

## 诚信保证(Integrity commitment)

本人知晓我校考场规则和违纪处分条例的有关规定, 保证遵守考场规则, 诚实做人。 本人签字(Signature):

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## 西北工业大学考试试题 (A 卷)

2020 — 2021 学年第 2 学期

开课学院 School of Computer Science

课程 Compiler Principles/编译原理(英) (U10M12008.01)

学时 48 hours

考试日期 2021.6.27 考试时间 2 hours 小时 考试形式 ( 闭 ) 卷

Question	Q1/10	Q2/10	Q3/7	Q4/8	Q5/15	Q6/15	Q7/10	Q8/15	Q9/10	Sum of Scores
Scores										

考生班级 (Class ID)		学号 (Student ID)	2018380130	姓名 (Name)	Khan Md Shahedul Islam
<p><b>【Q1】</b> (10:3+7 scores) For grammar G[S]: <math>S \rightarrow BS \mid B@</math>, <math>B \rightarrow (BH)B \mid H</math>, <math>B \rightarrow \epsilon \mid b</math>, <math>H \rightarrow (H) \mid h \mid \epsilon</math> Answer the following questions: (1) Is this grammar a recursive grammar? Give the answer and the reason for your answer. (3 scores) (2) Given a string "h(b(h))@" , is it a legal sentence defined by this grammar? Please draw the parsing tree for the input? (7:4+3 scores).</p>					

## Answer to the Question: 1

(1)

When a grammar is recursive at least one production has some Non-terminal at both Left-Hand-Side and Right-Hand-Side of the production.

When I take a look at the question,

Non-terminal =  $\{S, B, H\}$

Terminal =  $\{ @, (, ), h \}$

Hereby, we see,

Production  $S \rightarrow B S B @$ , has a Non-terminal  $S$  (underlined)

on both its Left-Hand-Side and Right-Hand-Side.

Even though, there are other production, considering only one production is enough to

prove that it is recursive grammar.

Therefore, I can say the following grammar is a recursive grammar.

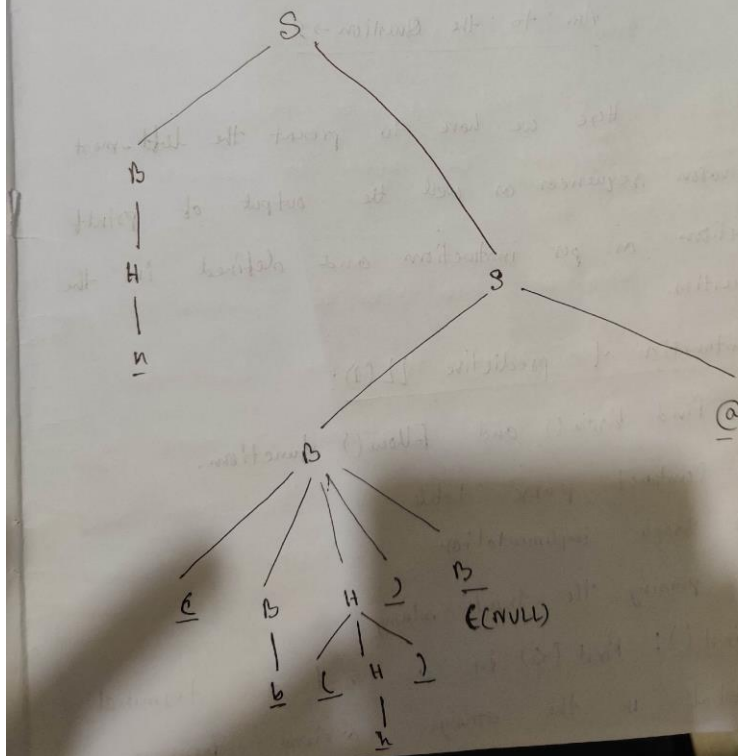
(2)

When we want to identify whether a string is a legal sentence defined by the grammar or not, we need to generate a parse tree for string.

When we are able to generate a parse tree for the string it means that the string is a legal sentence specified by the grammar and if not it means that it is not a legal sentence specified by the grammar.

In the following question we are given string "h(b(h))@"

Parse-tree for "h(b(h))@":



Since the parse tree for string "h(b(h))@" is generated,

As a result, the string is a legal sentence defined by the given grammar.

