## Agent types for Problem solving

- Four basic types:
  - Simple reflex agents
  - Model-based reflex agents
  - Goal-based agents
  - Utility-based agents
- Two ways:
  - Rule-based reasoning/inference
  - NN-based processing

**Knowledge-**based Agents

**Logical Agents** 

# Lecture 9: Logical Agents Chapter 7

LI Xiaoan (Dustin) 李孝安, Dr. & Associate Prof. MARS-lab School of Computer Science and Engineering Northwestern Polytechnical University

E-mail: dustinli@nwpu.edu.cn

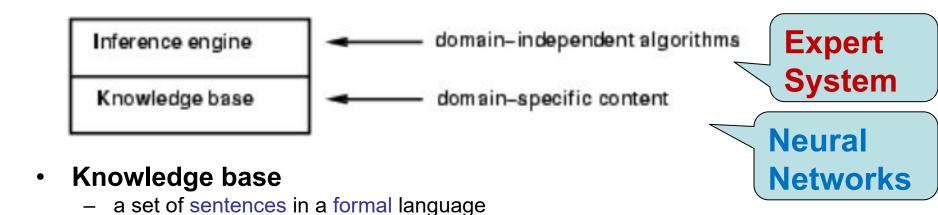
QQ group: Al-2021-Li

Cell phone: 18629662731

#### Outline

- Knowledge-based agents
- Wumpus world
- Logic in general models and entailment
- Propositional (Boolean) logic
- Equivalence, validity, satisfiability
- Inference rules and theorem proving
  - Forward chaining/backward chaining/resolution
- Summary

## Knowledge-based Agents



- Declarative approach to building an agent:
  - Tell it what it needs to know
  - it can Ask itself what to do answers should follow from the KB
  - Agents can be viewed at the knowledge level
     i.e., what they know, regardless of how implemented
- Procedural approach
  - encodes desired behaviors directly as program code
  - at the implementation level
     i.e., data structures in KB and algorithms that manipulate them
- Both Declarative approach and Procedural approach Why?

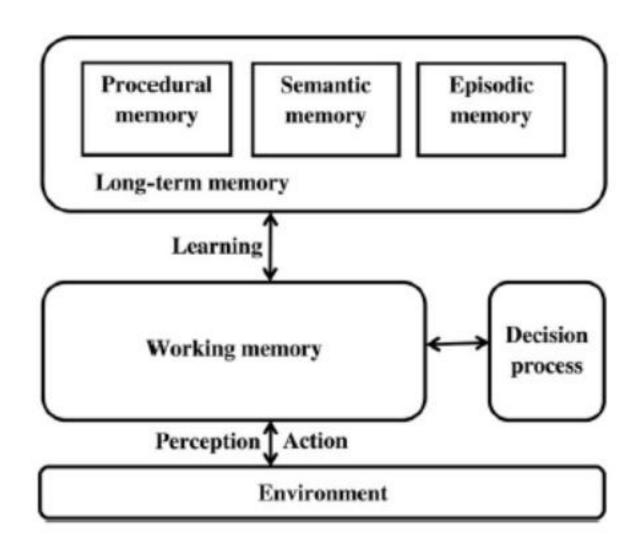
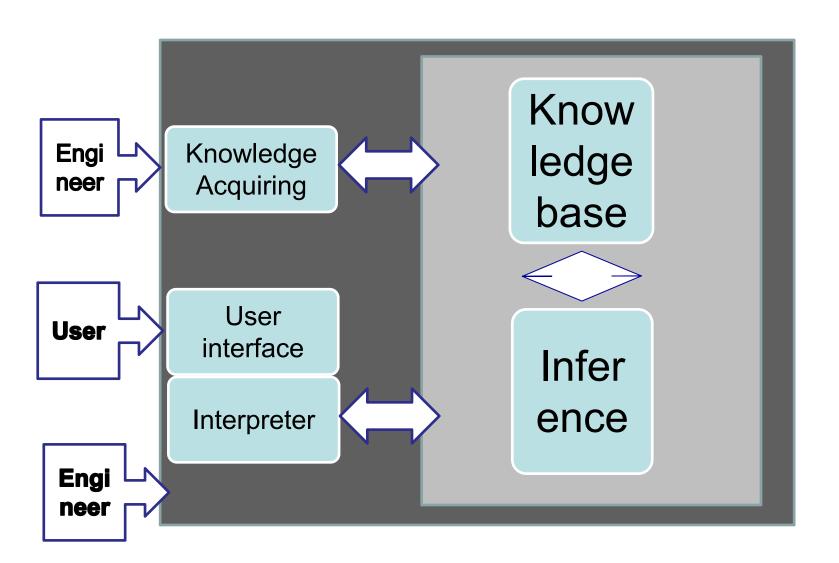
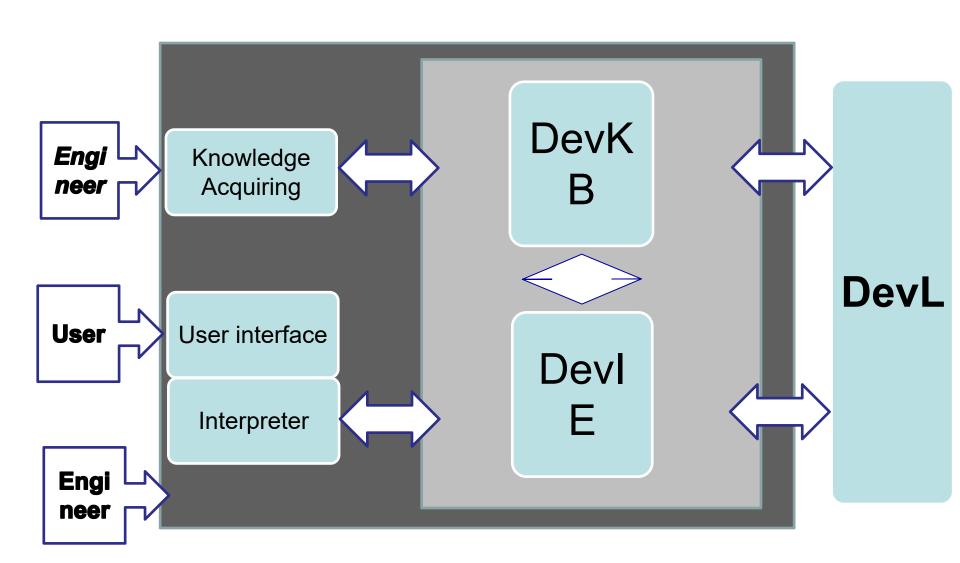


