

Aim:

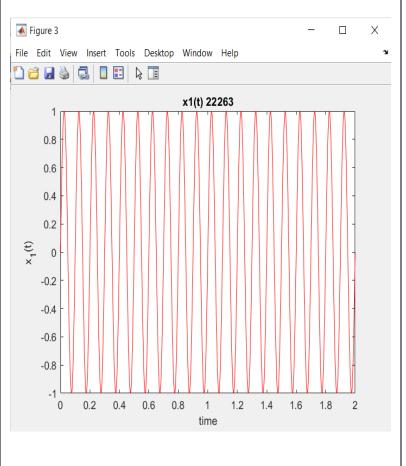
To generate elementary signals such as unit impulse, unit step and unit ramp signal using user defined functions in MATLAB

- To generate composite signals such as exponential, triangular, rectangular in MATLAB.
- To perform the following operations on signals: 1. Linear combination 2. Time scaling and Time shifting

Questions:

- 1. Write a function to generate the following signals
- a) unit impulse signal $\delta[n]$ and $\delta(t)$
- b) unit step signal u[n] and u(t)
- c) unit ramp signal r[n] and r(t)

```
t_22263=-4:0.01:4;
n_22263=-4:1:4;
impulse_conti_22263=t_22263>=0;
step_conti_22263=t_22263==0;
ramp_conti_22263=t_22263.*(t_22263>=0);
impulse_dis=n_22263>=0;
step_dis=n_22263==0;
ramp_dis=n_22263.*(n_22263>=0);
subplot(3,3,1);
plot(t_22263,impulse_conti_22263,'g');
title('Impulse Signal_22263');
xlabel('t');
ylabel('del(t)');
subplot(3,3,2);
plot(t_22263, step_conti_22263, 'r');
title('Step Signal_22263')
xlabel('t')
ylabel('u(t)')
subplot(3,3,3)
plot(t_22263,ramp_conti_22263,'b')
title('Ramp Signal_22263')
xlabel('t')
ylabel('r(t)')
subplot(3,3,4);
stem(n_22263,impulse_dis,'g');
```



```
title('Impulse Signal_22263');
xlabel('n');
ylabel('del(n)');

subplot(3,3,5);
stem(n_22263,step_dis,'r');
title('Step Signal_22263')
xlabel('n')
ylabel('u(n)')

subplot(3,3,6)
stem(n_22263,ramp_dis,'b')
title('Ramp Signal_22263')
xlabel('n')
ylabel('n')
```

We can observe a unit step signal, ramp signal and an impulse signal in the discrete and continuous form in the output graph.

- 2.Create a vector t = 0: 0.001 :2, find $x1(t) = \sin(2\pi 10t)$ and $x2(t) = \cos(2\pi 20t)$.
- a) Plot the signals x1 and x2 versus t in two figure windows. (Hint :Use plot ,xlabel, ylabel)
- b) Plot the signals x1 and x2 versus t in the same figure window. (Hint: Use subplot, plot)

for part a.)

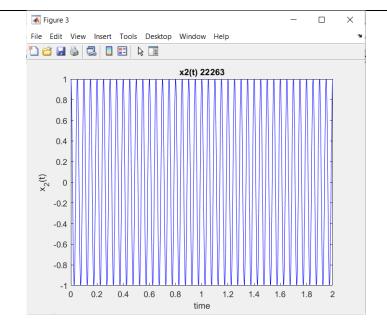
```
t_22263=0:0.001:2;

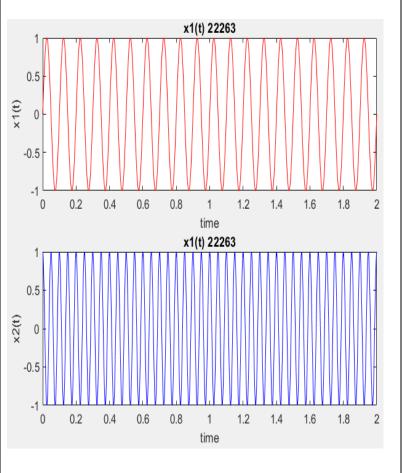
x1_t_22263=sin(2*pi*10*t_22263);

x2_t_22263=cos(2*pi*20*t_22263);

% for first figure window
plot(t_22263,x1_t_22263,'r')
xlabel('time')
ylabel('x_1(t)')
title('x1(t) 22263')

% for second figure window
plot(t_22263,x2_t_22263,'b')
xlabel('time')
ylabel('time')
ylabel('x_2(t)')
title('x2(t) 22263')
```





