

Message Passing Interface (MPI)

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Fall, 2022

Topics Overview

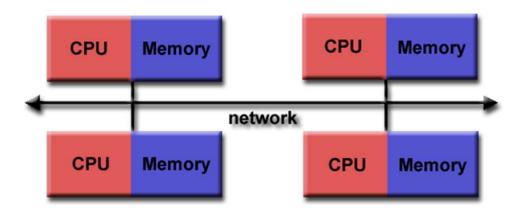
- What is MPI (MPI Basics)?
- Why MPI?
- Compiling and Running MPI programs
- MPI Routines-C and Fortran
- Examples

What is MPI (Message Passing Interface)?

- MPI defines a standard library of functions for messagepassing that can be used to develop portable messagepassing programs using either C/C++ or Fortran.
 - It is not a new programming language
 - MPI is a specification for the developers and users of message passing libraries. By itself, it is NOT a library - but rather the specification of what such a library should be.
- MPI primarily addresses the message-passing parallel programming model: data is moved from the address space of one process to that of another process through cooperative operations on each process.
- Each data element must belong to one of the partitions of the space; hence, data must be explicitly partitioned and placed.

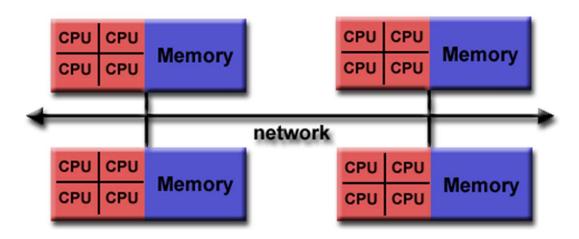
Programming Model:

 Originally, MPI was designed for distributed memory architectures, which were becoming increasingly popular at that time (1980s - early 1990s).



- As architecture trends changed, shared memory SMPs were combined over networks creating hybrid distributed memory / shared memory systems.
- MPI implementors adapted their libraries to handle both types of underlying memory architectures seamlessly. They also adapted/developed ways of handling different interconnects and protocols.

- Today, MPI runs on virtually any hardware platform:
 - Distributed Memory
 - Shared Memory
 - Hybrid
- The programming model <u>clearly remains a distributed memory</u> <u>model</u> however, regardless of the underlying physical architecture of the machine.
- All parallelism is explicit: the programmer is responsible for correctly identifying parallelism and implementing parallel algorithms using MPI constructs.



History and Evolution

- MPI has resulted from the efforts of numerous individuals and groups that began in 1992.
 - -1980s early 1990s: Distributed memory, parallel computing develops, as do a number of incompatible software tools for writing such programs usually with tradeoffs between portability, performance, functionality and price. Recognition of the need for a standard arose.
- Apr 1992: Workshop on Standards for Message Passing in a Distributed Memory Environment, sponsored by the Center for Research on Parallel Computing, Williamsburg, Virginia. The basic features essential to a standard message passing interface were discussed, and a working group established to continue the standardization process. Preliminary draft proposal developed subsequently.
- Nov 1992: Working group meets in Minneapolis. MPI draft proposal (MPI1) from ORNL presented. Group adopts procedures and organization to form the MPI Forum. It eventually comprised of about 175 individuals from 40 organizations including parallel computer vendors, software writers, academia and application scientists.
- Nov 1993: Supercomputing 93 conference draft MPI standard presented.
- May 1994: Final version of MPI-1.0 released
 - MPI-1.1 (Jun 1995)
 - MPI-1.2 (Jul 1997)
 - MPI-1.3 (May 2008).
- 1998: MPI-2 picked up where the first MPI specification left off, and addressed topics which went far beyond the MPI-1 specification.
 - MPI-2.1 (Sep 2008)
 - MPI-2.2 (Sep 2009)
- Sep 2012: The MPI-3.0 standard was approved.
 - MPI-3.1 (Jun 2015)

MPI-1.0

- Point-to-point communication
- Collective communication
- Data types
- Non-blocking communication

A Brief Word on MPI-2 and MPI-3

MPI-2:

- Intentionally, the MPI-1 specification did not address several "difficult" issues. For reasons of expediency, these issues were deferred to a second specification, called MPI-2 in 1998.
- MPI-2 was a major revision to MPI-1 adding new functionality and corrections.
- Key areas of new functionality in MPI-2:
 - Dynamic Processes extensions that remove the static process model of MPI. Provides routines to create new processes after job startup.
 - One-Sided Communications provides routines for one directional communications. Include shared memory operations (put/get) and remote accumulate operations.
 - Extended Collective Operations allows for the application of collective operations to inter-communicators
 - External Interfaces defines routines that allow developers to layer on top of MPI, such as for debuggers and profilers.
 - Additional Language Bindings describes C++ bindings and discusses Fortran-90 issues.
 - Parallel I/O describes MPI support for parallel I/O.

MPI-3:

- The MPI-3 standard was adopted in 2012, and contains significant extensions to MPI-1 and MPI-2 functionality including:
 - Nonblocking Collective Operations permits tasks in a collective to perform operations without blocking, possibly offering performance improvements.
 - New One-sided Communication Operations to better handle different memory models.
 - Neighborhood Collectives extends the distributed graph and Cartesian process topologies with additional communication power.
 - Fortran 2008 Bindings expanded from Fortran90 bindings
 - MPIT Tool Interface allows the MPI implementation to expose certain internal variables, counters, and other states to the user (most likely performance tools).
 - Matched Probe fixes an old bug in MPI-2 where one could not probe for messages in a multi-threaded environment.

More Information on MPI-2 and MPI-3:

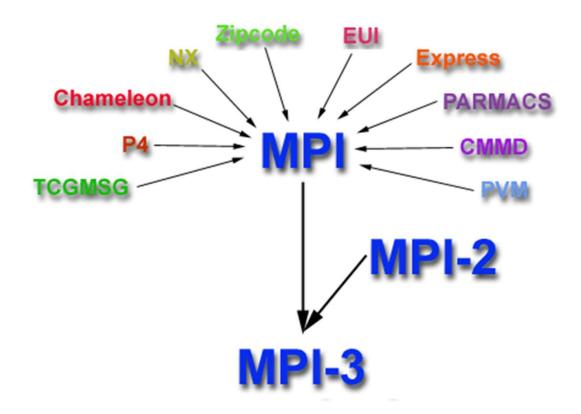
MPI Standard documents: http://www.mpi-forum.org/docs/

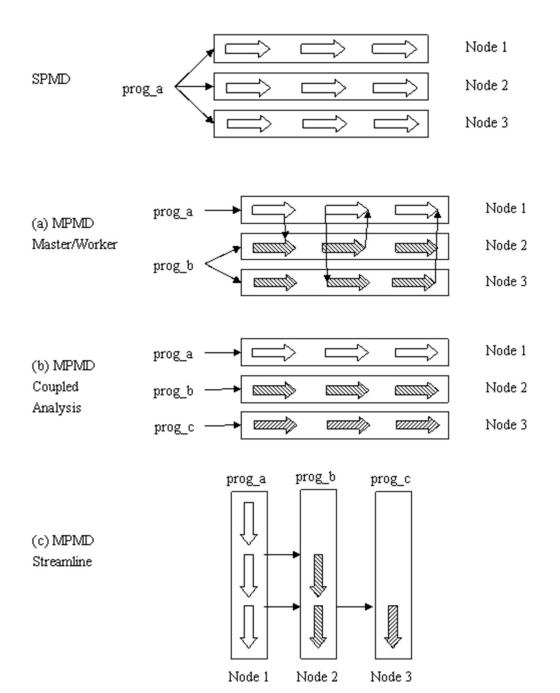
MPI-4.0

MPI-4.0 is a major update to the MPI standard. The largest changes are the addition of large-count versions of many routines to address the limitations of using an int or INTEGER for the count parameter, persistent collectives, partitioned communications, an alternative way to initialize MPI, application info assertions, and improvements to the definitions of error handling. In addition, there are a number of smaller improvements and corrections.

Documentation:

 Documentation for all versions of the MPI standard is available at: http://www.mpi-forum.org/docs/.





Why-Reasons for Using MPI:

- Standardization MPI is the only message passing library that can be considered a standard. It is supported on virtually all HPC platforms.
 Practically, it has replaced all previous message passing libraries.
- Portability There is little or no need to modify your source code when you port your application to a different platform that supports (and is compliant with) the MPI standard.
- Performance Opportunities Vendor implementations should be able to exploit native hardware features to optimize performance. Any implementation is free to develop optimized algorithms.
- Functionality There are over 430 routines defined in MPI-3, which
 includes the majority of those in MPI-2 and MPI-1. Most MPI programs can
 be written using a dozen or less routines
- Availability A variety of implementations are available, both vendor and public domain.

MPI Implementations and Compilers

- Although the MPI programming interface has been standardized, actual library implementations will differ in which version and features of the standard they support.
- The way MPI programs are compiled and run on different platforms may also vary.
 - MVAPICH (https://mvapich.cse.ohio-state.edu)
 - Open MPI (https://www.open-mpi.org)
 - Mpich (https://www.mpich.org)
 - Intel MPI





MVAPICH MPI is developed and supported by the <u>Network-Based Computing Lab</u> at Ohio State University.

MVAPICH2

 based on MPI 3.1 standard, delivers the best performance, scalability and fault tolerance for high-end computing systems and servers using InfiniBand, Omni-Path, Ethernet/iWARP, RoCE(v1/v2), Cray Slingshot 10 and 11, and Rockport Networks networking technologies.

The MVAPICH2 software is powering several supercomputers in the TOP500 list. Examples (from the June '22 ranking) include:

- 6th, 10,649,600-core (Sunway TaihuLight) at National Supercomputing Center in Wuxi, China
- 16th, 448, 448 cores (Frontera) at TACC
- 30th, 288,288 cores (Lassen) at LLNL
- · 42nd, 570,020 cores (Nurion) in South Korea
- · 47th, 367,024 cores (Stampede2) at TACC

Open MPI

- Open MPI is a thread-safe, open source MPI implementation developed and supported by a consortium of academic, research, and industry partners.
 - Full MPI-3.1 standards conformance
 - Thread safety and concurrency
 - Dynamic process spawning
 - Network and process fault tolerance
 - Support network heterogeneity
 - Single library supports all networks
 - Run-time instrumentation
 - Many job schedulers supported

- Many OS's supported (32 and 64 bit)
- Production quality software
- High performance on all platforms
- Portable and maintainable
- Tunable by installers and end-users
- Component-based design, documented APIs
- · Active, responsive mailing list
- Open source license based on the BSD license

[Open MPI Announce] Open MPI 4.1.4 released

Barrett, Brian via announce Thu, 26 May 2022 10:57:58 -0700

Members: 14Partners: 4Contributors:

• Contributors: 36

Individuals: 16Organizations: 38







Intel MPI

- The Intel MPI Library is available as a standalone product and as part of the Intel® oneAPI HPC Toolkit
- It implements the Message Passing Interface, version 3.1 (MPI-3.1) specification.
 - Scalability up to 340k processes
 - Low overhead enables analysis of large amounts of data
 - MPI tuning utility for accelerating your applications
 - Interconnect independence and flexible runtime fabric selection
 - Supported Languages:
 - o For GNU* compilers: C, C++, Fortran 77, Fortran 95
 - For Intel® compilers: C, C++, Fortran 77, Fortran 90, Fortran 95, Fortran 2008

```
[houzx@c01b03 ~]$ ls /public/software/intel/impi/2019.4.243/intel64/bin/mpi
mpicc
               mpiexec
                              mpif77
                                             mpifc
                                                                            mpiicpc
                                                            mpiqxx
                                                                                           mpirun
                                                                                                          mpivars.csh
               mpiexec.hydra mpif90
                                                            mpiicc
                                                                                                          mpivars.sh
mpicxx
                                             mpiqcc
                                                                                           mpitune
                                                                            mpilifort
```

MPI Build Scripts

- People usually developed MPI compiler wrapper scripts, which are used to compile MPI programs
- Automatically perform some error checks, include the appropriate MPI #include files, link to the necessary MPI libraries, and pass options to the underlying compiler.
- For additional information:
 - See the man page (if it exists)
 - Issue the script name with the -help option
 - View the script yourself directly

MVAPCH2	С	mpicc	C compiler for loaded compiler package	
	C++	mpicxx mpic++	C++ compiler for loaded compiler package	
	Fortran	mpif77	Fortran77 compiler for loaded compiler package. Points to mpifort.	
		mpif90	Fortran90 compiler for loaded compiler package. Points to mpifort.	
		mpifort	Fortran 77/90 compiler for loaded compiler package.	
Open MPI	С	mpicc	C compiler for loaded compiler package	
	C++	mpicc mpic++ mpicxx	C++ compiler for loaded compiler package	
	Fortran	mpif77	Fortran77 compiler for loaded compiler package. Points to mpifort.	
		mpif90	Fortran90 compiler for loaded compiler package. Points to mpifort.	
		mpifort	Fortran 77/90 compiler for loaded compiler package.	

General MPI Program Structure

MPI include file Declarations, prototypes, etc. **Program Begins** Serial code Initialize MPI environment Parallel code begins Do work & make message passing calls Terminate MPI environment Parallel code ends Serial code **Program Ends**

Header File:

Required for all programs that make MPI library calls.

C include file	Fortran include file	
#include "mpi.h"	include 'mpif.h'	

 With MPI-3 Fortran, the USE mpi_f08 module is preferred over using the include file shown above.

Format of MPI Calls:

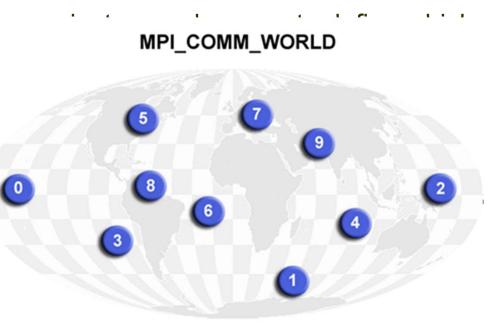
- C names are case sensitive; Fortran names are not.
- Programs must not declare variables or functions with names beginning with the prefix MPI_ or PMPI_ (profiling interface).

C Binding				
Format:	rc = MPI_Xxxxx(parameter,)			
Example:	rc = MPI_Bsend(&buf,count,type,dest,tag,comm)			
Error code:	Returned as "rc". MPI_SUCCESS if successful			
	Fortran Binding			
Format:	CALL MPI_XXXXX (parameter,, ierr) call mpi_xxxxx (parameter,, ierr)			
Example:	mple: CALL MPI_BSEND(buf,count,type,dest,tag,comm,ier:			
Error code:	Returned as "ierr" parameter. MPI_SUCCESS if successful			

//PI 20/88

Communicators and Groups:

- MPI uses objects called collection of processes management
- Most MPI routines require argument.
- Communicators and group now, simply use MPI_CO
 required it is the predefir MPI processes.



Rank:

- Within a communicator, every process has its own unique, integer identifier assigned by the system when the process initializes. A rank is sometimes also called a "task ID". Ranks are contiguous and begin at zero.
- Used by the programmer to specify the source and destination of messages. Often used conditionally by the application to control program execution (if rank=0 do this / if rank=1 do that).

The **if-else** construct makes our program SPMD.

