Brain Principles Programming

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Abstract. The monograph "Strong Artificial Intelligence. On the Approaches to Superintelligence", referenced by this paper, provides a cross-disciplinary review of Artificial General Intelligence (AGI). As an anthropomorphic direction of research, it considers Brain Principles Programming (BPP) - the formalization of universal mechanisms (principles) of the brain's work with information, which are implemented at all levels of the organization of nervous tissue. This monograph provides a formalization of these principles in terms of the category theory. However, this formalization is not enough to develop algorithms for working with information. In this paper, for the description and modeling of BPP, it is proposed to apply mathematical models and algorithms developed by us earlier that model cognitive functions, which are based on well-known physiological, psychological and other natural science theories. The paper uses mathematical models and algorithms of the following theories: P.K.Anokhin's Theory of Functional Brain Systems, Eleonor Rosh's prototypical categorization theory, Bob Rehter's theory of causal models and "natural" classification. As a result, the formalization of the BPP is obtained and computer examples are given that demonstrate the algorithm's operation.

Keywords: Brain principles, categorization, category theory, formal concepts.

1 Introduction

In the monograph "Strong Artificial Intelligence. On the approaches to superintelligence" [1] the first cross-disciplinary guide on Artificial General Intelligence (AGI) is given: "General artificial intelligence is the next step in the development of AI, not necessarily endowed with self-awareness, but, unlike modern neural networks, capable of coping with a wide range of tasks in different conditions." As an anthropomorphic direction of research, it considers Brain Principles Programming (BPP) – the formalization of universal mechanisms (principles) of the brain's work with information, which are implemented at all levels of the organization of nervous tissue. The book provides a formalization of these principles in terms of category theory. However, algorithms for working with information do not follow from this formalization.

In this paper, we apply mathematical models and algorithms developed by us earlier that modeling cognitive functions and based on the well-known physiological, psychological and natural science theories, to model Brain Principles Programming. We will rely on the following theories: P.K.Anokhin's Theory of Functional Brain Systems [2-3], Eleonor Rosh's prototypical categorization theory [4-5], Bob Rehter's theory of causal models [6-7] and works on "natural" classification [8].

Part I. Basic theories and formal models

1.1 Basic elements of perception and the world

1.1.1. "Natural" classification. The first philosophical analysis of the "natural" classification belongs to J.S. Mill [9]: ""artificial" classifications differ from "natural" in that they can be based on ... features, so that different classes differ in that they include objects with different meanings of these features. But if we consider the classes of "animals" or "plants", then they differ in such a large (potentially infinite) number of properties that they cannot be enumerated. And all these properties will be based on statements confirming this difference".

J.S. Mill's analysis has been confirmed by naturalists. L. Rutkovsky writes about the similarity of properties in "natural" classes [10]: "The more essential features of the compared objects are similar, the more likely their similarity is in other features." Smirnov E.S. [11]: "The taxonomic problem lies in the "indication": from an infinitely many number of features, we need to move to a limited number of them, which would replace all other features". From studies on "natural" classification, it follows that features in "natural" classes are strongly correlated, since a potentially infinite number of features are almost uniquely determined follow L. Rutkovsky from the indicator features. A formal model of "natural" classification is given in [6].

1.1.2. "Natural" concepts and prototypical theory of categorization. The high correlation of features for "natural" classes has been confirmed in cognitive studies. In the works of Eleanor Rosch [4-5], the following principle of categorization of "natural" categories was formulated, confirming the statements of J.S. Mill and naturalists: "Perceived World Structure: ... perceived world – is not an unstructured total set of equiprobable co-occurring attributes. Rather, the material objects of the world are perceived to possess ... high correlational structure (emphasis added by EV). ... In short, combinations of what we perceive as the attributes of real objects do not occur uniformly. Some pairs, triples, etc., are quite probable, appearing in combination sometimes with one, sometimes another attribute; others are rare; others logically cannot or empirically do not occur». Therefore, directly perceived objects (so called basic objects) are information—rich bundles of observable and functional properties that form a natural discontinuity that creates categorization. These bundles form "prototypes" of class objects. Further Eleanor Rosch's theory of "natural" concepts was called the prototypical theory of concepts (prototype theory).

