```
In [26]:
         import numpy as np
         import cv2
         import matplotlib.pyplot as plt
In [27]: def compute_integral_image(image):
             Compute the integral image (summed area table) of the input image.
             height, width = image.shape
             integral_image = np.zeros((height, width), dtype=np.int32)
             for y in range(height):
                 for x in range(width):
                     integral_image[y, x] = image[y, x]
                     if y > 0:
                         integral_image[y, x] += integral_image[y - 1, x]
                     if x > 0:
                         integral_image[y, x] += integral_image[y, x - 1]
                     if y > 0 and x > 0:
                         integral_image[y, x] -= integral_image[y - 1, x - 1]
             return integral_image
In [33]: def sum_region(integral_img, top_left_corner, bottom_right_corner):
             Compute the sum of the region in the integral image defined by the top-left
             start_col, start_row = top_left_corner # Top-left corner (start_col, start_
             end_col, end_row = bottom_right_corner # Bottom-right corner (end_col, end_
             # Integral image formula to compute the sum of the rectangle
             region_sum = integral_img[end_row, end_col]
             if start row > 0:
                 region_sum -= integral_img[start_row - 1, end_col]
             if start_col > 0:
                 region_sum -= integral_img[end_row, start_col - 1]
             if start_row > 0 and start_col > 0:
                 region sum += integral img[start row - 1, start col - 1]
             return region sum
In [35]: def apply_custom_filter(integral_img, filter_kernels):
             Apply a custom filter to the integral image using predefined filter kernels.
             filtered_img = np.zeros((integral_img.shape[0] - 3, integral_img.shape[1] -
             # Slide the 4x4 filter over the image
             for row in range(filtered_img.shape[0]):
                 for col in range(filtered_img.shape[1]):
                     # Sum of the 4x4 region
                     filter_sum = sum_region(integral_img, (col, row), (col + 3, row + 3)
                     for kernel in filter kernels:
                         kernel = np.array(kernel)
                         filter_sum -= 2 * sum_region(integral_img, (col + kernel[0, 0],
```

```
filtered_img[row, col] = filter_sum
return filtered_img
```

```
In [37]: # Load a grayscale image
         img_path = "hw2_iitk.png" # Replace with your image path
         img = cv2.imread(img_path, cv2.IMREAD_GRAYSCALE)
         # Compute the integral image
         integral_img = compute_integral_image(img)
          \text{orig\_kernels} = [[[-1,-1,1,1],[-1,-1,1],[1,1,-1,-1],[1,1,-1,-1]],[[-1,-1,-1,-1]] \\
                  [[1,1,-1,-1],[1,1,-1,-1],[-1,-1,1],[-1,-1,1,1]],[[-1,-1,-1,-1],[-1,-1]
         filter_kernels = [
             [[[0,0],[1,1]],[[2,2],[3,3]]],
             [[[0,0],[1,3]]],
             [[[0,0],[3,1]]],
             [[[0,2],[1,3]],[[2,0],[3,1]]],
             [[[0,0],[3,1]],[[0,2],[1,3]]],
             [[[1,1],[3,3]]]
         1
         filter_labels = ["Filter 1", "Filter 2", "Filter 3", "Filter 4", "Filter 5", "Fi
         filtered_imgs = [apply_custom_filter(integral_img, f) for f in filter_kernels]
         # Plot the filtered images in a 2x3 grid
         fig, axes = plt.subplots(2, 3, figsize=(15, 10))
         for i, ax in enumerate(axes.flat):
             ax.imshow(filtered_imgs[i], cmap='gray')
             ax.set_title(filter_labels[i])
             ax.axis("off")
         plt.tight_layout()
         plt.show()
```



