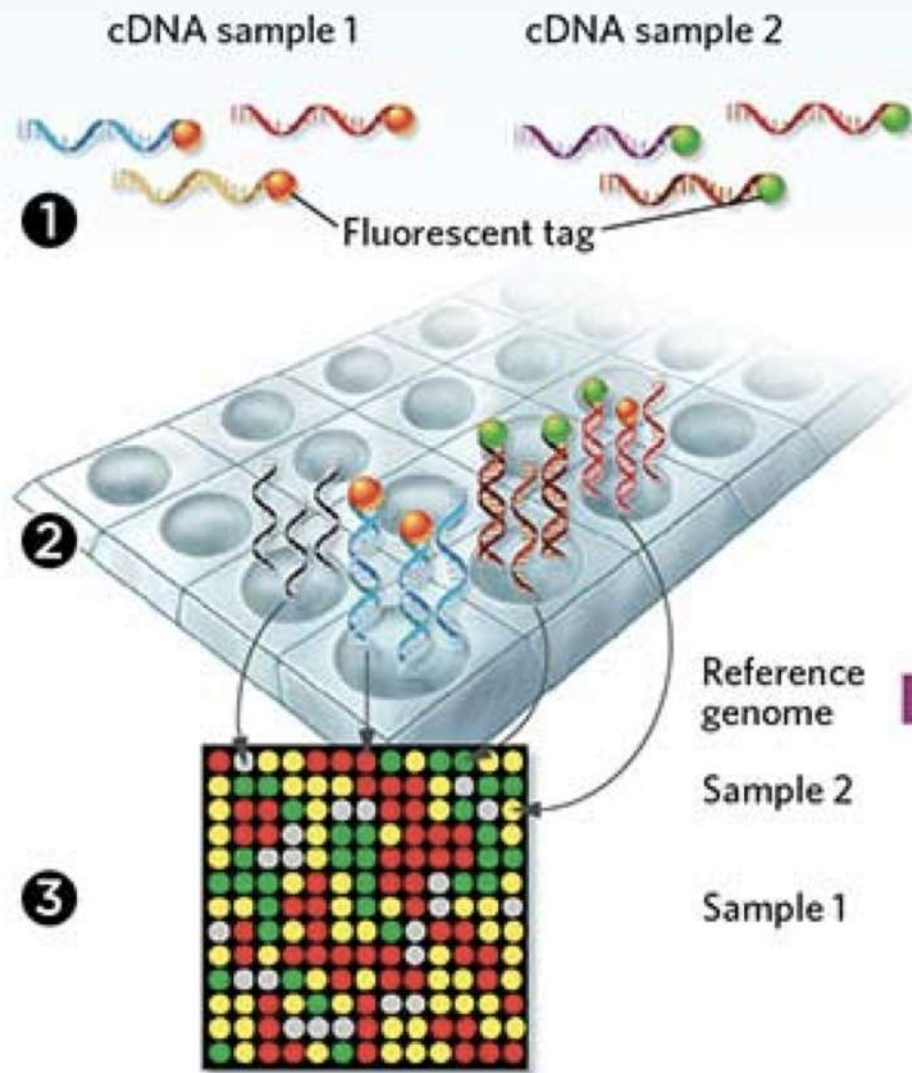