**【Q2】** (10 scores)

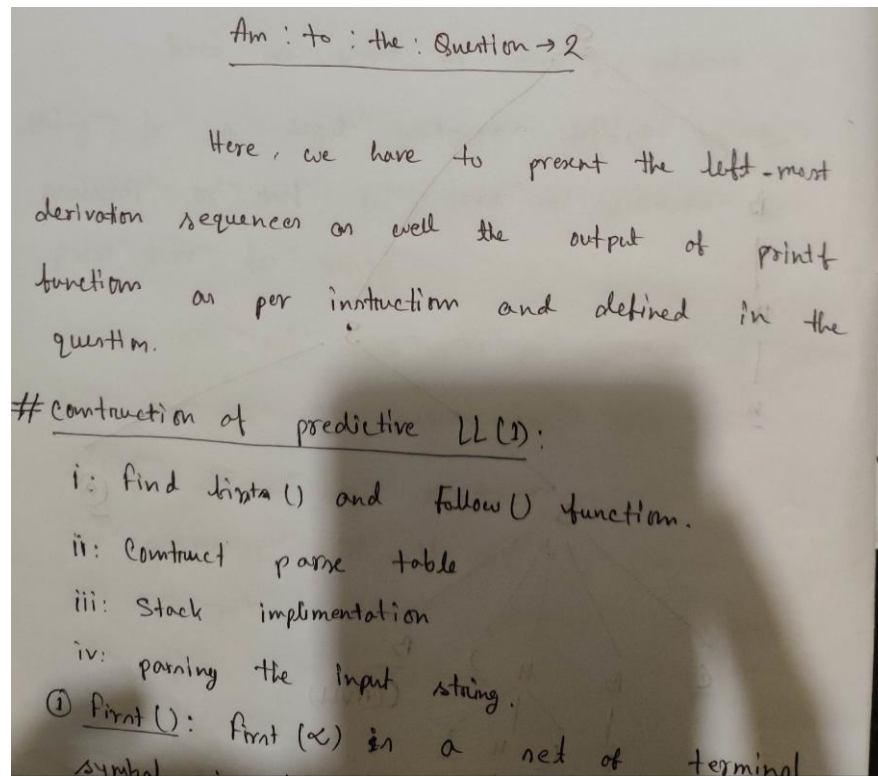
Given grammar G[S]:

- ①  $S \rightarrow A$  {printf( "1" );}
- ②  $A \rightarrow AaB$  {printf( "2" );}
- ③  $A \rightarrow \epsilon$  {printf( "3" );}
- ④  $B \rightarrow hB$  {printf( "4" );}
- ⑤  $B \rightarrow \epsilon$  {printf( "5" );}

Given "aah" as the input string, and supposed that we use LL(1) similar parsing

algorithm ( derivation based analysis), please present the left-most derivation sequences as well as the output of printf functions defined in the question. (5 scores)

Notation: here we suppose to execute the printf when we use the rule to do derivation.



Such as:  $A \rightarrow abc | def | ghi$   
then  $\text{first}(A) = \{a, b, g\}$

### Rules for creating First() function

i. For a production rule  $\alpha \rightarrow \epsilon$

$$\text{first}(\alpha) = \{\epsilon\}$$

ii. For any terminal symbol 'a'

$$\text{first}(a) = \{a\}$$

iii. For a production rule

$$\alpha \rightarrow y_1 y_2 y_3$$

Now, calculating  $\text{first}(x)$ :

i. If  $\epsilon \notin \text{first}(y_1)$ , then  $\text{first}(x) = \text{first}(y_1)$

ii. If  $\epsilon \in \text{first}(y_1)$ , then  $\text{first}(x) = \{\text{first}(y_1) - \epsilon\} \cup \{\text{first}(y_2 y_3)\}$

Calculating  $\text{first}(y_2, y_3)$ :

i. If  $\epsilon \notin \text{first}(y_2)$ , then  $\text{first}(y_2, y_3) = \text{first}(y_2)$

⑦

$\{ \text{first}(B) - \epsilon \} \cup \text{Follow}(A)$

Here, the most important point in construction of  $\text{first}()$  &  $\text{Follow}()$

- i.  $\epsilon$  May appear, in the first function of non-terminal.
- ii.  $\epsilon$  will never appear in the follow function of a non-terminal.
- iii. It is recommended to eliminate the left recursion from grammar, if present before calculating first and follow function.
- iv. We will calculate the follow function of a non-terminal by looking where it is present on RHS of a production rule.

Given.

$$S \rightarrow A_1$$

$$A \rightarrow AaB_2 \mid \epsilon_3$$

$$B \rightarrow hB_4$$

$$B \rightarrow \epsilon_5$$

Construction of  $\text{first}()$  &  $\text{follow}()$ :

<del>S</del>	$\text{first}()$	$\text{follow}()$
$S \rightarrow A$	$\{\epsilon, a\}$	$\{\$ \}$
$A \rightarrow AaB \mid \epsilon$	$\{\epsilon, a\}$	$\{\$, a\}$
$B \rightarrow hB \mid \epsilon$	$\{h, \epsilon\}$	$\{\$, a\}$

Parse table:

	a	h	\$
S	$S \rightarrow A$		$S \rightarrow A$
A	$A \rightarrow AaB$ $A \rightarrow \epsilon$		$A \rightarrow \epsilon$
B	$B \rightarrow \epsilon$	$B \rightarrow hB$	$B \rightarrow \epsilon$



③

Partialy Input String:

Stack	input String	Action
\$ S	a a h \$	$S \rightarrow A$
\$ A	a a h \$	$A \rightarrow A \circ B$
\$ B a A	a a h \$	$A \rightarrow A \circ B$
\$ B a B a A	a a h \$	$A \rightarrow \epsilon$
\$ B a B a	a a h \$	$B \rightarrow \epsilon$
\$ B a	a h \$	$B \rightarrow h B$
\$ B h	h \$	$B \rightarrow \epsilon$
\$	\$	Accept

Parse tree:

```

graph TD
    S --> A1[A = 1]
    A1 --> A2[A]
    A1 --> a1[a]
    A1 --> B1[B]
    A2 --> A3[A]
    A2 --> a2[a]
    A2 --> B2[B]
    B1 --> h1[h]
    B1 --> B3[B]
    A3 --> E1[E = 3]
    a2 --> E2[E = 5]
    B2 --> E3[E = 5]
    B3 --> E4[E = 5]
    
```

④

Therefore we get output on 1, 2, 2, 3, 5, 4, 5.