Part b)

```
t_22263=0:0.001:2;

x1_t_22263=sin(2*pi*10*t_22263);
x2_t_22263=cos(2*pi*20*t_22263);

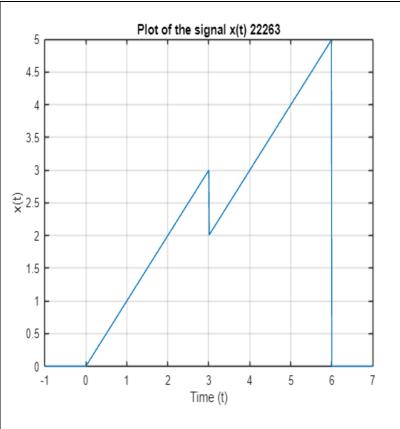
% same window
subplot(2,1,1)
plot(t_22263,x1_t_22263,'r')
xlabel('time')
ylabel('x1(t)')
title('x1(t) 22263')

subplot(2,1,2)
plot(t_22263,x2_t_22263,'b')
xlabel('time')
ylabel('time')
ylabel('x2(t)')
title('x1(t) 22263')
```

Result/Observation:

We can observe in part a, the figures are plotted in two separate windows, but in part b we use subplot to plot them in the same window.

3.Write a program to generate the following signals in MATLAB



```
(a) x(t) = 
 \begin{cases} t & 0 \le t \le 3 \\ t - 1 & 3 < t < 6 \\ 0 & Elsewhere \end{cases}
```

(b) x[n]=u[n]-u[n-2] where u[n] is unit step signal

Code:

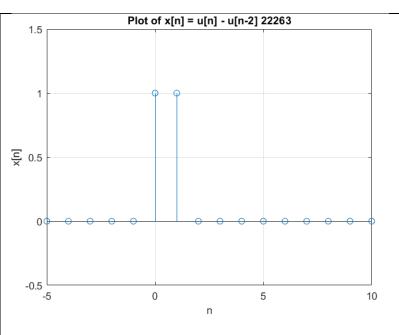
```
Part a:
t_22263 = -1:0.01:7;
% Initialize x(t) as a zero vector of the same
size as t
x_22263 = zeros(size(t_22263));
% Apply the conditions for x(t)
% For 0 \le t \le 3
x_22263(t_22263 >= 0 & t_22263 <= 3) =
t_22263(t_22263 >= 0 \& t_22263 <= 3);
% For 3 < t < 6
x_22263(t_22263 > 3 \& t_22263 < 6) =
t_22263(t_22263 > 3 \& t_22263 < 6) - 1;
% Plotting the signal
plot(t_22263, x_22263);
xlabel('Time (t)');
ylabel('x(t)');
title('Plot of the signal x(t) 22263');
grid on;
```

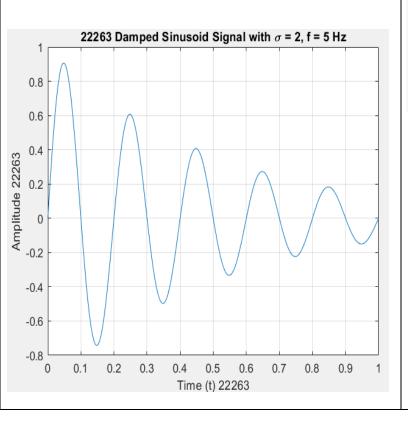
part b)

```
% Define the range for n
n_22263 = -5:10;

% Generate u[n]
u_22263 = n_22263 >= 0; % This creates a logical
array where the condition n >= 0 is true

% Generate u[n-2] by shifting u[n] two places to
the right
% For MATLAB indexing, you need to handle the
shift manually because MATLAB does not support
negative indexing
```





We can observe the output graphs x(t) and x(n) according to the given functions.

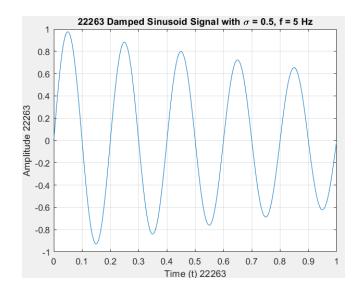
4. Write a user-defined function which generates an exponential damped sinusoid signal x(t) = e $-\sigma t \sin{(2\pi f t)}$. Generate the signal for various values of σ and observe the change in the signal generated (Hint: Take σ , f,t as parameters of the function)

