20-R-VIB-DY-45 Advanced.

A L-shaped bar of negligible mass is pinned to the ceiling by the corner at point O. Arm. A, length  $l_a = 2m$ , has a spring  $k_a = 10 \, \text{N/m}$  attached halfway and arm  $l_a = 2m$ , length  $l_b = 3m$ , has a damper  $c_b = 20 \, \text{Ns/m}$  attached  $l_a = 2m$ , and  $l_a = 2m$ , has a damper  $l_a = 2m$  and  $l_a = 2m$ , have a ball of equal mass at the end of their lengths. Determine the the mass of a single ball if the system is critically damped.

Solution: FBD

FR

Img

Img

 $ZM_{0} = I\alpha = 0 = \left(\frac{l_{A}}{2}\right)^{2}k\theta + \left(\frac{2l_{B}}{2}\right)^{2}c\theta - l_{A}mg\theta + l_{B}mg\theta + ml_{A}^{2}\theta + ml_{B}^{2}\theta$   $\dot{\Theta}_{m}(l_{A}^{2} + l_{B}^{2}) + \left(\frac{2l_{B}}{2}\right)^{2}c\dot{\theta} + \Theta\left(l_{B}mg - l_{A}mg + \frac{l_{A}^{2}}{4}k\right) = 0$   $(c = \sqrt{4nk} = c' = 80$   $l_{B}mg - l_{A}mg + \frac{l_{A}^{2}}{4}k\right) = 0$   $l_{B}mg - l_{B}mg + \frac{l_{B}mg}{4}k\right) = 0$   $l_{B}mg - l_{B}mg + \frac{l_{B}mg}{4}k\right)$   $l_{B}mg - l_{B}mg + \frac{l_{B}mg}{4}k\right)$   $l_{B}mg - l_{B}mg + \frac{l_{B}mg}{4}k$   $l_{B}mg - l_{B}mg + \frac{l_{B}mg}{4}k\right)$   $l_{B}mg - l_{B}mg + l_{B}mg$   $l_{B}mg - l_{B}mg + l_{B}mg$   $l_{B}mg - l_{B}mg + l_{B}mg$ 

13gm2+130m-1600=6

m= 17.169 kg