

Homework

1.1 Propositional Logic

2) Which of these are propositions?

What are the truth values of those that are propositions?

Ans: Propositions must have clearly defined truth values, so a proposition must be a declarative sentence with no free variables.

a) Do not pass go.

⇒ This is not a proposition; it's a command.

b) What time is it?

⇒ This is not a proposition; it's a question.

c) There are no black flies in Maine.

⇒ This is a proposition that is false

d) $4 + x = 5$

⇒ This is not a proposition; its truth value depends on the value of x

e) The moon is made of green cheese.

\Rightarrow This is a proposition that is false.

f) $2^n \geq 100$

\Rightarrow This is not a proposition, its truth value depends on the value of n

Ans No: 13

Let, p and q be propositions

p : It is below freezing.

q : It's snowing

Write these propositions using p and q and logical connectives (including negations).

① It is below freezing and snowing.

$\Rightarrow p \wedge q$

② It is below freezing but not snowing

$\Rightarrow p \wedge \neg q$

③ It is not below freezing and it is not snowing.

$\Rightarrow \neg p \wedge \neg q$

d) It's either snowing or below freezing
(or both)

$$\Rightarrow p \vee q$$

then

e) If it is below freezing, it is also snowing.

$$\Rightarrow p \rightarrow q$$

f) Either it is below freezing or it is snowing,
but it is not snowing if it is below freezing.

$$\Rightarrow (p \vee q) \wedge (p \rightarrow \neg q)$$

g) That it is below freezing is **necessary**
and **sufficient** for it to be snowing.

$$\Rightarrow p \leftrightarrow q$$

Ans No: 19

Determine whether each of these conditional statements is true or false.

a) If $1+1=2$, then $2+2=5$

⇒ Since the hypothesis is 'true' and the conclusion is 'false', this conditional statements is false.

b) If $1+1=3$, then $2+2=4$

⇒ " " " " 'false' and " "

" 'true' then conditional statements is true

c) If $1+1=3$, then $2+2=5$

⇒ " " " " 'false' and " "

" 'false' " " " " true

V.V.I Note: If hypothesis is "false" then always conditional statements is true

d) If monkeys can fly, then $1+1=3$

\Rightarrow Since, the hypothesis is 'false', the conditional statement is true

Ans No: 29

State the converse, contrapositive and inverse of each of these conditional statements.

a) If it snows today, I will ski tomorrow.

Converse: "I will ski tomorrow only if it snows today."

Contrapositive: "If I do not ski tomorrow, then it will not have snowed today."

Inverse: "If it does not snow today, then I will not ski tomorrow."

b) I come to class whenever there is going to be a quiz.

Converse: "If I come to class, then there will be a quiz."

Contrapositive: "If I do not come to class, then there will ^{not} be a quiz."

Inverse: "If there is not going to be a quiz, then I don't come to class."

c) A positive integer is a prime only if it has no divisors other than 1 and itself.

Converse: "A positive integer is a prime if it has no divisors other than 1 and itself"

Contrapositive: "If a positive integer has a divisor other than 1 and itself, then it is not prime."

Inverse: "If a positive integer is not prime, then it has a divisor other than 1 and itself."