

A

B

PTB

Space \Rightarrow Space Comp \times
Time \Rightarrow time comp. \checkmark

1. Read Prob.

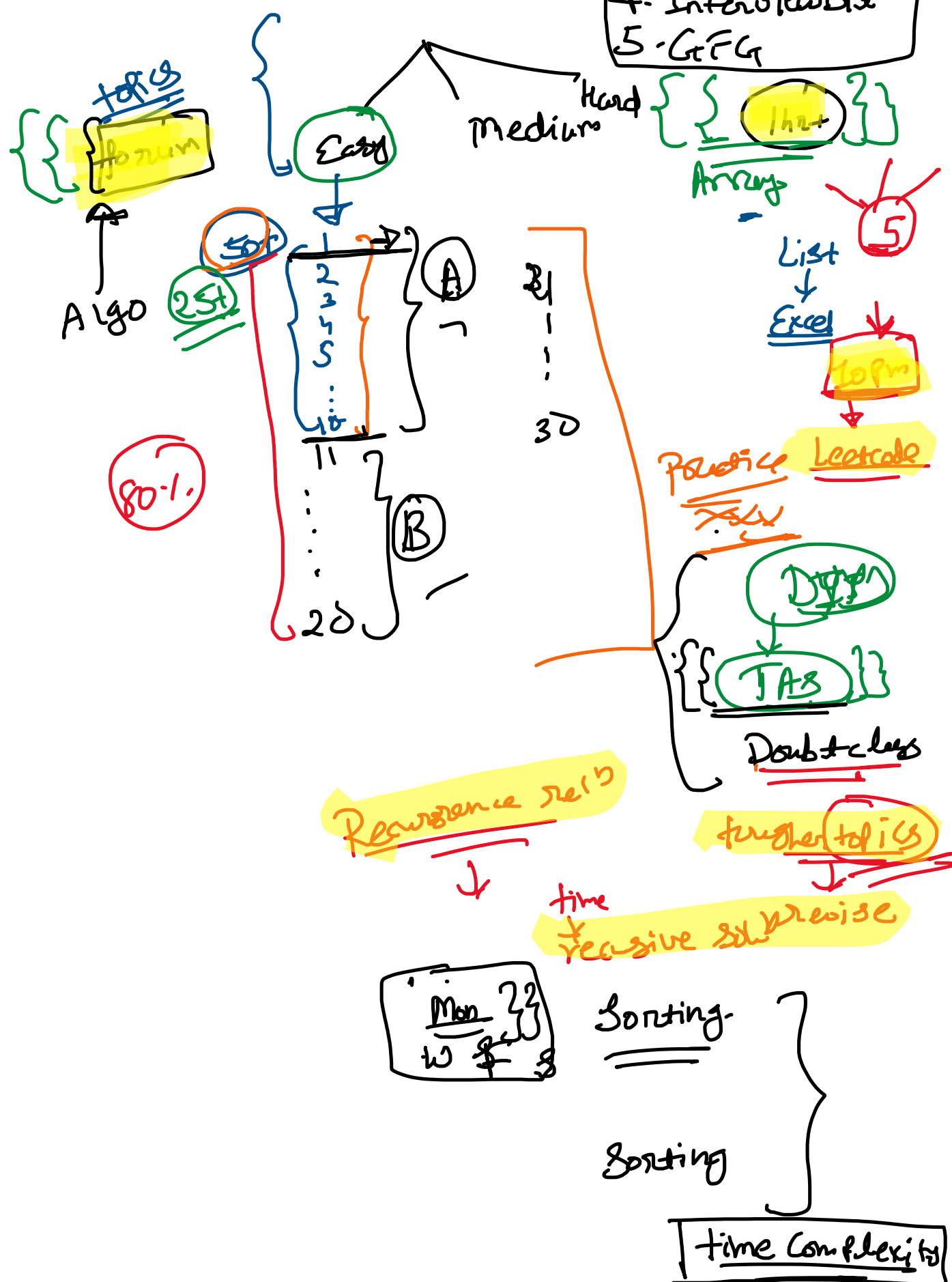
2. Choose algo./logic /process. 80%

3. Implement algo. 10%