1.1.3. The theory of causal models. Studies have shown that people's knowledge of categories is not reduced to the set of features, but includes a rich set of causal relationships between these features. In some experiments [7] it was shown that a

feature is more important if it is more strongly included in the causal network of interrelations of features. Considering these studies, Bob Rehder put forward the theory of causal models (causal-model theory), according to which the relation of an object to a category is no longer based on a set of features and proximity by features, but on the basis of similarity of the generative causal mechanism [7]. In [8] Bayesian networks were used to represent causal knowledge. However, they cannot model cyclic causal relationships because Bayesian networks do not support cycles. The probabilistic formal concepts, that developed earlier and presented in the supplement of work [12], model cyclic causal relationships by fixed points of causal relationships predictions.

1.2 Probabilistic formal concepts

We assume that "natural" classification and "natural" concepts are described by the same formalism. From our point of view, the information processes of the brain were tuned in the process of evolution to extract a highly correlated structure of features of "natural" objects by forming "natural" concepts of these objects. Causal relationships in the perception of "natural" objects close on themselves forming a certain "resonance". At the same time, "resonance" occurs if and only if these causal relationships reflect some holistic "natural" object. The resulting cycles of inferences on causal relationships are mathematically described by "fixed points" of mutually interconnected features, which gives an "image" or "prototype" of objects class. Therefore, the brain perceives a "natural" object not as a set of features, but as a "resonating" system of causal relationships that forms a causal model.

The formalization of cyclic causal relationships in the form of probabilistic formal concepts is given in the supplement of the work [12]. There is also a definition of causality in the form of the Most Specific Causal Relationships (MSCR) that solve the problem of statistical ambiguity (see references in the supplement). There is also an example of the probabilistic formal concepts discovery.

Probabilistic formal concepts can be used to context (latin contextus – cohesion, coherence, connection) detection as systems of interrelated concepts in a certain situation, discourse, a certain point of view, etc. In addition, in supplement, an example of the context detection is given on the example of the social networks analysis.

The definition of probabilistic formal concepts and the proof of its properties is carried out under the assumption that a probabilistic measure is known. In practical tasks, we cannot assume this. Therefore, it is necessary to use a statistical criterion to detect MSCR on data. For that a Fisher 's independence exact criterion with some level of significance α was used. Then we can got a set \mathcal{R}_{α} of statistical approximations of MSCR detected on data with a confidence level α . They can cause contradictions in fixed points of probabilistic formal concepts. Therefore, it is necessary to introduce a criterion of approximations \mathcal{R}_{α} consistency in predictions on some data A. As a result we can discover a fixed points by consistently applying the prediction operator $\Upsilon(A)$ to data A, taking into account the consistency of predictions. The operator $\Upsilon(A)$ adds some new element to the set A if it is predicted by some approximation from \mathcal{R}_{α} based on data A and it is not contradict to the predictions of others by approximations in such

a way that the consistency criterion strictly increases. Either the operator $\Upsilon(A)$ removes some element from A if there are approximations that predicting its negation and also in such a way that the consistency criterion again strictly increases. When the operator can no longer add a certain element to A, or remove an element in such a way that the operator strictly increases, we get a fixed point, which is denoted as $\Upsilon^{\infty}(A)$. A detailed description of this process is given in supplement of the work [12].

1.3 "Intelligent object" and "intelligent function"

The formalization of "Brain Principles Programming, (BPP)" described in [1] is based on the category theory and the concepts of "intellectual object" and "intellectual function" formulated in it. Here is an informal definition of "intellectual object" and "intellectual function" from [1]:

- "intellectual object", by which we mean any single integrity that we distinguish in this space for example, when we see a table, signals from the optic nerve are processed by the brain, and the combination of individual lines is recognized as a table:
- the "intellectual function", which describes all possible operations in the system under consideration, is all that the psyche can do with an intellectual object. When we identify a table as an object, we can estimate its size or figure out how to use it;
- "essence" is the specific meaning of an object for the psyche. That is, the knowledge
 of what the table can be used for.

Formally, an "intelligent object" is defined as a mapping [1]:

- some data set (A);
- the observer as a reflection of the world after interacting with it (Ω) ;
- the relation of the world to the observer, which is a function of the internal state/expectation (f) an intellectual function $A \xrightarrow{f} \Omega$.