Error Handling:

- Most MPI routines include a return/error code parameter, as described in the "Format of MPI Calls" section above.
- However, according to the MPI standard, the default behavior of an MPI call is to abort if there is an error. This means you will probably not be able to capture a return/error code other than MPI_SUCCESS (zero).
- The standard does provide a means to override this default error handler. You can consult the error handling section of the relevant MPI Standard documentation located athttp://www.mpi-forum.org/docs/.
- The types of errors displayed to the user are implementation dependent.

A Simple Framework - C

```
#include <mpi.h>
/* include other usual header files*/
main(int argc, char **argv)
{
    / * No MPI calls before this * /
    /* initialize MPI */
   MPI Init(&argc, &argv);
    /* main part of program */
    /* terminate MPI */
   MPI Finalize();
   / * No MPI calls after this */
   exit(0);
```

MPI helloworld.c

```
#include <mpi.h>
main(int argc, char **argv)
{
        int numtasks, rank;
        MPI Init(&argc, &argv);
        MPI Comm size(MPI COMM WORLD, & numtasks);
        MPI Comm rank(MPI COMM WORLD, &rank);
        printf("Hello World from process %d of %d\n",
            rank, numtasks);
        MPI Finalize();
```

Compiling and Running MPI programs

Compile and Run Commands

- Compile:
 - [mpicc helloworld.c -o helloworld (standard)]
- Run:

No. of processes

- mpirun -np 3 helloworld [hosts picked from configuration file automatically]
- mpirun -np 3 -machinefile machines.list helloworld
- The file machines.list contains nodes list:

```
node1node13
```

node1:8node2:8

Sample Run and Output

- A Run with 3 Processes:
 - mpirun -np 3 -machinefile machines.list helloworld
 - Hello World from process 0 of 3
 - Hello World from process 1 of 3
 - Hello World from process 2 of 3
- A Run by default
 - ./helloworld
 - Hello World from process 0 of 1
- You can also use mpirun to exec standard commands
 - mpirun -np 4 -machinefile machines.list hostname

Sample Run and Output

- A Run with 6 Processes:
 - manjra> mpirun -np 6 -machinefile machines.list helloworld
 - Hello World from process 0 of 6
 - Hello World from process 3 of 6
 - Hello World from process 1 of 6
 - Hello World from process 5 of 6
 - Hello World from process 4 of 6
 - Hello World from process 2 of 6
- Note: Process execution need not be in process number order.

MPI Routines-C and Fortran

- (1) Environment Management Routines
- (2) Point to Point Communication Routines
- (3) Collective Communication Routines
- (4) Derived Data Types
- (5) Process Group and Communicator Management Routines
- (6) Virtual Topologies
- Miscellaneous Routines

The minimal set (6) of MPI routines

MPI_Init	Initializes MPI.
MPI_Finalize	Terminates MPI.
MPI_Comm_size	Determines the number of processes.
MPI_Comm_rank	Determines the label of calling process.
MPI_Send	Sends a message.
MPI_Recv	Receives a message.

```
#include "mpi.h"
int main( int argc, char** argv )
int rank, size, tag=1;
int senddata, recvdata;
MPI_Status status;
MPI_Init(&argc, &argv);
MPI_Comm_rank(MPI_COMM_WORLD, &rank);
MPI_Comm_size(MPI_COMM_WORLD, &size);
if (rank==0){
senddata=9999;
MPI_Send( &senddata, 1, MPI_INT, 1, tag, MPI_COMM_WORLD);
if (rank==1)
MPI_Recv(&recvdata, 1, MPI_INT, 0, tag, MPI_COMM_WORLD, &status);
MPI_Finalize();
return (0);
```

(1) Environment Management Routines

Environment Management Routines						
MPI Abort	MPI Errhandler create	MPI Errhandler free				
MPI Errhandler get	MPI Errhandler set	MPI Error class				
MPI Error string	MPI Finalize	MPI Get processor name				
MPI Init	MPI Initialized	MPI Wtick				
MPI Wtime						

MPI_Init

Initializes the MPI execution environment. This function must be called in every MPI program, must be called before any other MPI functions and must be called only once in an MPI program. For C programs, MPI_Init may be used to pass the command line arguments to all processes, although this is not required by the standard and is implementation dependent.

MPI_Init (&argc, &argv)
MPI_INIT (ierr)

MPI_Comm_size

Returns the total number of MPI processes in the specified communicator, such as MPI_COMM_WORLD. If the communicator is MPI_COMM_WORLD, then it represents the number of MPI tasks available to your application.

```
MPI_COMM_size (comm,&size)
MPI_COMM_SIZE (comm,size,ierr)
```

MPI_Comm_rank

Returns the rank of the calling MPI process within the specified communicator. Initially, each process will be assigned a unique integer rank between 0 and number of tasks - 1 within the communicator MPI_COMM_WORLD. This rank is often referred to as a task ID. If a process becomes associated with other communicators, it will have a unique rank within each of these as well.

```
MPI_Comm_rank (comm,&rank)
MPI_COMM_RANK (comm,rank,ierr)
```

MPI Abort

Terminates all MPI processes associated with the communicator. In most MPI implementations it terminates ALL processes regardless of the communicator specified.

```
MPI_Abort (comm,errorcode)
MPI_ABORT (comm,errorcode,ierr)
```

MPI Get processor name

Returns the processor name. Also returns the length of the name. The buffer for "name" must be at least MPI_MAX_PROCESSOR_NAME characters in size. What is returned into "name" is implementation dependent - may not be the same as the output of the "hostname" or "host" shell commands.

```
MPI_Get_processor_name (&name,&resultlength)
MPI_GET_PROCESSOR_NAME (name,resultlength,ierr)
```

MPI Finalize

Terminates the MPI execution environment. This function should be the last MPI routine called in every MPI program - no other MPI routines may be called after it.

[MPI Finalize ()]

MPI_Finalize ()
MPI_FINALIZE (ierr)

Timers

- C: double MPI_Wtime(void)
 - Returns an elapsed wall clock time in seconds (double precision) on the calling processor.
- Time is measured in seconds
 - Time to perform a task is measured by consulting the time before and after



C Language - Environment Management Routines

```
// required MPI include file
 1
 2
      #include "mpi.h"
      #include <stdio.h>
 3
 4
 5
      int main(int argc, char *argv[]) {
 6
      int numtasks, rank, len, rc;
 7
      char hostname[MPI MAX PROCESSOR NAME];
 8
 9
      // initialize MPI
      MPI Init(&argc, &argv);
10
11
12
      // get number of tasks
      MPI Comm size (MPI COMM WORLD, &numtasks);
13
14
15
      // get my rank
      MPI Comm rank (MPI COMM WORLD, &rank);
16
17
18
      // this one is obvious
      MPI Get processor name (hostname, &len);
19
      printf ("Number of tasks= %d My rank= %d Running on %s\n", numtasks, rank, hostname);
20
21
22
23
           // do some work with message passing
24
25
      // done with MPI
26
      MPI Finalize();
27
28
```



Fortran - Environment Management Routines

```
1
      program simple
 2
 3
      ! required MPI include file
 4
      include 'mpif.h'
 5
 6
      integer numtasks, rank, len, ierr
7
      character (MPI MAX PROCESSOR NAME) hostname
8
9
      ! initialize MPI
10
      call MPI INIT (ierr)
11
      ! get number of tasks
12
13
      call MPI COMM SIZE (MPI COMM WORLD, numtasks, ierr)
14
15
      ! get my rank
      call MPI COMM RANK (MPI COMM WORLD, rank, ierr)
16
17
18
      ! this one is obvious
      call MPI GET PROCESSOR NAME (hostname, len, ierr)
19
      print *, 'Number of tasks=', numtasks,' My rank=', rank,' Running on=', hostname
20
21
22
23
           ! do some work with message passing
24
25
      ! done with MPI
26
27
      call MPI FINALIZE (ierr)
28
29
      end
```