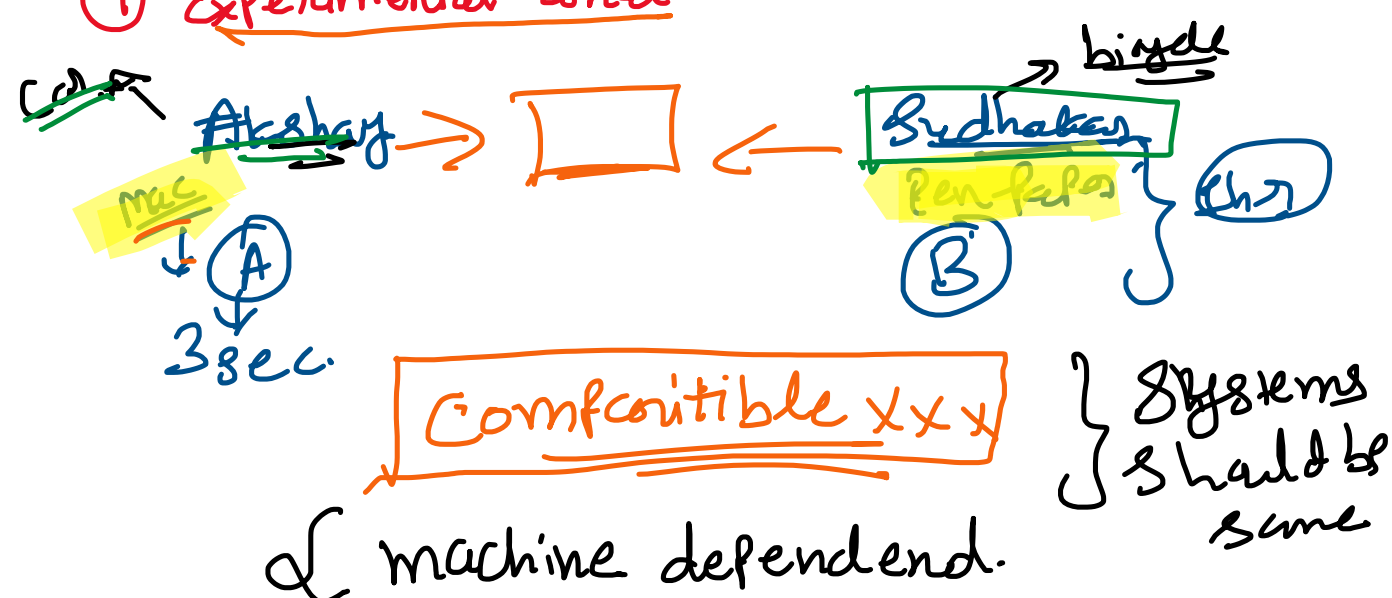
Practice.

- 1. leetcod
- 2. hackerrank
- 3. ...

1. LeetCode
2. Hackerrank
3. Hacker earth
4. InterviewBit
5. GFG



① Experimental anal.



