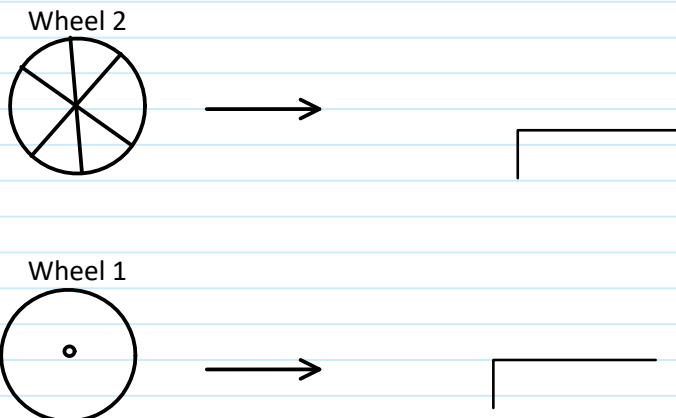


Two wheels roll over identical obstructions of a height $h=0.04\text{ m}$ on a road. One is a solid wooden wheel, with a mass $m_1=5\text{ kg}$ and radius $r_1=0.5\text{ m}$. The other wheel has 5 spokes, a mass of $m_2=0.7\text{ kg}$, and a radius of $r_2=0.55\text{ m}$. Which wheel needs a higher velocity to roll over the obstacle and by how much?



Both wheels:

Cons. of Angular Momentum

$$(H_u)_1 = (H_u)_2$$

$$m(r_1 - h)(v_{b1}) + I_G \omega_1 = r m(v_{b2}) + I_G \omega_2 \quad \omega_1 = \frac{v_{b1}}{r} \quad \omega_2 = \frac{v_{b2}}{r}$$

$$m(r_1 - h)(v_{b1}) + I_G \left(\frac{v_{b1}}{r}\right) = r m(v_{b2}) + I_G \left(\frac{v_{b2}}{r}\right)$$

$$v_{b1} = \frac{\left(r \cdot m + \frac{I_G}{r}\right)}{\left(m(r_1 - h) + \frac{I_G}{r}\right)} \cdot v_{b2} \quad (1)$$

Conservation of Energy: (climbing over obstacle)

$$T_2 + V_2 = T_3 + V_3$$

$$\frac{1}{2}mv^2 + \frac{1}{2}I\omega^2 = mgh \quad \omega = v/r$$

$$\frac{1}{2}mv^2 + \frac{1}{2}I\left(\frac{v}{r}\right)^2 = mgh$$

$$v_2 = \sqrt{\frac{2mgh}{m + \frac{I}{r^2}}} \quad (2)$$

Wheel 1:

$$m_1 = 5 \text{ kg} \quad r_1 = 0.5 \text{ m} \quad h = 0.04 \text{ m}$$

$$I_{G_1} = \frac{1}{2} m r^2 = \frac{5 \cdot (0.5)^2}{2} = 0.625 \quad \frac{I_G}{r} = 1.25$$

$$V_2 = \sqrt{\frac{2 \cdot 5 \cdot 0.04}{5 + \frac{0.625}{(0.5)^2}}} = 0.231 \text{ m/s}$$

$$V_1 = \frac{(5 \cdot 0.5 + 1.25)}{(5 \cdot (0.5 - 0.04) + 1.25)} \cdot 0.231 \quad \boxed{V_1 = 0.24401 \text{ m/s}}$$

Wheel 2

$$m_2 = 7 \text{ kg} \quad r_1 = 0.55 \text{ m} \quad h = 0.04 \text{ m}$$

$$I_{G_2} = 5 \cdot \frac{1}{3} m r^2 + m r^2 = 5 \cdot \frac{1}{3} (7) (0.55)^2 + (7) (0.55)^2 = 5.647 \quad \frac{I_G}{r} = 10.27$$

$$V_2 = \sqrt{\frac{2 \cdot 7 \cdot 0.04}{5 + \frac{5.647}{(0.55)^2}}} = 0.1915 \text{ m/s}$$

$$V_1 = \frac{(7 \cdot 0.55 + 10.27)}{(7 \cdot (0.55 - 0.04) + 10.27)} \cdot 0.1915 = 0.195 \text{ m/s}$$

$$V_{w_1} - V_{w_2} = 0.24401 - 0.195 = 0.049 \text{ m/s}$$

Wheel 1 needs a higher velocity by 0.049 m/s