

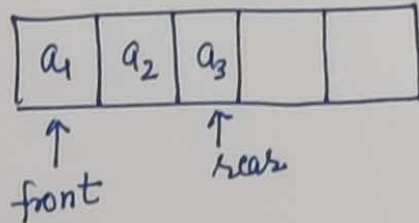
Queue

①

— Philosophy for insertion and deletion:

FIFO (FCFS).

— Elements inserted at the "rear" and removed from "front".



ADT:

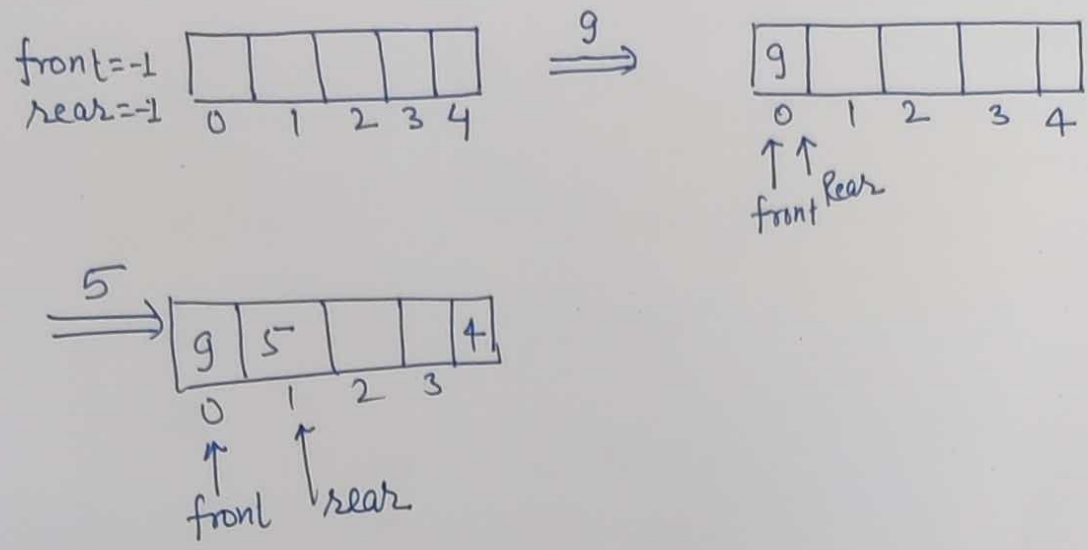
Operation:

- * $New()$: used for creation of new (empty) queue.
- * $Enqueue(s, x)$: to insert element 'x' at the rear
- * $Dequeue(s, x)$: Remove x from front
- * $front() / Peak()$: return the front element
- * $Size()$: # of elements (integer)
- * $isFull()$: Overflow (binary)
- * $is Empty$: Underflow (binary)

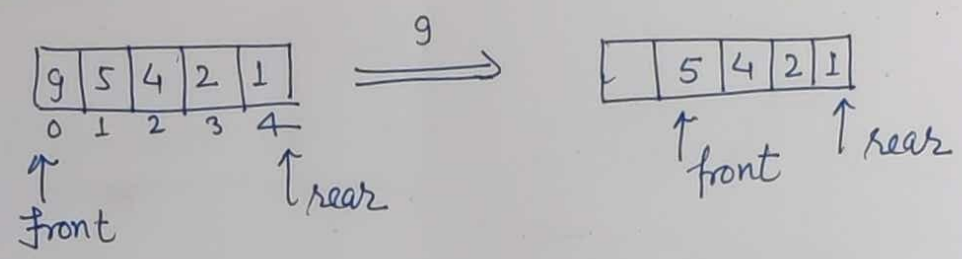
Axioms:-

- * $Front(Enqueue(New(), x)) = x$
- * $Dequeue(Enqueue(New(), x)) = New()$
- * $Front(Enqueue(Enqueue(Q, x), y)) = Front(Enqueue(Q, x))$
- * $Dequeue(Enqueue(Enqueue(Q, x), y)) =$
 $Enqueue(Dequeue(Enqueue(Q, x)), y)$

Example:- ENQUEUE



- DEQUEUE -



= IMPLEMENTATION =

USING STATIC ARRAY :-

- Realizes ~~the~~ queue of maximum possible size.
- front is maintained at the smallest index and rear at the max. index.

