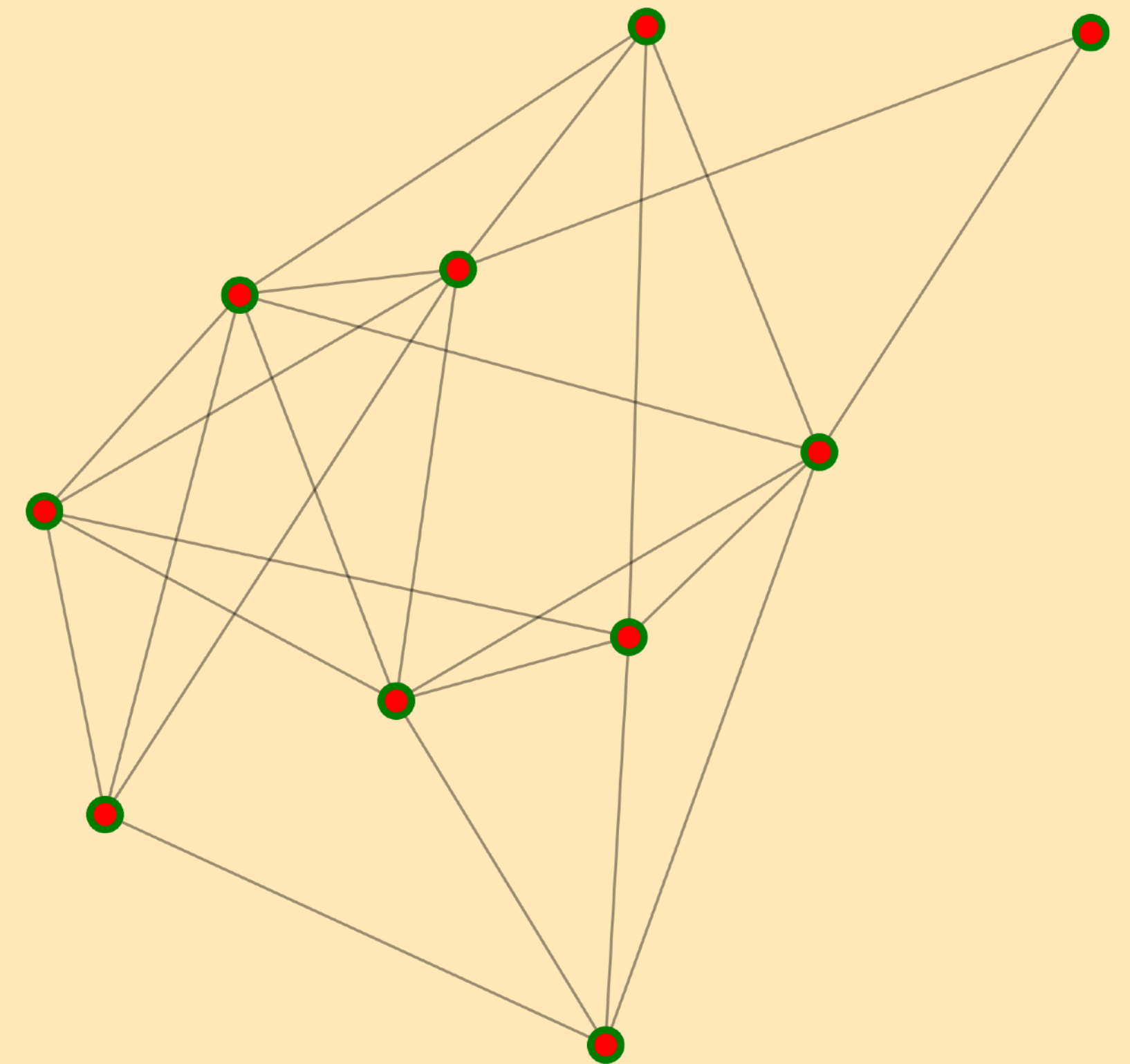


Intro to Graph Theory

Seminar 12.

