



## SCHOOL OF ADVANCED SCIENCES

FALL Semester 2023-2024 Continuous Assessment Test – I

Programme Name & Branch : B.Tech.,

Slot: C1+TC1+TCC1

Course Name & code: Complex Variables and Linear Algebra & BMAT201L

Exam Duration: 90 Min. Maximum Marks: 50

## Answer all questions (5X10=50)

Show, by considering the function f(z) defined by  $f(z) = \frac{2xy(x+iy)}{x^2+y^2}$  for  $z \neq 0$  and

f(0) = 0, that the C-R equations are not the sufficient conditions for a function to be analytic.

Show that  $v(x, y) = x^3 - 3x^2y + 2x + 1 + y^3 - 3xy^2$  is a harmonic function and obtain an analytic function for which v(x, y) is the imaginary part. Also find the conjugate harmonic of v(x, y).

Find the Bilinear transformation which maps  $z_1 = -2i$ ,  $z_2 = i$ ,  $z_3 = \infty$  onto  $w_1 = 0$ ,  $w_2 = -3$ ,  $w_3 = \frac{1}{3}$  respectively. Also find

In the invariant points of the transformation.

jif the image of |z| < 1 in the w-plane.

4. Find the Laurent's series for the function  $f(z) = \frac{1}{(z+1)(z+2)^2}$  in the following regions:

|y|z-1|<2 |y|>2<|z-1|<3

5. a) Find the location and nature of singularity of  $f(z) = \frac{1 - e^z}{z^3}$ .

6) Using Cauchy integral formula, evaluate  $\int_C \frac{z+1}{z^3 - 2z^2} dz$ , where C is a circle |z-2-i| = 2.

(4M+6M)

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