⑩

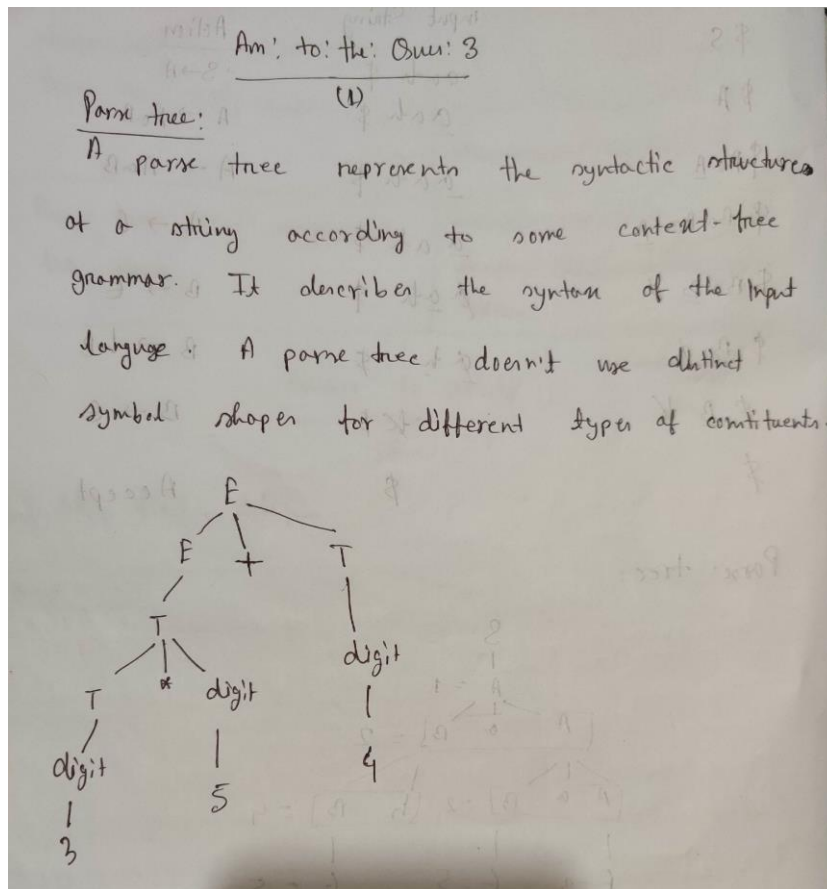
注：1. 答题请写在该试卷上相应位置。

2. 命题教师和审题教师姓名应在试卷存档时填写。

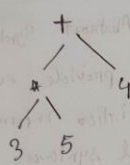
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**【Q3】** Answer the following questions: (7: 3.5+3.5 scores)

- (1) Describe the difference between parsing tree and abstract syntax tree.
- (2) Explain why intermediate representation (IR) were used in many compilers (explain the benefits!).



Syntax tree:



Abstract syntax tree describes the abstract syntactic structure of source code written in a programming language. It focuses on the rules rather than elements such as braces, semi-colons, that terminate statements in some languages.

Differences:

Parse Tree	Abstract Syntax Tree
Parse tree is a graphical representation of the replacement process in a derivation.	A syntax tree is the compact form of a parse tree.
Each interior node represents	Each interior node represents

a grammar rule. Each leaf node represents a derivation

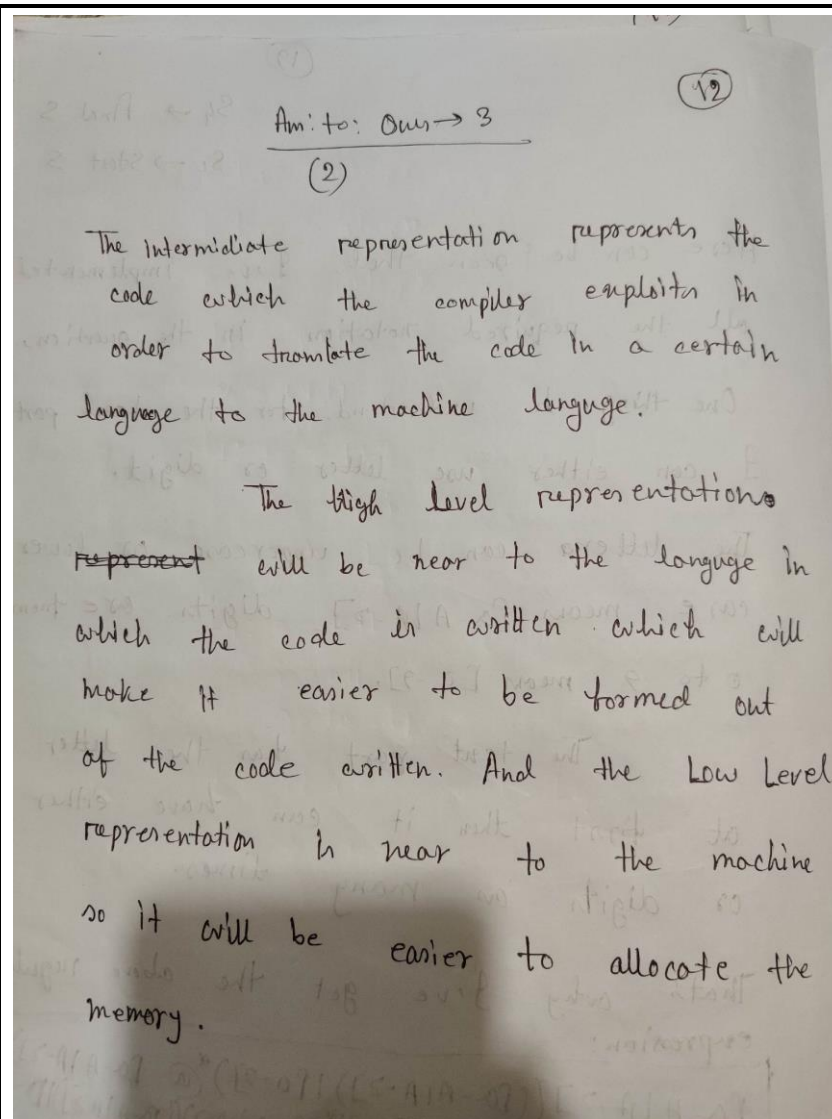
an operator. Each leaf node represents an operand.