Basic Definitions

- ***Graph***: pair of (V, E)
- ***Degree***: how many edges does vertex contain
- ***Complete***: all vertices are adjacent
- ***Component***: fully path-connected subgraph



Basic Definitions

Adjacency matrix

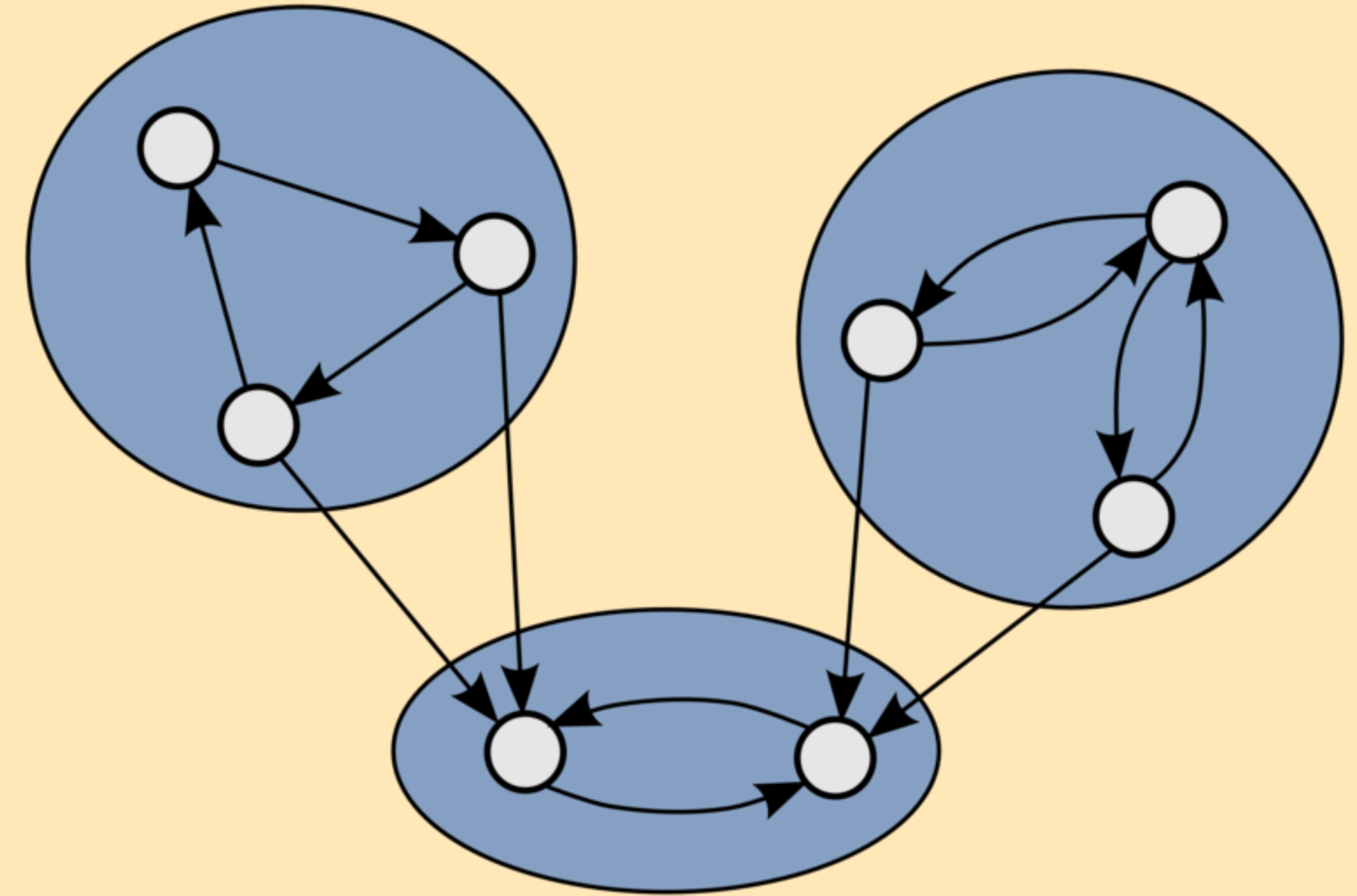
- square **matrix** of $N \times N$ size where N is the number of nodes in the graph
- it is used to represent the connections between the edges of a graph

