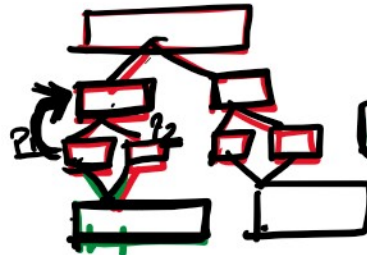


TC
36



Merge Sort

Recurrence relⁿ
↓
Substitution

Recursive Solⁿ



Use Cases

Divide-conquer } Class Problem }

Median } ⇒

arr1 :- 1 3 4 7 10 12 // Sorted

arr2 :- 2 3 6 15 // Sorted

1 2 3 3 4 6 7 10 12 15 ⇒ 10 elements

$\left(\frac{n}{2}\right) \Rightarrow$
 $n = 10$

$\left(\frac{10}{2}\right) \Rightarrow 5 + 6$

$\frac{n}{2} \Rightarrow 5 + 6$

$\frac{4+6}{2} \Rightarrow \frac{10}{2} \Rightarrow 5$

even?
Yes

odd 1 2 3 4 5
3

AP: 1

1. Merged two sorted arrays
2. Find out no. of elements.



$n = \text{no. of elem} = 10$

1 2 3 3 4 6 7 10 12 15
0 1 2 2 1 2 1 2 2 1

1 2 3 3 4 6 7 10 12 15
 0 1 2 3 4 5 6 7 8 9

$arr[n/2]$
 $arr[10/2] \Rightarrow arr[5] \Rightarrow 6$
 $arr[n/2+1]$
 $arr[n/2-1]$
 $5-1 \Rightarrow 4 \Rightarrow arr[4] = 4$

$\frac{6+4}{2}$
 $\frac{6+7}{2} \times \times$

```

if(n % 2 == 0){ //even
  med = (arr[n/2] + arr[(n/2)-1])/2;
}
else{
  med = arr[parseInt(n/2)]
}

```

new space

```

let arr = MergeTwoSortedArrays([1,3,4,7,10,12],[2,3,6,15]);
console.log(arr);

let med;
let n = arr.length;
if(n % 2 == 0){ //even
  med = (arr[n/2] + arr[(n/2)-1])/2;
}
else{
  med = arr[parseInt(n/2)]
}
console.log(`Median is ${med}`);

```

m n $m+n$
 $m < n$ $\times \times$

except variables

DS \Rightarrow array. \checkmark

Space complexity :- $O(m+n) \Rightarrow O(n)$

```

function MergeTwoSortedArrays(a1, a2){
    let res = [];
    let p1 = 0;
    let p2 = 0;
    let k = 0;

    while(p1 < a1.length && p2 < a2.length){
        if(a1[p1] < a2[p2]){
            res[k] = a1[p1];
            p1++;
            k++;
        }
        else{
            res[k] = a2[p2];
            p2++;
            k++;
        }
    }

    if(p1 === a1.length){
        while(p2 != a2.length){
            res[k] = a2[p2];
            k++;
            p2++;
        }
    }
    if(p2 === a2.length){
        while(p1 != a1.length){
            res[k] = a1[p1];
            k++;
            p1++;
        }
    }

    return res;
}

let arr = MergeTwoSortedArrays([1,3,4,7,10,12],[2,3,6,15]);
console.log(arr);

let med;
let n = arr.length;
if(n % 2 == 0){ //even
    med = (arr[n/2] + arr[(n/2)-1])/2;
}
else{
    med = arr[Math.floor(n/2)]
}
console.log(`Median is ${med}`);

```

TC:- $O(C)$?

SC:- $O(m+n)$ }
 $\rightarrow O(C)!!$

APP $\Rightarrow 2$

arr1:- 1 3 4 7 10 12 // Sorted

arr2:- 2 3 6 15 // Sorted

\rightarrow 1 2 3 3 4 | 6 7 10 12 15

arr1:- 1 3 4 7 10 12 // Sorted

arr2:- 2 3 6 15 // Sorted

① LH RH
 1 3 4 7 10 12
 2 3 6 15 } False Pick

② 1 3 4 7 10 12
 2 3 6 15

(2) 1 3 4 7 10 12
2 3 6 15

(3) 1 (3) 4 7 10 12 } false
2 3 (6) 15 } Pick

→ If my picked half is a valid one, then
7 has to be less than 3

7 < 3 \Rightarrow false.

→ In my 3rd obv,

3 < 15 \Rightarrow true. \hookrightarrow
6 < 4 \Rightarrow false. \hookrightarrow

(2) 1 3 4 7 10 12 }
2 3 6 15 } true

4 < 6 \Rightarrow true. } Perfect
88. 3 < 7 \Rightarrow true. } Pick

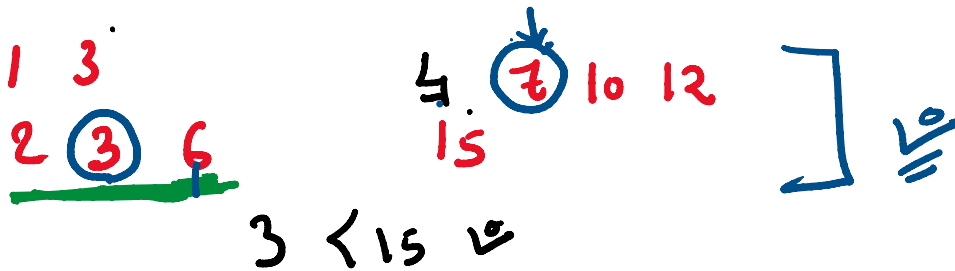
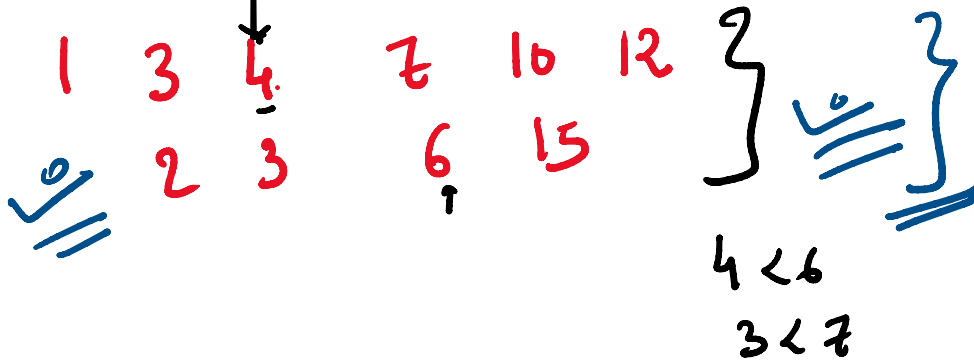
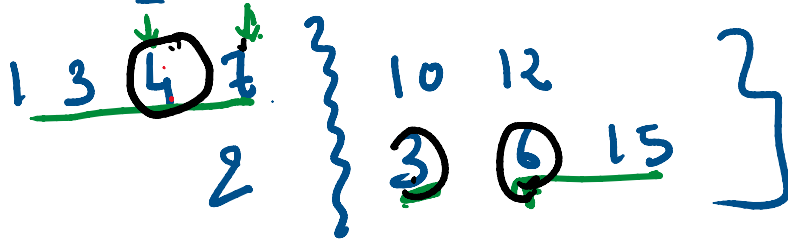
l_1, l_2, r_1, r_2

$$\frac{(\max(l_1, l_2) + \min(r_1, r_2))}{2}$$

$$\begin{cases} l_1 \leq r_2 \\ l_2 \leq r_1 \end{cases}$$

arr1: 1 3 4 7 10 12

arr2: 2 3 6 15



arr1:-



no. to

arr2:-



low \Rightarrow 0 high \Rightarrow 4

Cut:- $\frac{\text{low} + \text{high}}{2} \Rightarrow \frac{0 + 4}{2} \Rightarrow 2$

