



Name : .....

Roll No. : .....

Invigilator's Signature : .....

**CS/B.TECH(NEW)(APM/CSE/IT/AUE/CHE/BT/ME  
/PE/CE/CT/LT/TT/FT/SEM-4/M(CS)-401/2012**

**2012**

**NUMERICAL METHODS**

Time Allotted : 3 Hours

Full Marks : 70

*The figures in the margin indicate full marks.*

*Candidates are required to give their answers in their own words  
as far as practicable.*

**GROUP – A**

**( Multiple Choice Type Questions )**

1. Choose the correct alternatives for any *ten* of the following :

$$10 \times 1 = 10$$

- i) If  $\frac{5}{3}$  is approximated to 1.6667, then absolute error is

- a) 0.000033                      b) 0.000043  
c) 0.000034                      d) none of these.

- ii) If  $f(x) = \frac{1}{x^2}$  then the divided difference  $f(a, b)$  is

- a)  $\frac{(a + b)}{(ab)^2}$                       b)  $\frac{(a - b)}{(ab)^2}$   
c)  $\frac{1}{a^2} - \frac{1}{b^2}$                       d)  $\frac{1}{a^2 - b^2}$ .



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viii) Pivoting is very much essential because

- a) determinant of the coefficient matrix should be greater than zero
- b) pivot element should not have very large value compared to the elements of the matrix
- c) it reduces the possibility of division by zero
- d) change of convergence is higher.

ix) Which of the following is true ?

- a)  $\Delta^n x^n = (n + 1)!$
  - b)  $\Delta^n x^n = n!$
  - c)  $\Delta^n x^n = 0$
  - d)  $\Delta^n x^n = n.$
- x) An  $n \times n$  matrix  $A$  is said to be diagonally dominant if

- a)  $|a_{ii}| \geq \sum_{\substack{j=1 \\ i \neq j}}^n |a_{ij}|$
- b)  $|a_{ii}| \leq \sum_{\substack{j=1 \\ i \neq j}}^n |a_{ij}|$
- c)  $|a_{ii}| > \sum_{\substack{j=1 \\ i \neq j}}^n |a_{ij}|$
- d)  $|a_{ii}| < \sum_{\substack{j=1 \\ i \neq j}}^n |a_{ij}|.$

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xi) The condition of convergence of Newton-Raphson's method is

- a)  $|f(x) \cdot f'(x)| < \{f''(x)\}^2$
- b)  $|f(x) \cdot f''(x)| < \{f'(x)\}^2$
- c)  $|f(x) \cdot f'(x)| > \{f''(x)\}^2$
- d)  $|f(x) \cdot f''(x)| > \{f'(x)\}^2$ .

xii) For  $\frac{dy}{dx} = xy$  and  $y(0) = 2$ , the value of  $k_2$  according to

Runge-Kutta method of 2nd order is ( $h = 0.2$ )

- a) 0.1
- b) 0.01
- c) 0.4
- d) 0.04.

### GROUP - B

#### ( Short Answer Type Questions )

Answer any *three* of the following.  $3 \times 5 = 15$

2. Given  $u_0 + u_6 = 3$ ,  $u_1 + u_5 = 5$ ,  $u_2 + u_4 = 7$ . Find  $u_3$ , where  $v_x$

is a function of  $x$ .

3. Using the following table find  $\frac{dy}{dx}$  at  $x = 0$  &  $1.5$ .

$x$ :	0	1	2	3
$y$ :	1	2	11	34



4. Solve the following system of equations using Gaussian elimination method :

$$\begin{aligned}x + y + z &= 9 \\2x - 3y + 4z &= 13 \\3x + 4y + 5z &= 40\end{aligned}$$

5. Find the value of  $(19)^{\frac{1}{3}}$  correct to four decimal points by Newton-Raphson method.
6. Find the cubic polynomial by Lagrange's interpolation formula which takes the following value :

$x$	:	0	4	5	8
$f(x)$	:	1	2	1	10

### GROUP – C

#### ( Long Answer Type Questions )

Answer any *three* of the following.  $3 \times 15 = 45$

7. a) Find a root of the equation  $x^4 - x - 10 = 0$  that lies between 1 & 2 using Newton-Raphson method correct to 3 places of decimal.
- b) Solve the system of equations

$$\begin{aligned}x + y + 54z &= 110 \\27x + 6y - z &= 85 \\6x + 15y + 2z &= 72\end{aligned}$$

by Gauss-Seidel method.

7 + 8

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8. a) Solve the following system of equations by LU-factorization method :

$$3x + 2y + 7z = 4$$

$$2x + 3y + z = 5$$

$$3x + 4y + z = 7$$

- b) Using Runge-Kutta method of order 4, find  $y(0.2)$

given that  $\frac{dy}{dx} = 3e^x + 2y$ ,  $y(0) = 0$ , taking  $h = 0.1$ .

7 + 8

9. a) Find the root of the equation  $3x - \cos x - 1 = 0$  by Regula-falsi method, correct to three decimal places.

- b) Evaluate  $\int_0^{\frac{\pi}{2}} \sqrt{\cos x} dx$  by using (i) Trapezoidal and

(ii) Simpson's  $\frac{1}{3}$ rd rule, where  $h = 15^\circ$ . 7 + 8

10. a) Compute  $y(1.4)$  by Milne's predictor & corrector's

method from  $\frac{dy}{dx} = \frac{1}{2}(x + y)$  where  $y(1) = 3.595$ ,

$y(1.1) = 3.833$ ,  $y(1.2) = 4.088$ ,  $y(1.3) = 4.362$ .

- b) Derive Newton's divided difference formula.



- c) Given that  $\frac{dy}{dx} = \log_{10}(x+y)$  with the initial condition

that  $y = 1$  when  $x = 0$ . Find  $y$  for  $x = 0.2$  and  $x = 0.5$   
using Euler's modified formula. 5 + 5 + 5

11. a) If  $y = f(x)$  is a polynomial degree 5 with  
 $y_0 = f(0) = 0$ ,  $y_1 = f(1) = 3$ ,  $y_2 = f(2) = 14$ ,  
 $y_3 = f(3) = 45$ ,  $y_4 = f(4) = 84$ ,  $y_5 = f(5) = 170$ ,  
 $y_6 = f(6) = 258$ . It is found that there is one error in  
the value of  $y_3$ . Find the correct value of  $y_3$ .

- b) Why implicit method is preferred over explicit method  
though it requires more computations ?
- c) Show that the rate of convergence in Newton-Raphson  
method is quadratic. 8 + 3 + 4

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