Parse trees provide every characteristic information from the real syntax.

~~Syntax~~ Abstract Syntax trees do not provide every characteristic information from the real syntax.

Parse trees are comparatively less dense.

Abstract syntax trees are denser compare to parse trees.



**【Q4】** Please answer the following questions: (8: 4+4 scores)

(1) Given regular expression  $((a | b)^* | 01^*)^*$ , please draw the NFA.

(2) Write down the regular expression or NFA or DFA for the following language:

A language could send email to several email addresses at the same time, e.g:  
abcd@abc.com, xyz@nnn.edu, uvw@eee.edu.cn

The whole expression could be represented as:

{ abcd, xyz, uvw } @ { abc.com, nnn.edu, eee.edu.cn }

Notations:

All text parts (except @ ) could be defined only with letters and digits while started with at least one letter.

After @, at least one '.' must be included. That is abc@x.com is ok, but abc@ and abc@a and abc@a. are illegal.

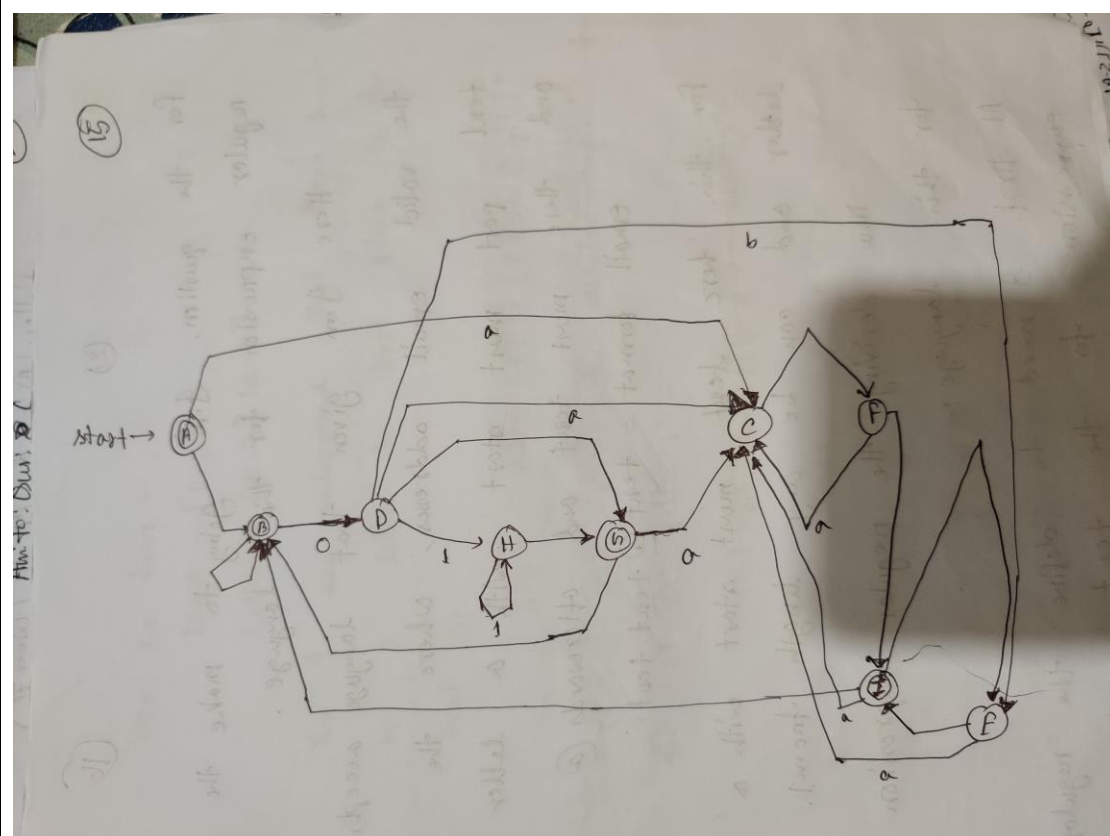
(14)