(2) Point to Point Communication Routines

- A simplest form of message passing
- One process sends a message to another
- Several variations on how sending a message can interact with execution of the sub-program

Point-to-Point Communication Routines			
MPI Bsend	MPI Bsend init	MPI Buffer attach	
MPI Buffer detach	MPI Cancel	MPI Get count	
MPI Get elements	MPI_Ibsend	MPI Iprobe	
MPI Irecv	MPI Irsend	MPI Isend	
MPI Issend	MPI_Probe	MPI Recv	
MPI Recv init	MPI Request free	MPI Rsend	
MPI Rsend init	MPI Send	MPI Send init	
MPI Sendrecv	MPI Sendrecv replace	MPI Ssend	
MPI Ssend init	MPI Start	MPI Startall	
MPI Test	MPI Test cancelled	MPI Testall	
MPI Testany	MPI Testsome	MPI Wait	
MPI Waitall	MPI Waitany	MPI Waitsome	

Types of Point-to-Point Operations:

- MPI point-to-point operations typically involve message passing between two, and only two, different MPI tasks. One task is performing a send operation and the other task is performing a matching receive operation.
- There are different types of send and receive routines used for different purposes. For example:
 - Blocking send / blocking receive
 - Non-blocking send / non-blocking receive
 - Synchronous send
 - Buffered send
 - Ready send
 - Combined send/receive
 - Any type of send routine can be paired with any type of receive routine.
- MPI also provides several routines associated with send receive operations, such as those used to wait for a message's arrival or probe to find out if a message has arrived.

Point-to-Point variations

- Blocking operations
 - only return from the call when operation has completed
- Non-blocking operations
 - return straight away can test/wait later for completion
 - The terms *blocking* and *non-blocking* describe the behavior of operations from the *local* view of the executing process, without taking the effects on other processes into account.
 - From a global viewpoint, it is reasonable to distinguish between synchronous and asynchronous communications.

Blocking vs. Non-blocking:

 Most of the MPI point-to-point routines can be used in either blocking or non-blocking mode.

Blocking:

- A blocking send routine will only "return" after it is safe to modify the application buffer (your send data) for reuse. Safe means that modifications will not affect the data intended for the receive task. Safe does not imply that the data was actually received it may very well be sitting in a system buffer.
- A blocking send can be synchronous which means there is handshaking occurring with the receive task to confirm a safe send.
- A blocking send can be asynchronous if a system buffer is used to hold the data for eventual delivery to the receive.
- A blocking receive only "returns" after the data has arrived and is ready for use by the program.

Non-blocking:

- Non-blocking send and receive routines behave similarly they will return almost immediately. They do not wait for any communication events to complete, such as message copying from user memory to system buffer space or the actual arrival of message.
- Non-blocking operations simply "request" the MPI library to perform the operation when it is able. The user can not predict when that will happen.
- It is unsafe to modify the application buffer (your variable space) until
 you know for a fact the requested non-blocking operation was actually
 performed by the library. There are "wait" routines used to do this.
- Non-blocking communications are primarily used to overlap computation with communication and exploit possible performance gains.

```
Non-blocking Send
             Blocking Send
myvar = 0;
                                        myvar = 0;
for (i=1; i<ntasks; i++) {
                                        for (i=1; i<ntasks; i++) {
  task = i;
                                           task = i;
  MPI_Send (&myvar ... task ...);
                                           MPI_Isend (&myvar ... task ...);
  myvar = myvar + 2
                                           myvar = myvar + 2;
                                           /* do some work */
  /* do some work */
                                           MPI Wait (...);
               Safe. Why?
                                                      Unsafe. Why?
```

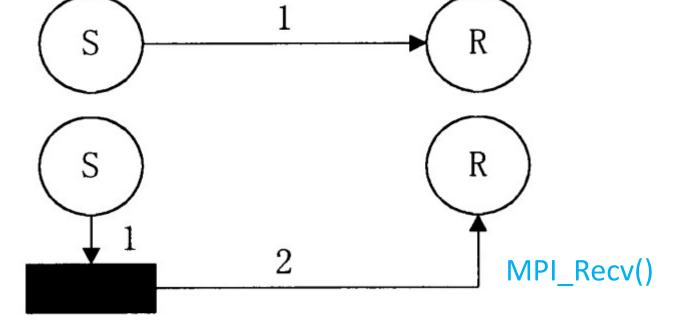
Communication Modes for both blocking and non-blocking communication operations

Standard

MPI_Send()

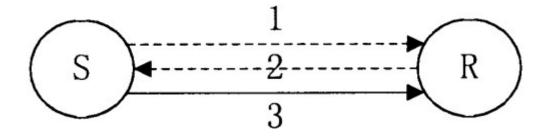
Buffering

MPI_Bsend()



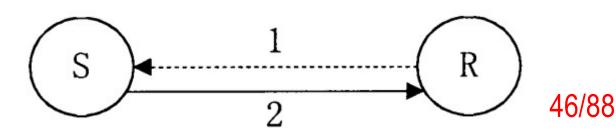
Synchronous

MPI_Ssend()



Ready

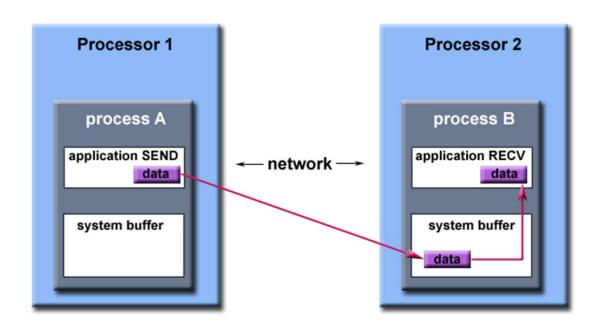
MPI_Rsend()



Buffering:

- In a perfect world, every send operation would be perfectly synchronized with its matching receive. This is rarely the case. Somehow or other, the MPI implementation must be able to deal with storing data when the two tasks are out of sync.
- Consider the following two cases:
 - A send operation occurs 5 seconds before the receive is ready where is the message while the receive is pending?
 - Multiple sends arrive at the same receiving task which can only accept one send at a time - what happens to the messages that are "backing up"?
- The MPI implementation (not the MPI standard) decides what happens to data in these types of cases. Typically, a system buffer area is reserved to hold data in transit. For example:

- System buffer space is:
 - Opaque to the programmer and managed entirely by the MPI library
 - A finite resource that can be easy to exhaust
 - Often mysterious and not well documented
 - Able to exist on the sending side, the receiving side, or both
 - Something that may improve program performance because it allows send receive operations to be asynchronous.
- User managed address space (i.e. your program variables) is called the application buffer. MPI also provides for a user managed send buffer.

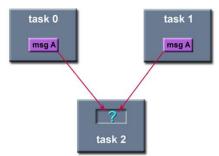


```
MPI Comm comm=MPI COMM WORLD;
MPI Init(&argc,&argv);
MPI_Comm(comm,&rank);
MPI Pack size(7,MPI CHAR,comm,&s1);
MPI_Pack_size(2,MPI_DOUBLE,comm,&s2);
 buffersize=2*MPI_BSEND_OVERHEAD+s1+s2;
 buf=(char*)malloc(buffersize);
MPI Buffer attach(buf,buffersize);
if(rank==src){
MPI Bsend(msg1,7,MPI CHAR,dest,tag,comm);
MPI Bsend(msg2,2,MPI DOUBLE,dest,tag,comm);
if(rank==dest){
       MPI Recv(rmsg1,7,MPI CHAR,src,tag,comm,MPI STATUS IGNORE);
      MPI Recv(rmsg2,2,MPI DOUBLE,src,tag,comm,MPI STATUS IGNORE);
  MPI_Buffer_detach(&buf,&buffersize);
 free(buf);
  MPI Finalize();
  return 0;
                                                    MPI 49/88
```

Example of

MPI Bsend()

Order and Fairness:



Order:

- MPI guarantees that messages will not overtake each other.
- If a sender sends two messages (Message 1 and Message 2) in succession to the same destination, and both match the same receive, the receive operation will receive Message 1 before Message 2.
- If a receiver posts two receives (Receive 1 and Receive 2), in succession, and both are looking for the same message, Receive 1 will receive the message before Receive 2.
- Order rules do not apply if there are multiple threads participating in the communication operations.