Code(Function):

```
function x_22263 =
generateDampedSinusoid(sigma_22263, f_22263,
t_22263)
    % generateDampedSinusoid generates an
exponential damped sinusoid signal
    % Inputs:
    % sigma - damping coefficient
    % f - frequency of the sinusoid in Hz
    % t - time vector

    % Calculate the signal
    x_22263 = exp(-sigma_22263 * t_22263) .* sin(2
* pi * f_22263 * t_22263);

    % Plot the signal
    plot(t_22263, x_22263);
    ++
    xlabel('Time (t) 22263');
```



```
ylabel('Amplitude 22263');
  title(['22263 Damped Sinusoid Signal with
\sigma = ', num2str(sigma_22263), ', f = ',
num2str(f_22263), ' Hz']);
  % num2str is useful for labeling and titling
plots with numeric values.
  grid on;
end
```

Code(main):

```
t_22263 = 0:0.001:1; % From 0 to 1 second with a
step of 1 ms

% Parameters for the signal
sigma1_22263 = 0.5;
f1_22263 = 5; % 5 Hz

figure;
generateDampedSinusoid(sigma1_22263, f1_22263,
t_22263);

% On trying different values of sigma and f
sigma2_22263 = 2;
f2_22263 = 5; % Keeping frequency same, increasing
damping

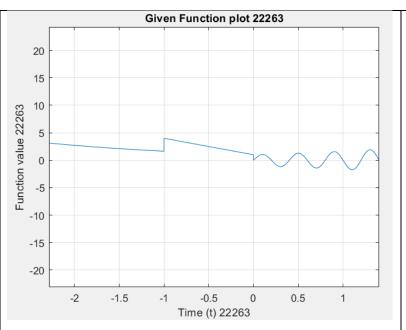
figure;
generateDampedSinusoid(sigma2_22263, f2_22263,
```

Result/Observation:

t_22263);

We can observe 2 examples of an exponential damped sinusoidal signal, also we can observe the change in the dampening on changing the values of σ .

5. Plot the signal given in Figure 1. (Hint: The first section in the figure is an exponentially decaying signal e –0.5 t , –3t+1 from -1 to 0 and last part is e 0.5t sin (5 πt)



Code:

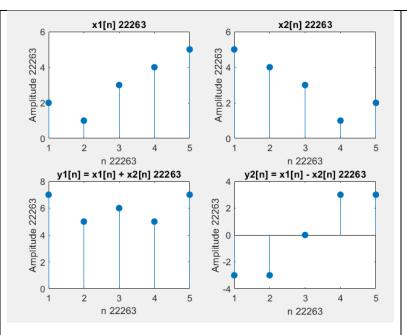
```
% Define the time vectors for each interval
t1 22263 = linspace(-10, -1, 1000); % From -10 to -
t2 22263 = linspace(-1, 0, 1000);
                                     % From -1 to 0
t3_22263 = linspace(0, 4, 1000);
                                    % From 0 to 4
% Calculate the function values for each interval
y1_22263 = exp(-0.5 * t1_22263);
y2_{22263} = -3 * t2_{22263} + 1;
y3_{22263} = exp(0.5 * t3_{22263}) .* sin(5 * pi *
t3_22263);
t_22263=[t1_22263,t2_22263,t3_22263];
y_22263=[y1_22263,y2_22263,y3_22263];
figure;
% Plot each part of the function
plot(t_22263,y_22263);
xlabel('Time (t) 22263');
ylabel('Function value 22263');
title('Given Function plot 22263');
grid on;
```

Result/Observation:

We can observe the output graph to be as how the function was given.

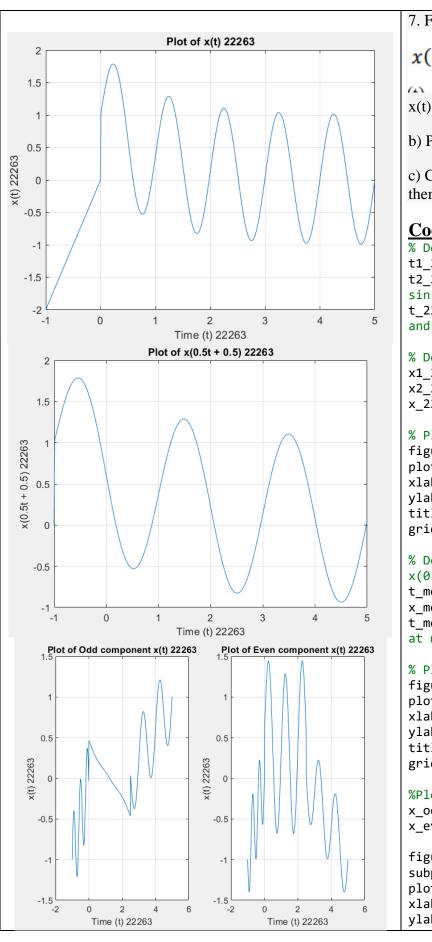
6. Write a function lincomp_RollNO which takes 4 inputs-a,b, x1[n] and x2[n] and generates the signal x3[n] = a x1[n] + b x2[n] where a and b are scalars. Using the abovementioned function, generate the following signals y1[n] = x1[n] + x2[n] and y2[n] = x1[n] - x2[n] where x1[n] = [2,1,3,4,5] and x2[n] = [5,4,3,1,2]. Assume the first value to be the amplitude corresponding to n=0 for both the signals.