Fig.1 The general architecture of SOAR

# **Expert System**



## DevES\*



## A simple knowledge-based agent

```
function KB-AGENT( percept) returns an action static: KB, a knowledge base t, a counter, initially 0, indicating time  \text{Tell}(KB, \text{Make-Percept-Sentence}(percept, t))   action \leftarrow \text{Ask}(KB, \text{Make-Action-Query}(t))   \text{Tell}(KB, \text{Make-Action-Sentence}(action, t))   t \leftarrow t+1   \text{return } action
```

- The agent must be able to:
  - Represent states, actions, etc.
  - Incorporate new percepts
  - Update internal representations of the world
  - Deduce hidden properties of the world
  - Deduce appropriate actions

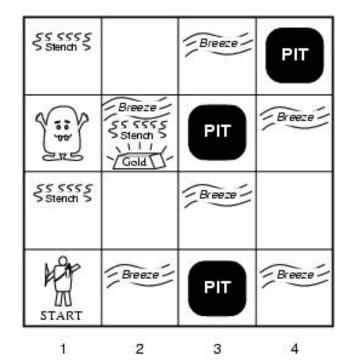
**Deduction** 

# Wumpus World PEAS description

3

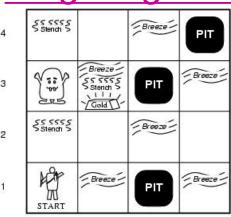
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- Wumpus World story
- Performance measure
  - gold +1000, death -1000
  - -1 per step, -10 for using the arrow
- Environment
  - Squares adjacent to wumpus are smelly
  - Squares adjacent to pit are breezy
  - Glitter iff gold is in the same square
  - Shooting kills wumpus if you are facing it 1
  - Shooting uses up the only arrow
  - Grabbing picks up gold if in same square
  - Releasing drops the gold in same square
- Sensors: Stench, Breeze, Glitter, Bump, Scream
- Actuators: Left turn, Right turn, Forward, Grab, Release, Shoot

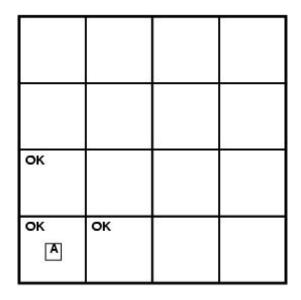


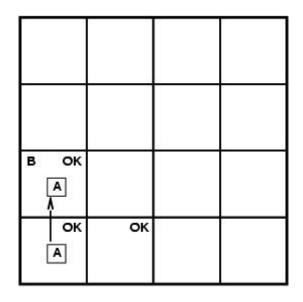
## Wumpus world characterization

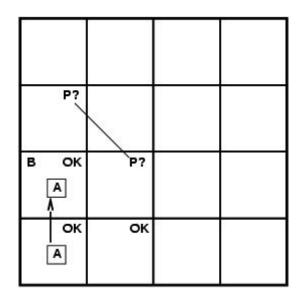
- Fully Observable?
   Deterministic?
- Episodic?
- Static?
- Discrete?
- Single-agent?

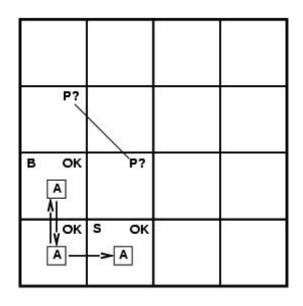


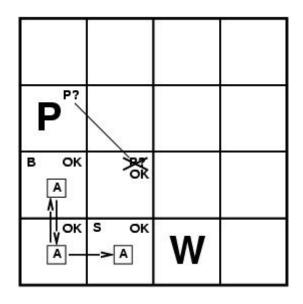
- Fully Observable? No only local perception
  - Yes outcomes exactly specified
  - No sequential at the level of actions
  - Yes Wumpus and Pits do not move
  - Yes
  - Yes Wumpus is essentially a natural feature

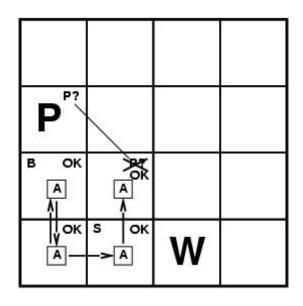


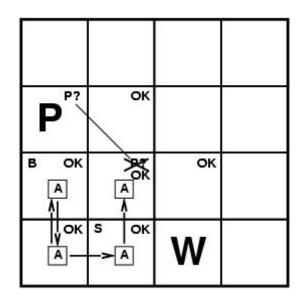


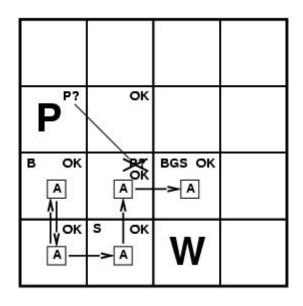












## Logic in general

- Logics are formal languages for representing information such that conclusions can be drawn
- Syntax defines the sentences in the language
- Semantics define the "meaning" of sentences
   i.e., define truth of a sentence in a world, well-formed sentence
- E.g., the language of arithmetic
  - $x+2 \ge y$  is a sentence;  $x2+y > {}$  is not a sentence
  - $-x+2 \ge y$  is true iff the number x+2 is no less than the number y
  - $-x+2 \ge y$  is true in a world where x = 7, y = 1
  - $-x+2 \ge y$  is false in a world where x = 0, y = 6

#### Entailment\*

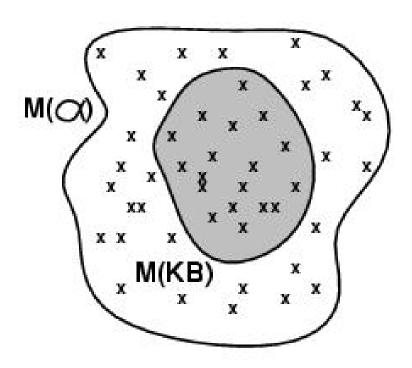
 Entailment means that one thing follows from another:

- Knowledge base KB entails sentence α if and only if α is true in all worlds where KB is true
  - E.g., the KB containing "the Giants won" and "the Reds won" entails "Either the Giants won or the Reds won"
  - E.g., x+y = 4 entails 4 = x+y
  - Entailment is a relationship between sentences (i.e., syntax) that is based on semantics