F₁ generation \rightarrow 1st cross

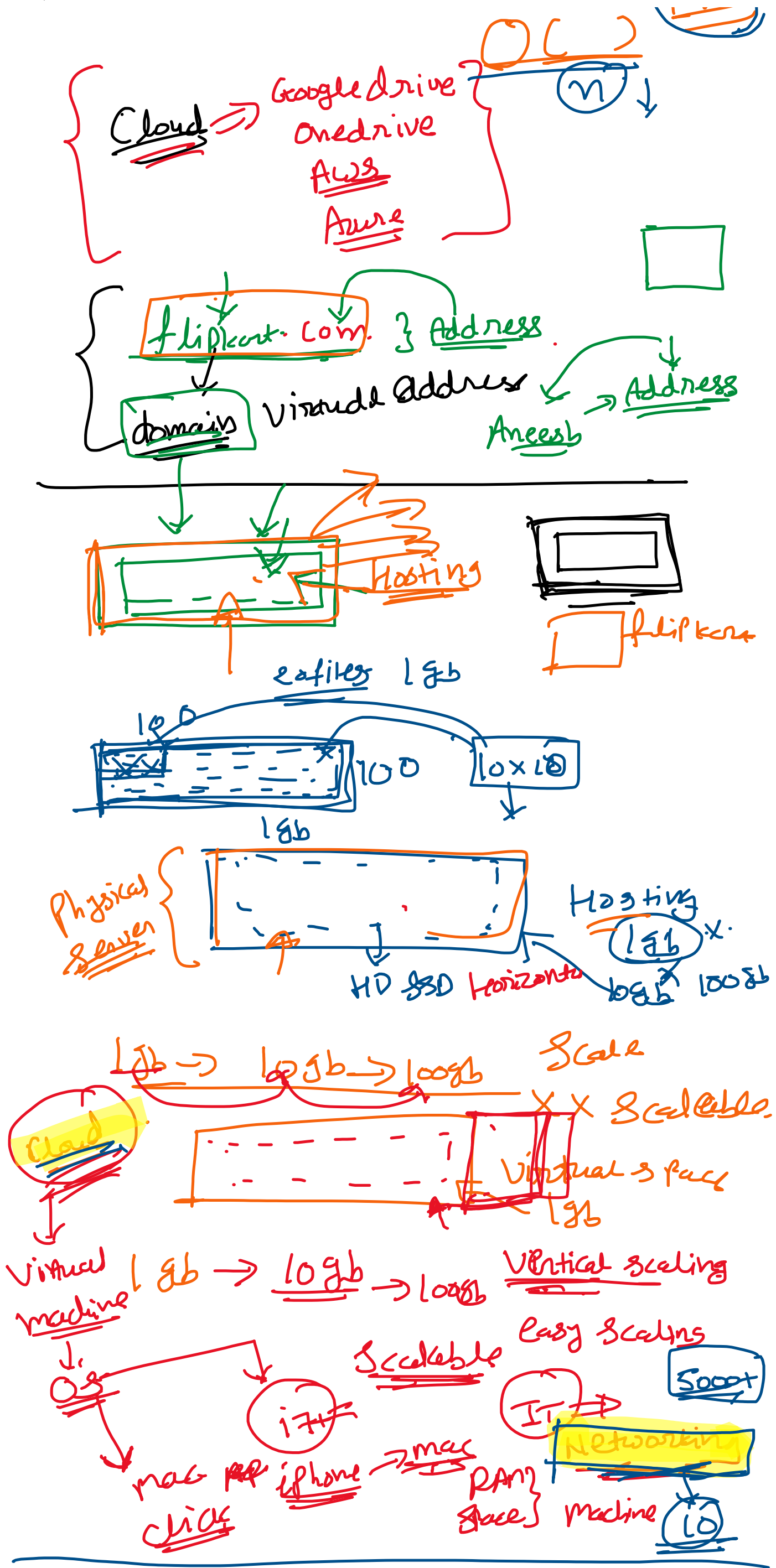
$\left. \begin{array}{l} \text{LOAD} \\ \text{INT} \end{array} \right\}$

2. Asymptotic analysis.

d machine x

d no. of
Computes
Steps

Pen
Paper



Sudhakar
Alg1
 no. of CS

Sudhanshu
Alg2.
 no. of CS

Analyze max

$n=5 \rightarrow 5$
 $n=10 \rightarrow 50$
 $n=100 \rightarrow 1000$

- 1. Best (Ω)
- 2. Avg (Θ)
- 3. Worst (O)

IP: 010100111 } ⇒ Best (1)
 OR 00061111 } ⇒ Worst (0)