$$l_1 = 12 \rightarrow r_1 = 14$$

$$l_2 = 3 \rightarrow r_2 = 4$$

$$12 \leq 4 \quad \underline{\underline{\text{false}}}$$

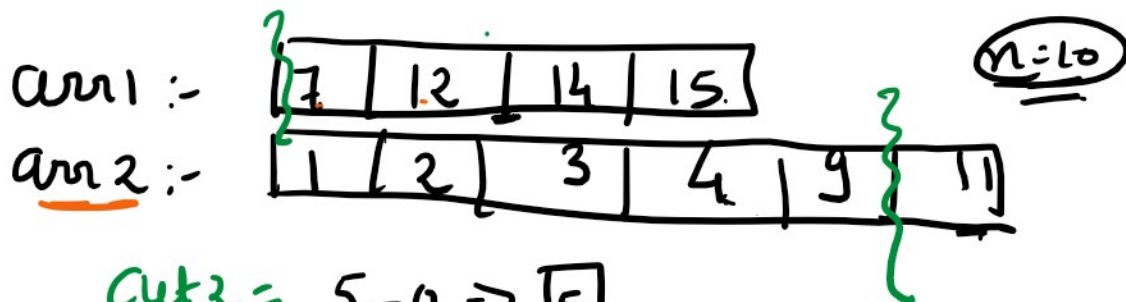
Not a valid partition

$$\downarrow \underline{12} \leq 4 \uparrow$$

$$\text{high} = \text{mid} - 1$$

$$\underline{\text{low}} \Rightarrow 0 \quad \underline{\text{high}} \Rightarrow 2 - 1 = 1$$

$$\underline{\text{cut1}} \Rightarrow \frac{\text{low} + \text{high}}{2} \Rightarrow \frac{0 + 1}{2} \Rightarrow \underline{0}$$



$$\text{cut2} = 5 - 0 \Rightarrow \underline{\underline{5}}$$

$$= \frac{n - \text{cut1}}{2}$$

X

$$\begin{array}{cccccc} 1 & 2 & 3 & 4 & 9 & 11 \end{array} \quad \begin{array}{c} \Downarrow \\ 12 \quad 14 \quad 15 \end{array}$$

$$l_1 = 1 \quad r_1 = 2$$

$$l_2 = 9 \quad r_2 = 11$$

$$1 < 11 \quad \checkmark$$

$$\underline{9} < 2 \quad \times \times$$

11

rn

$$\downarrow \downarrow \underline{9} < = \underline{7} \uparrow \uparrow$$

$$\text{low} = \text{mid} + 1 \Rightarrow 0 + 1 = \textcircled{1}$$

arr1 :-

7	12	14	15
---	----	----	----

 }

arr2 :-

1	2	3	4	9	11
---	---	---	---	---	----

 }

$$\text{low} \Rightarrow \text{mid} + 1 \Rightarrow 0 + 1 = 1$$

$$\text{high} \Rightarrow 1$$

$$\text{mid} \Rightarrow \frac{\text{low} + \text{high}}{2} \Rightarrow \frac{1 + 1}{2} = \textcircled{1}$$

arr1 :-

7	12	14	15
---	----	----	----

arr2 :-

1	2	3	4	9	11
---	---	---	---	---	----

$$\text{cut2} = 5 - 1 \Rightarrow \underline{4} \quad l_1 = \text{cut1} - 1$$

$$\begin{matrix} l_1 \\ \underline{7} \end{matrix} \}$$

$$1 \quad 2 \quad 3$$

$$\begin{matrix} l_2 \\ \underline{4} \end{matrix} \}$$

$$r_1$$

$$\underline{12}$$

$$14$$

$$15$$

$$\underline{9}$$

$$r_2$$

$$11$$

$$\begin{matrix} 7 < = 9 \\ 4 < = 12 \end{matrix} \quad \checkmark \quad \checkmark \quad \underline{\underline{\text{true}}}$$