Code(Function):



```
y1_22263 = lincomp_RollNO(1, 1, x1_22263, x2);
% Generate y2[n] = x1[n] - x2[n]
y2_22263 = lincomp_RollNO(1, -1, x1_22263, x2);
% Plot x1[n] and x2[n]
subplot(2, 2, 1);
stem(x1_22263, 'filled');
title('x1[n] 22263');
xlabel('n 22263');
ylabel('Amplitude 22263');
subplot(2, 2, 2);
stem(x2, 'filled');
title('x2[n] 22263');
xlabel('n 22263');
ylabel('Amplitude 22263');
% Plot y1[n] and y2[n]
subplot(2, 2, 3);
stem(y1_22263, 'filled');
title('y1[n] = x1[n] + x2[n] 22263');
xlabel('n 22263');
ylabel('Amplitude 22263');
subplot(2, 2, 4);
stem(y2_22263, 'filled');
title('y2[n] = x1[n] - x2[n] 22263');
xlabel('n 22263');
ylabel('Amplitude 22263');
```

We can observe that as we change the values of a and b we get the output graphs for y1 [n] = x1 [n] + x2[n] and y2 [n] = x1 [n] - x2[n] respectively.



7. For the signal

$$x(t) = \begin{cases} 2t & -1 < t \le 0 \\ e^{-t} + \sin(2\pi t) & 0 < t < 5 \end{cases}$$
a) Sketch

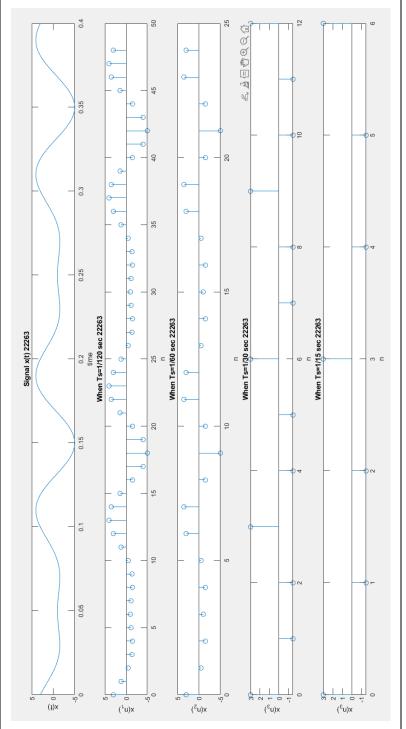
- b) Plot x(0.5*t+0.5)
- c) Compute the odd and even components of x(t) and plot

```
Code:
% Define the time vectors
t1_22263 = linspace(-1, 0, 500); % For 2t
t2_22263 = linspace(0, 5, 1000); % For e^(-t) +
sin(2*pi*t)
t 22263 = [t1 22263, t2 22263(2:end)]; % Combine
and avoid duplicating t=0
% Define x(t)
x1_22263 = 2*t1_22263;
x2_{22263} = exp(-t2_{22263}) + sin(2*pi*t2_{22263});
x 22263 = [x1 22263 x2 22263(2:end)]; % Combine
% Plot x(t)
figure;
plot(t_22263, x_22263);
xlabel('Time (t) 22263');
ylabel('x(t) 22263');
title('Plot of x(t) 22263');
grid on;
% Define the modified time vector and compute
x(0.5t + 0.5)
t_{mod_22263} = 0.5*t_{22263} + 0.5;
x_{mod_22263} = interp1(t_{22263}, x_{22263},
t_mod_22263, 'linear', 'extrap'); % Interpolate x
at modified time points
% Plot x(0.5t + 0.5)
figure;
plot(t_22263, x_mod_22263);
xlabel('Time (t) 22263');
ylabel('x(0.5t + 0.5) 22263');
title('Plot of x(0.5t + 0.5) 22263');
grid on;
%Plotting Even and Odd Components
x_odd_22263=(x_22263-fliplr(x_22263))/2;
x_{even_22263=(x_22263+fliplr(x_22263))/2;}
figure;
subplot(1,2,1);
plot(t_22263,x_odd_22263);
xlabel('Time (t) 22263');
ylabel('x(t) 22263');
```

```
title('Plot of Odd component x(t) 22263');
grid on;

subplot(1,2,2);
plot(t_22263,x_even_22263);
xlabel('Time (t) 22263');
ylabel('x(t) 22263');
title('Plot of Even component x(t) 22263');
grid on;
```

