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## PA #2: Graduate Group Assignment

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```
clear
clc
%%Default Values
theta1 = 180; %180
theta2 = 90; %90
theta3 = 90; %90
D4 = 1; %(Prismatic Joint)
theta4 = D4;
Theta = [theta1,theta2,theta3,theta4];
L2 = 1;
% We also store all the given joint types available in this program.
jointTypeDict = {'R', 'P'};
```

## User Inputs

Here we ask user to input parameters,to specify parameters of each joint, such as the type of joint, the value of joint variable, etc.

```
%{
n = input("How many joints are there in the mechanism?\n");
while (~isequal(size(n), [1,1]) || n <= 0)
    fprintf("Errors: The number of joints should be a positive number\n");
n = input("How many joints are there in the mechanism?\n");
end
Theta = [];
for i = 1:n
    joint_type = input('Please specify the type of the joint (e.g. R, P):\n','s');
    while (~any(strcmp(jointTypeDict, joint_type)))
        fprintf('Error: Invalid joint type!\n');
        joint_type = input('Please specify the type of the joint (e.g. R, P):\n','s');
    end
    if (joint_type == 'P')
        fprintf('Please enter the D value of the %d-th joint (prismatic) in base\n', i);
    end
end
}
```

---

```

frame:\n',i);
    d_i = input('');
    while (~isequal(size(d_i), [1,1]))
        fprintf('Error: Invalid value!\n');
        fprintf('Please specify the value of d_%d:\n', i);
        d_i = input('');
    end
    Theta(i) = d_i;
elseif (joint_type == 'R')
    fprintf('Please specify the Theta value of %d-th joint
(revolute) in base
frame:\n',i);
    theta_i = input('');
    while (~isequal(size(theta_i), [1,1]))
        fprintf('Error: Invalid value!\n');
        fprintf('Please specify the value of theta_%d:\n', i);
        theta_i = input('');
    end
    Theta(i) = theta_i;
end
end
%}

```

## FK Calculations - Final End-Effector Position and Orientation

Transformation Matrix DHmat(theta\_i,d,a,alpha)

```

T01 = DHmat(Theta(1), 0, 0, 0);
T12 = DHmat(Theta(2), 0, 0, 90);
T23 = DHmat(Theta(3)+90, 0, L2, 0);
T34 = DHmat(0, Theta(4), 0, 90);
T = T01*T12*T23*T34;
p_ee = T(1:3,4);
fprintf('Here is the Matrix Orientation of the End-Effector: \n');
T
fprintf('With the xyz co-ordinates of the End-Effector as: \n');
p_ee'
%Axis angle method
Rot_mat = T(1:3,1:3);
tr = trace(Rot_mat);
Rot_angle_ee = acosd((tr-1)/2);
fprintf('The Rotation angle of the End-Effector w.r.t. the base frame
is: \n');
Rot_angle_ee
k = (1/2*sind(Rot_angle_ee)).*[Rot_mat(3,2)-Rot_mat(2,3);
                                Rot_mat(1,3)-Rot_mat(3,1);
                                Rot_mat(2,1)-Rot_mat(1,2)];

k; %Base frame check [0,0,0]
% T-matrix w.r.t. Base Frame 0
T02=T01*T12;
T03=T02*T23;

```

---

```

T04=T03*T34;
% Joint Co-ordinates w.r.t. Base Frame
X=[T01(1,4) T02(1,4) T03(1,4) T04(1,4)];
Y=[T01(2,4) T02(2,4) T03(2,4) T04(2,4)];
Z=[T01(3,4) T02(3,4) T03(3,4) T04(3,4)];

```

## Simulation

```

a1 = linspace(0,Theta(1),3); %Theta1 = 180
a2 = linspace(0,Theta(2),3); %Theta2 = 90
a3 = linspace(0,Theta(3),3); %Theta3 = 90
disp4 = linspace(0,Theta(4),3); %Theta4 or D4 = 1
for i=1:length(a1)
    for j = 1:length(a2)
        for k = 1:length(a3)
            for l = 1:length(disp4)
                T01 = DHmat(a1(i), 0, 0, 0);
                T12 = DHmat(a2(j), 0, 0, 90);
                T23 = DHmat(a3(k)+90, 0, L2, 0);
                T34 = DHmat(0, disp4(l), 0, 90);
                T02=T01*T12;
                T03=T02*T23;
                T04=T03*T34;
                X=[T01(1,4) T02(1,4) T03(1,4) T04(1,4)];
                Y=[T01(2,4) T02(2,4) T03(2,4) T04(2,4)];
                Z=[T01(3,4) T02(3,4) T03(3,4) T04(3,4)];
                plot3(X,Y,Z, '-
o','LineWidth',2,'MarkerSize',6,'MarkerFaceColor','auto');
                xlabel("x");
                ylabel("y");
                zlabel("z");
                title("Simulation of the Open Chain Manipulator");
                grid on;
                axis([-2,2,-2,2,0,2]);
                pause(0.01);
            end
        end
    end
end
end
T = T01*T12*T23*T34;
fprintf('Here is the Matrix Orientation of the End-Effector after
simulation: \n');
T

```

## Functions

```

%DH Matrix Function
function [DH] = DHmat(thetai,d,a,alpha)
DH = [cosd(thetai) -sind(thetai) 0 a;
      sind(thetai)*cosd(alpha) cosd(thetai)*cosd(alpha) -sind(alpha)
      -d*sind(alpha);
      sind(thetai)*sind(alpha) cosd(thetai)*sind(alpha) cosd(alpha)
      d*cosd(alpha)];

```

---

```
    0 0 0 1];  
end
```

*Here is the Matrix Orientation of the End-Effector:*

*T =*

$$\begin{bmatrix} 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

*With the xyz co-ordinates of the End-Effector as:*

*ans =*

$$\begin{bmatrix} 1 & 0 & 1 \end{bmatrix}$$

*The Rotation angle of the End-Effector w.r.t. the base frame is:*

*Rot\_angle\_ee =*

*90*

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