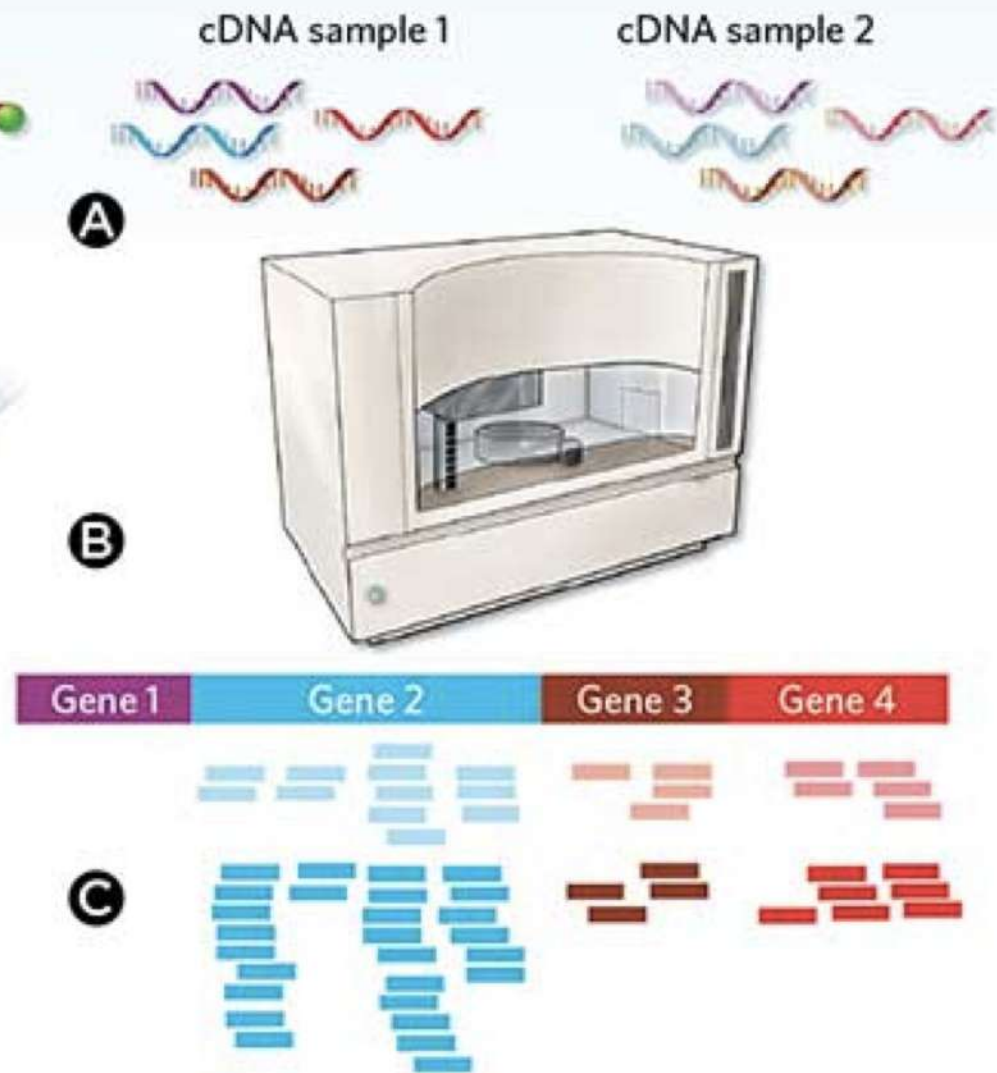