Here A is a data set that characterizes any unit wholeness;

 Ω – distinguishing ability: "the relationship of an intellectual object with "me" does not yet mean any awareness, representation of this intellectual object in consciousness – it is enough for something to be somehow perceived and recognized to a degree sufficient for this "something" to be taken into account in the future in one way or another ... since the main task of thinking ... is to predict or produce a competitive future, then how the perceived object will eventually appear to us will depend on our mood, or, as phenomenologists would say, on our intentionality" [13]. More formally, "Some requirements will be imposed on the object Ω modeling the distinguishing ability, thus: first of all, it should be a partially ordered set, the elements of which correspond to "more" or "less" high values" [13].

Next, the waiting function $Exp_A: A \times A \to \Omega$ is defined (expectation) and the following explanations of this function are given: "at all levels of perception ... we are essentially dealing with a situation, with some expected state of affairs ... *Our psyche*

irresistibly tends to put the whole set of stimuli into a kind of understandable, clear and seemingly consistent picture of reality (cursive 1-E.V.) ... These representations of reality, in turn, are a specific filter-interpreter – any new stimuli, finding themselves, figuratively speaking, in the field of gravity of the corresponding system of representations, inevitably seem to change their trajectory – some are repelled (ignored), others, complementary, on the contrary, are attracted, others are modified (interpreted) in favor of the prevailing attitudes (cursive 2-E.V.) ... As a result, with respect to any element x that is part of the intellectual object A, it is meaningful to say how different it is, firstly, from itself in the sense of what we expect to see in its place, and, secondly, how appropriate it is in the situation in general, i.e. how close it is to the rest of the elements distinguished in the situation."

More formally [13], the expectation function $Exp_A: A\times A\to \Omega$ assigns to each pair of elements $x,y\in A$ a measure of their consistency (coherence) on our existential partially-ordered scale Ω . At the same time, the measure of the object's $x\in A$ consistency with itself $Exp_A(x,x)$ can be understood as a measure of the proximity of x to its essence ... and denoted as $Ess_A(x)$ (essence). If we consider the prototype of class objects as an "invariant" of class objects, then the fixed point of the operator $\Upsilon^\infty(X(y))$ obtained on the set of properties $X(y)=\{P_1\&...\&P_m\}$ of some element $y\in A$ will differ from the attributes X(y) of the element itself exactly as a measure of the object's consistency with itself. Therefore, the operator Υ^∞ gives a certain measure of the proximity of the object to its essence (invariant).

The waiting function allows to define the intelligent object more fully [13]. By an intelligent object we will understand ... an object $\mathcal{A} := (A, Exp_A)$ that includes a set of data A and an expectation function $Exp_A : A \times A \to \Omega$ that essentially depends on the subject experience Ω and its internal state.

The structure of an intelligent object described in cursive 1 above actually means that an intelligent object is a context, represented by a probabilistic formal concept, in which an operator Υ^{∞} having the same meaning – minimizing contradictions in a set of stimuli – generates the most consistent picture of reality from the input set of stimuli A, supplementing it with all relevant information. At the same time (see cursive 2), new stimuli either change their trajectory, or repel, or attract. All these effects, which are taken into account in the expectation function $Exp_A: A \times A \to \Omega$, are modeled by the interaction of probabilistic formal concepts of elements of the set A. A change in the trajectory is the features moving closer to the prototype, repulsion is the braking of features, which is described in the supplement of the work [12], and attraction is mutual support at a fixed point.

Intelligent function. The work of the intellectual function is not only to recreate the intellectual objects associated with the data elements A and the set A itself, but also to connect these intellectual objects with all other intellectual objects that exist in the psyche and are relevant to a given situation, for example, to a need or some task (goal). The result of the work of the intellectual function is the creation of a "heavy intellectual object" by "enlarging the knowledge we have, which we believe relates to some problem that interests us" [13]. Thus, an intellectual object "is, as it were, raised to the

degree of the knowledge (intellectual objects) that we possess, and acquires an appropriate meaning for us" [13].

Raising of some intellectual object "to the degree" of knowledge is formally represented as a relation: "If (this) relation is thought of as a certain kind of directional connection, then it seems quite natural to designate intellectual objects with letters $\mathcal{A}, \mathcal{B}, \mathcal{C}$..., and the relations between them with arrows ... $\mathbf{r}: \mathcal{A} \to \mathcal{B}$ " [13]. In addition, this relation "must respect those differences and identifications that were posited by the expectation function $Exp_A: A \times A \to \Omega$ " and satisfy the following conditions:

$$\forall a,b \in A(Ess_B(r(a)) \le Ess_A(a)), \ Exp_A(a,b) \le Exp_B(r(a),r(b)).$$

All arrows of the ratio r, showing the path of enrichment of the intellectual object, form a "cone". The limit of the enrichment diagram is the cone generated by the "heavy" object contained in all other cones. The operator $\Upsilon^{\infty}(A)$ automatically forms a context generated by elements A of some intellectual object and probabilistic formal concepts of its elements, since for all causal relationships linking elements A with other knowledge available in the psyche, the predicted elements of the psyche will automatically be included in the context by these causal relationships.