$$\boxed{(\max(l_1, l_2) + \min(r_1, r_2))}$$

$$\left\{ \frac{(\max(l_1, l_2) + \min(r_1, r_2))}{2} \right\}$$

$$\frac{7 + 9}{2} \Rightarrow \frac{16}{2} = 8$$

$$l_1 = arr1[cut1-1]$$

$$l_2 = arr2[cut2-1]$$

$$r_1 = arr1[cut1]$$

$$r_2 = arr2[cut2]$$

$$cut1 = (low + high) / 2$$

$$cut2 = \frac{(n_1 + n_2)}{2} - cut1$$

1 2 3 4 7 9 11 12 14 15 16

$n_1 + n_2$

$2n \Rightarrow 11$

$n_1 \Rightarrow 8$

$n_2 \Rightarrow 5$

$$\Rightarrow \frac{(n_1 + n_2 + 1)}{2} \Rightarrow \frac{12}{2} = 6$$

$\max(l_1, l_2)$


```

function findMedianSortedArrays(nums1, nums2) {
    if(nums2.length < nums1.length){
        return findMedianSortedArrays(nums2,nums1)
    }

    let n1 = nums1.length;
    let n2 = nums2.length;
    let low = 0, high = n1;

    while(low<=high){
        let cut1 = (low+high) >> 1;
        let cut2 = parseInt((n1+n2+1)/2)-cut1;

        let left1 = cut1 == 0 ? Number.MIN_VALUE : nums1[cut1-1];
        let left2 = cut2 == 0 ? Number.MIN_VALUE : nums2[cut2-1];

        let right1 = cut1 == n1 ? Number.MAX_VALUE : nums1[cut1];
        let right2 = cut2 == n2 ? Number.MAX_VALUE : nums2[cut2];

        if(left1 <= right2 && left2 <= right1){
            if((n1+n2) % 2 == 0){
                return parseInt((Math.max(left1,left2) + Math.min(right1,right2))/2);
            }
            else{
                return Math.max(left1,left2);
            }
        }
        else if(left1 > right2){
            high = cut1 - 1;
        }
        else{
            low = cut1 + 1;
        }
    }
}

```

$$\frac{\max(l_1, l_2) + \min(r_1, r_2)}{2}$$

$$\frac{7 + 9}{2} \Rightarrow 16 \Rightarrow 8$$

$$l_1 = \text{arr1}[\text{cut1}-1]$$

$$l_2 = \text{arr2}[\text{cut2}-1]$$

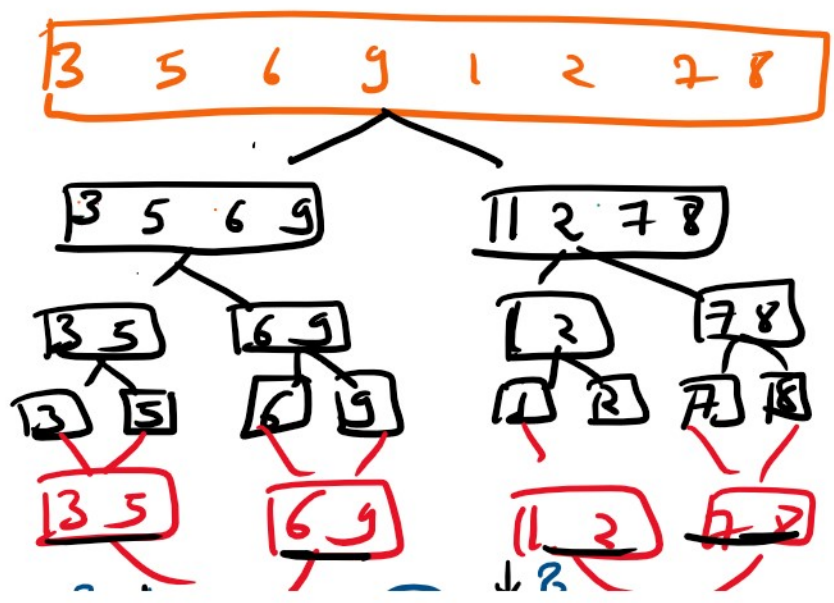
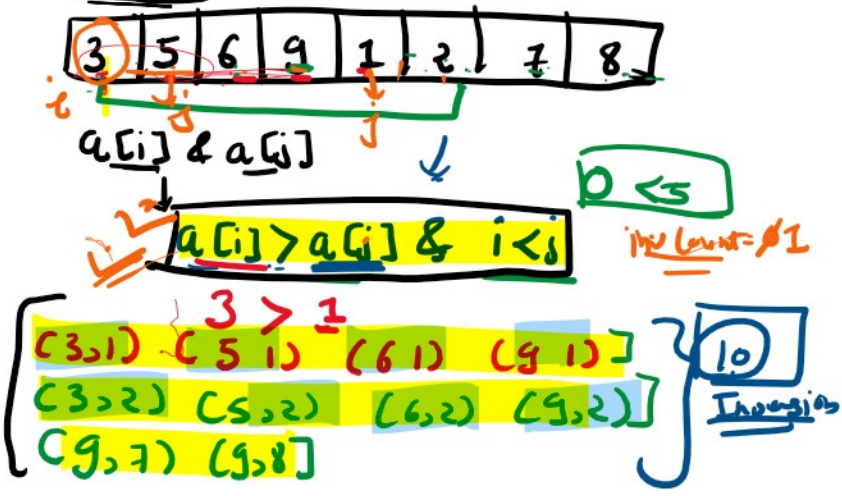
$$r_1 = \text{arr1}[\text{cut1}]$$