Answer: to the: 4

(9)

At first lets,

NFA state	DFA state	Type	0	1	a	b
{0, 1, 2, 3, 4, 7, 11, 15, 21}	A	accept	B		c	
{1, 2, 3, 4, 7, 11, 12, 13, 14, 20, 24}	B	accept	B	D	c	E
{25}	C		F			
{15, 16, 18}	D		G	H		
{3, 4, 7, 9, 10, 11}	E				c	
{3, 4, 6, 10, 11}	F				c	
{1, 2, 3, 4, 7, 11, 13, 14, 20, 21}	G	Accept	I		c	
{16, 17, 18}	H		D		c	
{1, 2, 3, 4, 7, 8, 11, 12, 13, 20}	I	Accept	B		c	E



(2)

(16)

for the question, I'm going to make the regular expression for this language.

Here I'm given that language accepts the valid email addresses, where the text part must start with a letter and there must text and afterwards @ email format = text@text.text

for this. here text must start with a letter and can be any length from 1.

Now, deriving the regular expression for this language:-

At first, I need to define the regular expression for the text part:-



Here, we have -

Digit = [0-9]

Letter = [A-Z][a-z]

Then I can understand that there must be a letter in first place in the text so,

text = ~~Letter~~ Letter (Letter Digit)\*

or I can write the regular expression for the text as follows:-

~~text = [a-zA-Z]([a-zA-Z][0-9])\*~~

or, I can write the regular expression for the text as follows:-

text = [a-zA-Z]([a-zA-Z][0-9])\*

So, I can see that after getting the first letter now this ~~right~~ either

(18)

can have the letters or digit or nothing, just one letter in the text.

The email is:-

email = text @ text . text

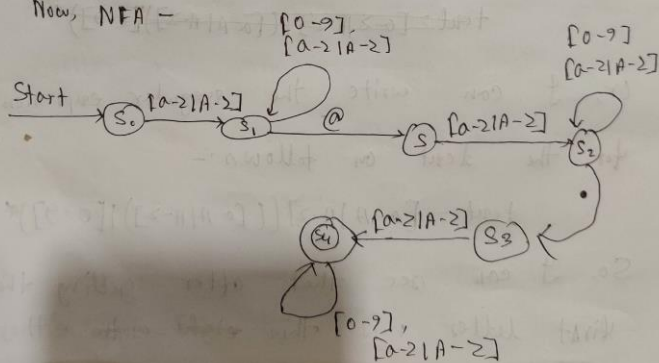
as we know that, text =  $[a-zA-Z]([a-zA-Z][0-9])^*$

So, the regular expression will be:

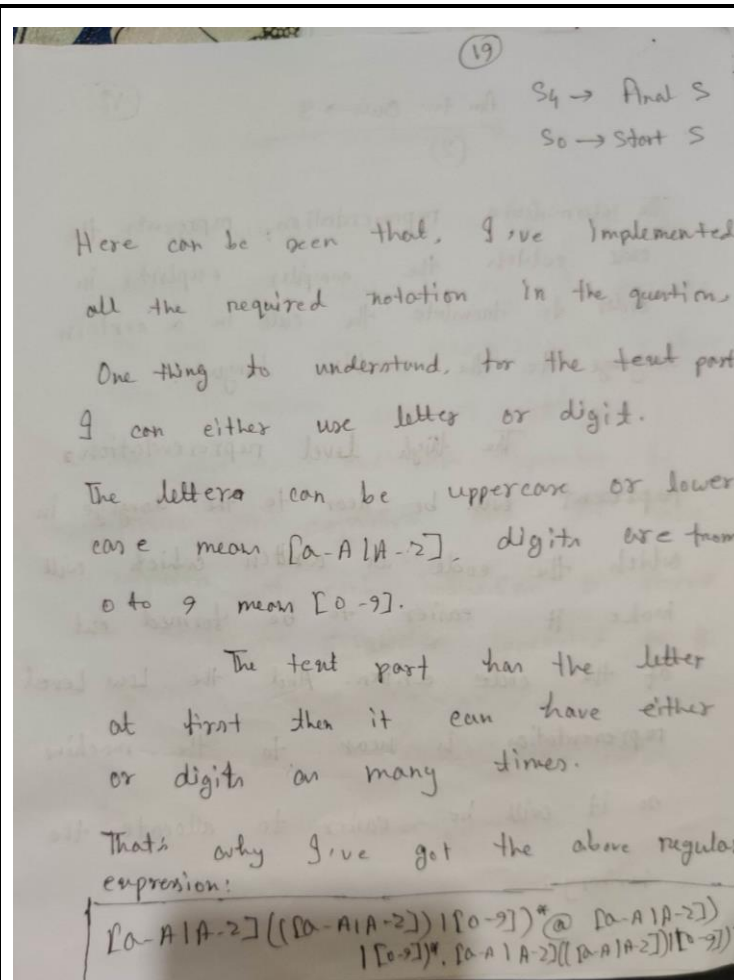
$[a-zA-Z]([a-zA-Z][0-9])^* @ [a-zA-Z]([a-zA-Z][0-9])^* .$