#### Models

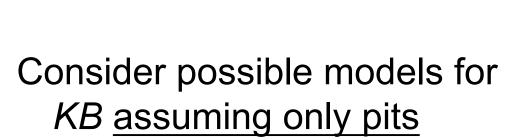
- Logicians typically think in terms of models, which are formally structured worlds with respect to which truth can be evaluated
- We say m is a model of a sentence α if α is true in m
- M(α) is the set of all models of α
- Then KB  $\models \alpha$  iff  $M(KB) \subseteq M(\alpha)$

```
- E.g. KB = Giants won and Reds won \alpha = Giants won So, M(KB) \subseteq M(\alpha) So, KB \models \alpha
```

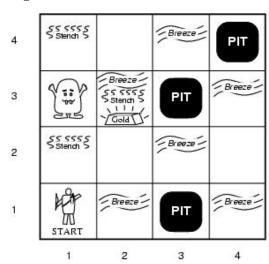


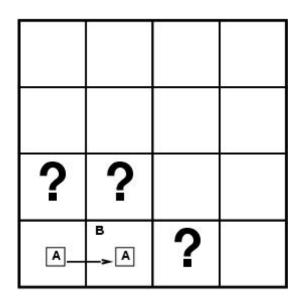
## Entailment in the wumpus world

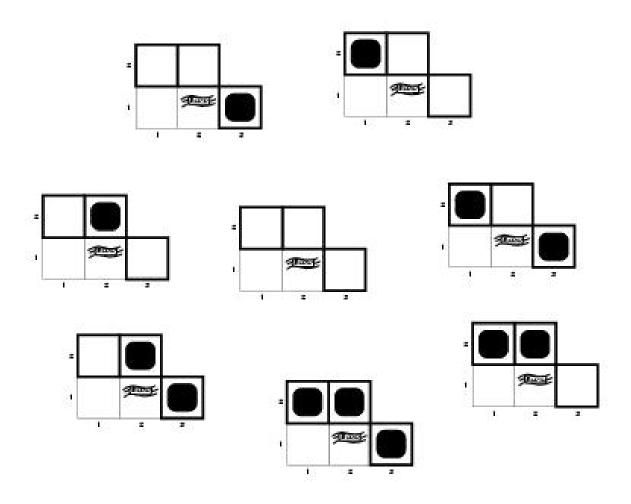
Situation after detecting nothing in [1,1], moving right, breeze in [2,1]

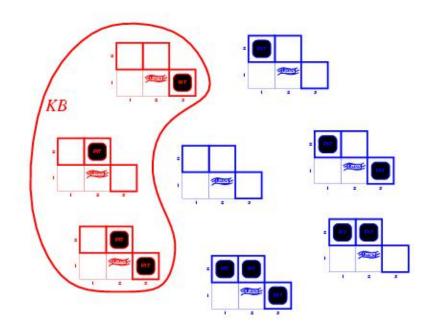


3 Boolean choices ⇒ <u>How</u>
<u>many possible</u> models (see Fig.) ?

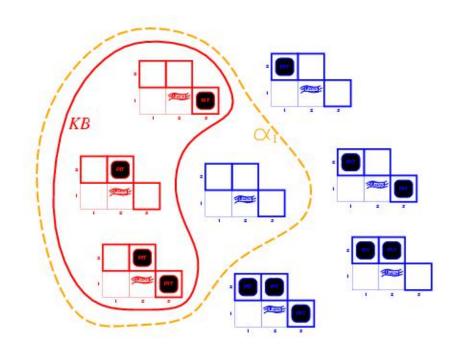




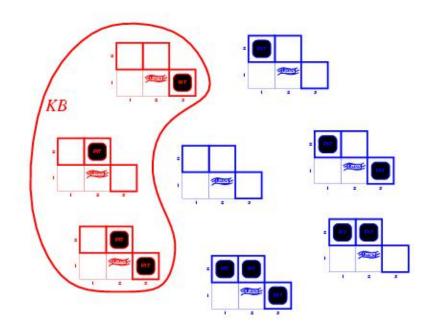




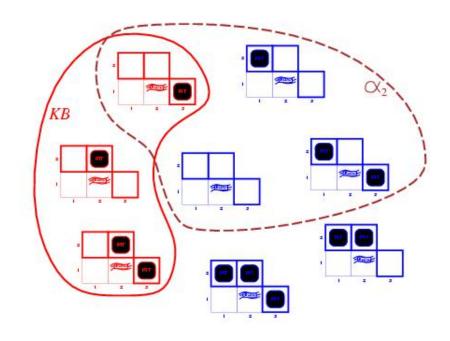
KB = wumpus-world rules + observations



- *KB* = wumpus-world rules + observations
- $\alpha_1 = "[1,2]$  is safe",  $KB \models \alpha_1$ , proved by model checking



KB = wumpus-world rules + observations



- KB = wumpus-world rules + observations
- $\alpha_2 = "[2,2]$  is safe",  $KB \not\models \alpha_2$

### Inference\*

- *KB* |<sub>i</sub>α
  - sentence α can be derived from KB by procedure (algorithm) i
- Soundness: *i* is sound if whenever  $KB \mid_{i} \alpha$ , it is also true that  $KB \models \alpha$
- Completeness: i is complete if whenever KB |= α, it is also true that KB |= α
- Preview:
  - we will define a logic (first-order logic) which is expressive enough to say almost anything of interest, and for which there exists a sound and complete inference procedure.
  - the procedure will answer any question whose answer follows from what is known by the KB.

## Propositional logic: Syntax

- Propositional logic is the simplest logic illustrates basic ideas
- The proposition symbols P<sub>1</sub>, P<sub>2</sub> etc are sentences
   We have the following results:
  - If S is a sentence, ¬S is a sentence (negation)
  - If  $S_1$  and  $S_2$  are sentences,  $S_1 \wedge S_2$  is a sentence (conjunction)
  - If  $S_1$  and  $S_2$  are sentences,  $S_1 \vee S_2$  is a sentence (disjunction)
  - If  $S_1$  and  $S_2$  are sentences,  $S_1 \Rightarrow S_2$  is a sentence (implication)
  - If  $S_1$  and  $S_2$  are sentences,  $S_1 \Leftrightarrow S_2$  is a sentence (biconditional)

## Propositional logic: Semantics

Each model specifies true/false for each proposition symbol

E.g.  $P_{1,2}$  is false,  $P_{2,2}$  is false,  $P_{3,1}$  is true

With these symbols, 8 possible models, can be enumerated automatically

Rules for evaluating truth with respect to a model *m*:

$\neg S$	is true iff	S is false	
$S_1 \wedge S_2$	is true iff	S <sub>1</sub> is true and	S <sub>2</sub> is true
$S_1 \vee S_2$	is true iff	S₁is true or	S <sub>2</sub> is true
$S_1 \Rightarrow S$	<sub>2</sub> is true iff	S <sub>1</sub> is false or	S <sub>2</sub> is true
i.e.,	is false iff	S <sub>1</sub> is true and	S <sub>2</sub> is false
$S_1 \Leftrightarrow S$	<sub>2</sub> is true iff	$S_1 \Rightarrow S_2$ is true a	$ndS_2 \Rightarrow S_1$ is true

Simple recursive process evaluates an arbitrary sentence, e.g.,

$$\neg P_{1,2} \land (P_{2,2} \lor P_{3,1}) = true \land (true \lor false) = true \land true = true$$

#### Truth tables for connectives

P	Q	$\neg P$	$P \wedge Q$	$P \lor Q$	$P \Rightarrow Q$	$P \Leftrightarrow Q$
false	false	true	false	false	true	true
false	true	true	false	true	true	false
true	false	false	false	true	false	false
true	true	false	true	true	true	true

## Wumpus world sentences

Let  $P_{i,j}$  be true if there is a pit in [i, j]. Let  $B_{i,j}$  be true if there is a breeze in [i, j].

```
\neg P_{1,1}
\neg B_{1,1}
B_{2,1}
```

"Pits cause breezes in adjacent squares"

$$\begin{array}{ll} \mathsf{B}_{1,1} \Leftrightarrow & (\mathsf{P}_{1,2} \vee \mathsf{P}_{2,1}) \\ \mathsf{B}_{2,1} \Leftrightarrow & (\mathsf{P}_{1,1} \vee \mathsf{P}_{2,2} \vee \mathsf{P}_{3,1}) \end{array}$$

### Truth tables for inference

$B_{1,1}$	$B_{2,1}$	$P_{1,1}$	$P_{1,2}$	$P_{2,1}$	$P_{2,2}$	$P_{3,1}$	KB	$\alpha_1$
false	true							
false	false	false	false	false	false	true	false	true
	ŧ			ŧ			:	
false	true	false	false	false	false	false	false	true
false	true	false	false	false	false	true	$\underline{true}$	$\underline{true}$
false	true	false	false	false	true	false	$\underline{true}$	$\underline{true}$
false	true	false	false	false	true	true	true	true
false	true	false	false	true	false	false	false	true
:	÷	:	:	:			:	:
true	false	false						

## Inference by enumeration

Depth-first enumeration of all models is sound and complete

```
function TT-Entails?(KB, \alpha) returns true or false
symbols \leftarrow \text{a list of the proposition symbols in } KB \text{ and } \alpha
\text{return TT-Check-All}(KB, \alpha, symbols, [])
function TT-Check-All}(KB, \alpha, symbols, model) \text{ returns } true \text{ or } false
\text{if Empty?}(symbols) \text{ then}
\text{if PL-True?}(KB, model) \text{ then return PL-True?}(\alpha, model)
\text{else return } true
\text{else do}
P \leftarrow \text{First}(symbols); rest \leftarrow \text{Rest}(symbols)
\text{return TT-Check-All}(KB, \alpha, rest, \text{Extend}(P, true, model) \text{ and}
\text{TT-Check-All}(KB, \alpha, rest, \text{Extend}(P, false, model)
```

• For *n* symbols, time complexity is  $O(2^n)$ , space complexity is O(n)

## Logical equivalence\*

 Two sentences are logically equivalent} iff true in same models: α ≡ ß iff α ⊨ β and β ⊨ α

```
(\alpha \wedge \beta) \equiv (\beta \wedge \alpha) commutativity of \wedge
           (\alpha \vee \beta) \equiv (\beta \vee \alpha) commutativity of \vee
((\alpha \wedge \beta) \wedge \gamma) \equiv (\alpha \wedge (\beta \wedge \gamma)) associativity of \wedge
((\alpha \vee \beta) \vee \gamma) \equiv (\alpha \vee (\beta \vee \gamma)) associativity of \vee
            \neg(\neg\alpha) \equiv \alpha double-negation elimination
       (\alpha \Rightarrow \beta) \equiv (\neg \beta \Rightarrow \neg \alpha) contraposition
       (\alpha \Rightarrow \beta) \equiv (\neg \alpha \lor \beta) implication elimination
      (\alpha \Leftrightarrow \beta) \equiv ((\alpha \Rightarrow \beta) \land (\beta \Rightarrow \alpha)) biconditional elimination
       \neg(\alpha \land \beta) \equiv (\neg \alpha \lor \neg \beta) de Morgan
       \neg(\alpha \lor \beta) \equiv (\neg \alpha \land \neg \beta) de Morgan
(\alpha \wedge (\beta \vee \gamma)) \equiv ((\alpha \wedge \beta) \vee (\alpha \wedge \gamma)) distributivity of \wedge over \vee
(\alpha \vee (\beta \wedge \gamma)) \equiv ((\alpha \vee \beta) \wedge (\alpha \vee \gamma)) distributivity of \vee over \wedge
```

# Validity\* and satisfiability\*

A sentence is valid if it is true in all models, e.g., *True*,  $A \lor \neg A$ ,  $A \Rightarrow A$ ,  $(A \land (A \Rightarrow B)) \Rightarrow B$ 

**Validity** is connected to inference via the Deduction Theorem:  $KB \models \alpha$  if and only if  $(KB \Rightarrow \alpha)$  is valid

A sentence is satisfiable if it is true in some model e.g., Av B, C

A sentence is unsatisfiable if it is true in no models e.g., A\¬A

**Satisfiability** is connected to inference via the following:  $KB \models \alpha$  if and only if  $(KB \land \neg \alpha)$  is unsatisfiable

#### Proof methods

- Proof methods divide into (roughly) two kinds:
  - Application of inference rules
    - Legitimate (sound) generation of new sentences from old
    - Proof = a sequence of inference rule applications
       Can use inference rules as operators in a standard search algorithm
    - Typically require transformation of sentences into a normal form
  - Model checking
    - truth table enumeration (always exponential in n)
    - improved backtracking, e.g., Davis--Putnam-Logemann-Loveland (DPLL)
    - heuristic search in model space (sound but incomplete)
       e.g., min-conflicts-like hill-climbing algorithms

#### Resolution

#### Conjunctive Normal Form (CNF)

conjunction of disjunctions of literals clauses

E.g., 
$$(A \vee \neg B) \wedge (B \vee \neg C \vee \neg D)$$

Resolution inference rule (for CNF):

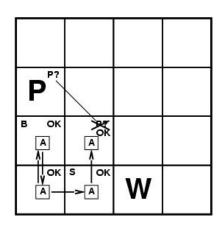
$$l_i \vee \ldots \vee l_k, \qquad m_1 \vee \ldots \vee m_n$$

$$l_i \vee \ldots \vee l_{i-1} \vee l_{i+1} \vee \ldots \vee l_k \vee m_1 \vee \ldots \vee m_{i-1} \vee m_{i+1} \vee \ldots \vee m_n$$

where  $l_i$  and  $m_i$  are complementary literals.

