

भारतीय सूचना प्रौद्योगिकी संस्थान कोटा  
INDIAN INSTITUTE OF INFORMATION TECHNOLOGY KOTA

B.Tech. (ECE)  
End Term Examination, Even Semester 2023-24

Electromagnetic Theory (ECT208); Close Book

Marks: 40 (Weightage – 40%)

Time: 120 minutes

Date: May 16, 2024

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1. What is volume current density? If the current density  $\mathbf{J} = (2\cos\theta \mathbf{a}_r + \sin\theta \mathbf{a}_\theta)/r^3$  A/m<sup>2</sup>, then calculate the current passing through a spherical shell of radius 10 cm. [2+6]
2. Two homogeneous isotropic dielectric materials have the boundary at  $z = 0$  plane. The dielectric constants  $\epsilon_{r1} = 4$  for  $z \geq 0$  and  $\epsilon_{r2} = 3$  for  $z \leq 0$ . If the electric field  $\mathbf{E}_1 = (5\mathbf{a}_x - 2\mathbf{a}_y + 3\mathbf{a}_z)$  kV/m exists for  $z \geq 0$  then find out the electric field  $\mathbf{E}_2$  for  $z \leq 0$ . Also find out the angle of  $\mathbf{E}_1$  and  $\mathbf{E}_2$  with the interface. [4+4]
3. A transmission line has the following per-unit-length parameters:  $L = 0.5$   $\mu$ H/m,  $C = 200$  pF/m,  $R = 4.0$   $\Omega$ /m, and  $G = 0.02$  S/m. Calculate the propagation constant and characteristic impedance of this line at 800 MHz. If the line is 30 cm long, what is the attenuation in dB? [2+3+3]
4. Write down the Maxwell equation which is based on the Faraday's law of electromagnetic induction. Starting from Maxwell's equations, develop the wave equations in source free region. [2+6]
5. A plane wave propagating in a lossless dielectric medium has an electric field given as  $\mathbf{E}_x = E_0 \cos(\omega t - \beta z) \mathbf{a}_x$  V/m with a frequency of 5.0 GHz and a wavelength in the material of 3.0 cm. Determine the propagation constant, phase velocity and permittivity of the medium. [2+2+4]

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