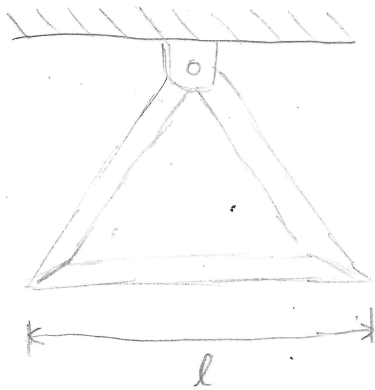


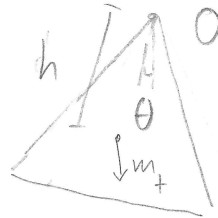
20-R-VIB-DY-50 Intermediate

An equilateral triangle frame is made up of three individual bars. Each bar is 3m in length and 2kg in mass. Given that the frame is hung on the ceiling by one of its corners, determine the natural frequency.



$$m_t = 3m = 6 \text{ kg}$$

Solution FBD:



$$h = \frac{2}{3}(3 \sin 60) \\ = 2 \sin 60$$

$$\sum M_o = -I_o \alpha$$

$$mg h \sin \theta = -I_o \ddot{\theta}$$

small θ

$$mg h \theta + I_o \ddot{\theta} = 0$$

$$I_o = 2\left(\frac{1}{3} m l^2\right) + \frac{1}{12} m l^2 + m d^2$$

$$d = 3 \sin 60$$

$$I_o = 27$$

$$\omega_n = \sqrt{\frac{m g h}{I_o}} = 1.943$$