$[a-zA-Z]([a-zA-Z][0-9])^*$

Now, NFA -







**【Q5】** (15 scores) Given the following C program:

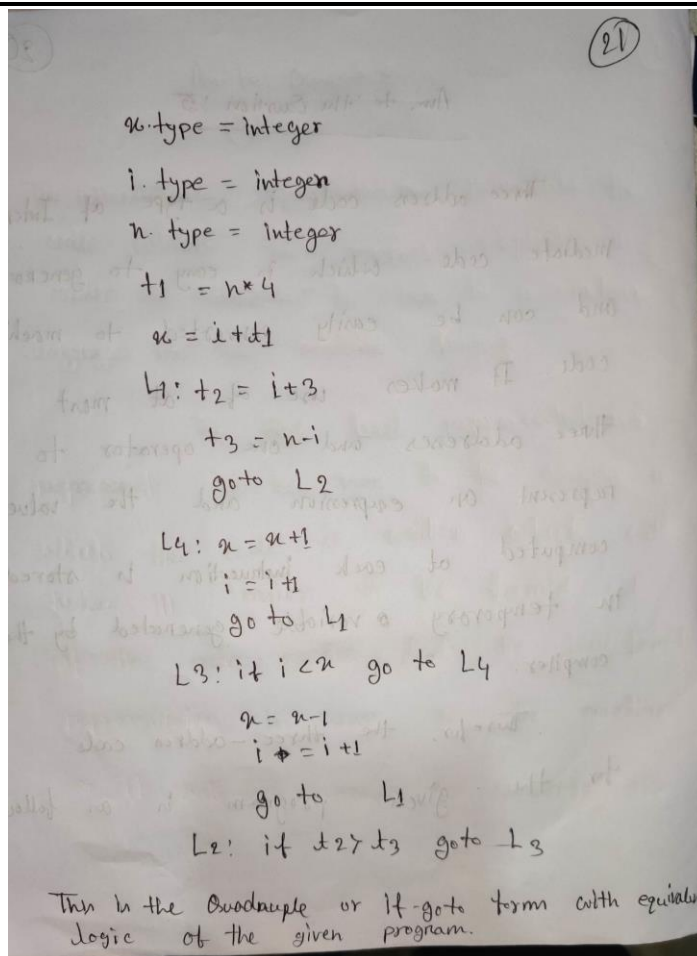
```
int x, i, n;
x=i+n*4;
while (i+3 > n-i)
{
    if (i<x) { x=x+1; }
    else
    {
        x=x-1;
    };
    i++;
}
```

Please present the Quadruple ( three-address code) or if-goto forms with equivalent logic to above program. ( 15 scores)

Ans. to the Question 15

Three address code is a type of Intermediate code which is easy to generate and can be easily converted to machine code. It makes use of at most three addresses and one operator to represent an expression and the value computed at each instruction is stored in temporary variable generated by the compiler.

Therefore, the three-address code for the given program is as follows:-



**【Q6】** (15 scores)

Given G[S] as following:

$S \rightarrow A=E$

$A \rightarrow H \text{ id} \mid \text{id}$

$H \rightarrow * \mid \epsilon$

$E \rightarrow \text{id} + E \mid A$

(1) Present the First set for each production rule. (3 scores)

(2) Present the Follow Set for each non-terminal symbol. (3 scores )

	First	Follow
$S \rightarrow A=E$		
$A \rightarrow H \text{ id}$		
$A \rightarrow \text{id}$		
$H \rightarrow \epsilon$		
$H \rightarrow *$		
$E \rightarrow \text{id} + E$		
$E \rightarrow A$		

(3) Present the LL(1) table. Is this grammar LL(1)? (5 +2 scores)

	id	=	+	*	#
S					
A					
H					
E					

(4) Given input string "a=b+\*c", present the derivation sequences according to the LL(1) table: (2 scores)

(22)

Ans to Ques: 6

(1)

$$S \rightarrow A = E$$

$$A \rightarrow H \text{ id } | \text{id}$$

$$H \rightarrow * | \epsilon$$

$$E \rightarrow \text{id} + E | A$$

Sol<sup>n</sup> - First  $\Rightarrow$

$$\text{First}(S) = \text{id}, *, \epsilon = \text{first}(A)$$

$$\text{first}(A) = \text{id}, *, \epsilon = \text{first}(H)$$

$$\text{first}(H) = *, \epsilon$$

$$\text{first}(E) = \text{id}, \text{first}(H)$$

$$= \text{id}, *, \epsilon$$

(2)

Follow(A) = It contain set of all terminals that may follow immediately right of A.

