Abjad, A Python API for Formalized Score Control

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ABSTRACT

Place your abstract at the top left column on the first page. Please write about 150-200 words that specifically highlight the purpose of your work, its context, and provide a brief synopsis of your results. Avoid equations in this part.

1. INTRODUCTION

2. BACKGROUND & HISTORY

2.1 Composition as Notation

Conventional western notation implies two kinds of information analysis: graphic specification divides an instruction into perceptually fused but independently specified aspects (pitch, rhythm, dynamic) and segregates event information (notes) from sound production information (instructions for how to play an instrument to produce sound, described via performance practice or graphically through tablature notation) [1, 83]. While many environments for both notation and sound production have arisen within the last twenty years, the following discussion focuses solely on the production of notation: Abjad enables composers to express both low- and high-level compositional ideas with the aid of a widely used programming language that provides a sufficiently detailed object model of common practice musical notation. The present discussion defines composition narrowly as the act of creating a document.

2.2 Computational Models of Music/Composition

Computational models of music might entail the representation of higher-level musical entities apparent in the acts of listening and analysis but absent in the symbols of notation themselves, as determined to be creatively exigent. Programming researchers and musical artists have modeled many such extrasymbolic musical entities, such as large-scale form and transition [2], [3], [4], [5], [6], texture [7], contrapuntal relationships [8], [9], [10], [11], [12], [3], [13], [14], [15], [16], [17], [18], harmonic tension and resolution [19], [20], [21], melody [22], [23], meter [24],

rhythm [25], [26], [27], timbre [28], [29], [30], temperament [31], [32], and ornamentation [33], [34]. This work overlaps fruitfully with analysis tasks, and models of listening and cognition can enable novel methods of high-level musical structures and transformations, like dramatic direction, tension, and transition between sections [35, 108].

The set of typographical notation symbols overlaps with the set of extra-symbolic musical entities, often causing confusion in discourse and program architecture. For example, a "chord" might be a vertically ordered collection of pitch classes in a harmonic conceit, or it might refer to the specific arrangement of pitched noteheads, stemmed together into a composite notation symbol that instructs a performer to perform a sound that consists of several component pitches. Due to substantial overlap in vocabulary between musical and notational concepts, it can be difficult to separate a system's model of music/composition from its model of notation.

A system that affords a detailed model of music/composition without linking it to a sufficiently detailed model of musical notation does not afford automated notation — sufficiency, however, depends heavily on generative task. For example, if a composer requires an automated notation system to render complex rhythmic ideas that depend typographically on nested tuplets, a system that produces a notation only via a combination of MIDI and quantization must reduce rhythms to a non-hierarchical stream of event times, eliminating the temporally divisive approach of tuplet notation. For many rhythmic applications, though, MIDI suffices.

2.3 Computational Models of Notation

Many automated notation systems exist to model musical notation and the act of typographical layout without explicitly affording the computational modeling of music or composition [40], [41], [42], [43]; many of these systems strongly imply a model of music, such as Grégoire for Gregorian chant, Django for guitar tablature, and GOOD-FEEL for Braille notation [44]. In this light, feature-rich systems oriented toward classical composers, such as Finale, Sibelius, SCORE, Igor, Berlioz, and Nightingale fit into the mold of systems that model notation with genre as a primary determinant of generative task. Such a system might go so far as to enable a text-based object-oriented model of notation that automates some aspect of an other-

wise point-and-click interface, as in the case of Sibelius's ManuScript scripting language [45].

Many models of musical notation were created for purposes of corpus-based computational musicology. Formats such as DARM, SMDL, HumDrum, and MuseData model notation with the generative task of searching through a large amount of data [46]. Commercial notation software developers attempted to establish a data interchange standard for optical score recognition (NIFF) [47]; since its release in 2004, MusicXML has become a valid interchange format for over 160 applications and maintains a relatively application-agnostic status, as it was designed with the generative task of acting as an interchange format between variously tasked systems [48].

Notation representations that underly many of these GUI-based systems often go undescribed as computer representations of notation, in favor of discussions about human-computer interaction. For example, Barker and Cantor developed an early model of music notation that underlies a four-oscilloscope GUI and describe their work entirely in terms of user interaction [49]; likewise, discussions of modern commercial notation systems remain similarly oriented, without much awareness or criticism of the underlying computational models of notation. This results in insufficiently detailed models of notation; systems, for example, that provide models only of mensural notation and enable nonmensural notations only as modified instantiations of notations based on measures.

2.4 The Development of Hierarchical Object Models of Notation

Many early models of musical notation were not hierarchical, and Lejaran Hiller, in reflecting on decades of automated notation work, identifies the lack of hierarchical organization as a limitation of early work — although Nick Collins points out that even Hiller's program PHRASE addresses the hierarchical organization of a score up to the level of a phrase, without moving beyond this mid-level musical structure to concerns of large-scale form [35, 108].