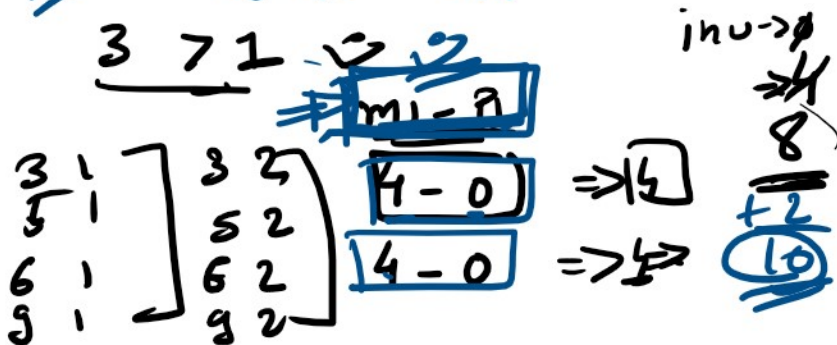
$$r_2 = \text{arr2}[\text{cut2}]$$

$$\text{cut1} = \frac{\text{low} + \text{high}}{2}$$

$$\text{cut2} = \frac{(n_1 + n_2) - \text{cut1}}{2}$$

Q Inversion

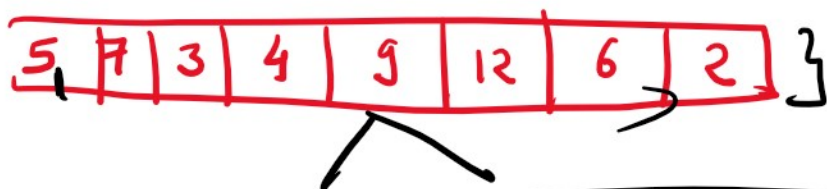
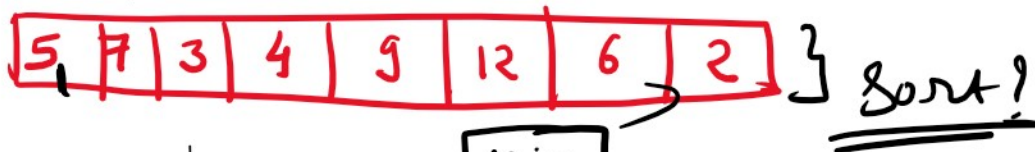