	0	1	2	3	4
0	0	1	1	0	0
1	0	0	1	0	1
2	0	0	0	1	0
3	0	0	0	0	1
4	0	0	0	0	0

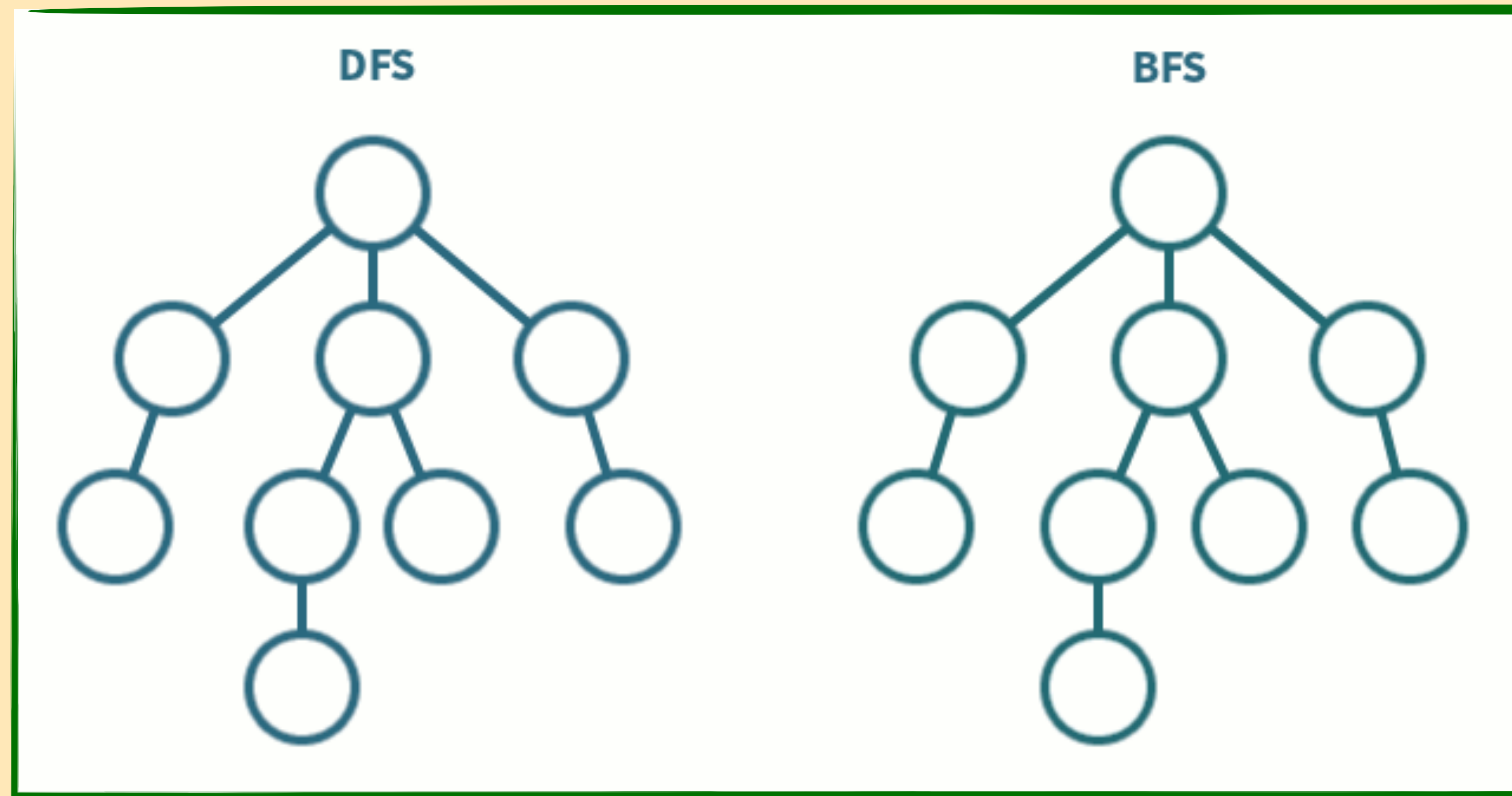
Basic Definitions

Strong Components

- ***Strong connection:*** equivalence relation between nodes
- ***Strongly connected component:*** every vertex is reachable from every other
- directed graphs only!