Part II. Brain Principles Programming formalization

2.1 The principle of the complexity generation

The principle of the complexity generation in [1, p. 217] is formulated as follows: "The brain works with a very limited amount of information from the surrounding reality coming to its sensors ... As this initially scarce information is used, the brain, at all levels of its organization, repeatedly increases its volume, correlating the received introductory data with the data already existing in it ... The principle of complexity generation allows the brain, having received the smallest external signal, to reproduce knowledge (an intellectual object) with incomparably greater power in the human mind, enriching the model of this object with information, which is relevant for the brain within the framework of its tasks (its goals)." This complexity generation is performed by the intellectual function introduced earlier in [1, p. 214], which "seems to be raised to the degree of the knowledge (intellectual objects) that we possess, and acquires an appropriate meaning for us".

The formalization of the "intellectual object" and "intellectual function" by probabilistic formal concepts gives us the following models of complexity generation:

- 1. If we consider the features of digits (see fig. 2 in supplement of the work [12]) as features perceived by the primary visual cortex, and the set A as a set of perceived digits, then the set of probabilistic formal concepts that have been discovered for these digits generates a set of intellectual objects $A_0 := (0, \operatorname{Exp}_0)$, $A_1 := (1, \operatorname{Exp}_1)$, ..., $A_9 := (9, \operatorname{Exp}_9)$ "invariants" of these digits. They are examples of generated complexity based on the simplest features (see description in supplement of work [12]).
- 2. The formation of contexts as probabilistic formal concepts, which generates a typology of social network users (see description in the supplement of the work [12]).

3. In general, when a certain task or a certain goal is set, the generation of complexity by the corresponding intellectual function will consist in generation of the context according to the given initial conditions A by "raising them to the degree" of the knowledge that is directly related to them. Formally, this generation is a probabilistic formal concept generated by an operator $\Upsilon(A)^{\infty}$ under conditions A, using all the knowledge related to the task or goal, represented by a set of MSCR approximations \mathcal{R}_{α} .

2.2 The principle of the relationship

In psychology, this principle was originally called the Gestalt principle. The brain reacts not to a specific stimulus, but to what this stimulus becomes when corresponding with the information that is already contained in the brain [1]. "The evaluation of information arising in the brain ... is carried out exclusively through the act of correlating one information with another, and the brain itself reacts not to the object of reality as such, but to how it correlates with other information located in the brain" [1].

Gestalt psychology puts forward the principle of integrity as the main explanatory principle. "The integrity of perception is a property of perception, consisting in the fact that every object, and even more a spatial objective situation, is perceived as a *stable systemic whole*, even if some parts of it cannot be observed at the moment (for example, the back of a thing)" (Wikipedia). The integrity of perception, which is formed in the process of perception of a "natural" concept or prototype of a class, as well as the context of a certain task, is formally expressed in a probabilistic formal concept by cyclic mutual prediction of features of the concept or elements of the context. Therefore, the probabilistic formal concepts form the very "stable system whole" that characterizes integrity.

Therefore, formally, the operator $\Upsilon(A)^{\infty}$ is just the "stable system whole" in which, not individual elements of A are perceived, but their inseparable relationship with the rest of the fixed point $\Upsilon(A)^{\infty}$ elements.

2.3 The principle of approximation to the essence

The principle of approximation described in [1] as follows: "... in reality, there are no absolutely identical objects, so the brain performs approximation, that is, ignores differences if it manages to assign one or another "essence" to an object by specific features. At the same time, "essence" means the functionality of an object – what meaning it has for the brain (what role it performs) within the framework of the tasks it solves (its goals) ... when a person is tired and wants to rest – in the forest, a stump can serve as a chair, since you can sit on it".