Fairness:

- MPI does not guarantee fairness it's up to the programmer to prevent "operation starvation".
- Example: task 0 sends a message to task 2. However, task 1 sends a competing message that matches task 2's receive. Only one of the sends will complete.

MPI primitive	blocking	non-blocking
Standard Send	MPI_Send	MPI_Isend
Synchronous Send	MPI_ Ssend	MPI_ Issend
Buffered Send	MPI_ Bsend	MPI_ Ibsend
Ready Send	MPI_ Rsend	MPI_Irsend
Receive	MPI_Recv	MPI_Irecv
Completion Check	MPI_Wait	MPI_Test

	Point-to-point	Collective
Blocking	MPI_Send() MPI_Ssend() MPI_Bsend() MPI_Recv()	MPI_Barrier() MPI_Bcast() MPI_Scatter()/ MPI_Gather() MPI_Reduce() MPI_Reduce_scatter() MPI_Allreduce()
Nonblocking	MPI_Isend() MPI_Irecv() MPI_Wait()/MPI_Test() MPI_Waitany()/ MPI_Testany() MPI_Waitsome()/ MPI_Testsome() MPI_Waitall()/ MPI_Testall()	N/A

 MPI's communication modes and a nonexhaustive overview of the corresponding subroutines.

MPI Message Passing Routine Arguments

 MPI point-to-point communication routines generally have an argument list that takes one of the following formats:

Blocking sends	MPI_Send(buffer,count,type,dest,tag,comm)	
Non-blocking sends	MPI_Isend(buffer,count,type,dest,tag,comm,request	
Blocking receive	MPI_Recv(buffer,count,type,source,tag,comm,status)	
Non-blocking receive	MPI_Irecv(buffer,count,type,source,tag,comm,request)	

Buffer

Program (application) address space that references the data that is to be sent or received. In most cases, this is simply the variable name that is be sent/received. For C programs, this argument is passed by reference and usually must be prepended with an ampersand: &var1

Data Count

 Indicates the number of data elements of a particular type to be sent.

Data Type

 For reasons of portability, MPI predefines its elementary data types. The table below lists those required by the standard.

C Data Types			Fortran Data Types		
MPI_CHAR	char	MPI_CHARACTER	character(1)		
MPI_WCHAR	wchar_t - wide character				
MPI_SHORT	signed short int				
MPI_INT	signed int	MPI_INTEGER MPI_INTEGER1 MPI_INTEGER2 MPI_INTEGER4	integer integer*1 integer*2 integer*4		
MPI_LONG	signed long int				
MPI_LONG_LONG_INT MPI_LONG_LONG	signed long long int				
MPI_SIGNED_CHAR	signed char				
MPI_UNSIGNED_CHAR	unsigned char				
MPI_UNSIGNED_SHORT	unsigned short int				
MPI_UNSIGNED	unsigned int				
MPI_UNSIGNED_LONG	unsigned long int				
MPI_UNSIGNED_LONG_LONG	unsigned long long int				
MPI_FLOAT	float	MPI_REAL MPI_REAL2 MPI_REAL4 MPI_REAL8	real real*2 real*4 real*8		

MPI_DOUBLE	double	MPI_DOUBLE_PRECISION	double precision
MPI_LONG_DOUBLE	long double		
MPI_C_COMPLEX MPI_C_FLOAT_COMPLEX	float _Complex	MPI_COMPLEX	complex
MPI_C_DOUBLE_COMPLEX	double _Complex	MPI_DOUBLE_COMPLEX	double complex
MPI_C_LONG_DOUBLE_COMPLEX	long double _Complex		
MPI_C_BOOL	_Bool	MPI_LOGICAL	logical
MPI_INT8_T MPI_INT16_T MPI_INT32_T MPI_INT64_T	int8_t int16_t int32_t int64_t		
MPI_UINT8_T MPI_UINT16_T MPI_UINT32_T MPI_UINT64_T	uint8_t uint16_t uint32_t uint64_t		
MPI_BYTE	8 binary digits	MPI_BYTE	8 binary digits
MPI_PACKED	data packed or unpacked with MPI_Pack()/ MPI_Unpack	MPI_PACKED	data packed or unpacked with MPI_Pack()/ MPI_Unpack

Notes:

- Programmers may also create their own data types (see <u>Derived Data Types</u>).
- MPI_BYTE and MPI_PACKED do not correspond to standard C or Fortran types.
- Types shown in GRAY FONT are recommended if possible.
- Some implementations may include additional elementary data types (MPI_LOGICAL2, MPI_COMPLEX32, etc.). Check the MPI header file.

Destination

 An argument to send routines that indicates the process where a message should be delivered. Specified as the rank of the receiving process.

Source

 An argument to receive routines that indicates the originating process of the message. Specified as the rank of the sending process. This may be set to the wild card MPI_ANY_SOURCE to receive a message from any task.

Tag

Arbitrary non-negative integer assigned by the programmer to uniquely identify a message. Send and receive operations should match message tags. For a receive operation, the wild card MPI_ANY_TAG can be used to receive any message regardless of its tag. The MPI standard guarantees that integers 0-32767 can be used as tags, but most implementations allow a much larger range than this.

Communicator

 Indicates the communication context, or set of processes for which the source or destination fields are valid. Unless the programmer is explicitly creating new communicators, the predefined communicator MPI_COMM_WORLD is usually used.

Status

For a receive operation, indicates the source of the message and the tag of the message, MPI_error. In C, this argument is a pointer to a predefined structure MPI_Status (ex. stat.MPI_SOURCE stat.MPI_TAG). In Fortran, it is an integer array of size MPI_STATUS_SIZE (ex. stat(MPI_SOURCE) stat(MPI_TAG)). Additionally, the actual number of bytes received is obtainable from Status via the MPI_Get_count routine. The constants MPI_STATUS_IGNORE and MPI_STATUSES_IGNORE can be substituted if a message's source, tag or size will be queried later.

- Status is useful when one receiver receives different messages with different size and different tag from some processes.
- e.g. if multiple client processes send messages to the server process, the server process adopts different service according to the tags.

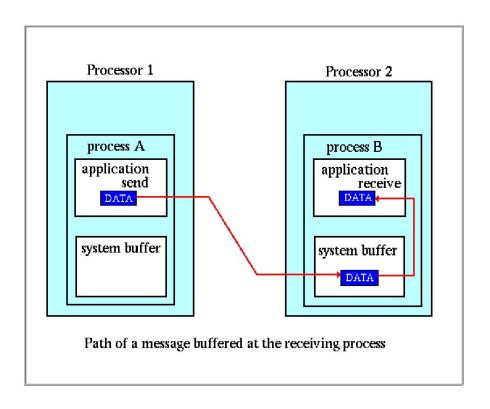
```
while (true){
    MPI_Recv(received_request,100,MPI_BYTE,MPI_Any_source,MPI_Any_tag,comm,&Status);
    switch (Status.MPI_Tag) {
        case tag_0: perform service type0;
        case tag_1: perform service type1;
        case tag_2: perform service type2;
    }
}
```

Request

Used by non-blocking send and receive operations. Since non-blocking operations may return before the requested system buffer space is obtained, the system issues a unique "request number". The programmer uses this system assigned "handle" later (in a WAIT type routine) to determine completion of the non-blocking operation. In C, this argument is a pointer to a predefined structure MPI_Request. In Fortran, it is an integer.