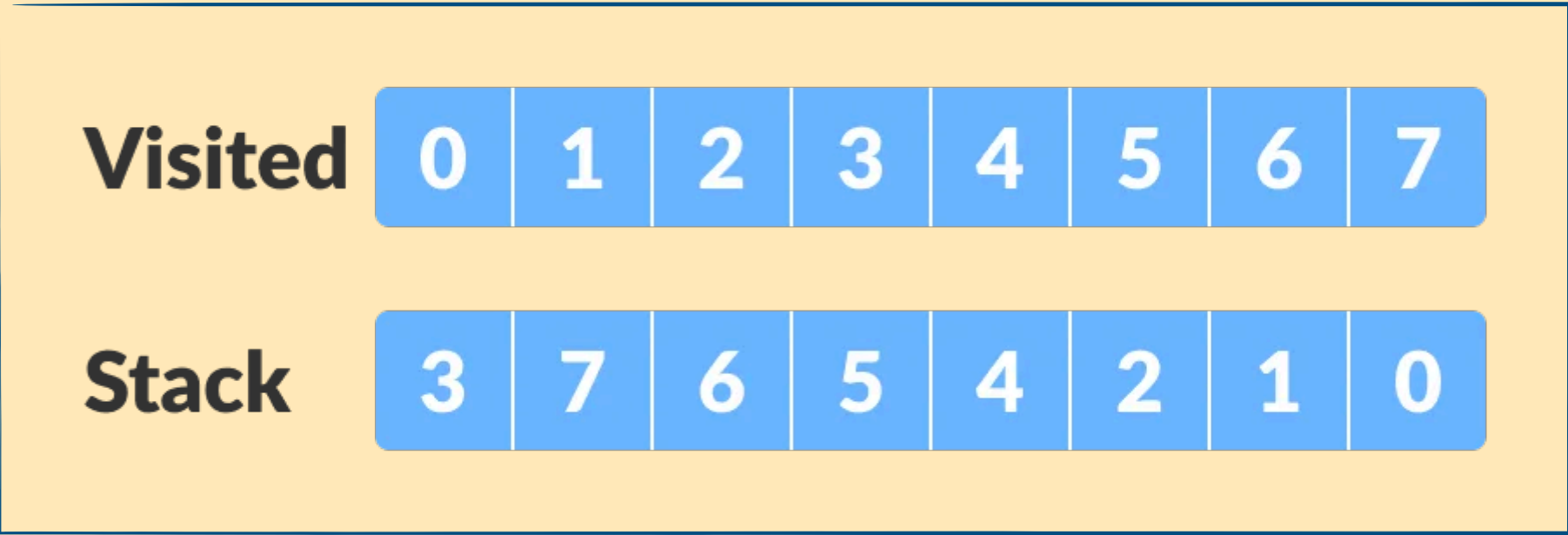
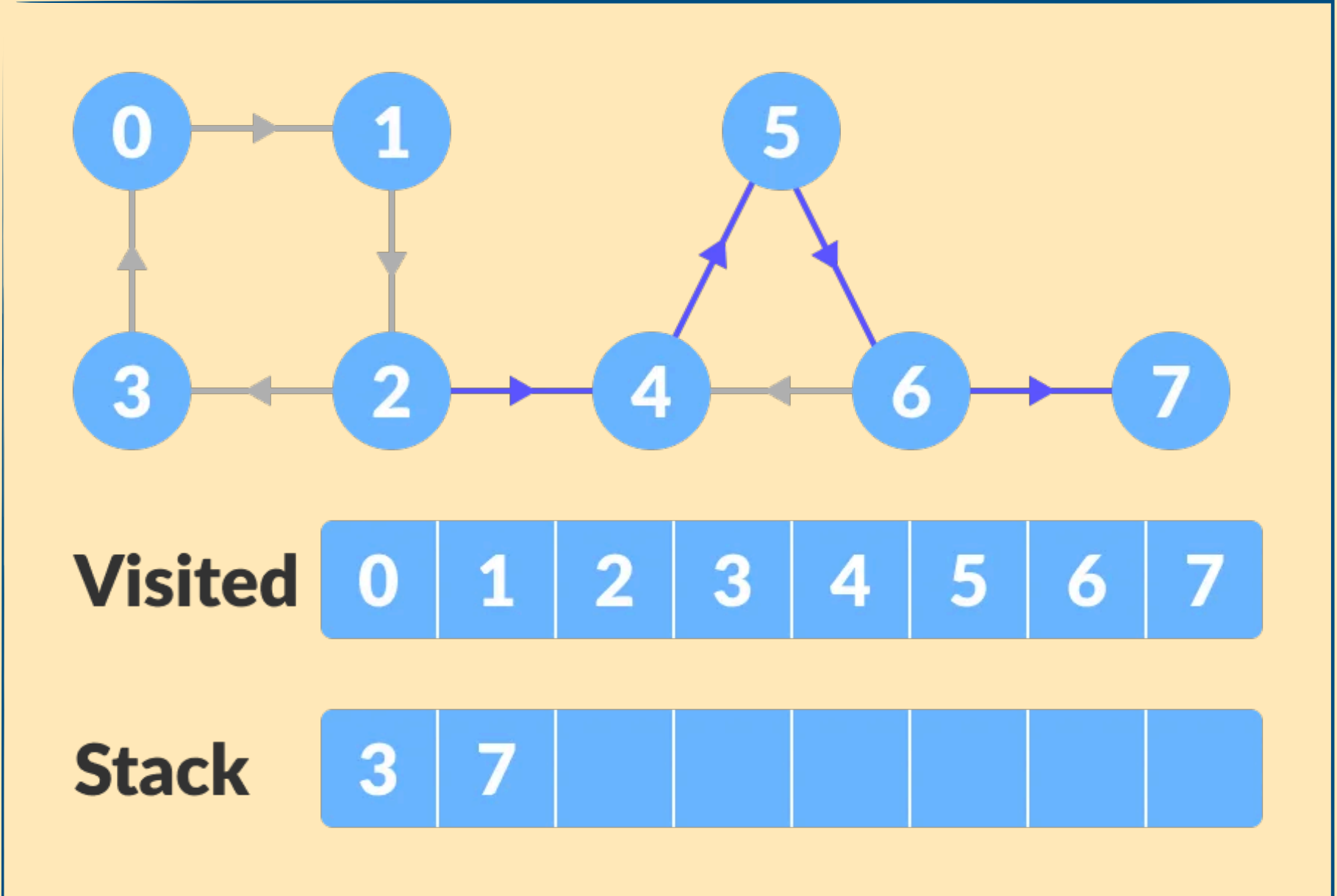