\* If A is valuable & A is stack symbol so

(22)

$$\text{Follow}(A) = \$ \text{ or } \# \text{ (Given \# in test)} \quad (1)$$

$\text{Follow}(S) = \{\$ \} = \{\#\}$   $\rightarrow$  no  $S$  on R.H.S of any production

$$\text{Follow}(A) = \text{first of } (= E) \text{ \& } \text{follow}(E) \neq \#.$$

$$\text{follow}(E) = \text{follow}(E) \cap \text{follow}(S)$$

$$\Rightarrow \{\$ \} = \{\#\}$$

$$\rightarrow \text{follow}(A) = \{=, \$ \} = \{=, \# \}$$

$$\text{Follow}(H) = \text{first}(id) = \{id\}$$

$$\text{Follow}(E) = \{\$ \} = \{\#\}$$

$$\text{Follow}(S) = \{\#\}$$

$$\text{Follow}(A) = \{\#, = \}$$

$$\text{Follow}(H) = \{id\}$$

$$\text{Follow}(E) = \{\#\}$$

~~Answer Question 2~~  
(3)

(24)

LL1

	id	=	+	A	#
S	$S \rightarrow A = E$			$S \rightarrow A = E$	$S \rightarrow A = E$
A	$A \rightarrow id$	$A \rightarrow id$		$A \rightarrow id$	$A \rightarrow id$
H	$H \rightarrow e$			$H \rightarrow e$	
E	$E \rightarrow id + E$			$E \rightarrow A$	$E \rightarrow A$

Point 4: if  $e$  is in  $first(s)$  then go  
for follow of  $s$ .  $s$  placed, the prediction  
on that terminal.

Eg:  
 $first(s) = \{id, +, \frac{e}{1}\}$

So find follow(s) → where  $\in \Sigma^{\#}$

So placed production  $S \rightarrow A = E$  at # place in table.

(4)

$A = b + K C$

(i)  $S \rightarrow A = E$

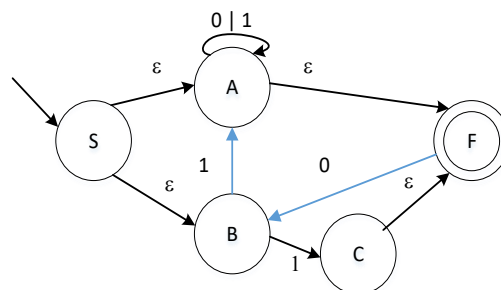
(ii)  $E \rightarrow id + E$

(iii)  $E \rightarrow A$

(iv)  $A \rightarrow H id$

(v)  $H \rightarrow \epsilon$

**【Q7】** (10 scores)  
Given the following NFA:



(1) Present the equivalent Matrix representation of this NFA. (8 scores)

	0	1	$\epsilon$
S			
A			
B			
C			

(2) Transform the NFA to DFA. (7 scores)

(27)

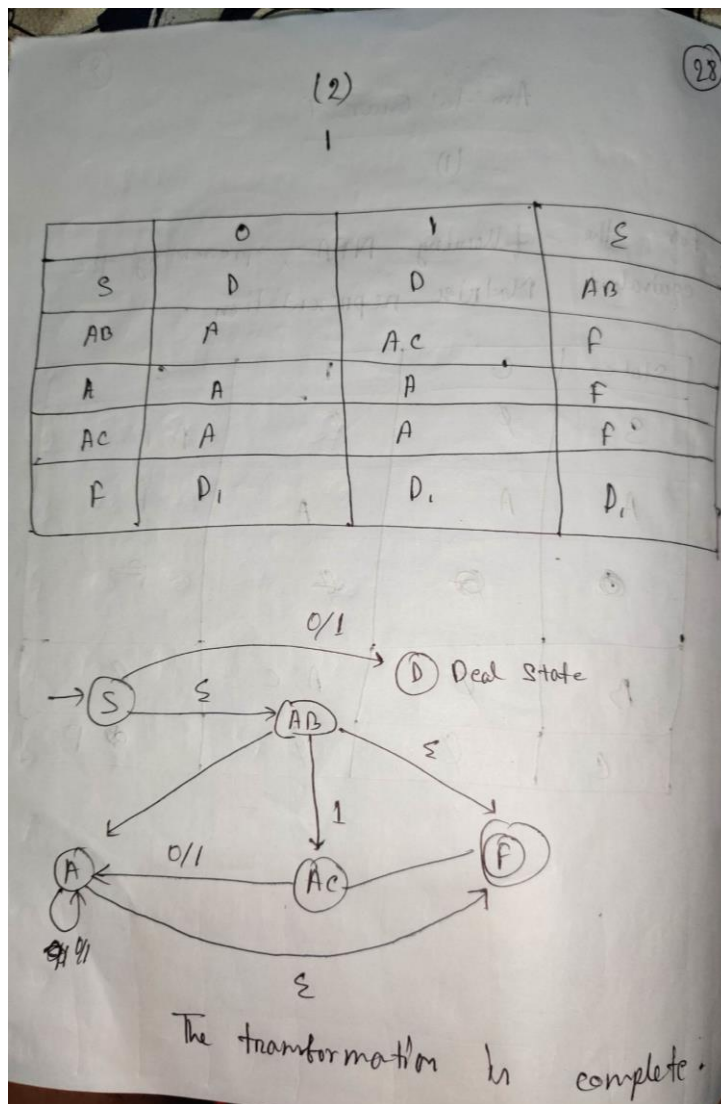
Am: to: Ques: 7

(1)

for the following NFA, presenting the equivalent NFA representation:

State	$\emptyset$	1	$\epsilon$
S	$\emptyset$	$\emptyset$	A, B
A	A	A	F
<del>Q</del>	<del>Q</del>	<del>Q</del>	<del>F</del>
B	$\emptyset$	A, C	$\emptyset$
C	$\emptyset$	$\emptyset$	<del>Q</del> F





【Q8】 (15 scores)

Given the following grammar  $G[S]$ :