Gene Set Enrichment Analysis

DNA MICROARRAY



RNA-SEQ



What do we do with that MUCH information?

Fastq

```
@61DFRAAXX100204:1:100:10494:3070/1
AAACAACAGGGCACATTGTCACCTTGTATTGAAAAACACTTCCGGCCAT
+
ACCCCCCCCCCCCCCCCCCCCCCCCCCCCCBC?CCCCCCCC@@CACCCCA
```

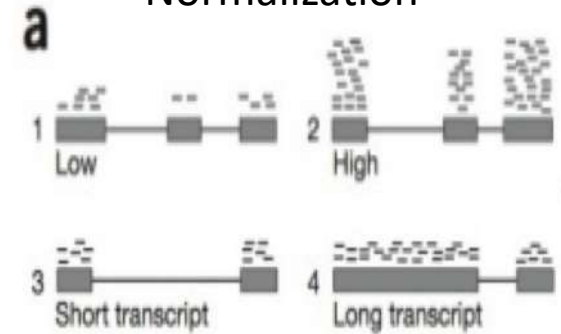
Trimming and QC

Reading Alignment

SAM/BAM

Reference genome

Normalization



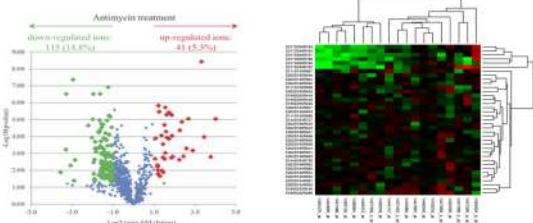
Transcript assembly

Reference genome

D.E table

GENE	FC	p-value	FDR
CTCF	-2	0.006	0.00013
BORIS	+2	0.0009	0.0003

Data display



Differential Expression

Count

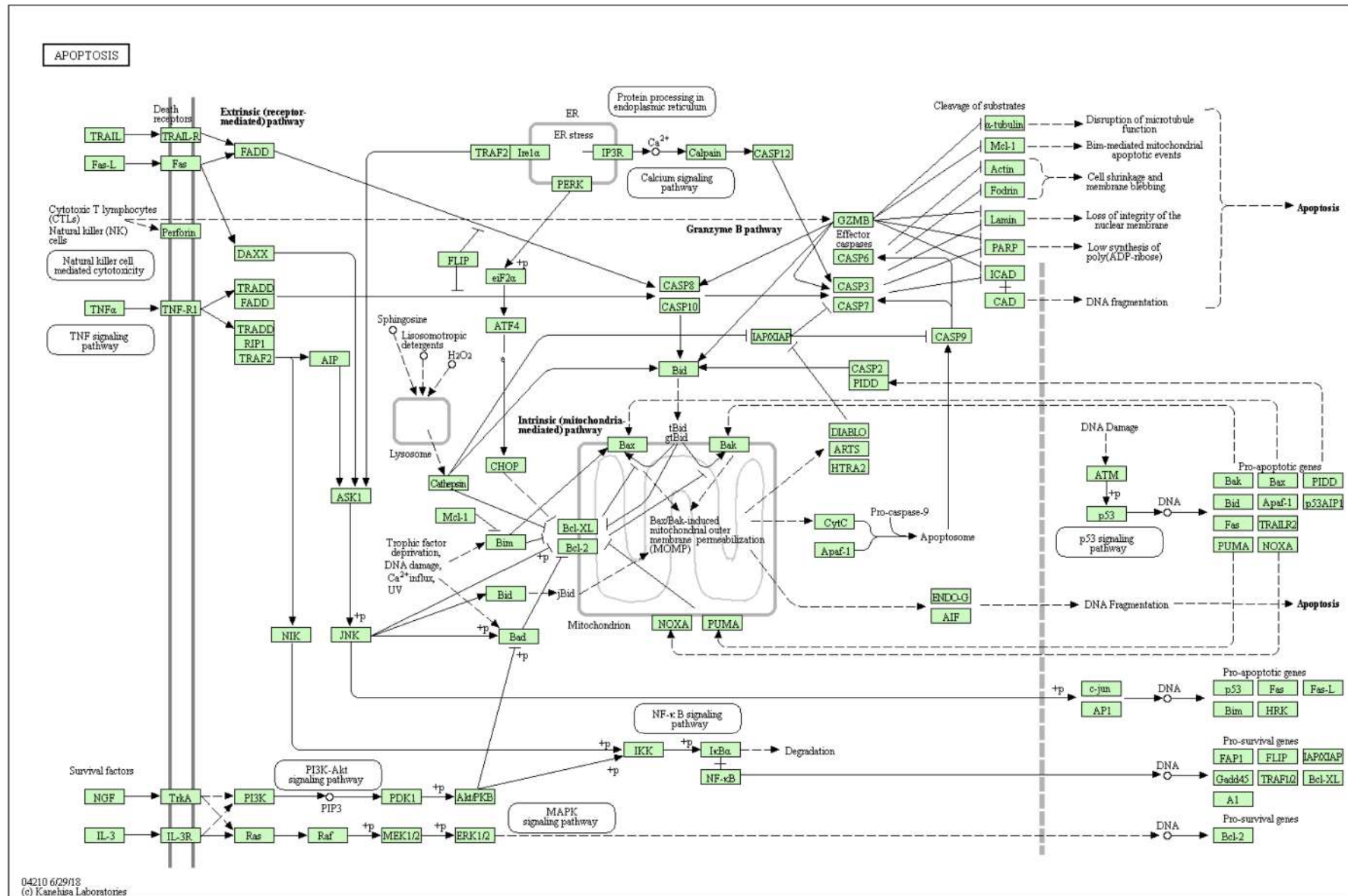
GENE	A	B	C
CTCF	13	1	7
BORIS	0	18	5



What do we do with that MUCH information?