E.g., 
$$P_{1,3} \vee P_{2,2}, \neg P_{2,2}$$

 Resolution is sound and complete for propositional logic



#### Resolution

Soundness of resolution inference rule:

$$\neg(l_{i} \vee \ldots \vee l_{i-1} \vee l_{i+1} \vee \ldots \vee l_{k}) \Rightarrow l_{i}$$

$$\neg m_{j} \Rightarrow (m_{1} \vee \ldots \vee m_{j-1} \vee m_{j+1} \vee \ldots \vee m_{n})$$

$$\neg(l_{i} \vee \ldots \vee l_{i-1} \vee l_{i+1} \vee \ldots \vee l_{k}) \Rightarrow (m_{1} \vee \ldots \vee m_{j-1} \vee m_{j+1} \vee \ldots \vee m_{n})$$

#### Conversion to CNF

$$B_{1,1} \Leftrightarrow (P_{1,2} \vee P_{2,1}) \beta$$

- 1. Eliminate  $\Leftrightarrow$ , replacing  $\alpha \Leftrightarrow \beta$  with  $(\alpha \Rightarrow \beta) \land (\beta \Rightarrow \alpha)$ .  $(B_{1,1} \Rightarrow (P_{1,2} \lor P_{2,1})) \land ((P_{1,2} \lor P_{2,1}) \Rightarrow B_{1,1})$
- 2. Eliminate  $\Rightarrow$ , replacing  $\alpha \Rightarrow \beta$  with  $\neg \alpha \lor \beta$ .  $(\neg B_{1,1} \lor P_{1,2} \lor P_{2,1}) \land (\neg (P_{1,2} \lor P_{2,1}) \lor B_{1,1})$
- 3. Move inwards using de Morgan's rules and double-negation:

$$(\neg B_{1,1} \lor P_{1,2} \lor P_{2,1}) \land ((\neg P_{1,2} \lor \neg P_{2,1}) \lor B_{1,1})$$

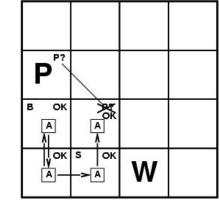
4. Apply distributivity law (∧ over ∨) and flatten:

$$(\neg B_{1,1} \lor P_{1,2} \lor P_{2,1}) \land (\neg P_{1,2} \lor B_{1,1}) \land (\neg P_{2,1} \lor B_{1,1})$$

#### Resolution algorithm

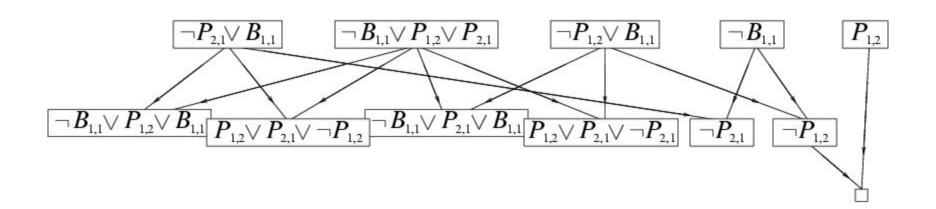
```
function PL-RESOLUTION(KB, \alpha) returns true or false
clauses \leftarrow \text{the set of clauses in the CNF representation of } KB \land \neg \alpha
new \leftarrow \{\}
loop do
for each <math>C_i, C_j in clauses do
resolvents \leftarrow \text{PL-RESOLVE}(C_i, C_j)
if resolvents \text{ contains the empty clause then return } true
new \leftarrow new \cup resolvents
if new \subseteq clauses \text{ then return } false
clauses \leftarrow clauses \cup new
```

# Resolution example



• 
$$KB = (B_{1,1} \Leftrightarrow (P_{1,2} \vee P_{2,1})) \land \neg B_{1,1}, \quad \alpha = \neg P_{1,2}$$

• ideas: Proof by contradiction, i.e., show KB∧¬α unsatisfiable



#### Summary

- Logical agents apply inference to a knowledge base to derive new information and make decisions
- Basic concepts of logic:
  - syntax: formal structure of sentences
  - semantics: truth of sentences wrt models
  - entailment: necessary truth of one sentence given another
  - inference: deriving sentences from other sentences
  - soundness: derivations produce only entailed sentences
  - completeness: derivations can produce all entailed sentences
- Wumpus world requires the ability to represent partial and negated information, reason by cases, etc.
- Resolution is complete for propositional logic Forward, backward chaining are linear-time, complete for Horn clauses
  - Propositional logic lacks expressive power, so it does not scale to environment of unbounded size

#### Assignment

- Reading
  - Chapter 7: 7.1-7.4, 7.7, 7.8
- Exercises
  - -7.1, 7.4

#### To be continued

#### Forward and backward chaining

- Horn Form (restricted)
   KB = conjunction of Horn clauses
  - Horn clause =
    - proposition symbol; or
    - (conjunction of symbols) ⇒ symbol
  - E.g.,  $C \wedge (B \Rightarrow A) \wedge (C \wedge D \Rightarrow B)$
- Modus Ponens (for Horn Form): complete for Horn KBs

$$\alpha_1, \ldots, \alpha_n, \qquad \alpha_1 \wedge \ldots \wedge \alpha_n \Rightarrow \beta$$

β

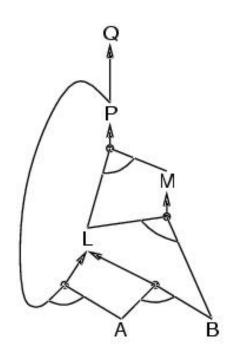
(or implication elimination)

- Can be used with forward chaining or backward chaining.
- These algorithms are very natural and run in linear time

#### Forward chaining

- Idea: fire any rule whose premises are satisfied in the KB,
  - add its conclusion to the KB, until query is found

