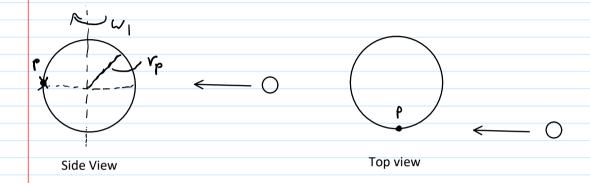
August 7, 2020 5:36 PM

An uninhabited rogue planet is spinning in space with a mass of 11944*10^24 kg, and a radius of 12742km. It is spinning with an angular velocity of 5.402*10^-5 rad/s clockwise, when an asteroid collides at point P and sticks with the edge of the planet. The mass of the asteroid is 2.9*10^21 kg, and collides with a speed of 33,528 m/s. The asteroid collides with the planet along its equator, in the same direction as its rotation. What is the new angular velocity of the planet?

Assume the asteroid is a point mass.



$$(H_{sys})_1 = (H_{sys})_2$$
 $m_a = 2.9 \cdot 10^2 kg$ $V_a = 33521 mls$ $V_p = 12742 km = 12742 000 m$ $V_p = 1.742 km = 1.742 000 m$ $V_1 = 5.402 \times 10^{-5} \text{ rad/s}$ $V_2 = 11.944 \times 10^{24} \text{ kg}$

$$I_{P_1} = \frac{2}{5} m_P r_P^2 = \frac{3}{5} (11.944 \times 10^{24}) (12.742000 m)^2$$

- 7.757 x 1038

$$I_{P2} = \frac{2}{5} \left(m_{P} + m_{a} \right) \left(r_{P}^{2} \right) = \frac{2}{5} \left(2.9 \times 10^{21} + 11.944 \times 10^{24} \right) \cdot \left(12742000 \right)^{2}$$

$$= 7.759 \times 10^{38}$$

$$W_2 = \underbrace{\frac{\text{I}p_1 W_1 + (m_a \cdot v_a \cdot r_p)}{\text{I}p_2}}$$

$$= 7.757 \times 10^{38} \cdot 5.402 \times 10^{-5} + 2.9 \times 10^{21} \cdot 33528 \cdot 12742000$$

$$7.759 \times 10^{38}$$

The new angular velocity is 5.56 radls in the clackwise direction