1. Determine the truth value of each of these statements, where the domain is the set of real numbers.

1.
$$\exists x (x^2 + 1 = 0)$$

2.
$$\forall x \ \forall y \ (x + y \neq y + x)$$

3.
$$\forall x \ \forall y \ \exists z \ (z = \frac{x+y}{2})$$

- 2. Express each of these statements using predicates, quantifiers, logical connectives, and mathematical operators.
 - 1. The set of real numbers has the density property. There is a real number between any two real numbers.
 - 2. Express the other two cases of the $ax^2 + bx + c = 0$ where it has one repeated root, and no real roots at all.

- 3. Let F(x, y) be the statement "x can fool y," where the domain consists of all people in the world. Use quantifiers to express each of these statements.
 - 1. Everybody can fool Yassir.
 - 2. There's somebody who can fool exactly two people.
 - 3. There is exactly one person whom everybody can fool.

- The submission deadline is: Saturday, June 8th 2024, 23:59:59 GMT+2.
- Upload a clearly captured photocopy of your answer-sheet to: https://forms.gle/zKwBG7oeinWdncw4A
- In cases of cheating, the student will suspect themselves to **strict** cheating penalties.