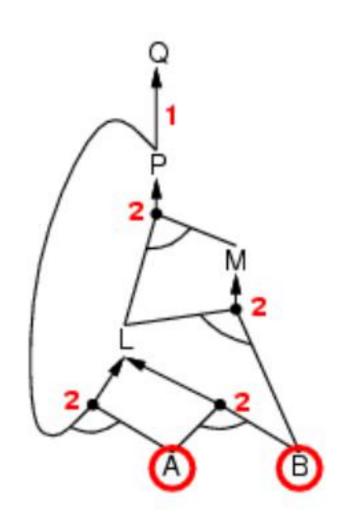
$$P \Rightarrow Q$$
 $L \land M \Rightarrow P$ 
 $B \land L \Rightarrow M$ 
 $A \land P \Rightarrow L$ 
 $A \land B \Rightarrow L$ 
 $A$ 

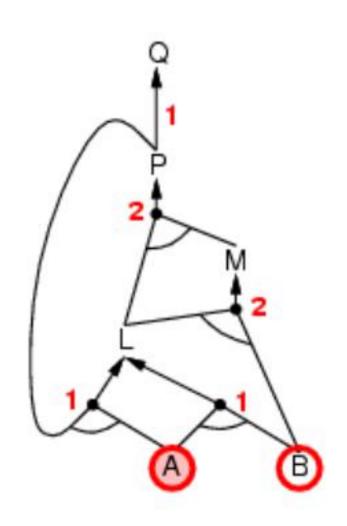


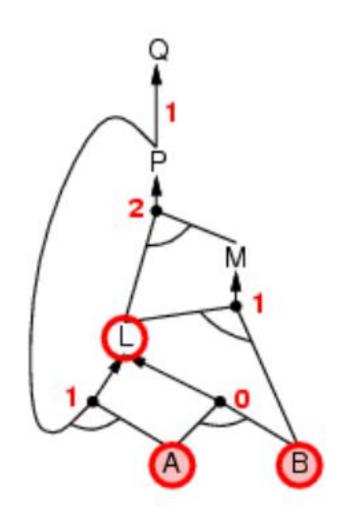
#### Forward chaining algorithm

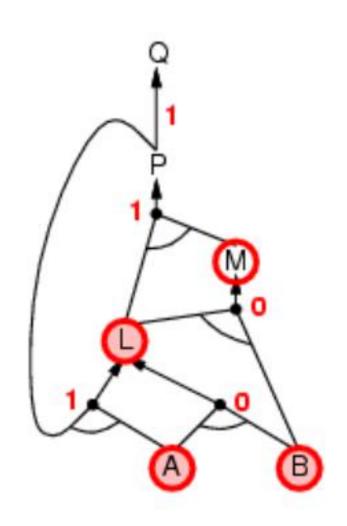
```
function PL-FC-Entails?(KB, q) returns true or false
  local variables: count, a table, indexed by clause, initially the number of premises
                      inferred, a table, indexed by symbol, each entry initially false
                     agenda, a list of symbols, initially the symbols known to be true
   while agenda is not empty do
       p \leftarrow Pop(agenda)
       unless inferred[p] do
            inferred[p] \leftarrow true
            for each Horn clause c in whose premise p appears do
                 decrement count[c]
                 if count[c] = 0 then do
                     if HEAD[c] = q then return true
                     Push(Head[c], agenda)
   return false
```

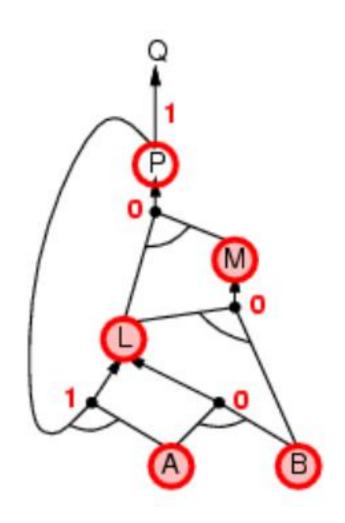
 Forward chaining is sound and complete for Horn KB

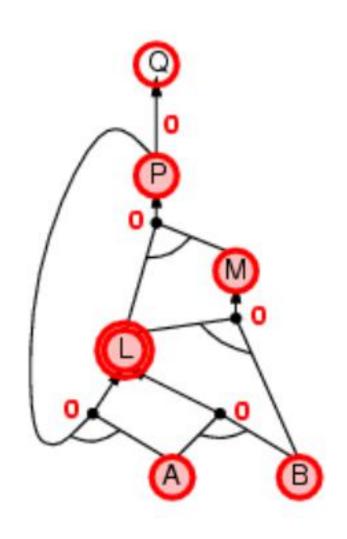


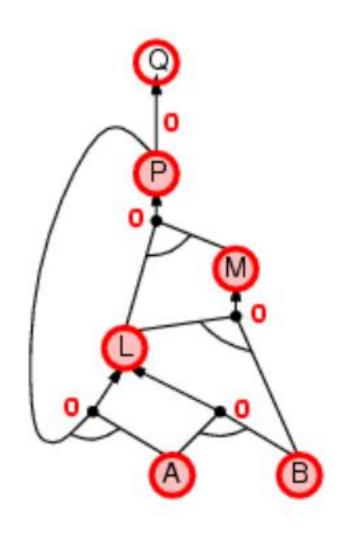


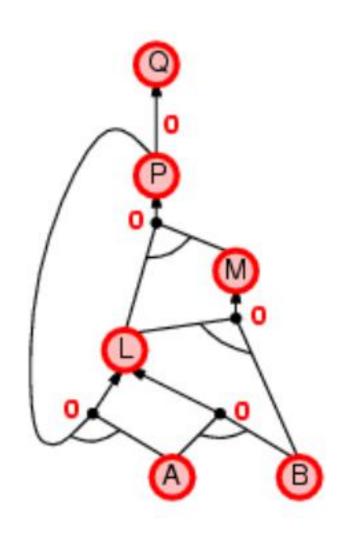












#### Proof of completeness

- FC derives every atomic sentence that is entailed by KB
  - 1. FC reaches a fixed point where no new atomic sentences are derived
  - 2. Consider the final state as a model *m*, assigning true/false to symbols
  - 3. Every clause in the original *KB* is true in m  $a_1 \wedge ... \wedge a_{k \Rightarrow} b$
  - 4. Hence *m* is a model of *KB*
  - 5. If  $KB \models q, q$  is true in every model of KB, including m

