# Wind Farm Layout Optimization Case Studies

IEA Task 37 on System Engineering in Wind Energy

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## 1 Introduction

Two major factors that affect wind farm layout optimization are 1) the optimization approach and 2) the wake model. This document defines two case studies designed to study these factors. One may elect to participate in either or both cases.

- 1. Optimization-Only Case Study: user chooses optimization approach, wake model is fixed and supplied.
- 2. Combined Case Study: user is free to choose both optimization approach and wake model.

Participants will optimize turbine locations to maximize annual energy production, submit solutions, and provide details on their methodology. After all submissions are received, participants will be expected to perform a cross comparison of other participant solutions. Data will be consolidated, processed, and made available to all participants.

#### 2 Problem Definition

#### Objective

The objective of each scenario is to maximize annual energy production, which we define simply as the expected value of aerodynamic power. The wind resource for each case has a wind rose binned into 16 discrete directions, with a constant wind speed. In other words:

$$AEP = \left(\sum_{i=1}^{16} f_i P_i\right) 8760 \frac{\text{hrs}}{\text{yr}}$$

where  $P_i$  is the power produced for wind direction i, and  $f_i$  is the corresponding wind direction probability.

#### **Design Variables**

The design variables are the (x, y) locations of each turbine. All locations in this document refer to the hub location. Every turbine in the farm is identical.

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#### Constraints

Each scenario has a fixed circular boundary centered at (0,0). All turbine (x,y) locations must remain on or within this boundary. No turbine can be closer than two rotor diameters to any other turbine.

#### **Parameters**

The wind turbine is the IEA37 3.35 MW onshore reference turbine [1] with the following characteristics:

Rotor Diameter	130	m
Turbine Rating	3.35	MW
Cut-In Wind Speed	4	m/s
Rated Wind Speed	9.8	m/s
Cut-Out Wind Speed	25	m/s

The power curve is defined as:

$$P(V) = \begin{cases} 0 & V < V_{cut-in} \\ P_{rated} \left( \frac{V - V_{cut-in}}{V_{rated} - V_{cut-in}} \right)^{3} & V_{cut-in} \leq V \leq V_{rated} \\ P_{rated} & V > V_{rated} \end{cases}$$

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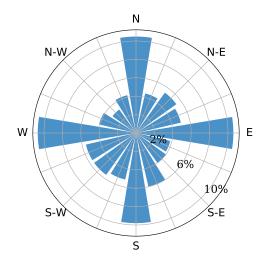
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The wind rose is defined by 16 discrete bins tabulated in iea37-bothcs-windrose.yaml and depicted pictorially below.



## 2.1 Optimization Only

This problem defines three different wind farm sizes, and corresponding number of turbines, meant to test scalability of the optimization approach. These three scenarios are:

- 1. 16 turbines, boundary radius of 1,300 m.
- 2. 36 turbines, boundary radius of 2,000 m.
- 3. 64 turbines, boundary radius of 3,000 m.

The user is only free to choose the optimization approach. The wake model for this study is fixed and is a version of Bastankhah's Gaussian wake model [2, 3, 4]. A Python implementation is supplied for convenience (iea37-optocs-aepcalc.py). Alterations to the implementation are permitted, as long as the governing physics equations are not altered. Participants may use other programming languages, but must use the same physics equations. To aid with this, the relevant equations are defined in a separate document (iea37-bothcs-wakemodel.pdf), and example layouts with corresponding AEP values are provided in iea37-optocs-exampleXX.yaml to verify implementations. The example designs are only for verification, and do not need to be used as starting points in your optimization.

#### 2.2 Combined

This problem defines one scenario where the user is free to choose both the optimization algorithm and the wake model. The wind farm contains nine turbines with a boundary radius of 900 m. If needed by the wake model, the turbulence intensity is 0.075, and the wind shear is a power-law with a shear exponent of 0.15 using the hub height as the reference height.

## 3 Reporting and Evaluation

Participants will submit:

- 1. Optimal turbine placement solution for each scenario using the format in the example .yaml files.
- 2. A survey describing your methodology and simulation environment here.

## 3.1 Optimization Only

Results will be compared by running iea37-optocs-aepcalc.py using the submitted .yaml file from each participant. Submissions must adhere to the format in order to receive a ranking. While other implementations may be used in the optimization, all evaluations will be done with the provided iea37-optocs-aepcalc.py code, so it is essential that you check that your implementation is consistent.

## 3.2 Combined

Because the wake models differ in this case, determining a "best" solution is generally not possible. Comparisons will be made using two approaches:

- 1. Every participant will evaluate every other participant's solutions using their own wake models. It is essential that the .yaml format is adhered to so that cross-comparisons are painless. If the optimizations behave as expected, each participant's wake model will judge their own solution as best, but it is possible a solution is found that other wake models agree is better.
- 2. Each solution will be compared using a higher-fidelity simulation, in this case large-eddy simulations (LES) using SOWFA. This introduces its own modeling assumptions and is an imperfect way to compare, but does provide another piece of information on relative performance between solutions. It is expected that solutions with minor LES performance differences would lie within the error of the methodology, and thus only major differences will be used in drawing conclusions on relative performance.

## 4 Enclosures

Files included with this document, needed for full participation in the Case Studies are:

- iea37-bothcs-windrose.yaml binned wind frequency in .yaml format
- iea37-optocs-aepcalc.py Python coding of AEP wake model for Optimization Only Case Study
- iea37-optocs-wakemodel.pdf description of AEP wake model for Optimization Only Case Study
- iea37-optocs-example16.yaml 16 turbine scenario example layout
- iea37-optocs-example36.yaml 36 turbine scenario example layout
- iea37-optocs-example64.yaml 64 turbine scenario example layout

# References

- [1] Bortolotti, P., Dykes, K., Merz, K., Sethuraman, L., and Zahle, F., "IEA Wind Task 37 on System Engineering in Wind Energy, WP2 Reference Wind Turbines," Tech. rep., National Renewable Energy Laboratory (NREL), Golden, CO., May 2018.
- [2] Thomas, J. J. and Ning, A., "A method for reducing multi-modality in the wind farm layout optimization problem," *Journal of Physics: Conference Series*, The Science of Making Torque from Wind, Milano, Italy, June 2018.
- [3] Bastankhah, M. and Porté-Agel, F., "A new analytical model for wind-turbine wakes," Renewable Energy, January 2014.
- [4] Bastankhah, M. and Porté-Agel, F., "Experimental and theoretical study of wind turbine wakes in yawed conditions," *J. Fluid Mech.*, Vol. 806, 2016, pp. 506–541.