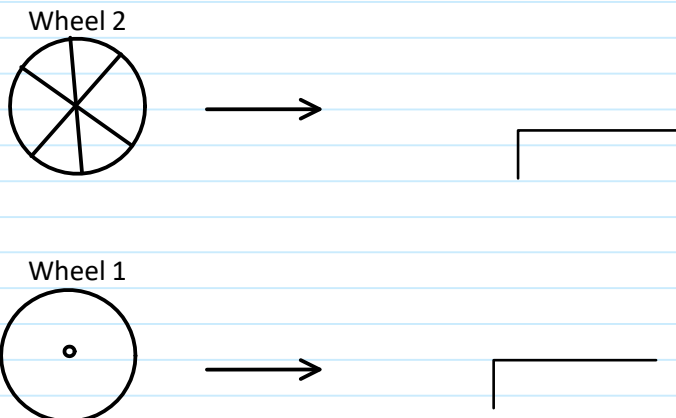


## 20-R-IM-PT-3

July 3, 2020 7:06 PM

Two wheels roll over identical obstructions of a height  $h = 0.04 \text{ m}$  on a road. One is a solid wooden wheel, with a mass  $m_1 = 5 \text{ kg}$  and radius  $r_1 = 0.5 \text{ m}$ . The other wheel has 5 spokes, a rim with mass  $m_2 = 3 \text{ kg}$ , and a radius of  $r_2 = 0.55 \text{ m}$ . Each spoke has a mass of  $0.25 \text{ kg}$ . Which wheel needs a higher velocity to roll over the obstacle and by how much?



Both wheels:

Cons. of Angular Momentum

$$(H\omega)_1 = (H\omega)_2$$

$$r_1 = r$$

$$m(r_1 - h)(v_{b1}) + I_G \omega_1 = r m(v_{b2}) + I_G \omega_2 \quad \omega_1 = \frac{v_{b1}}{r} \quad \omega_2 = \frac{v_{b2}}{r}$$

$$m(r_1 - h)(v_{b1}) + I_G \left(\frac{v_{b1}}{r}\right) = r m(v_{b2}) + I_G \left(\frac{v_{b2}}{r}\right)$$

$$v_{b1} = \frac{\left(r \cdot m + \frac{I_G}{r}\right)}{\left(m(r_1 - h) + \frac{I_G}{r}\right)} \cdot v_{b2} \quad (1)$$

Conservation of Energy: (climbing over obstacle)

$$T_2 + V_2 = T_3 + V_3$$

$$\frac{1}{2}mv^2 + \frac{1}{2}I\omega^2 = mgh \quad \omega = v/r$$

$$\frac{1}{2}mv^2 + \frac{1}{2}I\left(\frac{v}{r}\right)^2 = mgh$$

$$v_2 = \sqrt{\frac{2mgh}{m + \frac{I}{r^2}}} \quad (2)$$

$$v_2 = \sqrt{\frac{2mgh}{m + \frac{m r^2}{r^2}}}$$

$$v_2 = \sqrt{gh}$$

Wheel 1:

$$m_1 = 5 \text{ kg} \quad r_1 = 0.5 \text{ m} \quad h = 0.04 \text{ m}$$

$$I_{G_1} = \frac{1}{2} m r^2 = \frac{5 \cdot (0.5^2)}{2} = 0.625 \quad \frac{I_G}{r} = 1.25$$

$$V_2 = \sqrt{\frac{2 \cdot 5 \cdot 0.04}{5 + \frac{0.625 \cdot 2}{(0.5)^2}}} = 0.626 \text{ m/s}$$

$$V_1 = \frac{(5 \cdot 0.5 + 1.25)}{(5 \cdot (0.5 - 0.04) + 1.25)} \cdot 0.626 \quad V_1 = 0.66126 \text{ m/s}$$

Wheel 2

$$m_2 = 3 \text{ kg} \quad r_2 = 0.55 \text{ m} \quad h = 0.04 \text{ m} \quad m_s = 0.25$$

$$I_{G_2} = 5 \cdot \frac{1}{3} m_s r^2 + m r^2 = 5 \cdot \frac{1}{3} (0.25)(0.55^2) + (3)(0.55)^2 = 1.0335 \quad \frac{I_G}{r} = 1.879$$

$$V_2 = \sqrt{\frac{2 \cdot (5 \cdot 0.25 + 3) \cdot 0.04}{(5 \cdot 0.25 + 3) + \frac{1.0335 \cdot 2}{(0.55)^2}}} = 0.3009 \text{ m/s}$$

$$V_1 = \frac{((5 \cdot 0.25 + 3) \cdot 0.55 + 1.879)}{((5 \cdot 0.25 + 3) \cdot (0.55 - 0.04) + 1.879)} \cdot 0.3009 \approx 0.31358$$

$$V_{W_1} - V_{W_2} = 0.66126 - 0.31358 = 0.347 \text{ m/s}$$

Wheel 1 needs a higher velocity by 0.347 m/s