We can observe that as we change the values of a and b we get the output graphs for y1 [n] = x1 [n] + x2[n] and y2 [n] = x1 [n] - x2[n] respectively.



Date:5/2/2024

Work Sheet No. 2 Sampling and its effects

Aim:

To understand the effect of sampling a continuous time signal at Nyquist rate, Under sampling and Oversampling condition.

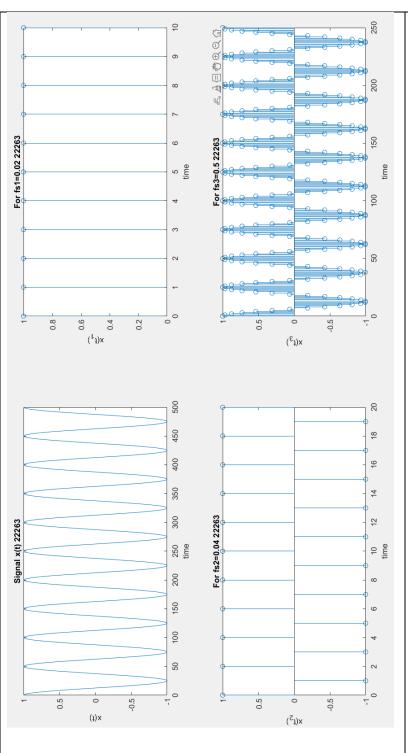
Questions:

- 1. Generate and plot the signal $x(t) = 3\cos(20\pi t) 2\sin(30\pi t)$ over a time range of 0 < t < 400msec. Also plot the discrete time signal formed by sampling this function at the following sampling intervals:
- a) $Ts = 1 \ 120 \ sec$
- b) Ts = 160 sec
- c) $Ts = 1 \ 30 \ sec$
- d) Ts = 1 15 sec Based on your results, comment on how fast this signal should be sampled so that it could be reconstructed from the samples?

```
t_22263=0:0.001:0.4;
x_t_22263= 3*cos(20*pi*t_22263)-
2*sin(30*pi*t_22263);
subplot(5,1,1)
plot(t_22263,x_t_22263)
xlabel('time')
ylabel('x(t)')
title('Signal x(t) _22263')
t1_22263=0:(1/120):0.4;
x1_t_22263 = 3*cos(20*pi*t1_22263)-
2*sin(30*pi*t1 22263);
subplot(5,1,2)
stem(t1_22263*120,x1_t_22263)
xlabel('n')
ylabel('x(n_1)')
title('When Ts=1/120 sec _22263')
t2=0:(1/60):0.4;
x2_t = 3*cos(20*pi*t2)-2*sin(30*pi*t2);
subplot(5,1,3)
```

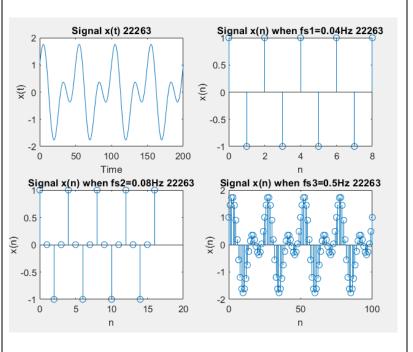
```
stem(t2*60,x2_t)
xlabel('n')
ylabel('x(n_2)')
title('When Ts=1/60 sec _22263')
t3_22263=0:(1/30):0.4;
x3_t_22263 = 3*cos(20*pi*t3_22263)-
2*sin(30*pi*t3_22263);
subplot(5,1,4)
stem(t3_22263*30,x3_t_22263)
xlabel('n')
ylabel('x(n_3)')
title('When Ts=1/30 sec _22263')
t4_22263=0:(1/15):0.4;
x4_t_{22263} = 3*cos(20*pi*t4_{22263}) -
2*sin(30*pi*t4_22263);
subplot(5,1,5)
stem(t4_22263*15,x4_t_22263)
xlabel('n')
ylabel('x(n_3)')
title('When Ts=1/15 sec _22263')
```

