

## Black Scholes Call Price,

Using the Black Scholes formula

$$C_0 = S_0 N(d_1) - X e^{-rT} N(d_2)$$

Given the information

$$S_0 = \text{stock price} = \$40$$

$$X = \text{Strike price} = \$45$$

$$T = \text{time of expiration} = 4 \text{ months} = \frac{4}{12} = 0.33 \text{ yrs}$$

$$r = \text{risk of free interest rate} = 3\% = \frac{3}{100} = 0.03$$

$$\sigma = \text{standard deviation of log returns (i.e. volatility)} = 40\% = \frac{40}{100} = 0.4$$

Where;

$$d_1 = \frac{\ln\left(\frac{S_0}{X}\right) + \left(r + \frac{\sigma^2}{2}\right)T}{\sigma\sqrt{T}}$$

$$d_1 = \frac{\ln\left(\frac{40}{45}\right) + \left(0.03 + \frac{(0.4)^2}{2}\right)0.33}{0.4\sqrt{0.33}}$$

$$d_1 = \frac{-0.1178 + 0.0363}{0.2298}$$

$$d_1 = -0.3547$$

$$d_1 \approx -0.35$$

Also,

$$d_2 = d_1 - \sigma\sqrt{T}$$

$$d_2 = -0.3547 - 0.2298$$

$$d_2 = -0.5845$$

$$d_2 \approx -0.58$$

Because  $d_1$  and  $d_2$  are negative, we use

$$N(d_1) = 1 - N(-d_1) \quad \text{and} \quad N(d_2) = 1 - N(-d_2)$$

Looking up the standard normal distribution table,

$$d_1 = 0.35 \quad d_2 = 0.58$$

From the table.

$$d_1 = 0.6368$$

$$d_2 = 0.7190$$

Therefore

$$N(d_1) = 1 - 0.6368$$

$$N(d_1) = 0.3632$$

Also,

$$N(d_2) = 1 - 0.7190$$

$$N(d_2) = 0.281$$

Using these values in our Black-Scholes formula, we have;

$$C_0 = \$40 (0.3632) - \$45 (e^{-0.03(0.33)} \times 0.281)$$

$$C_0 = \$40 (0.3632) - \$45 (0.9901 \times 0.281)$$

$$C_0 = \$14.528 - \$45 (0.2782)$$

$$C_0 = \$14.528 - \$12.520$$

$$C_0 = \$2.008$$

Therefore, the Black Scholes call price is **\$2.008**