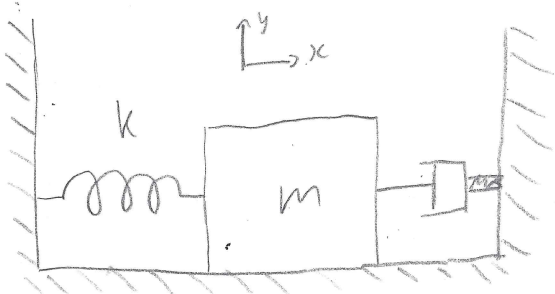
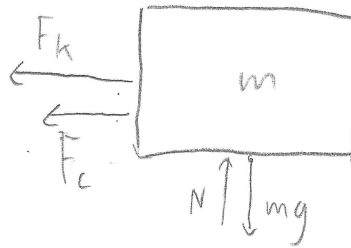


20-R-VIB-DY-25 Beginner

A box of mass $m = 5 \text{ kg}$ is connected to a spring, $k = 10 \text{ N/m}$, and a viscous damper, $c = 10 \frac{\text{Ns}}{\text{m}}$. If the box is subject to a initial displacement $x_0 = 0$ and initial velocity $v_0 = 1 \frac{\text{m}}{\text{s}}$, find the equation of the solution



Solution: FBD



$$\sum F_x = ma$$

$$0 = A \sin \phi \quad \phi = 0$$

$$1 = -A \sin \phi - A \cos \phi$$

$$1 = -A (\sin \phi + \cos \phi)$$

$$A = -1$$

$$\omega_n = \sqrt{2}$$

$$\zeta = \frac{c}{2m\omega_n} = \frac{1}{\sqrt{2}}$$

$$x(t) = -e^{-t} \sin(-t)$$

roots are complex

$$r_{1,2} = -\omega_n \zeta \pm i \omega_n \sqrt{1 - \zeta^2}$$

$$= -1 \pm i$$

$$x(t) = a e^{(-1+i)t} + b e^{(-1-i)t} = e^{-t} (a e^{it} + b e^{-it})$$

$$= A e^{-t} \sin(-t + \phi)$$

$$v(t) = -A e^{-t} \sin(-t + \phi) - A e^{-t} \cos(-t + \phi)$$