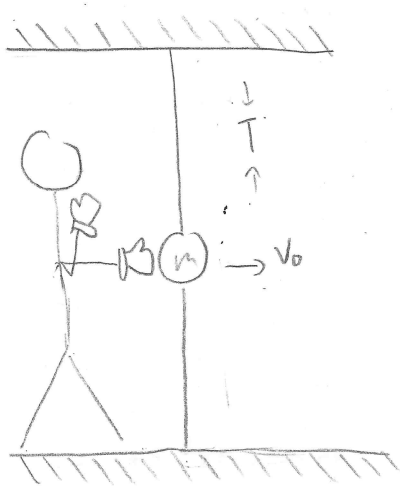
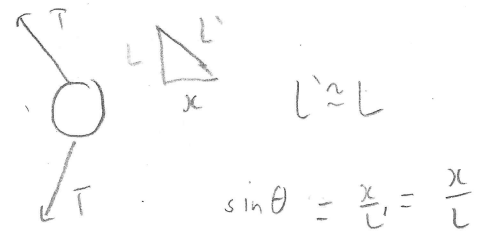


20-R-VIB-DY-3 Intermediate

A new type of punching bag to be used in space consists of a 5kg ball suspended mid air by 2m long elastic ropes, each with a tension of 25N. One rope connects the ball to the ceiling and the other to the ground. If an impact results in an initial velocity of 2 m/s , find the equation of motion.



Solution:



$$\sum F_x = m a_x$$

$$-2T \sin \theta = m a_x$$

$$-2T \frac{x}{L} = m \ddot{x}$$

$$m \ddot{x} + 2T \frac{x}{L} = 0$$

$$\ddot{x} + \frac{2T}{mL} x = 0 \quad \omega_n = \sqrt{\frac{2T}{mL}} = \sqrt{5}$$

$$x = A \sin \omega_n t + B \cos \omega_n t$$

$$\dot{x} = A \omega_n \cos \omega_n t - B \omega_n \sin \omega_n t$$

$$x(0) = B = 0$$

$$\dot{x}(0) = A \omega_n = 2 \text{ m/s} \quad A = \frac{2}{\sqrt{5}}$$

$$x = \frac{2}{\sqrt{5}} \sin \sqrt{5} t$$