Based on my results, this signal should be sampled greater than the Nyquist rate to prevent aliasing, Here the Nyquist rate is 30Hz, therefore fs>=30Hz in order to get a faster reconstructed sample



2.A signal $x(t) = \cos(2\pi f m t)$ with fm=0.02 is sampled at frequencies a) fs1 = 0.02 b) fs2 = 0.04 c) fs3 = 0.5 Generate the signal x(t) and the discrete time signals x[n] for the corresponding sampling frequencies.

```
time_22263=0:0.01:500;
fm 22263=0.02;
fs1=fm_22263;
fs2 22263=0.04;
fs3_22263=0.5;
xoft_22263=cos(2*pi*fm_22263*time_22263);
subplot(2,2,1)
plot(time_22263,xoft_22263);
xlabel('time');
ylabel('x(t)');
title('Signal x(t) 22263');
time1_22263=0:(1/fs1):500;
xoft1 22263=cos(2*pi*fm 22263*time1 22263);
subplot(2,2,2)
stem(time1_22263*0.02,xoft1_22263)
xlabel('time');
ylabel('x(t_1)');
title('For fs1=0.02 22263');
time2_22263=0:(1/fs2_22263):500;
xoft2_22263=cos(2*pi*fm_22263*time2_22263);
subplot(2,2,3)
stem(time2 22263*0.04,xoft2 22263)
xlabel('time');
ylabel('x(t_2)');
title('For fs2=0.04 22263');
time3_22263=0:(1/fs3_22263):500;
xoft3_22263=cos(2*pi*fm_22263*time3_22263);
subplot(2,2,4)
stem(time3_22263*0.5,xoft3_22263)
xlabel('time');
ylabel('x(t_3)');
title('For fs3=0.5 22263');
```

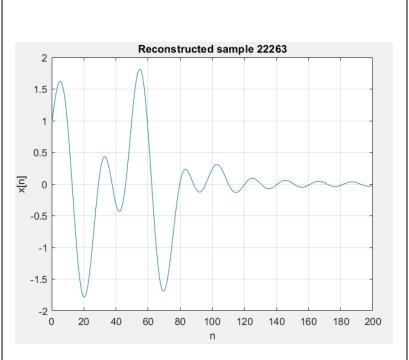


Result:

We have generated the signal x(t) and the discrete time signals x[n] for the corresponding sampling frequencies.

3. Given a signal $x(t) = \cos(0.04\pi t) + \sin(0.08\pi t)$, find the discrete time signal obtained after sampling if the sampling rate is a) fs1=0.04Hz b) fs2=0.08Hz c) fs3=0.5Hz. Generate the signal x(t) and the discrete time signals x[n] for the corresponding sampling frequencies. What do you observe?

```
Time 22263=0:0.001:200;
X_t_{22263}=cos(0.04*pi*Time_{22263}) +
sin(0.08*pi*Time_22263);
subplot(2,2,1)
plot(Time_22263, X_t_22263)
xlabel('Time')
ylabel('x(t)')
title('Signal x(t) 22263')
Fs1 22263=0.04;
Fs2 22263=0.08;
Fs3 22263=0.5;
Time1_22263=0:(1/Fs1_22263):200;
X_{t1_22263}=cos(0.04*pi*Time1_22263) +
sin(0.08*pi*Time1 22263);
subplot(2,2,2)
stem(Time1_22263*Fs1_22263,X_t1_22263)
xlabel('n')
ylabel('x(n)')
title('Signal x(n) when fs1=0.04Hz 22263')
Time2_22263=0:(1/Fs2_22263):200;
X t2 22263 = cos(0.04*pi*Time2 22263) +
sin(0.08*pi*Time2_22263);
subplot(2,2,3)
stem(Time2_22263*Fs2_22263,X_t2_22263)
xlabel('n')
ylabel('x(n)')
title('Signal x(n) when fs2=0.08Hz 22263')
```



```
Time3_22263=0:(1/Fs3_22263):200;
X_t3_22263 = cos(0.04*pi*Time3_22263) +
sin(0.08*pi*Time3_22263);
subplot(2,2,4)
stem(Time3_22263*Fs3_22263,X_t3_22263)
xlabel('n')
ylabel('x(n)')
title('Signal x(n) when fs3=0.5Hz 22263')
sum_22263 =0;
for i=0:2:100
sum_22263 = sum_22263 + ((cos(0.04*pi*i) +
sin(0.08*pi*i)).* sinc((0.3/pi)*(Time_22263-i)));
X_{t4_{22263}} = ((0.3/pi)*2)*sum_{22263};
figure;
plot(Time_22263,X_t4_22263);
title('Reconstructed sample 22263');
xlabel('n');
ylabel('x[n]');
grid on;
```

At frequencies greater than Nyquist rate which in this case is 0.08, we can see a perfectly or more accurately reconstructed signal in the discrete time domain if we see the second graph in column 2. For fs=0.04 we see that aliasing occurs and for fs=0.08 we can see that it is not sampled very accurately but is better than the first graph. Also the final reconstructed signal is also observed.

