



In the 2D system above, the springs are stretched and are in static equilibrium. If the unstretched length of spring  $AB$  is  $x_{AB0}$  m, find the mass of the block at D. Assume the spring  $AB$  includes the uncoiled length between A and B.

What is the stretch in spring  $AB$ ?

$$|AB| = \sqrt{3^2 + 4^2} = 5 \text{ m}$$

$$|AC| = \sqrt{3^2 + 3^2} = 3\sqrt{2} \text{ m}$$

$$\text{If } x_{ABf} = |AB| = 5 \text{ m,}$$

$$\Delta x_{AB} = x_{ABf} - x_{AB0} = (5 - x_{AB0}) \text{ m}$$

Determine the force exerted by the  $AB$  spring.

$$T_{AB} = (30 * \Delta x_{AB}) \text{ N}$$

Finally, find the mass of the block at D.

$$\Sigma F_x = 0 \rightarrow \frac{d_3}{|AB|} T_{AB} - \frac{d_2}{|AC|} T_{AC} \rightarrow T_{AB} = \frac{d_2 |AB|}{d_3 |AC|} T_{AC} = \frac{15}{12\sqrt{2}} T_{AC} \rightarrow T_{AB} = \frac{5}{4\sqrt{2}} T_{AC}$$

$$\text{or } T_{AC} = \frac{4\sqrt{2}}{5} T_{AB}$$

$$\Sigma F_y = 0 \rightarrow \frac{d_1}{|AB|} T_{AB} + \frac{d_1}{|AC|} T_{AC} - T_{AD} = 0$$

$$\rightarrow T_{AD} = \frac{d_1(d_2 + d_3)}{d_3 |AC|} T_{AC} = \frac{21}{12\sqrt{2}} T_{AC} = \frac{7}{5} T_{AB}$$

$$T_{AD} = m_D * g$$

$$\rightarrow m_D = \frac{42}{g} (5 - x_{AB0}) \text{ kg}$$