

Machine learning Homework- Deep Learning

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1 Activation Function

Problem 1:

The matrix operation $w^T + b$ is essentially a linear operation. When we stack linear operations over other linear operations we essentially get a linear function. It is impossible to approximate complex functions with just linear operations, therefore non-linearity is introduced to overcome this problem.

Problem 2:

The sigmoid activation function is

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

The tanh activation is

$$\begin{aligned} \tanh(x) &= \frac{e^{2x} - 1}{e^{2x} + 1} \\ \tanh\left(\frac{x}{2}\right) &= \frac{e^x - 1}{e^x + 1} \\ \tanh\left(\frac{x}{2}\right) &= \frac{1 - e^{-x}}{1 + e^{-x}} \\ \tanh\left(\frac{x}{2}\right) &= (1 - e^{-x})\sigma(x) \end{aligned}$$

Problem 3:

2 Numerical Stability

Problem 4:

Problem 5:

Problem 6: