions will fail when applied to vectors with an `NA`

```
> myAtomicVector_01 <- c(99.1, 98.2, 97.3, 96.4, NA)
[1] 99.1 98.2 97.3 96.4    NA
```

```
> sum(myAtomicVector_01)
[1] NA
```

```
> mean(myAtomicVector_01)
[1] NA
```



- You can avoid this by providing the argument `na.rm = TRUE`

```
> sum(myAtomicVector_01, na.rm = TRUE)
[1] 391
```

```
> mean(myAtomicVector_01, na.rm = TRUE)
[1] 97.75
```



To check the type of a vector, use `typeof()`, or more specifically

- `is.character()`
- `is.double()`
- `is.integer()`
- `is.logical()`
- `is.na()`



Coercion is a great feature in \mathbb{R} which can make coding easy, but may also have unintended consequences.

- All elements in an atomic vector must be the same type
- If you attempt to combine different types in an atomic vector they will be coerced to the most flexible type
- **Most to least flexible types** ↓
 - character
 - double
 - integer
 - logical

- When a logical vector is coerced to numeric (double or integer), TRUE = 1 and FALSE = 0

```
> x <- c("abc", 123)
```

```
> typeof(x)
```

```
[1] "character"
```

You can explicitly coerce using `as.character()`, `as.double()`, `as.integer()`, and `as.logical()`



- A quick way to figure out what data structure an object is composed of is to use `str()`, which is short for structure
- `str()` provides a concise description for any R data structure



- The syntax is awkward and takes some time to get used to
- Once you understand the sequence of events in conditional subsetting, it will feel more natural
- Try to figure out what is happening in the following example:

```
> (myAtomicVector_01 <- c(99.1, 98.2, 97.3, 96.4))  
[1] 99.1 98.2 97.3 96.4
```

```
> myAtomicVector_01[myAtomicVector_01 > 98]  
[1] 99.1 98.2
```

What is actually happening in the last slide:

- 1 The `myAtomicVector_01 > 98` part of the statement tests each element of the vector to see whether it is > 98 and returns a `LOGICAL` value for each test which, in this case, returns the logical vector `(T T F F)`
- 2 The vector `(T T F F)` is passed to `myAtomicVector_01`, which returns the first two elements and omits the final two
 - An equivalent statement would be
`myAtomicVector_01[c(T, T, F, F)]`



Function	Action
----------	--------

<code>seq(from, to, by)</code>	Creates a vector of numbers from <code>from</code> to <code>to</code> in increments of <code>by</code>
--------------------------------	--

<code>rep(x, times)</code>	Creates a vector that repeats the values in <code>x</code> exactly <code>times</code> number of times
----------------------------	---

<code>x + (-, /, *) y</code>	For <code>x</code> and <code>y</code> of the <i>same length</i> , calculates a vector of the same length where each entry is the entry-wise summation (subtraction, division, or product) of <code>x</code> and <code>y</code>
------------------------------	---



- If you would like to create a vector that is a sequence of numbers from x to y that increase by exactly one, then you can simply write

$x:y$

- `rep()` can be applied to a `seq()`, providing a flexible means to create sequences with repeating patterns.

Example:

```
> rep(seq(1, 1.3, .1), 2)
[1] 1.0 1.1 1.2 1.3 1.0 1.1 1.2 1.3
```

Example



```
> x <- rep(c(1,2), 3)
```

```
> y <- seq(from = .5, to = 3, by = .5)
```

```
> x
```

```
[1] 1 2 1 2 1 2
```

```
> y
```

```
[1] 0.5 1.0 1.5 2.0 2.5 3.0
```

```
> x+y
```

```
[1] 1.5 3.0 2.5 4.0 3.5 5.0
```

```
> x/y
```

```
[1] 2.0000000 2.0000000 0.6666667 1.0000000 0.4000000 0.6666667
```

A List of Logical Operators



Operator	Description
<code><</code>	Less than
<code><=</code>	Less than or equal to
<code>></code>	Greater than
<code>>=</code>	Greater than or equal to
<code>==</code>	Exactly equal to
<code>!=</code>	Not equal to
<code>!x</code>	Not x
<code>x y</code>	x or y
<code>x & y</code>	x and y
<code>isTRUE(x)</code>	Test if x is TRUE

Vector example: names



- A name is a vector **attribute**
- Can be identified using the `names()` function

```
> x <- c(1, 2, 3)
> names(x)
NULL
```

```
> x <- c(1, 2, 3); names(x) <- c("a", "b", "c")
> names(x)
[1] "a" "b" "c"
```

```
> x <- c(a = 1, b = 2, c = 3)
> names(x)
[1] "a" "b" "c"
```

```
> x <- c(a = 1, b = 2, 3)
> names(x)
[1] "a" "b" ""
```


Part II: Matrices and Arrays



- By giving an atomic vector a dimension attribute, it behaves like a multi-dimensional array
- A special case of the array is a matrix, a two-dimensional array
- A matrix has 2 dimensions, and an array has $n \geq 2$ - dimensions.
- Matrices and arrays are created with `matrix()` and `array()`



```
> x <- matrix(1:10, nrow = 2, ncol = 5)  
# can drop nrow and ncol to shorten but keep in this order
```

```
> x  
      [,1] [,2] [,3] [,4] [,5]  
[1,]    1    3    5    7    9  
[2,]    2    4    6    8   10
```



```
> y <- array(1:12, c(2, 3, 2))
```

```
> y
```

```
, , 1
```

	[,1]	[,2]	[,3]
[1,]	1	3	5
[2,]	2	4	6

```
, , 2
```

	[,1]	[,2]	[,3]
[1,]	7	9	11
[2,]	8	10	12



1-D Function n-D Functions

<code>length()</code>	<code>nrow()</code> , <code>ncol()</code> , <code>dim()</code>
<code>names()</code>	<code>rownames()</code> , <code>colnames()</code> , <code>dimnames()</code>
<code>c()</code>	<code>cbind()</code> , <code>rbind()</code>

Note: a matrix or array can also be one-dimensional, e.g., an object that is defined as a matrix is permitted to only have one column or one row; although they may look and behave alike, a vector and a one-dimensional matrix behave differently and may generate strange output when using certain functions, e.g., `tapply()`



Function	Purpose
----------	---------

<code>length(object)</code>	Number of elements
<code>dim(object)</code>	Dimensions of an object
<code>str(object)</code>	Structure of an object
<code>class(object)</code>	Type of an object
<code>c(object, object,)</code>	Combines objects into a vector
<code>cbind(object, object,)</code>	Combines objects as columns
<code>rbind(object, object,)</code>	Combines objects as rows
<code>object</code>	Prints the object
<code>head(object)</code>	Prints the first part of the object
<code>tail(object)</code>	Prints the last part of the object
<code>ls()</code>	Lists current objects
<code>rm(object, object, ...)</code>	Deletes one or more objects