

**NATIONAL INSTITUTE OF TECHNOLOGY, KURUKSHETRA**  
**THEORY EXAMINATION**  
**Question Paper**

Month and year: **Dec. 2019**  
Program: **B.Tech.-CS**  
Subject: **DAA**  
Maximum Marks: **50**  
Number of Questions to be attempted: **5**

Total no. of pages used: **2**  
Semester: **III**  
Course code: **CSPC-21**  
Time allowed: **03 Hours**  
Total No of Questions: **5**

**Note 1:** Question No. 5 has an internal choice. Attempt any one part of it.

**Note 2:** Unless stated otherwise, the symbols have their usual meanings in context with subject. Assume suitably and state, additional data required, if any.

<b>Q-1.</b>	(a). Define Heap and analyze the complexity of min heap function.	2
	(b). Explain Prim's Algorithm for minimum Spanning tree. Also compute its time complexity.	2
	(c). Define B-Tree with its terminology. Also insert following in a B-Tree having order 3. 7, 3, 5, 11, 16, 4, 9, 2	2
	(d). How backtracking algorithm solves the Hamiltonian problem? Explain.	2
	(e). Write pseudo code to find strongly connected component in a graph.	2
<b>Q-2.</b>	(a). Solve following recurrence relation using recursion tree method. $T(n) = \begin{cases} 1 & \text{if } n = 1 \\ T(n/3) + T(2n/3) + \theta(n) & \text{if } n > 1 \end{cases}$	3
	(b). What is graph coloring problem? Write the pseudo code to color a graph and also analyze its complexity.	3
	(c). Write the pseudo code to solve 8-queen problem using the backtracking algorithm. Show all the steps of 4-queen problem and analyze the complexity of n-queen problem.	4
<b>Q-3.</b>	(a). Prove the master theorem.	5
	(b). Write the algorithms to solve the rod-cutting problem. Also analyze its time complexity.	5
<b>Q-4.</b>	(a) Define the elements of the Dynamic Programming. Write all the steps to find the LCS of two string X = <ABCDGH> and Y = <AEDFHR>.	4
	(b) Write the pseudo code for Johnson's algorithm. Professor Greenstreet claims that there is a simpler way to reweight edges than the method used in Johnson's algorithm. Letting $w^* = \min_{(u,v) \in E} \{w(u,v)\}$ , just define $\hat{w}(u,v) = w(u,v) - w^*$ for all edges $(u,v) \in E$ . what is wrong with the professor's method of reweighting?	6

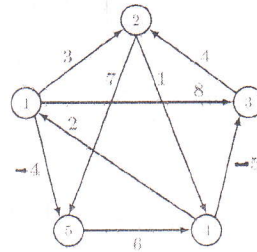
Q-5.

- (a) What is task scheduling problem? Find optimal sequence of Jobs for following jobs using greedy algorithm.

Job	J <sub>1</sub>	J <sub>2</sub>	J <sub>3</sub>	J <sub>4</sub>	J <sub>5</sub>
Deadline	2	1	3	2	1
Profit	60	100	20	40	20

- (b). Find the optimal parenthesis of matrix chain multiplication where sequence of dimensions is A1:10×100, A2: 100×5, A3:5×50, A4:50×20

- (c) Explain Floyd-Warshall Algorithm to find all pair shortest path. Find all pair shortest path of following problem also analyze its complexity.



OR

- (a) What is priority queue? Illustrate the operation of HEAP-EXTRACT-MAX on the heap A = <15, 13, 9, 5, 12, 8, 7, 4, 0, 6, 2, 1>.

- (b) Write the pseudo code for Huffman codes. Generate the Huffman code for following symbols.

Symbol	a	b	c	d	e	f
Frequency	6	11	9	2	20	5

- (c) Let  $G=(V, E)$  be a weighted, directed graph with nonnegative weight function  $w: E \rightarrow \{0, 1, \dots, W\}$  for some nonnegative integer  $W$ . Modify Dijkstra's algorithm to compute the shortest paths from a given source vertex  $s$  in  $O(WV + E)$  time.