ENQUEUE:-

n : size of array
 Q : queue.

```

if (rear == n-1)
    "Print overflow"
else if (front == -1 & rear == -1)
    front ← 0
    rear ← 0
else
    rear ← rear + 1
    Q[rear] ← item
    
```

Precondition for Enqueue: Q has been initialized and not full

Postcondⁿ :- new item at rear of queue.

Deque

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Precondⁿ: Q has been initialized and is not empty

Postcondⁿ: front element has been removed

1. If ($\text{front} = -1 \parallel \text{front} > \text{rear}$)

Print "underflow"

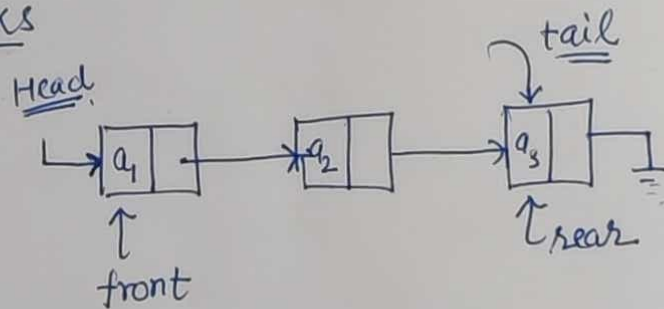
else

$\text{item} \leftarrow Q[\text{front}]$

$\text{front} \leftarrow \text{front} + 1$

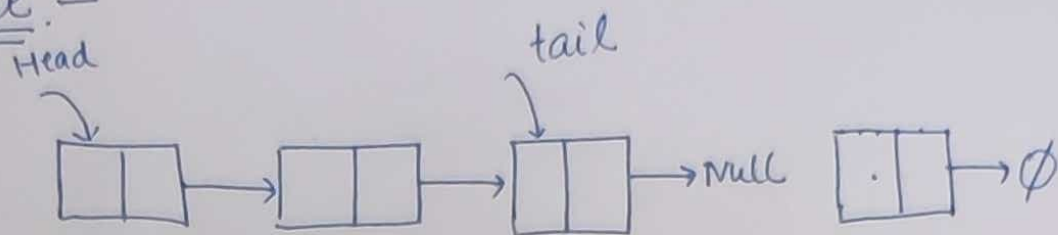
Dynamic linked list Implementation

1. Node (data, Ptr) connected in a chain by links

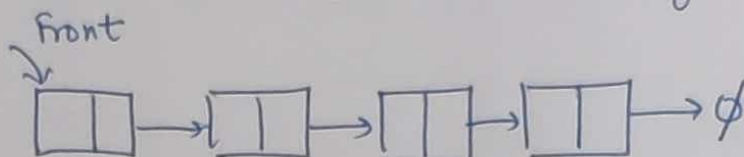


[Head of the list : front]
[Tail : rear]

Enqueue:-



- Create a node at tail
- add it and move the tail reference.



Algo:-

1. create a node pointer, say. temp.
2. temp[data] \leftarrow item
3. temp[next] \leftarrow \emptyset
4. if (front = \emptyset)
 - front \leftarrow temp
 - rear \leftarrow temp
- else
 - rear[next] \leftarrow temp
 - rear \leftarrow temp

Dequeue:-

If (front = null)

Print "underflow"

else . Initialize a node pointer temp & set it to front

if (front = rear)

