

① Transformada de Laplace (Dom. tempo a S)

$$\rightarrow V_e(s) = R I_1(s) + L S [I_1(s) - I_2(s)] + R [I_1(s) - I_2(s)]$$

$$\rightarrow L S [I_1(s) - I_2(s)] + R [I_1(s) - I_2(s)] = R I_2(s) + R I_2(s) + \frac{I_2(s)}{CS}$$

$$\rightarrow V_e(s) = R I_2(s) + \frac{I_2(s)}{CS}$$

② Procedimento algébrico

$$\rightarrow V_e(s) = (R + L S + R) I_1(s) - (L S + R) I_2(s)$$

$$= (L S + 2R) I_1(s) - (L S + R) I_2(s)$$

$$\rightarrow L S [I_1(s) - I_2(s)] + R I_1(s) - R I_2(s) = 2R I_2(s) + \frac{I_2(s)}{CS}$$

$$L S [I_1(s) - I_2(s)] + R I_1(s) = 3R I_2(s) + L S I_2(s) + \frac{I_2(s)}{CS}$$

$$(L S + R) I_1(s) = \left[ 3R + L S + \frac{1}{CS} \right] I_2(s)$$

$$I_1(s) = \frac{3CRS + CLS^2 + 1}{CS(LS + R)} I_2(s) = \frac{CLS^2 + 3CRS + 1}{CS(LS + R)} I_2(s)$$

$$\rightarrow \frac{CRS + 1}{CS} I_2(s), \text{ substituir } \leftarrow \uparrow :$$

$$V_e(s) = \frac{(LS + 2R)(CLS^2 + 3CRS + 1)}{CS(LS + R)} I_2(s) - (LS + R) I_2(s)$$

$$= \left[ \frac{(LS + 2R)(CLS^2 + 3CRS + 1)}{CS(LS + R)} - \frac{CS(LS + R)(LS + R)}{CS(LS + R)} \right] I_2(s)$$

multiplicar  $\rightarrow$  (juntar termos)

$$CL^2S^3 + 3CLRS^2 + LS + 2CLRS^2 + 6CR^2S + 2R$$

$$* -CL^2S^3 - 2CLRS^2 - CR^2S \rightarrow 5CR^2S, \text{ substituir}$$

$$V_e(s) = \frac{3CLRS^2 + (5CR^2 + L)S + 2R}{CS(LS + R)} I_2(s)$$

$$V_s(s) = \frac{\frac{CRS + 1}{CS} I_2(s)}{\frac{3CLRS^2 + (5CR^2 + L)S + 2R}{CS(LS + R)} I_2(s)}$$

$$\rightarrow [CRS + 1][LS + R] = CLRS^2 + CR^2S + LS + R$$

$$\frac{V_s(s)}{V_e(s)} = \frac{CLRS^2 + (CR^2 + L)S + R}{3CLRS^2 + (5CR^2 + L)S + 2R}, \quad \begin{aligned} C &= 100 \mu F \\ R &= 1 k\Omega \\ L &= 68 \mu H \end{aligned}$$



## Estabilidad en lazo abierto

- Colocar los polos de la función de transferencia

$$\frac{V_s(s)}{V_e(s)} = \frac{CLRs^2 + (CR^2 + L)s + R}{3CLRs^2 + (5CR^2 + L)s + 2R}$$

$$\text{den} = [3 * C * L * R, s * C * R^2 * 2 + L, 2 * R]$$

$$L = \text{np.roots}(\text{den})$$

→ print: Las raíces son  $\{L[0]\}$  y  $\{L[1]\}$

$$\begin{aligned} \lambda_1 &= -24509803.25490185 \\ \lambda_2 &= -4.000000000000001 \end{aligned} \quad \left. \begin{array}{l} \text{respuesta} \\ \text{estable} \end{array} \right\} \begin{array}{l} 2 \text{ raíces reales negativas d.f.} = \text{sobremortiguado} \end{array}$$

## Error en estado estacionario

$$e(s) = \lim_{s \rightarrow 0} s V_e(s) \left[ 1 - \frac{V_s(s)}{V_e(s)} \right]$$

$$\begin{aligned} V_e(t) &= 1V \\ V_e(s) &= 1/s \end{aligned}$$

$$= \lim_{s \rightarrow 0} s * \frac{1}{s} \left[ 1 - \frac{CLRs^2 + (CR^2 + L)s + R}{3CLRs^2 + (5CR^2 + L)s + 2R} \right] = \frac{R}{2R} \quad e(t) = \frac{1}{2} \checkmark$$

