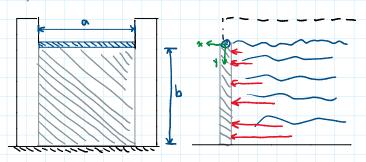
20-R-IM-DK-3

Principle of Impulse and Momentum Advanced

Inspiration: None



A salmon hatchery has a gate to release water whenever water levels get too high. The gate is normally locked into place, but when the water reaches the top of the gate, the lock is instantly removed. While the water would flow out of the gate by itself, there is a pump located upstream from the gate to push water forward. The pump is old so its power slowly ramps up with time. The gate consists of a slender rod in which a 20 kg thin plate is attached. The plate has dimensions a = 1.5 m, b = 2m and rotates about the slender rod as if it were a pin. Although there is a seal such that water may not get out, assume the contact between the plate and other surfaces is frictionless. If the gate is subjected to water from the pump that applies a force distribution with a magnitude that is related to both the y-coordinate and time  $dF = (-t(y-2)^2 + 8t) dy N$ , determine the angular velocity of the gate after t = 2 seconds if the gate

Add hint to Webwork suggesting to use external solver



F = SaF = 52 (- (4-2) + 9+ ) dy = + 52 (-(4-2) + 9) dy = t [ - \frac{1}{3} + 24 + 44 + 44 ] = t [ - \frac{1}{3} + 24 + 44 ] = \frac{1}{9} t

a is the location of the

Equivalent singular force F

To find where the equivalent force is located, equate the moments on each side of the equivalent force  $\int_0^a y dF = \int_a^2 y dF$  y dF is  $rF \Rightarrow M$ 

\* (-42+44+4) dy = \$ (2 4 (-42+44) dy

=> ( -43 +442+44 dy = ( -43 +442+44 d4

- 4 a" + 4 a3 + 2a2 = (-4(2)" + 4(2)" + 2(2)") - (-4 a" + 4 a3+2a2)

-12 a4 + \$ a3 + 4 a2 = 14.66

a= 1.46501 or 6.46255 within bounds not within bounds a should be in between 0 and 2 as the height of the gate goes up to 2

Equivalent force F=40t is located at a which is at y=1.46501

Ipw, + 2 1th Mp at = Ipw2 => Irod Wi + Iprote W, + St r F at = Irod Wz + Iprote Wz

O(0) + 12mb2(0) + 10 a F dt = 12mb2 wz

So (1.46501) (40 t) dε = 12 (20)(2) ω2

(1.46501)(42) [ 1/2 t2] = 1/2 (20)(2) wz

39.066933 = 20 W2 | W2 = 5.86004 (ad/s