Message

- Messages are packets of data moving between sub-programs.
- Messge buffer (content) (buf, count, datatype)
- Message envelope (dest, tag, comm)



Common Blocking Message Passing Routines

MPI Send

__Basic blocking send operation. Routine returns only after the application buffer in the sending task is free for reuse. Note that this routine may be implemented differently on different systems. The MPI standard permits the use of a system buffer but does not require it. Some implementations may actually use a synchronous send (discussed below) to implement the basic blocking send.

```
MPI_Send (&buf,count,datatype,dest,tag,comm)
MPI_SEND (buf,count,datatype,dest,tag,comm,ierr)
```

```
1 <type> buf(*)
                                                        int MPI_Send(
2 integer :: count, datatype, dest, tag, comm, ierror
                                                               void*
                                                                                 msg_buf_p
                                                                                                  /* in */.
3 call MPI Send(buf,
                      ! message buffer
                                                                                 msq_size
                                                                                                 /* in */.
                                                               int
                      ! # of items
             count.
             datatype, ! MPI data type
                                                               MPI_Datatype
                                                                                 msg_type
                                                                                                  /* in */.
                      ! destination rank
             dest,
                                                                                 dest
                                                                                                  /* in */.
                                                               int
                      ! message tag (additional label)
             tag,
                                                               int
                                                                                                  /* in */.
                                                                                 tag
                      ! communicator
             comm,
                                                                                 communicator
                                                               MPI_Comm
                                                                                                  /* in */):
                      ! return value
             ierror)
```

```
1 <type> buf(*)
                                                      int MPI_Recv(
1 integer :: count, datatype, source, tag, comm,
                                                            void*
                                                                           msg_buf_p
                                                                                         /* out */,
3 integer :: status(MPI_STATUS_SIZE), ierror
                                                                           buf_size
 call MPI Recv (buf,
                                                            int
                                                                                         /* in */.
                      ! message buffer
                      ! maximum # of items
              count,
                                                            MPI_Datatype buf_type
                                                                                         /* in */.
              datatype, ! MPI data type
                                                                           source
                                                                                         /* in */.
                                                            int
              source, ! source rank
                                                            int
                                                                                       /* in */,
                                                                           tag
                      ! message tag (additional label)
              tag,
                                                                           communicator /* in */,
              comm,
                     ! communicator
                                                            MPI_Comm
              status, ! status object (MPI Status* in C)
                                                            MPI_Status*
                                                                           status_p
                                                                                         /* out */);
              ierror) ! return value
```

MPI Recv

Receive a message and block until the requested data is available in the application buffer in the receiving task.

```
MPI_Recv (&buf,count,datatype,source,tag,comm,&status)
MPI_RECV (buf,count,datatype,source,tag,comm,status,ierr)
```

Suppose process q calls MPI_Send with

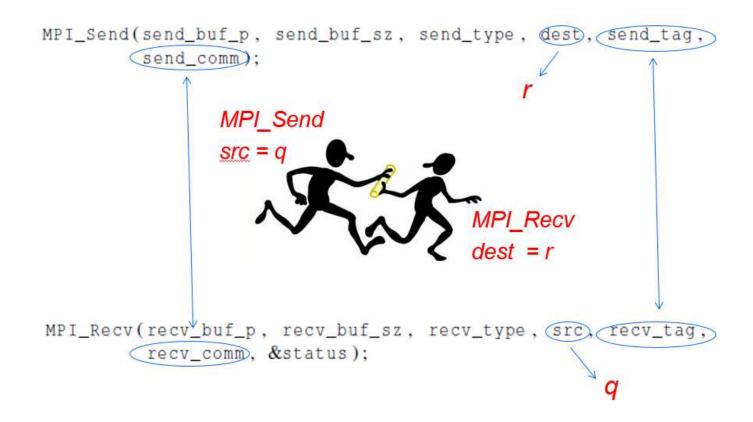
Also suppose that process r calls MPI_Recv with

```
MPI_Recv(recv_buf_p, recv_buf_sz, recv_type, src, recv_tag, recv_comm, &status);
```

Then the message sent by q with the above call to MPI_Send can be received by r with the call to MPI_Recv if

- recv_comm = send_comm,
- recv_tag = send_tag,
- dest = r, and
- src = q.

Message matching



• Are these conditions enough for the message to be successfully received?

If recv_type = send_type and recv_buf_sz \geq send_buf_sz, then the message sent by q can be successfully received by r.

Receiving messages

- A receiver can get a message without knowing:
 - the amount of data in the message,
 - the sender of the message,
 - or the tag of the message.

```
MPI_Recv(recv_buf_p, recv_buf_sz, recv_type, src, recv_tag, recv_comm, &status);

MPI_Status*

MPI_Status*

MPI_Status*

MPI_SOURCE

MPI_TAG

MPI_TAG

MPI_TAG

MPI_ERROR
```

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MPI Ssend

Synchronous blocking send: Send a message and block until the application buffer in the sending task is free for reuse and the destination process has started to receive the message.

```
MPI_Ssend (&buf,count,datatype,dest,tag,comm)
MPI_SSEND (buf,count,datatype,dest,tag,comm,ierr)
```

MPI Sendrecv

Send a message and post a receive before blocking. Will block until the sending application buffer is free for reuse and until the receiving application buffer contains the received message

Examples: Blocking Message Passing Routines

C Language - Blocking Message Passing Example

```
1
      #include "mpi.h"
 2
      #include <stdio.h>
 3
 4
      main(int argc, char *argv[]) {
 5
      int numtasks, rank, dest, source, rc, count, tag=1;
 6
      char inmsq, outmsq='x';
 7
      MPI Status Stat; // required variable for receive routines
 8
 9
      MPI Init (&argc, &argv);
10
      MPI Comm size (MPI COMM WORLD, &numtasks);
      MPI Comm rank (MPI COMM WORLD, &rank);
11
12
13
      // task 0 sends to task 1 and waits to receive a return message
14
      if (rank == 0) {
15
        dest = 1;
16
        source = 1:
17
        MPI Send(&outmsg, 1, MPI CHAR, dest, tag, MPI COMM WORLD);
18
        MPI Recv (&inmsq, 1, MPI CHAR, source, tag, MPI COMM WORLD, &Stat);
19
20
21
      // task 1 waits for task 0 message then returns a message
      else if (rank == 1) {
22
23
        dest = 0;
24
        source = 0;
        MPI Recv (&inmsg, 1, MPI CHAR, source, tag, MPI COMM WORLD, &Stat);
25
        MPI Send (&outmsq, 1, MPI CHAR, dest, taq, MPI COMM WORLD);
26
27
28
29
      // query recieve Stat variable and print message details
30
      MPI Get count (&Stat, MPI CHAR, &count);
      printf("Task %d: Received %d char(s) from task %d with tag %d \n",
31
             rank, count, Stat.MPI SOURCE, Stat.MPI TAG);
32
33
34
      MPI Finalize();
35
```