There were several object-oriented music environments by 1990 [50, 139], most created in or inspired by the newly popular Smalltalk-80 programming language; while they facilitated the hierarchical modeling of musical abstractions, they omitted or radically simplified the hierarchical nature of common notation. For example, Glen Krasner (Xerox Systems Science Laboratory) created Machine Tongues VIII, a music system that created an object-oriented model of the score/orchestra distinction inherited from Max Mathews' Music N languages, with a simple linear model of "partOn" and "partOff" command sequences [51], omitting hierarchical organization entirely when the system produced notational output; although subsequent Machine Tongues systems introduced some hierarchical organization via "note" objects that inhabited "event lists," systems did not attempt to model the hierarchical detail of all a traditional score's elements. Like Hiller's PHRASE program, Andreas Mahling's CompAss system organized events hierarchically up to the mid-level "phrase" level of musical structure [52]. These systems extend Smalltalk-80 with interfaces to the MIDI

communications protocol: as extensions of Smalltalk, they enabled the user to arbitrarily extend the system with new objects, creating a detailed and hierarchical model of music, usually flattened into a list of noteOn and noteOff commands to be notated or played back via MIDI interface.

By 1989, Glendon Diener's Nutation system (written in Objective C for the NeXT computer) modeled both musical and notational structure hierarchically through the use of directed graphs [55], [56], [57].

3. NOTATIONAL ISOMORPHISM

Abjad models objects on the page according to common practice notation.

3.1 Notational aggregation

We assume notational primitives are the elements of composition.

We consider the act of composition then to revolve around the iterative aggregation of notational primitives into arbitrarily complex score objects.

- append(), extend(), insert()
- attach()

3.2 Notational visualization

Abjad makes visualizing notational artifacts simple.

Any notational element or aggregate can be displayed at any time as a PDF via calls to its top-level show() function.

3.3 Explicit notational modeling

Abjad models notation explicitly. All notational primitives expressed by Abjad must conform to the principles of common practice notation. When compositional inputs cannot be expressed in terms of these principles, we provide affordances for massaging them into valid notational states.

For example, Abjad expresses the durations of all score components in terms of rational values – fractions and integers – rather than floating point numbers. Likewise Abjad expresses all pitches in terms of triples of diatonic note names, accidentals and octave numbers, rather than MIDI numbers or frequencies. While we provide alternative representations of pitch and rhythm, as well as affordances for moving between them, the format actually stored in and used by score components for rendering notation is always the most notationally-explicit.

3.4 Written, assignable and prolated durations

All Note, Chord and Rest objects in Abjad must be instantiated with a duration corresponding to the written glyphs on the page – a *written* duration.

Written durations must be *assignable*, a category we invented to model durational initialization. Durational assignability describes whether a duration can be represented as a power-of-two flag count combined with zero or more dots. 1/4, 3/16 and 7/16 are assignable durations while 5/32, 9/8 and 1/12 are not.

Non-assignable durations cannot be represented in common practice notation by a single glyph. They require two

or more glyphs with assignable durations tied together, for the score component to be tupletted, or both.

Abjad will not automatically render a single note with a duration of 5/16 as two or more notes tied together. We consider such behavior to be too implicit. There are too many potentially compositionally valid ways to render a duration such as 5/16 into a series of tied assignable durations: `1/4 + 1/16, 3/16 + 2/16, 2/16 + 3/16, 1/16 + 1/4, 1/8 + 1/8 + 1/16` etc. Instead we provide affordances for generating tied notes from non-assignable durations. One such affordance is our `scoretools.make_notes()` function, which chooses smart defaults for generating tied glyphs from otherwise un-notateable input.

```
>>> staff = Staff(selection)
>>> show(staff)
```

All score components also have a *prolated* duration - the product of their written duration and their *prolation*. Prolation is the cumulative product of all the *multiplier* of every tuplet found in the *parentage* of a score component. A score component's prolation depends on its location in the score hierarchy, and is not an inherent property of itself independent that hierarchy.

Three `Note` objects each having a prolated duration of 1/12 can be represented as either three 1/16 notes in a 3:4 tuplet or as three 1/8 notes in a 3:2 tuplet. As all Abjad `Note` objects must have an assignable written duration, the three notes above must have written durations of either 1/8 or 1/16, and the tuplet must be correspondingly an explicit diminution or augmentation to provide the desired prolation of 2/3 or 4/3.

```
>>> tuplet = selection[0]
>>> show(tuplet)
```

```
>>> show(tuplet)
```

The durational information of any aggregate score object in Abjad is therefore always explicit and unambiguous with regard to its notational reality.

4. RELATIONSHIP MODELING

5. SCORE ADDRESSABILITY

6. EXTENSIBILITY

7. EMBEDDABILITY

Abjad is an importable Python library. It can be used in whole or in part as a component of any Python-compatible system. Abjad has few Python package dependencies and is not bound to any specific user application or graphic user interface. These qualities make Abjad an ideal project ideal for embedding in other software systems.

For example, Abjad supports IPython Notebook [1], a web-based interactive computational environment combining code execution, text, mathematics, plots and rich media into a single document. Notational output from Abjad can be transparently captured and embedded directly into an IPython Notebook which has loaded Abjad's IPython Notebook extension.

8. OPEN SOURCE

Acknowledgments

You may acknowledge people, projects, funding agencies, etc. which can be included after the second-level heading "Acknowledgments" (with no numbering).

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