The formation of "entities" occurs in the context of tasks being solved. Every context clarifies and correlates the elements of the context with a system of mutually predicted properties by causal relationships. This leads to the formation of "essences" associated with the context. For example, a knife in different contexts: cooking, combat situations, office work and hiking conditions should have different properties arising

from the context: for a kitchen knife, the relationship of width, weight and blade edge is important, for a combat knife – the ratio of tip, length, weight and width, for a stationery knife – small weight, length and safety, for a penknife – relative smallness of size. Therefore, "essences" of "kitchen knife", "combat knife", "stationery knife", "penknife" are formed, which automatically generate probabilistic formal concepts in appropriate situations, since features and fix-points of their interrelation are different.

The context of the task, goal or need to be solved will automatically force you to choose the most suitable objects with the appropriate "functionality". This functional, which has a certain meaning for the brain within the framework of the tasks and goals it solves, will in a certain way affect the totality of the properties of the object, which, mutually assuming each other, and hence automatically form the corresponding probabilistic formal concept corresponding to its functional "essence".

Therefore, "essence" is a probabilistic formal concept $\Upsilon(A)^{\infty}$ generated by such elements A – features of the objects used, which will be selected in accordance with the context of the task being solved or the goal being achieved.

2.4 The principle of locality-distribution

The principle of locality-distribution [1]: "All information entering the brain can be duplicated many times in it, and its copies are processed in parallel by different structures independently, and only then this information is integrated into a holistic image." The brain processes information about a certain object in several modalities at once and in parallel – visual, auditory, tactile, etc. In each of these modalities, a hierarchy of the simplest "natural" concepts is formed, for example, in the visual cortex, on the basis of perceived sticks, images of digits can be formed, as in the example (see supplement of the work [12]) and "secondary" features – lines, angles, circles, etc., in the auditory cortex phonemes, words, text, etc. The integration of modalities is carried out through the perception of the integrity of the object, which integrates and binds the perception of parts into a "stable system whole" by some probabilistic formal concept.

Therefore, formally, this principle is also represented by an operator $\Upsilon(A)^{\infty}$ generating probabilistic formal concepts, for elements of A coming in parallel from different modalities.

2.5 The principle of heaviness

The principle of heaviness [1]: "The number of neural connections included in the creation of the object model, the number of relationships between the elements of the continuum of intelligent objects, the amount of information introduced into the object (attributes of the entity), the number of ways to calculate information about the object and the combination of multi-channel (modality) information about it into a single whole, correlated with the relevance of the task (goal) of the system, determine the "heaviness" of the intellectual object. The "heaviness" of the intellectual object determines the decision of the system. So, for example, if a person is hungry, he will look for food that will satisfy his hunger, but if he begins to face immediate danger (for

example, from a predator), then a defensive strategy will begin to prevail, and he will stop looking for food and begin to escape".

In 1911, the dominant principle was put forward by A.A. Ukhtomsky [17]. This principle has also been preserved in the theory of functional systems [2-3], as the dominance principle of the leading functional system, which creates the most "heaviness" context for satisfaction of some need (see supplement of the work [12]).

In general, when it comes to solving a certain task or achieving a certain goal, possible solutions are obtained by different ways of enriching the original intellectual object "problem statement" or goal and form the corresponding "cones" and the contexts generated by them, which in the case of functional systems, we denote by a set $\{\mathcal{C} := (C, Exp_{\mathcal{C}})\}$. The choice of the "heaviest" of them is determined by the choice of the most desirable "heavy" solution, generated by the "heavy" object contained in all other cones.

Therefore, formally, the principle of heaviness consists in choosing the most desirable "heavy" intellectual object generated by one of the contexts that are generated by the operator $\Upsilon^\infty(A \cup C)$, depending on the initial statement of the task/goal $\mathcal{A} := (A, Exp_A)$ and the available experience C of solution of such a tasks/goals.

2.6 Conclusions

Algorithms for detecting probabilistic formal concepts, class prototypes, "natural" concepts and contexts are practically confirmed in the works (see supplement of the work [12]). The model of functional systems has also shown its effectiveness [13-16].

This approach can be generalized to the tasks-driven approach to the artificial general intelligence, as planned in [1]. This approach solves the AGI problem formulated in [1] as: "general intelligence in AGI recognizes the ability to achieve goals in a wide range of environments, taking into account limitations". Therefore, Brain Principles Programming, formulated in [1] as principles of brain programming, based on research in cognitive sciences, can be implemented as a task-based approach to AGI, which, on the one hand, is able to solve a fairly wide class of tasks, and, on the other hand, corresponds fairly accurately to models of cognitive processes.

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