BSDS 100: Intro to Data Science with R Assignment 4

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Directions: For all questions in this assignment, write complete sentences and fully answer any question that is asked. Provide all R code and solutions by *knitting* your final RStudio file into a single file named [your_name]_CA4.pdf. This assignment is due next Tuesday at the beginning of class. Late assignments will automatically have 10 points deducted.

1. Create the vector

> myAtomicVector <- c(1, 4, 3, 2, NA, 3.22, -44, 2, NA, 0, 22, 34)

- (a) How many positive numbers (>0) are there in this vector?
- (b) How many negative numbers (<0) are there in this vector?
- (c) How many 0's are there in this vector?
- (d) How many NAs are there is this vector?
- (e) How many numbers in the vector are non-zero and not NAs?
- (f) What is the sum of the positive numbers is this vector?
- (g) What is the sum of the negative numbers is this vector?
- 2. Consider a vector of length 1000, where F_n is the *n*th number in the sequence. Then the Fibonacci sequence is the vector where the following recursion holds:

$$F_n = F_{n-1} + F_{n-2}$$

That is, the nth number in the sequence will be the sum of the previous two numbers.

- (a) Using the rep() and seq() commands, create a vector named Fib.vec (but don't print it out!) that contains the first 1000 Fibonacci numbers starting from the first two numbers (1, 1).
- (b) What are the first 8 and last 8 entries of Fib.vec?
- (c) Using the Fibonacci numbers generated above, generate a vector (of length 999) with values (again, don't print these out)

$$Z_n = \frac{F_{n+1}}{F_n}$$

- (d) Plot the vector Z_n using the command $plot(Z_n)$. Then add a line to the plot using the following command abline(h = (1 + sqrt(5)/2)). This value is known as the golden ratio in mathematics.
- (e) Comment on the plot that you obtain. What do you observe?

- 3. Using the Fibonacci vector above, create the following data structures.
 - A matrix of size 100×10 named Fib.matrix1 whose columns, when stacked on top of one another will return the original vector.
 - A matrix of size 100×10 named Fib.matrix2 whose rows, when stacked side by side will return the original vector.
 - An array of dimension $10 \times 10 \times 10$ names Fib.array where each 10×10 matrix in the array is such that when its columns are stacked on top of one another would generate a Fibbonaci vector of length 100.

Answer the following questions

- (a) What is the mean of the 18th row of Fib.matrix1?
- (b) What is the standard deviation of the 8th column of Fib.matrix2?
- (c) What is the entry in the 5th row of the 2nd column of the 8th matrix in Fib.array?