Pathway analysis



Pathway analysis



[Login](#) | [Register](#)

Transcription Pathways Ontologies Disease/Drugs Cell Types Misc Legacy Crowd

Description Sample gene list (375 genes)

ChEA 2016

Bar Graph Table Grid Network **Clustergram**

Enriched Terms are the columns, input genes are the rows, and cells in the matrix indicate if a gene is associated with a term.



Row Order

Cluster Sum

Column Order

Cluster Sum

Gene Search

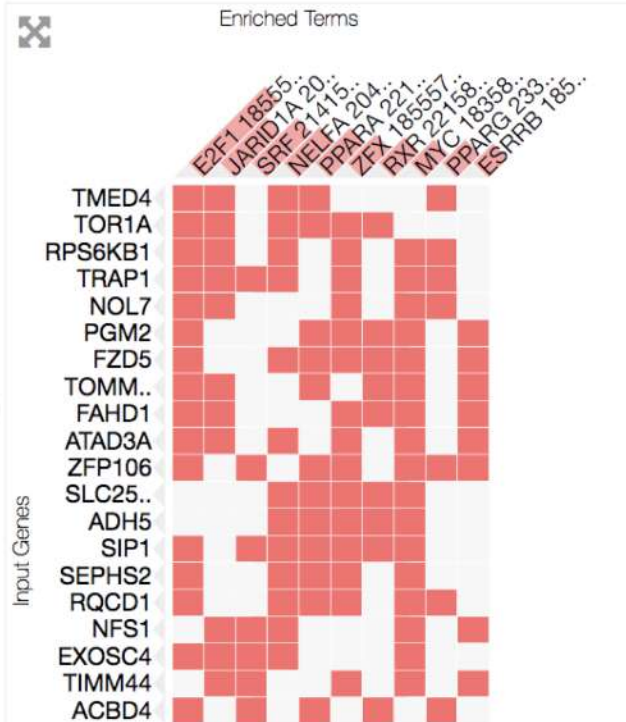
Combined Score

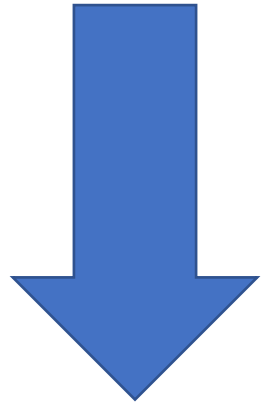
P-Value

Z-score

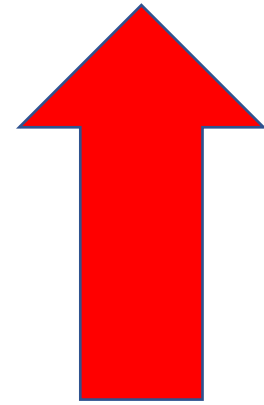
Top Enriched Terms: 10

Top rows sum: 20 rows





And the Fold Change?



First described by Mootha et al., 2003.