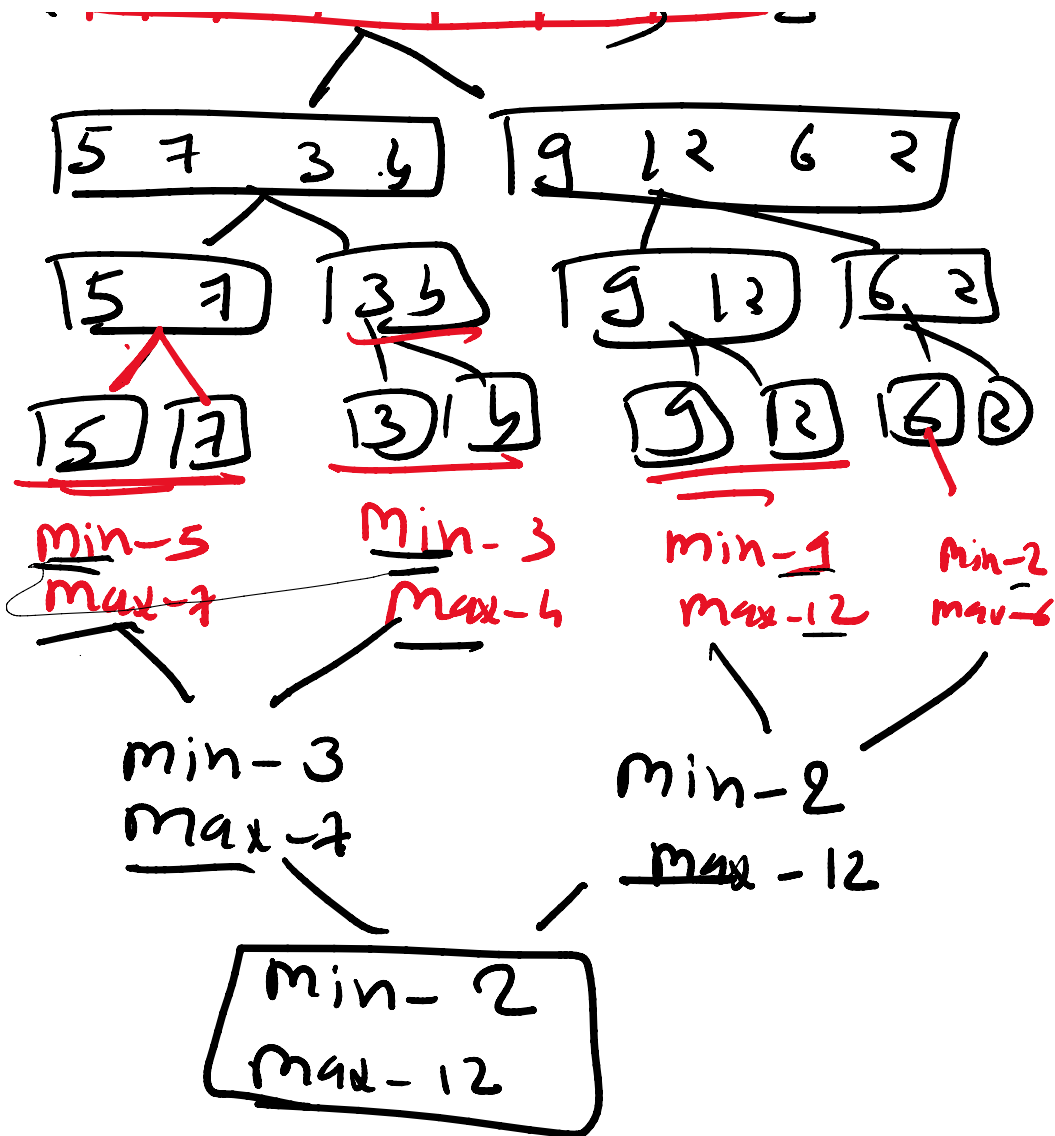


$a[i] > a[j] \& i < j$ \Rightarrow Single ino

$a[i] > 2 * a[j] \& i < j$

double ino





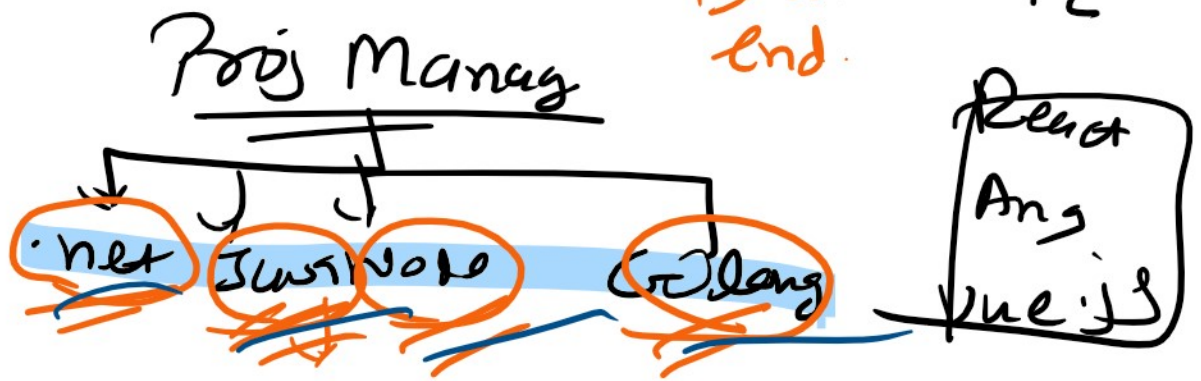
- ① Median → Hard LeetCode
 - ② Inversion
 - ③ Double inversion
 - ④ Min-Max.
- 9 AM

Quick sort - 1
Quick sort - 2

Golang → Google

Node JS

Backend FE



Person icon →

Javascript

logic

✓

Node.js

~~React.js~~

Call api

Hello

Eng kind?