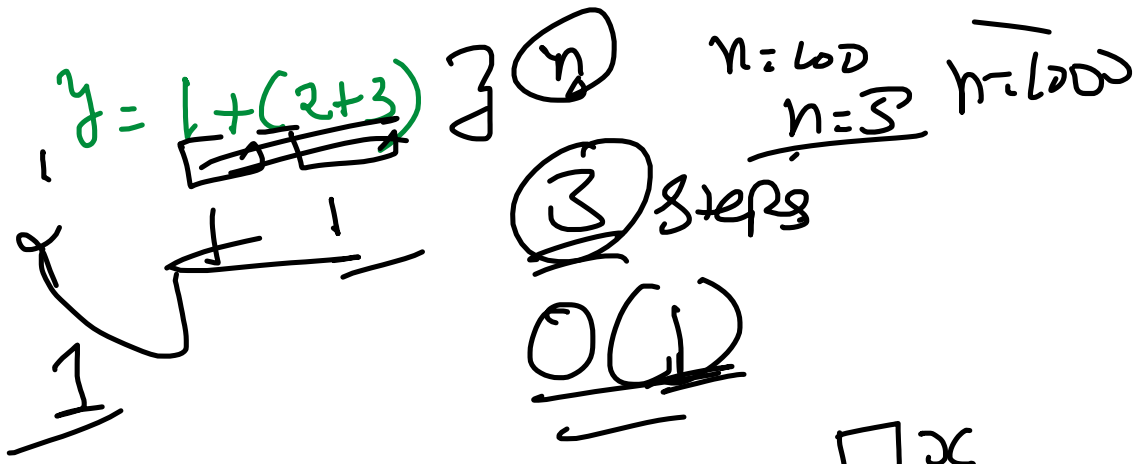
IP: 000011111 } ⇒ Worst (0)

1. 11111 0000

Aug.

100001101

Rules:-



1. Ignore const.
2. Statements \Rightarrow Sequential } + $\square x$
 $\square y$
 \downarrow
 $x + y$
3. Nested $x \{ \square y \} \Rightarrow \underline{x \cdot y}$ $\underline{x + y}$
4. Ignorable. \downarrow $n^2 + n$ \uparrow

\Rightarrow lower

$n = 3$

9

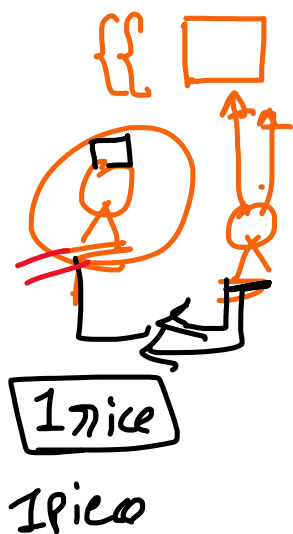
$3 \times 2 \times 1$
 6

$n = 10$

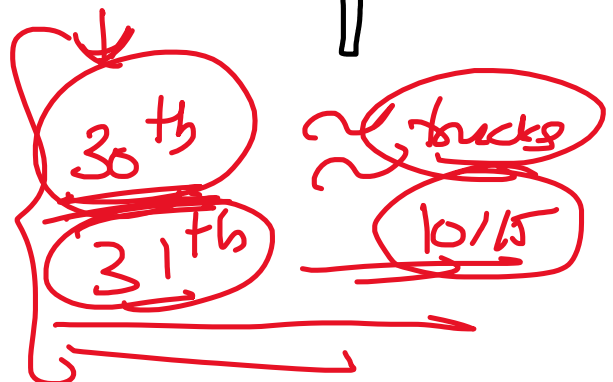
$1000 +$

$10 \times 9 \times 8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1$

	0	1	2	3	4
0	1	1	1	1	1
1	32	64	128	256	512
2	64	-	-	-	-
3	-	-	-	-	-
4	-	-	-	-	-



Compounding



```

a = 0  b = 0
for(i = 0; i < n; i++)
{
    a = a + rand();
}
for(j = 0; j < m; j++)
{
    b = b + rand();
}

```

1. $TC \Rightarrow O(N \times m)$
 $SC \Rightarrow O(1)$
2. $TC \Rightarrow O(m)$
 $SC \Rightarrow O(1)$
3. $TC \Rightarrow O(N + m)$
 $SC \Rightarrow O(N + m)$
4. $TC \Rightarrow O(N \times m)$
 $SC \Rightarrow O(1)$