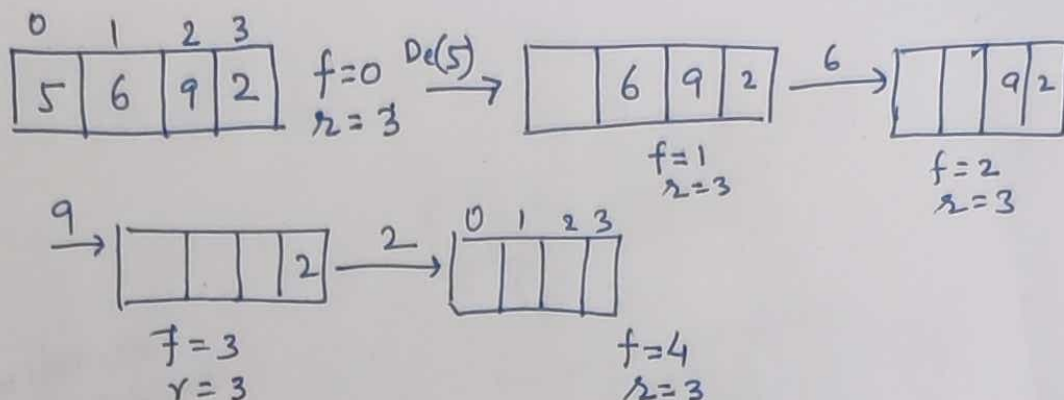
front = rear = \emptyset

else

front \leftarrow front[next]

release memory location pointed by temp.

- Problem with simple Queue -



\Rightarrow $rear = n-1$: means overflow

\Rightarrow But, queue is empty.

CIRCULAR QUEUES / Double-Ended Queue

It Support Insertion & Deletion from front & rear.

\rightarrow Operation:

InsertFirst(s, x) : insert at beginning of queue.

InsertLast(s, x) : ——— end —

RemoveFirst(s) : remove the first

RemoveLast(s) : ——— last —

First(s) : return first element

Last(s) : return last —

Issue(s) In implementing queue with "simple" array :-

ENQUEUE :-

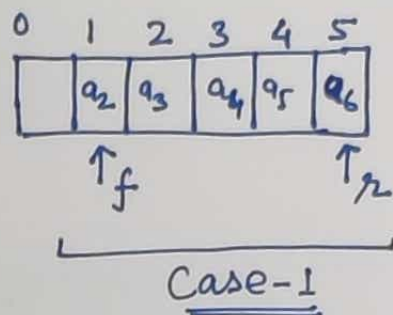
To do enqueue:-

function :- Add new item to rear of the queue

Precondⁿ :- queue is not full

$$r < n-1$$

Postcondⁿ :- new item should be added to rear of queue.



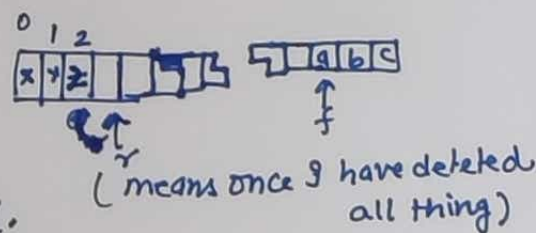
- * Case 1 :-
 - Insertion & Deletion is $O(1)$ time but created new problem.
 - Can't insert new element. even place(s) available at the start of array.

* Soln :- Allow the queue to "wrap around"
↓
use "circular array"

$$f = r \text{ } ??$$

→ means ⇒ Queue is empty }
sometimes :- Queue is full }

↓
Ambiguity whether
Q is empty or full.



Overcome the Ambiguity :-

One way :- Q can never hold " $n-1$ " elements., where n is the size of array.

Ans

$$\text{Size}(Q) \cdot (n - f + r)$$

$(n - r + f) \bmod n$ - correct for both the cases: normal array or circular array.

\Rightarrow When " $f = r$ ", Q will be empty.

ENQUEUE ~~IN~~ USING ARRAY IN CIRCULAR FASHION

Precondition:

queue is not full means.

$$(n - r + f) \bmod n \neq n - 1$$

or

$$\text{size}() \neq n - 1$$

Post condition:

$$r \leftarrow (r + 1) \bmod n$$

Enqueue(Q , item)

if $(n - r + f) \bmod n = n - 1$

return "Overflow cond"

else

$Q[r] \leftarrow \text{item}$

$r \leftarrow (r + 1) \bmod n$

Dequeue(Q)

If $f = r$

return "underflow cond"

else

temp $\leftarrow Q[f]$

$Q[f] \leftarrow \text{null}$

$f \leftarrow (f + 1) \bmod n$

return temp

Precondⁿ.

$f \neq r$

Post:- $f \leftarrow (f + 1) \bmod n$