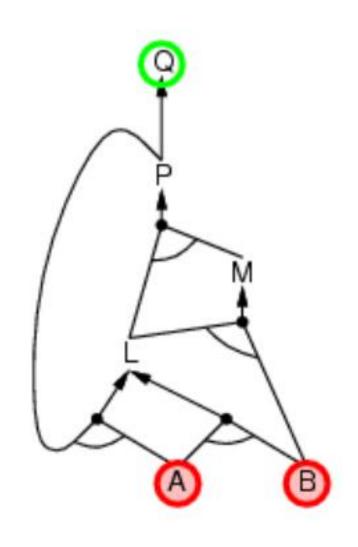
#### Backward chaining

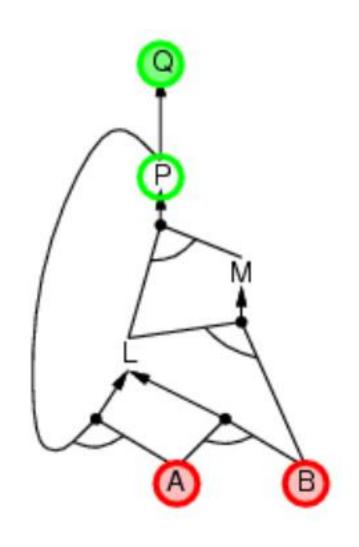
Idea: work backwards from the query q:
to prove q by BC,
check if q is known already, or
prove by BC all premises of some rule concluding q

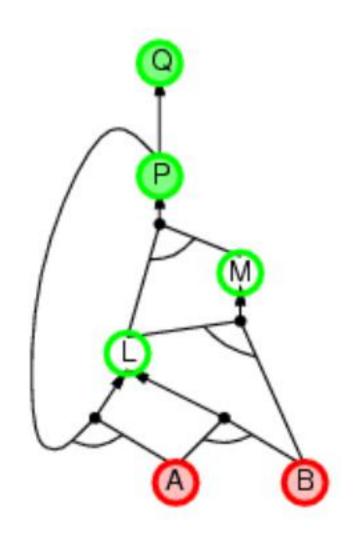
Avoid loops: check if new subgoal is already on the goal stack

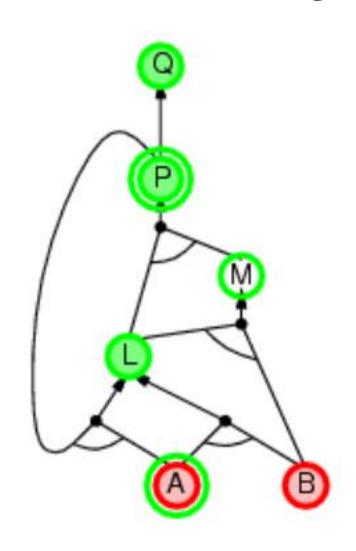
Avoid repeated work: check if new subgoal

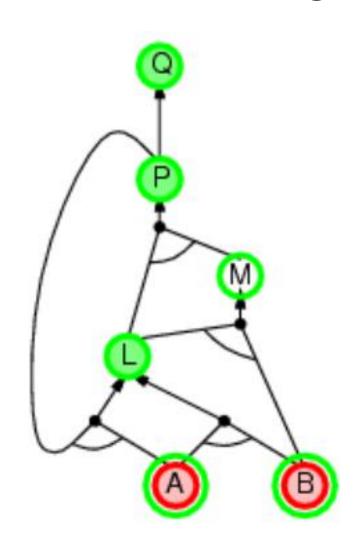
- 1. has already been proved true, or
- 2. has already failed

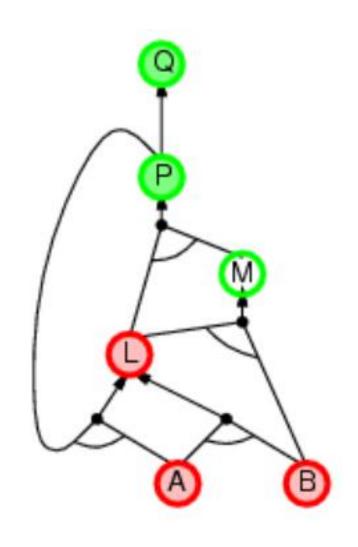


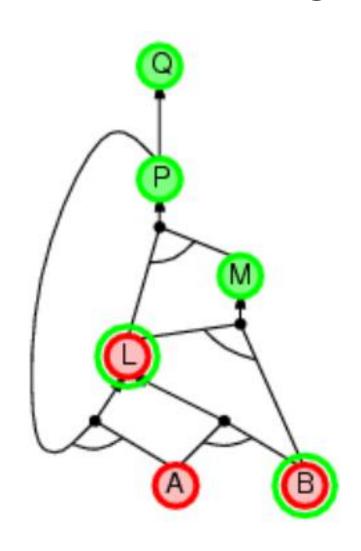


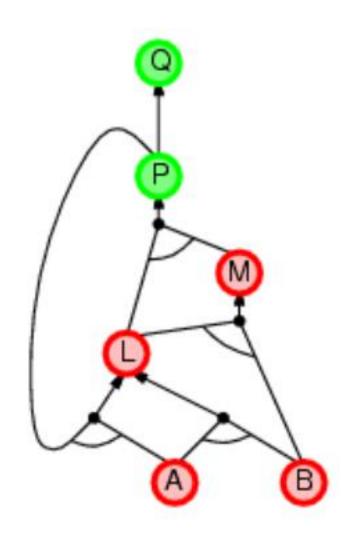


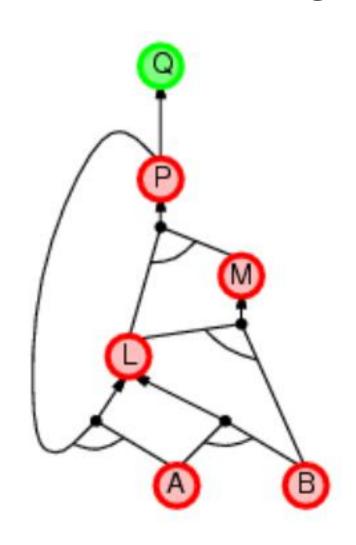


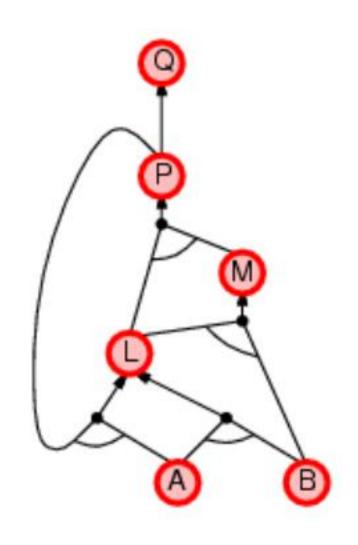












#### Forward vs. backward chaining

- FC is data-driven, automatic, unconscious processing,
  - e.g., object recognition, routine decisions
  - May do lots of work that is irrelevant to the goal
- BC is goal-driven, appropriate for problem-solving,
  - e.g., Where are my keys? How do I get into a PhD program?
- Complexity of BC can be much less than linear in size of KB