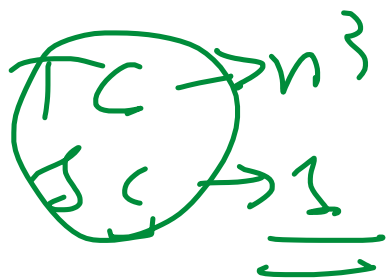
no. of f^n calls

\hookrightarrow call stack
 space comp

```

for(i = 0; i < n; i++)
{
    for(j = n; j > 1; j++)
    {
        a = a + i + j;
    }
}

```



$$\begin{aligned} &\text{let } i, j, k = 0 \\ &\text{for } (j = n/2; i < n; j++) \\ &\quad \text{for } (k = 2; j < n; j = j * 2) \{ \\ &\quad \quad k = k + n/2; \\ &\quad \} \end{aligned}$$

$n/2 \times \log n$
 $n \times \frac{1}{2} \times \log n$
 $n \log n$

$$\begin{matrix} T_C \\ S_C \end{matrix}$$

$$\begin{matrix} \downarrow & \uparrow \\ \text{Generalize} \end{matrix}$$

$SC \Rightarrow 1$

$\log 16 \Rightarrow 4$

$n = 16 \Rightarrow j = 8 \Rightarrow j \Rightarrow 2, 4, 8, 16$
 $n = 32 \Rightarrow j = 2, 4, 8, 16, 32$
 $\log 32 \Rightarrow 5$
 $\log 36 \Rightarrow 6$

$$\begin{aligned} &\text{for } (j = n/2; i < n; j++) \\ &\{ \\ &\quad \text{for } (k = 2; j < n; j = j * 2) \{ \\ &\quad \quad k = k + n/2; \\ &\quad \} \\ &\} \end{aligned}$$

$n = 8 \Rightarrow j = 2, 4, 8, 16$

$a = 0; i = n$

$\text{while } (i > 0) \{$

$a = a + i;$

$i = i / 2;$

$\}$

$a \cdot O(n)$

$b \cdot O(\log n)$

$c \cdot O(n/2)$

$d \cdot O(\log n)$

$n = 16 \Rightarrow i = 16 / 8 / 4 / 2 / 1$

$$\begin{matrix} 0.5 \\ 1/4 & 1/8 & 1/16 \end{matrix}$$

1. Substitution method

2. Master th²

3. Recursion tree

a

$$T(n) = \begin{cases} 1, & \text{if } n = 1 \\ n + T(n-1) & \text{if } n \geq 1 \end{cases}$$

$T(1) = 1$

$T(n) = n + T(n-1)$

$T(n) = n + T(n-1) - 1$

$T(n) = (n-1) + T(n-1-1)$

$$T(n-1) = (n-1) + T(n-2)$$

$$T(n-2) = (n-2) + T(n-3)$$

$$T(n-3) = (n-3) + T(n-4)$$

→ Put (2) \Rightarrow (1)

$$T(n) = n + (n-1) + T(n-2)$$

$$T(n) = n + (n-1) + T(n-2) \quad (4)$$

→ Put (3) \Rightarrow (4)

$$T(n) = n + (n-1) + (n-2) + T(n-3)$$

$$= n + (n-1) + (n-2) + \dots + T(n-(n-1))$$

$$n \times (n-1) \times (n-2) \dots T(1)$$

$$n \times (n-1) \times (n-2) \times \dots \times 1$$

$$n \times \frac{n}{2} \times \frac{n}{4} \times \dots \times \frac{n}{2^{k-1}}$$

$$2 \times 2 \times 2 \times 2$$

$$2^k$$

$$\dots \times \frac{n}{2^{k-1}} \times \frac{n}{2^{k-2}} \times \dots \times \frac{n}{2}$$

$$\boxed{n^k} \Rightarrow \underline{n!}$$

$$Q. T(n) = \begin{cases} 1, & n=1 \\ 2T\left(\frac{n}{2}\right) + n, & \text{otherwise} \end{cases} \quad T(1) = 1$$