Fortran - Blocking Message Passing Example

```
1
      program ping
 2
      include 'mpif.h'
 3
      integer numtasks, rank, dest, source, count, tag, ierr
 4
      integer stat (MPI STATUS SIZE) ! required variable for receive routines
 5
      character inmsq, outmsq
 6
      outmsq = 'x'
7
      tag = 1
 8
9
      call MPI INIT(ierr)
10
11
      call MPI COMM RANK (MPI COMM WORLD, rank, ierr)
      call MPI COMM SIZE (MPI COMM WORLD, numtasks, ierr)
12
13
      ! task 0 sends to task 1 and waits to receive a return message
14
1.5
      if (rank .eq. 0) then
16
         dest = 1
17
         source = 1
         call MPI SEND (outmsq, 1, MPI CHARACTER, dest, tag, MPI COMM WORLD, ierr)
18
19
         call MPI RECV (inmsq, 1, MPI CHARACTER, source, tag, MPI COMM WORLD, stat, ierr)
20
21
      ! task 1 waits for task 0 message then returns a message
22
      else if (rank .eq. 1) then
         dest = 0
23
24
         source = 0
25
         call MPI RECV (inmsq, 1, MPI CHARACTER, source, tag, MPI COMM WORLD, stat, err)
         call MPI SEND (outmsq, 1, MPI CHARACTER, dest, taq, MPI COMM WORLD, err)
26
27
      endif
28
29
      ! query recieve Stat variable and print message details
      call MPI GET COUNT(stat, MPI CHARACTER, count, ierr)
30
31
      print *, 'Task ', rank,': Received', count, 'char(s) from task', &
               stat (MPI SOURCE), 'with tag', stat (MPI TAG)
32
33
34
      call MPI FINALIZE (ierr)
35
36
      end
```

Non-blocking Message Passing Routines

MPI_Isend

Identifies an area in memory to serve as a send buffer. Processing continues immediately without waiting for the message to be copied out from the application buffer. A communication request handle is returned for handling the pending message status. The program should not modify the application buffer until subsequent calls to MPI_Wait or MPI_Test indicate that the non-blocking send has completed.

```
MPI_Isend (&buf,count,datatype,dest,tag,comm,&request)
MPI_ISEND (buf,count,datatype,dest,tag,comm,request,ierr)
```

```
1 <tvpe> buf(*)
2 integer :: count, datatype, dest, tag, comm, request, ierror
 call MPI Isend (buf,
                            ! message buffer
                count, ! # of items
                datatype, ! MPI data type
                           ! destination rank
                dest,
                           ! message tag
                tag,
                            ! communicator
                comm,
                request,
                            ! request handle (MPI Request* in C)
                ierror)
                            ! return value
```

MPI_Irecv

Identifies an area in memory to serve as a receive buffer. Processing continues immediately without actually waiting for the message to be received and copied into the the application buffer. A communication request handle is returned for handling the pending message status. The program must use calls to MPI_Wait or MPI_Test to determine when the non-blocking receive operation completes and the requested message is available in the application buffer.

```
MPI_Irecv (&buf,count,datatype,source,tag,comm,&request)
MPI_IRECV (buf,count,datatype,source,tag,comm,request,ierr)
```

```
1 <type> buf(*)
2 integer :: count, datatype, source, tag, comm, request, ierror
 call MPI Irecv (buf,
                          ! message buffer
                count,
                          ! # of items
                datatype, ! MPI data type
                source, ! source rank
                          ! message tag
                tag,
                comm,
                           ! communicator
                          ! request handle
               request,
                ierror)
                           ! return value
```

MPI_Wait
MPI_Waitany
MPI_Waitall
MPI_Waitsome

MPI_Wait blocks until a specified non-blocking send or receive operation has completed. For multiple non-blocking operations, the programmer can specify any, all or some completions.

```
while (Not Done){
  if (X==Xbuf0)
      {X=Xbuf1; Y=Ybuf1; Xin=Xbuf0; Yout=Ybuf0;}
  else {X=Xbuf0; Y=Ybuf0; Xin=Xbuf1; Yout=Ybuf1;}
  MPI Irevc(Xin, ..., recv handle);
  MPI Isend(Yout, ..., send_handle);
  Y=Q(X);
                /* overlap comp. and comm.*/
  MPI Wait(recv handle,recv status);
  MPI Wait(send_handle,send_status);
```

MPI Issend

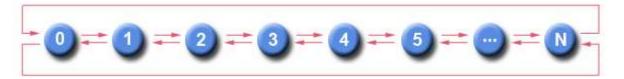
Non-blocking synchronous send. Similar to MPI Isend(), except MPI Wait() or MPI Test() indicates when the destination process has received the message.

```
MPI_Issend (&buf,count,datatype,dest,tag,comm,&request)
MPI_ISSEND (buf,count,datatype,dest,tag,comm,request,ierr)
```

MPI_Test checks the status of a specified non-blocking send or receive operation. The "flag" parameter is returned logical true (1) if the operation has completed, and logical false (0) if not. MPI_test will not be blocked. For multiple non-blocking operations, the programmer can specify any, all or some completions.

Examples: Non-blocking Message Passing Routines

Nearest neighbor exchange in a ring topology



C Language - Non-blocking Message Passing Example

```
1
      #include "mpi.h"
 2
      #include <stdio.h>
 3
 12
      main(int argc, char *argv[]) {
 5
      int numtasks, rank, next, prev, buf[2], tag1=1, tag2=2;
 6
      MPI Request reqs[4]; // required variable for non-blocking calls
 7
      MPI Status stats[4]; // required variable for Waitall routine
 8
 9
      MPI Init (&argc, &argv);
10
      MPI Comm size (MPI COMM WORLD, &numtasks);
11
      MPI Comm rank (MPI COMM WORLD, &rank);
12
13
      // determine left and right neighbors
14
      prev = rank-1;
15
      next = rank+1;
16
      if (rank == 0) prev = numtasks - 1;
      if (rank == (numtasks - 1)) next = 0;
17
18
19
      // post non-blocking receives and sends for neighbors
20
      MPI Irecv(&buf[0], 1, MPI INT, prev, tag1, MPI COMM WORLD, &reqs[0]);
21
      MPI Irecv (&buf[1], 1, MPI INT, next, tag2, MPI COMM WORLD, &regs[1]);
22
23
      MPI Isend (&rank, 1, MPI INT, prev, tag2, MPI COMM WORLD, &regs[2]);
24
      MPI Isend (&rank, 1, MPI INT, next, tag1, MPI COMM WORLD, &reqs[3]);
25
26
         // do some work while sends/receives progress in background
27
28
      // wait for all non-blocking operations to complete
29
      MPI Waitall (4, regs, stats);
30
31
         // continue - do more work
32
33
      MPI Finalize();
34
```

Fortran - Non-blocking Message Passing Example

```
1
      program ringtopo
 2
      include 'mpif.h'
 3
 4
      integer numtasks, rank, next, prev, buf(2), tag1, tag2, ierr
5
      integer regs (4) I required variable for non-blocking calls
 6
      integer stats (MPI STATUS SIZE, 4) ! required variable for WAITALL routine
7
      tag1 = 1
8
      tag2 = 2
9
10
      call MPI INIT(ierr)
11
      call MPI COMM RANK (MPI COMM WORLD, rank, ierr)
12
      call MPI COMM SIZE (MPI COMM WORLD, numtasks, ierr)
13
14
      ! determine left and right neighbors
15
      prev = rank - 1
16
      next = rank + 1
17
      if (rank .eq. 0) then
18
         prev = numtasks - 1
19
      endif
20
      if (rank .eq. numtasks - 1) then
21
         next = 0
22
      endif
23
24
      ! post non-blocking receives and sends for neighbors
25
      call MPI IRECV(buf(1), 1, MPI INTEGER, prev, tag1, MPI COMM WORLD, reqs(1), ierr)
26
      call MPI IRECV(buf(2), 1, MPI INTEGER, next, tag2, MPI COMM WORLD, regs(2), ierr)
27
28
      call MPI ISEND (rank, 1, MPI INTEGER, prev, tag2, MPI COMM WORLD, regs(3), ierr)
29
      call MPI ISEND (rank, 1, MPI INTEGER, next, tag1, MPI COMM WORLD, regs(4), ierr)
30
31
         ! do some work while sends/receives progress in background
32
33
      ! wait for all non-blocking operations to complete
34
      call MPI WAITALL (4, reqs, stats, ierr);
35
36
         ! continue - do more work
37
38
      call MPI FINALIZE (ierr)
39
40
      end
```

Example1: MPI Send/Receive a Character

```
// mpi com.c
#include <mpi.h>
#include <stdio.h>
int main(int argc, char *argv[])
int numtasks, rank, dest, source, rc, tag=1;
char inmsg, outmsg='X';
MPI Status Stat;
MPI Init(&argc,&argv);
MPI Comm size(MPI COMM WORLD, &numtasks);
MPI Comm rank(MPI COMM WORLD, &rank);
if (rank == 0) {
 dest = 1:
rc = MPI_Send(&outmsg, 1, MPI_CHAR, dest, tag, MPI_COMM_WORLD);
 printf("Rank0 sent: %c\n", outmsg);
source = 1:
 rc = MPI Recv(&inmsg, 1, MPI CHAR, source, tag, MPI COMM WORLD, &Stat);
```

Example1: MPI Send/Receive a Character(cont.)

