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# PA #1: Calculate DoF using user inputs

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## Grubler's Formula

Grubler's Formula can be used to calculate the number of degrees of freedom of a robot (DoF) by subtracting the number of independent constraints from sum of degrees of the bodies.

Or in mathematical form,

$$DoF = m(N - 1 - J) + \sum_{i=1}^J f_i$$

, where

$m$  is the number of freedom of a rigid body ( $m = 3$  for planar and  $m = 6$  for spatial mechanism)

$N$  is the number of links,

$J$  is the number of joints, and

$f_i$  are the number of freedoms provided by joint  $i$ .

## Parameters

The parameters should be given interactively, like

```
m = input("Is the mechanism planar [3] or spatial [6]?");
```

```
N = input("How many links are there in the mechanism?");
```

```
J = input("What about the number of joints?");
```

```
f = input("Finally, give me the number of freedoms provided by these joints. It should be a vector, the dimension of which is same as the number of joints.")
```

However, we will demonstrate the usage with several sets of fixed input values.

The first example represents open chain mechanism with 3 revolute joints. (RRR). The second example represents closed chain mechanism with 4 revolute joints (RRRR). The third one is a spatial example with 4 universal joints (UUUU). The rest ones are error cases.

```
calcDof(3, 4, 3, ones([3, 1]))
calcDof(3, 4, 4, ones([4, 1]))
calcDof(6, 5, 4, ones([4, 1])*2)
calcDof(4, 5, 4, ones([4, 1])*2)
```

```
calcDof(3, 4, 3, ones([2, 3])*2)
```

## Matlab Implementation and Output

```
function dof = calcDof(m, N, J, f)
    if m ~= 3 && m ~= 6
        disp("m should either be 3 or 6!");
    elseif sum(size(f) ~= [J, 1]) ~= 0 && sum(size(f) ~= [1, J]) ~= 0
        disp("The size of f does not match J!");
    else
        dof = m * (N - 1 - J) + sum(f);
    end
end
```

```
ans =
```

```
3
```

```
ans =
```

```
1
```

```
ans =
```

```
8
```

```
m should either be 3 or 6!
```

```
The size of f does not match J!
```

*Published with MATLAB® R2020b*