$$T(n) = 2T\left(\frac{n}{2}\right) + n \quad (1)$$

$$T\left(\frac{n}{2}\right) = 2T\left(\frac{n}{4}\right) + \frac{n}{2}$$

$$T\left(\frac{n}{4}\right) = 2T\left(\frac{n}{8}\right) + \frac{n}{4} \quad (2)$$

$$T\left(\frac{n}{8}\right) = 2T\left(\frac{n}{16}\right) + \frac{n}{8} \quad (3)$$

$$2 \times \frac{n}{2}$$

$$\begin{aligned}
 T(n) &= \underline{2} \left[\underline{2T\left(\frac{n}{2}\right) + \underline{n}} \right] + \underline{n} \\
 &= 2^2 T\left(\frac{n}{2^2}\right) + \underline{n} + \underline{n} \\
 &= 2^2 T\left(\frac{n}{2^2}\right) + \underline{2n} \\
 &= 2^2 \left[2T\left(\frac{n}{4}\right) + \underline{\frac{n}{2}} \right] + 2n \\
 &= 2^3 T\left(\frac{n}{2^3}\right) + \underline{n} + 2n \\
 &= 2^3 T\left(\frac{n}{2^3}\right) + \underline{3n} \\
 &= 2^4 T\left(\frac{n}{2^4}\right) + \underline{4n} \\
 &= \underline{2^5 T\left(\frac{n}{2^5}\right) + \underline{5n}}
 \end{aligned}$$

$$2^k T\left(\frac{n}{2^k}\right) + \underline{kn}$$

$$T(1) = 1$$

$$\begin{aligned}
 \frac{n}{2^k} &= 1 \\
 \underline{n} &= \underline{2^k}
 \end{aligned}$$

$$\log_a b \Rightarrow b \log_a a$$

$$\log_a a \Rightarrow 1$$

$$\log n = \underline{\log 2^k}$$

$$\log n = k \log 2$$

$$\underline{\log n = k}$$

$$2^k T(1) + kn$$

$$2^k + kn$$

$$n + kn$$

$$n + \log n \times n$$

$$\textcircled{n} + \underline{n \log n}$$

$$\approx O(n \log n)$$

$$T(n) = \begin{cases} 1, & n=1 \\ T(n-1) + \log n, & n \geq 1 \end{cases}$$

$$T(n) = T(n-1) + \log n \quad \text{--- (1)}$$

$$T(n-1) = T(n-2) + \log(n-1) \quad \text{--- (2)}$$

$$T(n-2) = T(n-3) + \log(n-2) \quad \text{--- (3)}$$

$$T(n) = T(n-2) + \log(n-1) + \log n$$

$$T(n) = T(n-3) + \log(n-2) + \log(n-1) + \log n$$

$$= T(n-4) + \log(n-3) + \log(n-2) + \log(n-1) + \log n$$

$$= T(n-k) + \log(n-(k-1)) + \log(n-(k-2)) + \log(n-(k-3)) + \log n$$

$$T(1) = 1$$

$$n-k = 1$$

$$k = n-1$$

$$= T(n - (n-1)) + \log(n - (n-1-1)) + \log(n - (n-1-2)) + \log(n - (n-1-3)) + \log n$$

$$= T(1) + \log 2 + \log 3 + \log 4 + \dots + \log n$$

$$= 1 + \log 2 + \log 3 + \log 4 + \dots + \log n$$

$$= 1 + \log(2 \times 3 \times 4 \times 5 \times \dots \times n) \quad \text{--- (5)}$$

$$= 1 + \log(1 \times 2 \times 3 \times 4 \times 5 \times \dots \times n)$$

$$= 1 + \log(n!)$$

$$- 1 + \log(n!)$$
$$n \times (n-1) \times (n-2) \times \dots \times 1$$

$$\underbrace{n \times n \times n \times n \times \dots \times n}_n$$

$$= 1 + \log(n^n)$$

$$= 1 + n \log n$$

$$\boxed{\approx O(n \log n)}$$