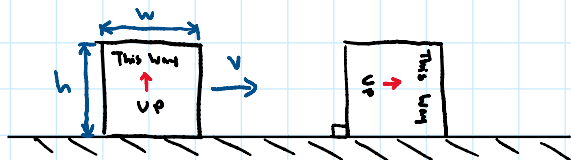


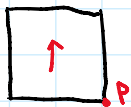
Intermediate Eccentric Impact

Inspiration: 19-45 Hibbeler

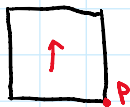


You are helping your friend move into their new place. While sliding a box full of fragile things on a frictionless floor, the box gets caught on a small bar in the doorway and tips over on its side. Oops. If the box has a mass $m = 20 \text{ kg}$, a height of $h = 0.4 \text{ m}$, and a width of $w = 0.4 \text{ m}$, determine how fast the box had to be moving in order for this to happen. Assume the weight of the box during the impact was non-impulsive and that the size of the bar is negligible.

Stage 1
Just before impact



Stage 2
Just after impact



Stage 3



$$\begin{aligned} I_P &= \frac{1}{12} m (a^2 + b^2) + m d^2 \\ &= \frac{1}{12} (20) (0.4^2 + 0.4^2) + (20) (\sqrt{0.2^2 + 0.2^2})^2 \\ &= \frac{32}{15} \end{aligned}$$



$$\frac{0.2}{h_3} = \sin 45 \quad h_3 = \frac{0.2}{\sin 45} = \frac{\sqrt{2}}{5}$$

Set datum as the ground

$$T_2 + V_2 = T_3 + V_3$$

$$\frac{1}{2} I_O \omega_1^2 + mgh_2 = 0 + mgh_3$$

$$\frac{1}{2} \left(\frac{32}{15} \right) \omega_1^2 + (20)(9.81)(0.2) = (20)(9.81) \left(\frac{\sqrt{2}}{5} \right)$$

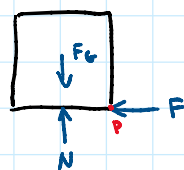
$$\omega_1 = 3.90357$$

$$(H_P)_1 = (H_P)_2$$

$$I_G \vec{\omega}_1 + \left(-\frac{w}{2} \hat{i} + \frac{h}{2} \hat{j} \right) \times (m)(v_G \hat{i}) = I_G \vec{\omega}_2 + r_{G/P} \times \vec{L}_2$$

$$0.2 (20) v = \frac{32}{15} (3.90357)$$

$$v = 2.0819 \text{ m/s}$$



$\int F_G dt$ and $\int N dt$ are negligible
Angular momentum conserved about P