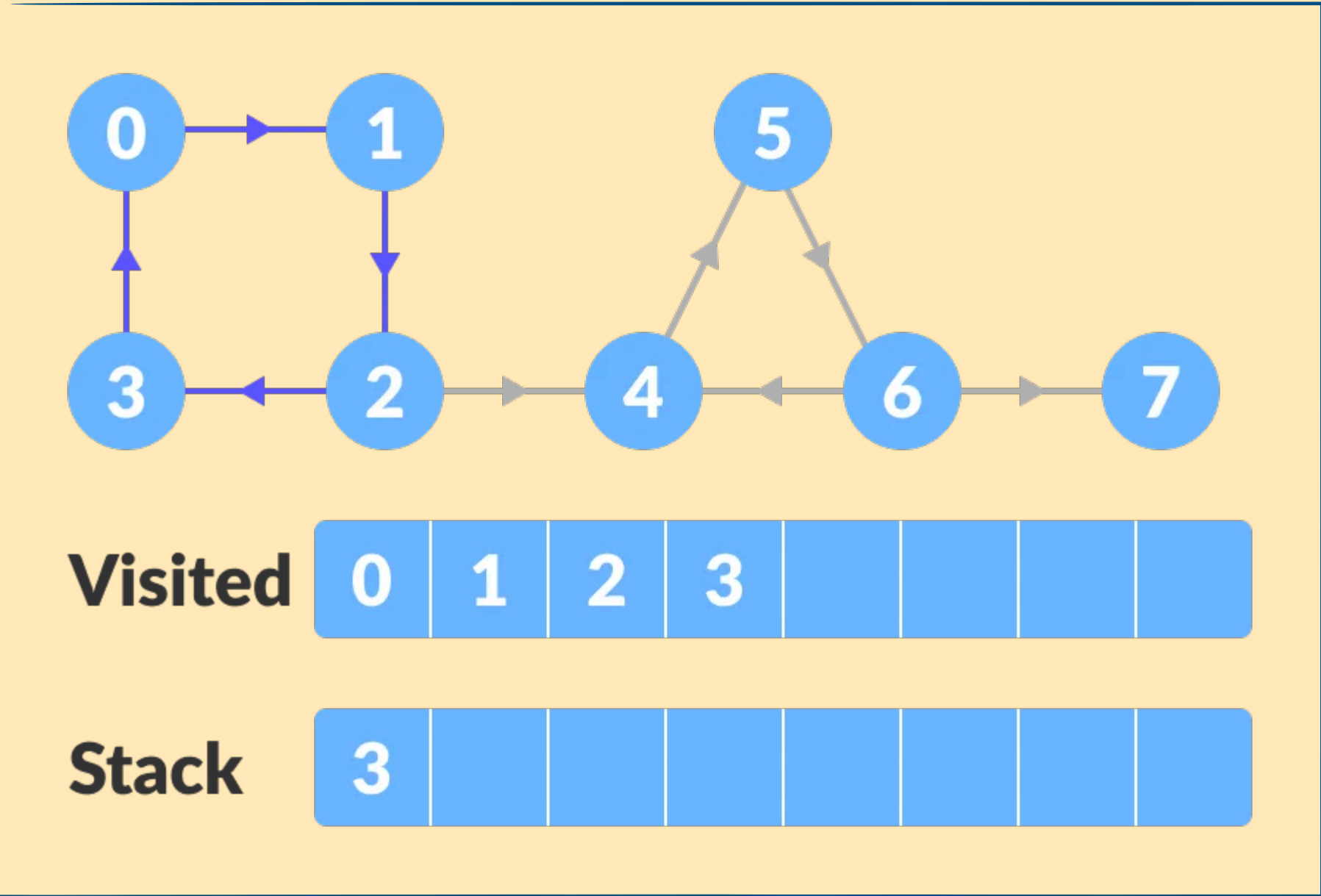


