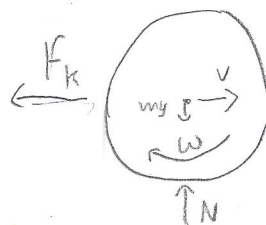
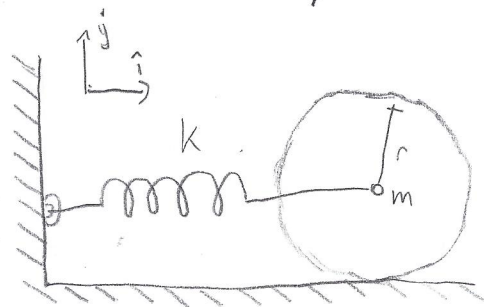


20-R-VIB-DY-22 Intermediate

A new pizza cutter consists of a spring ($k = 10 \text{ N/m}$) and a lightweight ($m = 0.5 \text{ kg}$) circular blade with the radius $r = 0.25 \text{ m}$. Assuming that the wheel does not slip with the ground, if the blade is given an initial velocity of 2 m/s find the equation of motion. Solution: FBD



$$I_G = \frac{1}{2} m r^2 = 0.015625$$

$$T = \frac{1}{2} I_G \omega^2 + \frac{1}{2} m v^2 =$$

$$v = \omega r = 0.25 \omega$$

$$= 0.0234375 \omega^2$$

$$V = \frac{1}{2} k x^2 = \frac{1}{2} (10) (0.25 \theta)^2 = 0.3125 \theta^2$$

$x = r \theta$

$$E = T + V = 0.0234375 \dot{\theta}^2 + 0.3125 \theta^2$$

$$\dot{E} = 0.046875 \ddot{\theta} \dot{\theta} + 0.625 \dot{\theta} \theta$$

$$= \dot{\theta} (0.046875 \ddot{\theta} + 0.625 \theta)$$

$$\ddot{\theta} + \frac{40}{3} \theta = 0 \quad \omega_n = \sqrt{\frac{40}{3}}$$

$$\theta = A \sin \omega_n t + B \cos \omega_n t$$

$$\dot{\theta} = A \omega_n \cos \omega_n t - B \omega_n \sin \omega_n t$$

$$\theta_p(0) = B = \theta_0 = 0$$

$$v_0 = \omega_0 r \quad \omega_0 = 8 \text{ rad/s}$$

$$\dot{\theta}_p(0) = A \omega_n = \omega_0$$

$$A = 8 \sqrt{\frac{3}{40}}$$

$$\theta(t) = \underline{8 \sqrt{\frac{3}{40}} \sin \sqrt{\frac{40}{3}} t}$$