#### Efficient propositional inference

Two families of efficient algorithms for propositional inference:

- Complete backtracking search algorithms
  - DPLL algorithm (Davis, Putnam, Logemann, Loveland)
- Incomplete local search algorithms
  - WalkSAT algorithm

#### The DPLL algorithm

Determine if an input propositional logic sentence (in CNF) is satisfiable.

Improvements over truth table enumeration:

#### 1. Early termination

A clause is true if any literal is true.

A sentence is false if any clause is false.

#### 2. Pure symbol heuristic

Pure symbol: always appears with the same "sign" in all clauses.

e.g., In the three clauses (A  $\vee \neg$ B), ( $\neg$ B  $\vee \neg$ C), (C  $\vee$  A), A and B are pure, C is impure.

Make a pure symbol literal true.

#### 3. Unit clause heuristic

Unit clause: only one literal in the clause

The only literal in a unit clause must be true.

#### The DPLL algorithm

```
function DPLL-Satisfiable?(s) returns true or false
   inputs: s, a sentence in propositional logic
   clauses \leftarrow the set of clauses in the CNF representation of s
   symbols \leftarrow a list of the proposition symbols in s
   return DPLL(clauses, symbols, [])
function DPLL(clauses, symbols, model) returns true or false
   if every clause in clauses is true in model then return true
   if some clause in clauses is false in model then return false
   P, value \leftarrow \text{FIND-Pure-Symbol}(symbols, clauses, model)
   if P is non-null then return DPLL(clauses, symbols-P, [P = value | model])
   P, value \leftarrow \text{FIND-UNIT-CLAUSE}(clauses, model)
   if P is non-null then return DPLL(clauses, symbols-P, [P = value | model])
   P \leftarrow \text{First}(symbols); rest \leftarrow \text{Rest}(symbols)
   return DPLL(clauses, rest, [P = true | model]) or
            DPLL(clauses, rest, [P = false|model])
```

#### The WalkSAT algorithm

- Incomplete, local search algorithm
- Evaluation function: The min-conflict heuristic of minimizing the number of unsatisfied clauses
- Balance between greediness and randomness

#### The WalkSAT algorithm

```
function WalkSat(clauses, p, max-flips) returns a satisfying model or failure inputs: clauses, a set of clauses in propositional logic p, the probability of choosing to do a "random walk" move max-flips, number of flips allowed before giving up model \leftarrow a random assignment of true/false to the symbols in clauses for i=1 to max-flips do if model satisfies clauses then return model clause \leftarrow a randomly selected clause from clauses that is false in model with probability p flip the value in model of a randomly selected symbol from clause else flip whichever symbol in clause maximizes the number of satisfied clauses return failure
```

# Inference-based agents in the wumpus world

A wumpus-world agent using propositional logic:

$$\begin{array}{l} \neg P_{1,1} \\ \neg W_{1,1} \\ B_{x,y} \Leftrightarrow (P_{x,y+1} \vee P_{x,y-1} \vee P_{x+1,y} \vee P_{x-1,y}) \\ S_{x,y} \Leftrightarrow (W_{x,y+1} \vee W_{x,y-1} \vee W_{x+1,y} \vee W_{x-1,y}) \\ W_{1,1} \vee W_{1,2} \vee \ldots \vee W_{4,4} \\ \neg W_{1,1} \vee \neg W_{1,2} \\ \neg W_{1,1} \vee \neg W_{1,3} \\ \ldots \end{array}$$

⇒ 64 distinct proposition symbols, 155 sentences

```
function PL-Wumpus-Agent (percept) returns an action
   inputs: percept, a list, [stench, breeze, glitter]
   static: KB, initially containing the "physics" of the wumpus world
            x, y, orientation, the agent's position (init. [1,1]) and orient. (init. right)
            visited, an array indicating which squares have been visited, initially false
            action, the agent's most recent action, initially null
            plan, an action sequence, initially empty
   update x, y, orientation, visited based on action
   if stench then Tell(KB, S_{x,y}) else Tell(KB, \neg S_{x,y})
   if breeze then Tell(KB, B_{x,y}) else Tell(KB, \neg B_{x,y})
   if glitter then action \leftarrow grab
   else if plan is nonempty then action \leftarrow Pop(plan)
   else if for some fringe square [i,j], ASK(KB, (\neg P_{i,j} \land \neg W_{i,j})) is true or
            for some fringe square [i,j], ASK(KB, (P_{i,j} \vee W_{i,j})) is false then do
        plan \leftarrow A^*-Graph-Search(Route-PB([x,y], orientation, [i,j], visited))
        action \leftarrow Pop(plan)
   else action \leftarrow a randomly chosen move
   return action
```

# Expressiveness limitation of propositional logic

- KB contains "physics" sentences for every single square
- For every time *t* and every location [*x*, *y*],

$$L_{x,y}^{t} \wedge FacingRight^{t} \wedge Forward^{t} \Rightarrow L_{x+1,y}^{t}$$

Rapid proliferation of clauses leads to *representational frame problem*!

#### Summary

- Logical agents apply inference to a knowledge base to derive new information and make decisions
- Basic concepts of logic:
  - syntax: formal structure of sentences
  - semantics: truth of sentences wrt models
  - entailment: necessary truth of one sentence given another
  - inference: deriving sentences from other sentences
  - soundness: derivations produce only entailed sentences
  - completeness: derivations can produce all entailed sentences
- Wumpus world requires the ability to represent partial and negated information, reason by cases, etc.
- Resolution is complete for propositional logic Forward, backward chaining are linear-time, complete for Horn clauses
  - Propositional logic lacks expressive power, so it does not scale to environment of unbounded size

#### Assignment

- Reading
  - Chapter 7: 7.1-7.5, 7.7, 7.8
- Exercises
  - -7.7, 7.8, 7.13