Graph Search algorithms



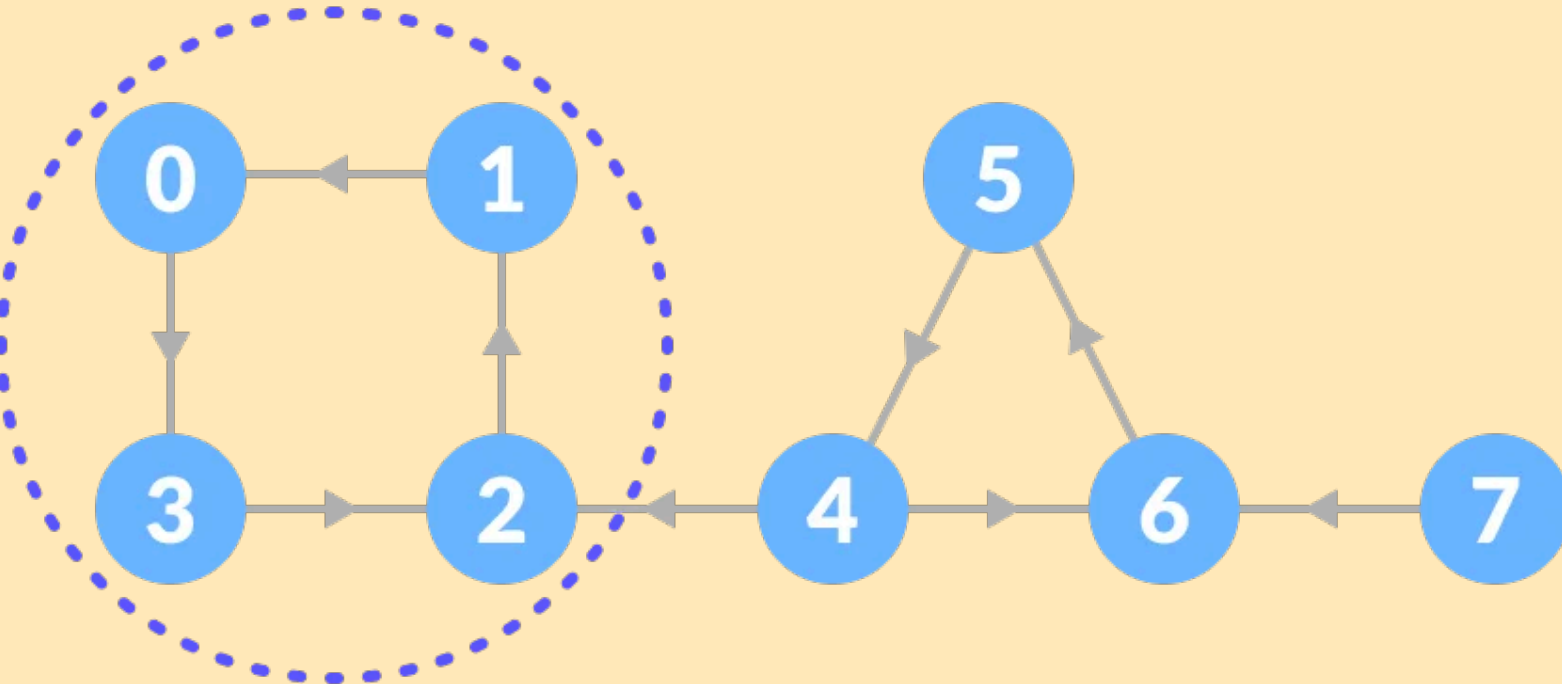
Graph Search algorithms

Kosaraju's algorithm

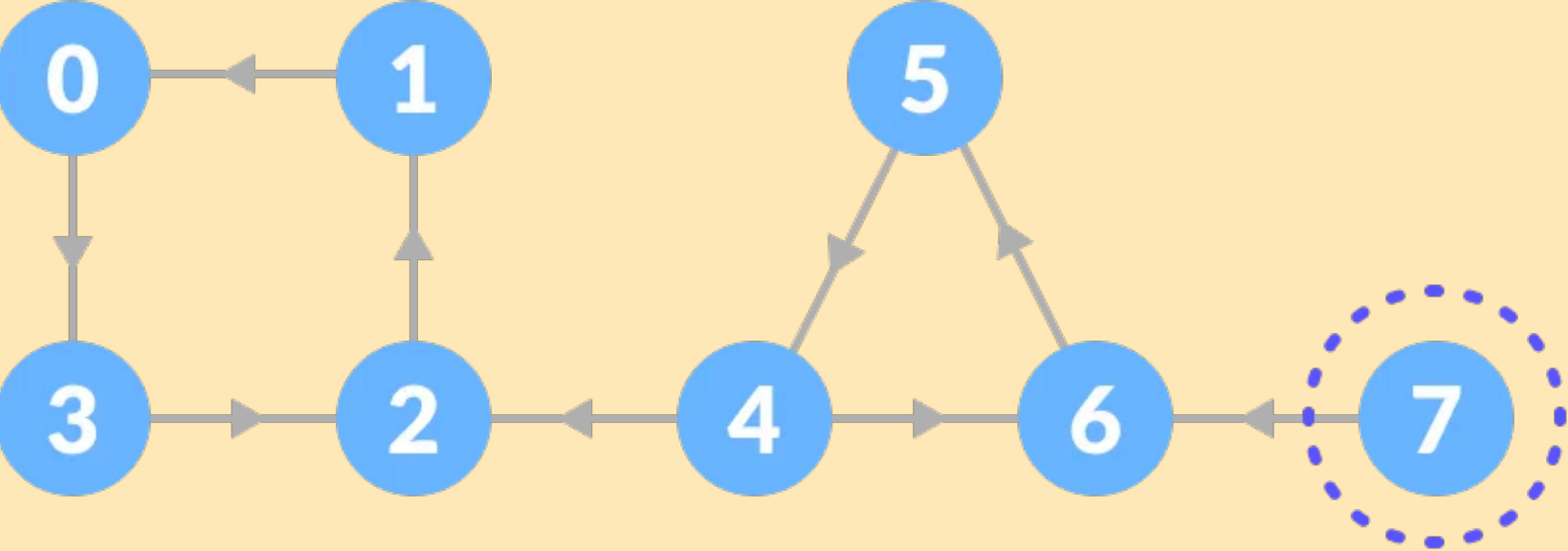


Graph Search algorithms

Kosaraju's algorithm



Visited	0	1	2	3				
Stack	3	7	6	5	4	2	1	
SCC	0	1	2	3				



Visited	0	1	2	3	4	5	6	
Stack								
SCC	7							



Visited	0	1	2	3	4	5	6	7
Stack	3	7	6	5	4	2	1	0

Graph Search algorithms

Dijkstra algorithm

