

# Physics

## \* Lecture 3 \*

### Vectors المتجهات :-

If:  $\vec{A} = 2\vec{i} + 3\vec{j} + \vec{k}$  ,  $\vec{B} = \vec{i} - \vec{k}$

$\therefore \vec{A} \cdot \vec{B} = 2 \times 1 + 3 \times 0 + 1 \times -1 = 2 - 1 = 1$  "dot product."

$\vec{A} \times \vec{B} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 2 & 3 & 1 \\ 1 & 0 & -1 \end{vmatrix} = -3\vec{i} + 3\vec{j} - 3\vec{k}$  "Cross product."

\*  $\vec{A} \cdot \vec{B} = \|\vec{A}\| \|\vec{B}\| \cos \theta$

\*  $\vec{A} \times \vec{B} = \|\vec{A}\| \|\vec{B}\| \sin \theta$

\*  $\vec{A} \times \vec{B} = -\vec{B} \times \vec{A}$

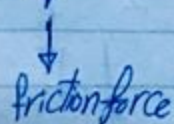
\*  $W = F \cdot S$

\*  $E = K.E + P.E$   
 $= \frac{1}{2}mv^2 + mgh$

\*  $P = \frac{W}{t}$

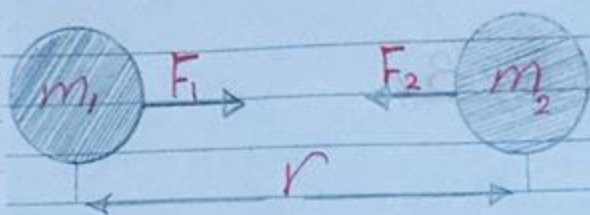
W	→ work	→ الشغل
F	→ force	→ القوة
S	→ distance	→ المسافة
KE	→ Kinetic energy	→ طاقة الحركة
P.E	→ potential energy	→ طاقة الوضع
P	→ power	→ القدرة

### \* Newton's Laws \*

$\rightarrow F = ma = T - W - F_f$   


T	↑	↑ a
W	↓	





$$F_1 = F_2 = G \frac{m_1 m_2}{r^2}$$

$G$ : gravitational Constant ثابت الجاذبية  
 $= 6.67 \times 10^{-11}$

Newton's Second Law:  $F = ma$   
 $F = G \frac{m_1 m_2}{r^2}$

$$\therefore ma = G \frac{m_1 m_2}{r^2}$$

$$\therefore a = G \frac{M}{r^2}$$

$a$ : acceleration due to gravity عجلة الجاذبية  
on Earth:  $a = 9.81 \text{ m/s}^2$

\* Stress  $\propto$  linear strain \*

$$\rightarrow \frac{F}{A} \propto \frac{\Delta l}{l} \quad \therefore \frac{F}{A} = \gamma \frac{\Delta l}{l}$$

$$\therefore F = \gamma \frac{\Delta l}{l} A$$

$$\text{Stress up} = \frac{F}{A}$$

$V \rightarrow$  Volume  $\rightarrow$  حجم  
 $A \rightarrow$  Area  $\rightarrow$  مساحة  
 $l \rightarrow$  length  $\rightarrow$  طول  
 $V = Al$

$$\int dw = \int F dl$$

$$W = \int \gamma \frac{\Delta l}{l} A dl$$

$$= \frac{\gamma A}{l} \int \Delta l dl = \frac{\gamma A}{l} \times \frac{1}{2} (\Delta l)^2$$

$$= \frac{1}{2} \frac{\gamma A \Delta l}{l} \cdot \Delta l$$

$$= \frac{1}{2} \cdot F \cdot \Delta l$$

work done per unit volume:  $\frac{W}{V} = \frac{1}{2} \cdot \frac{F}{A} \cdot \frac{\Delta l}{l}$

### \* Stress $\propto$ Volumetric Strain \*

$$P \propto \frac{\Delta V}{V}, \therefore P = B \frac{\Delta V}{V}$$

$$P = \frac{F}{A} \Rightarrow F = PA$$

$$, AL = V$$

$$, W = \int F dl$$

$$= \int PA dl$$

$$= \int P dv = \int B \frac{\Delta V}{V} dv$$

$$= \frac{B}{V} \int \Delta V dv$$

$$= \frac{B}{V} \cdot \frac{1}{2} \Delta V^2 = \frac{1}{2} B \frac{\Delta V}{V} \cdot \Delta V$$

$$= \frac{1}{2} P \Delta V$$

work done per unit volume:  $\frac{W}{V} = \frac{1}{2} P \frac{\Delta V}{V} = \frac{1}{2} \text{ Stress} \times \text{Strain}$

### \* Stress $\propto$ Shear Strain \*

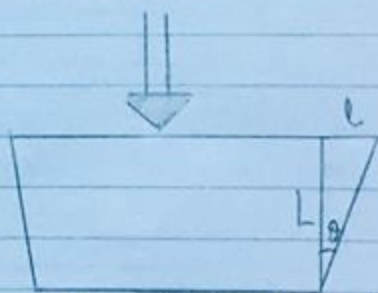
$$\frac{F}{A} \propto \theta, \therefore \frac{F}{A} = N \theta, F = N \theta A$$

$$, W = \int F dl, \therefore \theta = \tan \theta = \frac{l}{L}$$

$$\therefore W = \int N \cdot \frac{l}{L} A dl$$

$$= \int N \frac{l}{L} L^2 dl = NL \int l dl$$

$$= NL \times \frac{1}{2} l^2 = \frac{1}{2} Fl$$



$\theta$ : very small angle  
 $\theta = \tan \theta$

$$A = L^2$$

$$V = AL$$

work done per unit volume:  $\frac{W}{V} = \frac{1}{2} \frac{F}{A} \cdot \frac{l}{L} = \frac{1}{2} \text{ Stress} \times \text{Strain}$