

1st Semester B.Tech Mid Term Examination 2019-2020

ENGINEERING MATHEMATICS-1(18BS1T01)

Duration: 01:30

Full Marks: 25

1 Answer All

- a What is the curvature at any point on a circle with radius 5? 1
- b Find the asymptotes to the curve $xy^3 - x^2y + xy + 2x - y - 6 = 0$ which are parallel to the axes. 1
- c Solve $y' = \frac{\sqrt{y^2-1}}{x^2+25}$. 1
- d Solve $y' = e^x e^y$. 1
- e Find the integrating factor of $2xydx + 3x^2dy = 0$. 1

2 Answer any Two

- a Find the radius of curvature for the curve given parametrically by $x = 3t$ and $y = t^2 - 6$ at $t=1$ 2
- b Find all the asymptotes of $r = \frac{a\theta}{\theta-1}$. 2
- c Draw the graph of the function $y = 2x + [x - 1]^2$, $0 \leq x \leq 2$. 2
- d Find all the asymptotes of $x^3 - x^2y + y^2 = 0$. 2

3 Answer any Two

- a Solve the homogeneous equation $xy' - y = xy$. 2
- b Solve $xy' + 4y = 8x^4$ where $y(1) = 2$ 2
- c Solve the linear differential equation $\frac{dx}{dy} + \frac{x}{y} = y^2$. 2
- d Solve $(x + y)dy = dx - dy$ 2

4 Answer any Two

- a Find the radius of curvature of the curve $x = a \cos 3t$, $y = a \sin^3 t$ at $t = \frac{\pi}{4}$. 3
- b Find the ranges for the value of x for which $y = x^4 - 6x^3 + 12x^2 + 5x + 7$ is concave upward or downward. Also find the points of inflection. 3
- c Find all the asymptotes to the curve $(x + y)^2(x + 2y + 2) = x + 9y - 2$. 3
- d Find all asymptotes of the curve $(x + y)(x - y)(2x - y) - 4x(x - 2y) + 4x = 0$ 3

5 Answer any Two

- a Find the integrating factor of $2x \tan y dx + \sec^2 y dy = 0$ and solve it. 3
- b Solve $2xyy' + (x-1)y^2 = x^2e^x$ 3
- c Solve the Bernoulli's equation $y' + y/x = x^2y^2$. 3
- d Solve $\frac{dy}{dx} = \frac{x+2y+3}{2x+y+3}$ 3