

Fixed Length code & Variable Length Code:

If we have a finite set of symbols $x^0, x^1, x^2, \dots, x^n$,
Then the number of bits N required for unique coding
when n is a power of 2,

$$N = \log_2 n \quad \text{and}$$

when n is not a power of 2,

$$N = (\log_2 n) + 1.$$

In generally ; $N \geq \log_2 n$.

eg. To encode the letters of the English alphabet, we use

$$N \geq \log_2 26$$

$$N \geq 4.7$$

$$N = 5 \text{ bits needed}$$

In a FLC all the symbols are equally important or equiprobable and hence each one requires 5 bits for representation.

If we consider English alphabet, some letters are less common (x, q, z etc) and some are frequently used (s, t, e etc). Represent more frequently occurring letters by fewer number of bits and lesser frequently occurring ones by larger number of bits. This method is called Variable length coding. When some symbols are not equally probable, more efficient method is VLC.

eg:

Source symbol	code F	code G	code H.
A	000	00	0
B	001	010	1
C	010	011	00
D	011	100	01
E	100	101	10
F	101	110	11
G	110	1110	000
H	111	1111	111

Code the sentence : "A BAD CAB"

FEC : Code F : '000 001 000 011 010 000 001' total bits : 21

VLC : { Code G : '00 010 00 100 011 00 010' " : 18
Code H : '0 1 0 01 00 01' " : 9

Problem with code H : For decoding we are able to regroup it using any manner i.e. it is not uniquely decodable.

(01) (00) (10) (00) (1)

D C E C B

or (0) (1) (0) (0) (1) (0) (0) (0) (1)

A B A A B A A A B.

Kraft Inequality (Kraft - McMillan Inequality) :

A necessary and sufficient condition for the existence of an instantaneous code with code word lengths l_1, l_2, \dots, l_q is that

$$\sum_{i=1}^q r^{-l_i} \leq 1 \quad \text{when}$$

$r \rightarrow$ Number of different symbols used.

$l_i \rightarrow$ word length in binary digits of the codeword corresponding to i th source symbol.

$q \rightarrow$ number of source symbols.

for binary codes, we have $r=2$, So Kraft inequality for binary code,

$$\sum_{i=1}^q 2^{-l_i} \leq 1.$$