article amsmath $\,$ To prove that the function is defined and integrable on I, observe that

$$\frac{1}{1+x^2}$$
 iscontinuouson R

so that f is continuous on I.

Since f is continuous on I, it is integrable on I.