Date:19/2/2024

Work Sheet No. 3 Sampling and its effects

Aim:

To understand the effect of sampling a continuous time signal at Nyquist rate, Under sampling and Oversampling condition.

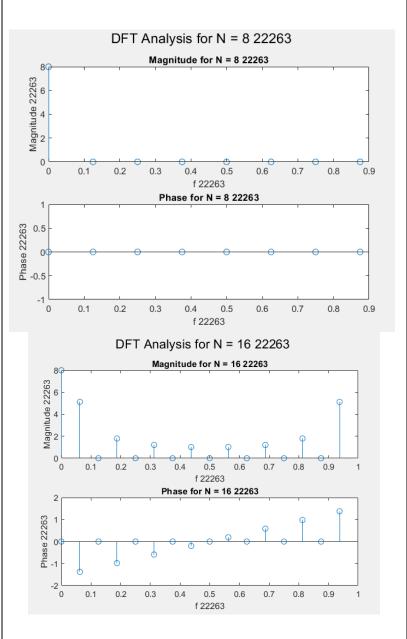
Questions:

1. Write a function to calculate the DTFT of a given signal given by $X(\Omega) = \sum x[n]e \ N-1 - j\Omega n$ n=0. (Hint: Take Ω , n and x[n] as input to the function) and use it to compute the DTFT of the signal x[n]=u[n]-u[n-8].

Code(Function):

Code(Main):

```
n 22263=0:10;
omega 22263=0:0.001:2*pi;
x_22263=[ones(1,8),zeros(1,3)];
X_22263=dtft(x_22263,n_22263,omega_22263);
subplot(3,1,1);
plot(omega 22263,X 22263);
title('Plot of \Omega Vs X(\Omega)');
xlabel('\Omega (radians/sample)');
ylabel('X(\Omega)');
grid on;
subplot(3,1,2);
plot(omega_22263,abs(X_22263));
title('Magnitude of DTFT 22263');
xlabel('\Omega (radians/sample)');
ylabel('|X(\Omega)|');
grid on;
```

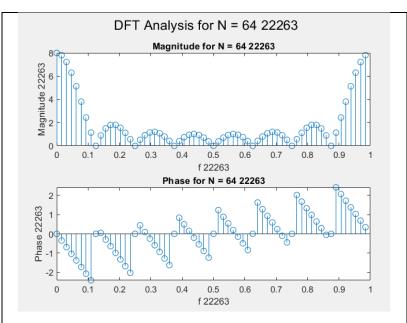


```
subplot(3,1,3);
plot(omega_22263,angle(X_22263))
title('Phase of DTFT 22263');
xlabel('\Omega (radians/sample)');
ylabel('\ZX(\Omega)');
grid on;
```

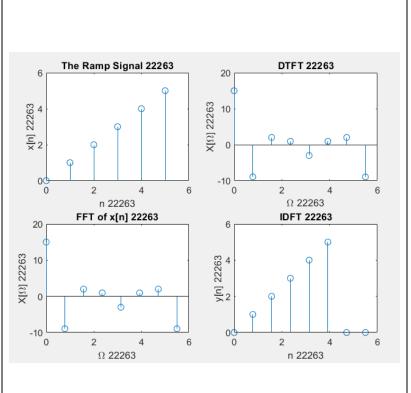
We have generated DTFT of $X(\Omega)$ and plotted the magnitude and phase spectrum.

2. A discrete time signal is given as x[n] = 1 for $0 \le n \le 7$. Find the DFT of x[n] for N=8, N=16 and N=64. (Use MATLAB command fft). Plot magnitude response and phase spectrum and observe the changes in both the spectra while changing N.

```
n 22263 = 0:7;
x_{22263} = ones(size(n_{22263}));
N_values_22263 = [8, 16, 64];
for N = N_values_22263
X_{22263} = fft(x_{22263}, N);
f_{22263} = (0:N-1) / N;
mag 22263 = abs(X 22263);
phase_22263 = angle(X_22263);
figure;
subplot(2, 1, 1);
stem(f_22263, mag_22263);
title(['Magnitude for N = ', num2str(N),'
22263']);
xlabel('f 22263');
ylabel('Magnitude 22263');
subplot(2, 1, 2);
stem(f_22263, phase_22263);
title(['Phase for N = ', num2str(N),' 22263']);
xlabel('f 22263');
ylabel('Phase 22263');
sgtitle(['DFT Analysis for N = ', num2str(N),'
22263']);
end
```



For the three values of N we have generated the fft and we can observe the change in the magnitude and phase response for all 3 values of N. The higher the value of N the better is the magnitude and phase.