Execution Demo

- mpicc –o mpi_com mpi_com.c
- [raj@manjra mpi]\$ mpirun -np 2 mpi_com

Rank0 sent: X

Rank1 received: X

Example 2: Ping Pong

- 1. Write a program in which two processes repeatedly pass a message back and forth.
- 2. Insert timing calls to measure the time taken for one message.
- 3. Investigate how the time taken to exchange messages varies with the size of the message.

Example 2: A simple Ping Pong.c (cont.)

```
#include <mpi.h>
#include <stdio.h>
int main(int argc, char *argv[])
int numtasks, rank, dest, source, rc, tag=1;
char inmsg, outmsg='X';
char pingmsg[10]; char pongmsg[10]; char buff[100];
MPI Status Stat;
strcpy(pingmsg, "ping");
strcpy(pongmsg, "pong");
MPI Init(&argc,&argv);
MPI Comm size(MPI COMM WORLD, &numtasks);
MPI Comm rank(MPI COMM WORLD, &rank);
                                                               Why + 1?
if (rank == 0) { /* Send Ping, Receive Pong */
 dest = 1;
 source = 1;
 rc = MPI Send(pingmsg, strlen(pingmsg)+1, MPI CHAR, dest, tag, MPI COMM WORLD);
 rc = MPI Recv(buff, strlen(pongmsg)+1, MPI CHAR, source, tag, MPI COMM WORLD, &Stat);
 printf("Rank0 Sent: %s & Received: %s\n", pingmsg, buff);
```

Example 2: A simple Ping Pong.c (cont..)

```
else if (rank == 1) { /* Receive Ping, Send Pong */
 dest = 0;
 source = 0;
 rc = MPI_Recv(buff, strlen(pingmsg)+1, MPI_CHAR, source, tag,
  MPI_COMM_WORLD, &Stat);
 printf("Rank1 received: %s & Sending: %s\n", buff, pongmsg);
 rc = MPI_Send(pongmsg, strlen(pongmsg)+1, MPI_CHAR, dest, tag,
  MPI COMM WORLD);
MPI Finalize();
```

Example 3.1: Calculation of π

return(4.0/(1.0+x*x));

```
#include "mpi.h"
#include <stdio.h>
#include <math.h>
double f(double x);/* Definition of f(x) */
```

```
f(x) = 4/(1+x^2)
\int_0^1 f(x)dx = \pi
```

```
\pi \approx \sum_{i=1}^{n} f(\frac{2 \times i - 1}{2 \times N}) \times \frac{1}{N}= \frac{1}{N} \times \sum_{i=1}^{n} f(\frac{i - 0.5}{N})
```

```
int main (int argc,char * argv[])
{
    int done =0,n,myid,numprocs,i;
    double PI25DT=3.141592653589793238462643;
    double mypi,pi,h,sum,x;
    double startwtime=0.0,endwtime;
    int namelen;
    char processor_name[MPI_MAXPROCESSOR_NAME];
    MPI_Status status;
```

```
MPI_Init(&argc,&argv);
MPI_Comm_size(MPI_COMM_WORLD,&numprocs);
MPI_Comm_rank(MPI_COMM_WORLD,&myid);
MPI_Get_processor_name(processor_name,&namelen);
fprint(stdout,"Process %d of %d on % s\n",myid,numprocs,
  processor_name);
n=0;
if (myid==0)
    printf("Please give N=");
    scanf(&n);
    startwtime=MPI_Wtime();
    for (j=1;j<numprocs;j++)</pre>
      MPI_Send(&n,1,MPI_INT,j,99,MPI_COMM_WORLD);
```

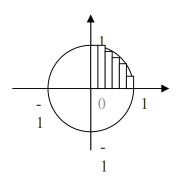
```
else
  MPI_Recv(&n,1,MPI_INT,MPI_ANY_SOURCE,99,MPI_COMM_
  WORLD, & status);
    h=1.0/(double) n;
    sum=0.0;
    for(i=myid+1;i<=n;i+=numprocs)</pre>
/* Each process computes some part of the rectangle, e.g. if
  numprocs is 4, 0-1 area is divided by 100 rectangles, then the 4
  processes compute the rectangles respectively as follows:
     P0 1, 5, 9, 13, ....., 97
     P1 2, 6, 10, 14, ....., 98
     P2 3, 7, 11, 15, ....., 99
     P3 4, 8, 12, 16, ....., 100 */
```

```
x=h*((double)i-0.5);
      sum+=f(x);
    mypi=h*sum; /* part of sum for each process*/
/* Accumulate all the part of sum to obtain the area of all the
rectangles, this area is the approximate value of PI.*/
  if (myid != 0)
  MPI_Send(&mypi,1,MPI_DOUBLE,0,myid,MPI_COMM_WORLD);
  else
    pi=0.0;
    pi=pi+mypi;
```

```
for (j=1;j<numprocs;j++)
     MPI_Recv(&mypi,1,MPI_DOUBLE,MPI_ANY_SOURCE,
            MPI_ANY_TAG,MPI_COMM_WORLD,&status);
     pi=pi+mypi;
     printf("pi is approximately %.16f,Error is %.16f\n",
          pi,fabs(pi-PI25DT));
     endwtime=MPI_Wtime();
     printf("wall clock time=% f\n",endwtime-startwtime);
     fflush(stdout);
MPI_Finalize();
```

Example 3.2: Calculation of π

$$rac{1}{4}\pipprox\sum_{x=0}^{N-1}rac{1}{N}\sqrt{1-\left(rac{x}{N}
ight)^2}$$



```
1. #include<iostream>
2. #include"mpi.h"
3. #include<ctime>
4. #include<cmath>
5. using namespace std;
7. const int N = 1000000;
8. double start, finish;
9. int main(int argc, char* argv[])
10.{
11.
        MPI Init(&argc, &argv);
12.
        int numprocs, myid;
13.
        MPI Comm size(MPI COMM WORLD, &numprocs);
14.
        MPI Comm rank(MPI COMM WORLD, &myid);
15.
           start = MPI Wtime();
16.
        double partSum = 0.0;
        double pi = 0.0;
17.
18.
        for (int i = myid; i < N; i += numprocs)
19.
20.
                 partSum += sgrt(1 - (double(i) / N)*(double(i) / N)) / N;
21.
22.
        MPI Reduce(&partSum, &pi, 1, MPI DOUBLE, MPI SUM, 0,
   MPI COMM WORLD);
23.
24.
        cout << "Myid" << myid << ", partSum:" << partSum << endl;</pre>
        if (myid == 0)
25.
26.
27.
         pi *= 4.0;
28.
         finish = MPI Wtime();
         cout << " The value of pi:" << pi << endl;</pre>
29.
         cout<<"#"<<numprocs<<"run time:"<< finish - start<< endl;</pre>
30.
31.
32.
33.
        MPI Finalize();
34.
        return 0;
35.}
```

Thank you!