- (1)  $S \rightarrow ABD$   
 (2)  $A \rightarrow Aa \mid a$   
 (3)  $B \rightarrow bD \mid \epsilon$   
 (4)  $D \rightarrow d$

(1) Please write down the LR(0) automata. (6 scores)

(2) Please present the SLR(1) parsing table. (7 scores)

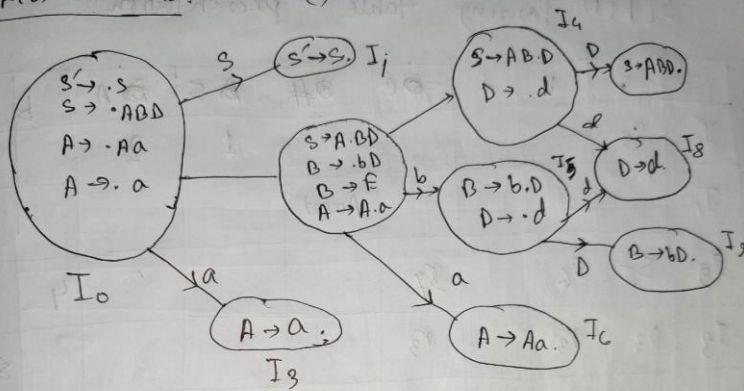
	a	b	d	#	S	A	B	D
I0								
I1								
...	...	...	...	...	...	...		

Ans. to the Ques: 8

(29)

LR(0) automata:

(1)



Follow (S) = \$ = #

Follow (A) = {a, b, d, e}

Follow (B) = d

Follow (D) = Follow (B) ∪ Follow (S)

(2)

First 9 items generate assembly of production rule

$S \rightarrow ABD$  (1)

$A \rightarrow Aa$  (2)

$A \rightarrow a$  (3)

$B \rightarrow bD$  (4)

$B \rightarrow e$  (5)

$D \rightarrow d$  (6)

Q20

SLR(1) Parsing table presentation:

	a	b	d	<del>c</del>	#	\$	A	A
$I_0$	$S_3$					1	2	
$I_1$				Accept				
$I_2$	$S_5$	$S_6$		$r_7$				4
$I_3$	$r_3$	$r_3$		$r_3$				8
$I_4$	<del><math>r_3</math></del>	<del><math>r_3</math></del>	$S_9$	<del><math>r_3</math></del>				
$I_5$	$r_2$	$r_2$		$r_2$				10
$I_6$			$S_9$					
$I_7$			$r_5$					
$I_8$					$r_1$			
$I_9$			$r_6$		$r_6$			
$I_{10}$			$r_7$					

【Q9】 For the following three addresses IR code, write down the basic blocks and draw the control flow graph of it. (10 scores).

- (1)  $X := X+2$
- (2) if  $X \geq 10$  goto (4)
- (3) goto (6)
- (4)  $X := X-1$
- (5) goto (2)
- (6) if  $A < 4$  goto (L\_out) //L\_out is outside of this code sequence
- (7)  $X := X-2$
- (8)  $Y := X+5$
- (9) goto (2)

Ans. to Ques. 9

(31)

At first, I'm going to find leaders in our given three address IP cod.

If I go through the given statements in order and check whether any rule is applicable because of the statement

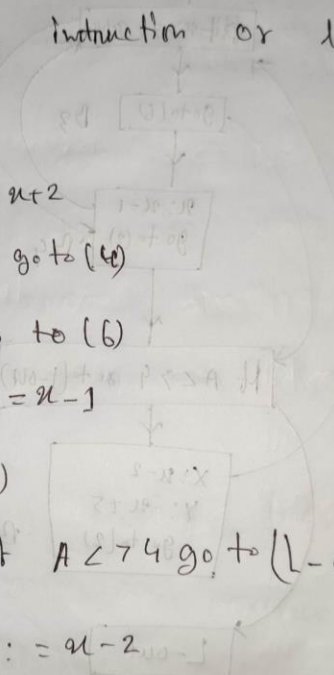
- 1st statement is a leader (By Rule 1)
- 4th " " " " (Rule 1, Statement 2)
- 3rd " " " " (Rule 3, Statement 3)
- 6th " " " " (Rule 2, Statement 3)
- 4th " " " " (Rule 3, Statement 4)
- 2nd " " " " (Rule 2, Statement 5)
- 6th " " " " (Rule 2, Statement 5)

(32)

- L-out is a Leader (Rule 2, Statement 6)
- 7th statement is leader (Rule 3, Statement 6)
- 2nd " " " " (Rule 2, Statement 9)

So, we get leaders are: 1, 2, 3, 4, 6, 7, L-out

A basic block will begin with first instruction and instructions are added until a jump instruction or label is encountered.



```

(2)
B1: x := x + 2
    if x > 10 goto (4)
B2: goto (6)
B3: x := x - 1
    goto (2)
B4: if A < 7 goto (1-out)
    goto (4)
B5: x := x - 2
    y := x + 5
    goto (2)
  
```

(2)  
for basic block, it will start from one leader to next leader but excluding next leader.

Based on that I'm finding basic blocks and drawing an arrow from one basic block to another basic block according to the flow/target statements in code.

When ~~used~~ a cycle is found in CFG, optimization can be applied.