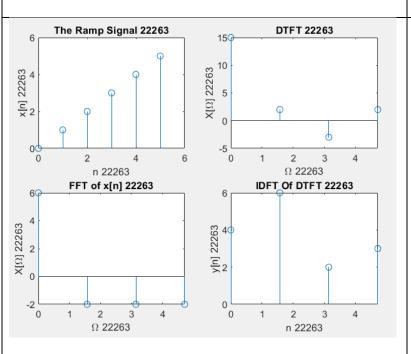


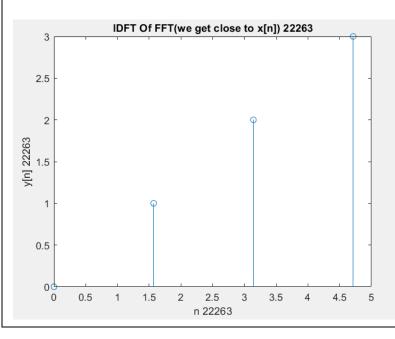
- 3. The sequence x[n] is a length-6 sequence defined for $0 \le n \le 5$ and given as $x[n]=\{0,1,2,3,4,5\}$.
- (a) Using the function prepared in Question 1, Calculate the DTFT of x[n] at eight equally spaced point given by $\Omega k = 2\pi k \ 8 \ 0 \le k \le 7$. Also apply an eight-point inverse DFT to these DFT samples to get y[n]. From the result, observe how to extract the original sequence x[n].
- (b) Using the function prepared in Question 1, Calculate the DTFT of x[n] at four equally spaced points given by $\Omega k = 2\pi k \ 4 \ 0 \le k \le 3$. Also apply a four-point inverse-DFT to these DFT samples to get y[n]. From the result, observe how to extract the original sequence x[n]. (Hint: For inverse DFT use the inbuilt function ifft)

Code: Part a)

```
n_22263=0:1:5;
x_22263=n_22263;
k 22263=0:7;
omega_22263=(2*pi*k_22263)/8;
X 22263=dtft(x 22263,n 22263,omega 22263);
X1 22263=fft(x 22263,8);
X2_22263=ifft(X_22263,8);
subplot(2,2,1);
stem(n_22263,x_22263);
xlabel('n 22263')
ylabel('x[n] 22263')
title('The Ramp Signal 22263')
subplot(2,2,2);
stem(omega_22263,X_22263);
xlabel('\Omega 22263')
ylabel('X[\Omega] 22263')
title('DTFT 22263')
subplot(2,2,3);
stem(omega_22263,X1_22263)
xlabel('\Omega 22263')
ylabel('X[\Omega] 22263')
title('FFT of x[n] 22263')
```

```
subplot(2,2,4);
stem(omega_22263,X2_22263);
xlabel('n 22263')
ylabel('y[n] 22263')
title('IDFT 22263')
```





```
Part b)
n 22263=0:1:5;
x_22263=n_22263;
k_22263=0:3;
omega_22263=(2*pi*k_22263)/4;
X_22263=dtft(x_22263,n_22263,omega_22263);
X1_22263=fft(x_22263,4);
X2_22263=ifft(X_22263,4);
subplot(2,2,1);
stem(n 22263,x 22263);
xlabel('n 22263')
ylabel('x[n] 22263')
title('The Ramp Signal 22263')
subplot(2,2,2);
stem(omega_22263,X_22263);
xlabel('\Omega 22263')
ylabel('X[\Omega] 22263')
title('DTFT 22263')
subplot(2,2,3);
stem(omega_22263,X1_22263)
xlabel('\Omega 22263')
ylabel('X[\Omega] 22263')
title('FFT of x[n] 22263')
subplot(2,2,4);
stem(omega_22263,X2_22263);
xlabel('n 22263')
ylabel('y[n] 22263')
title('IDFT 22263')
```

From the resultant graphs, we observe how to extract the original sequence x[n], which is by taking the IDFT of the DTFT in part (a), in part b if we take the IDFT of FFT we get x[n] to some extent but not a perfect signal.