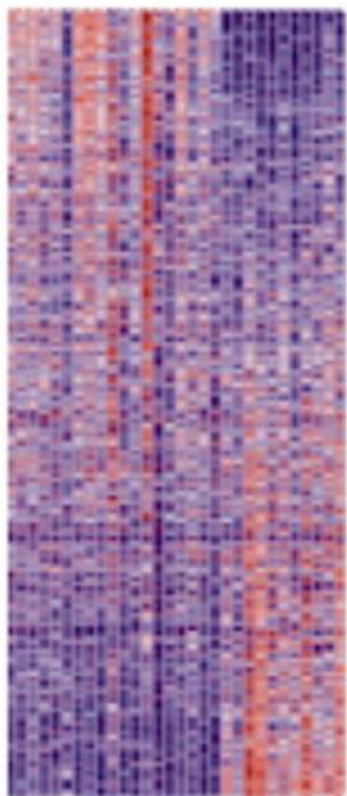
- Analysis of second generation pathways.
 - Significance analysis of function and expression (SAFE).
-
- Four step approach.
 - A) Calculate the local statistic (at the gene level).
 - B) Calculate the global statistic (at the level of pathway or set of genes).
 - C) Determine a significance value.
 - D) Adjust for multiple comparisons.

A Phenotype
Classes

A B

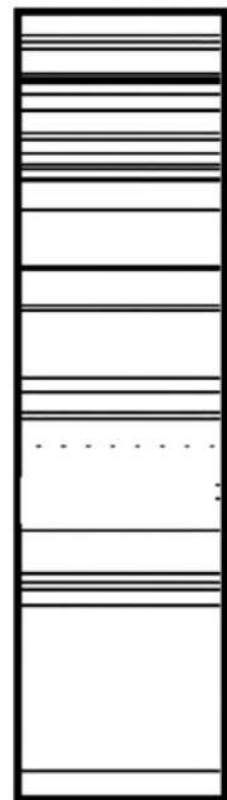


Ranked Gene List



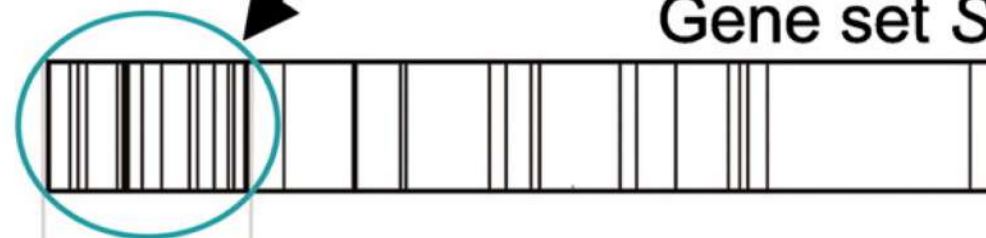
B

Gene set S

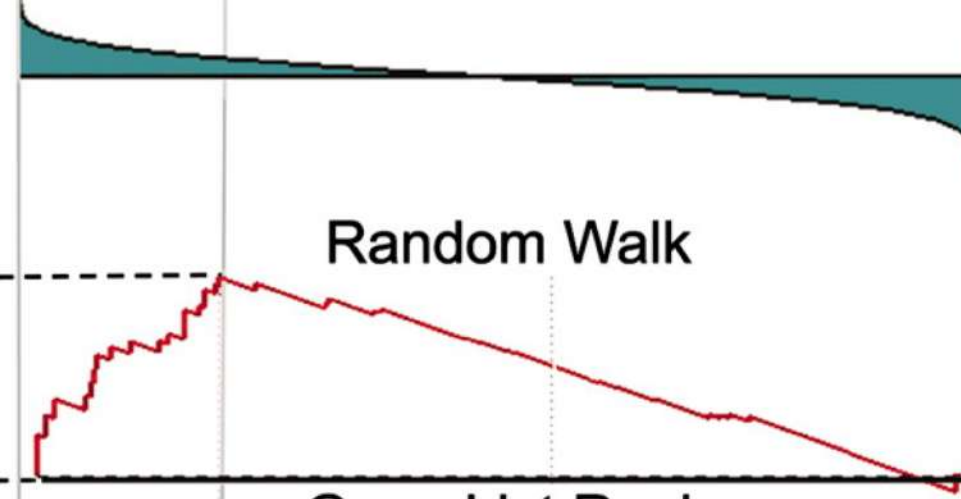


Leading edge subset

Gene set S



Correlation with Phenotype



Random Walk

$ES(S)$

Maximum deviation
from zero provides the
enrichment score $ES(S)$

Gene List Rank

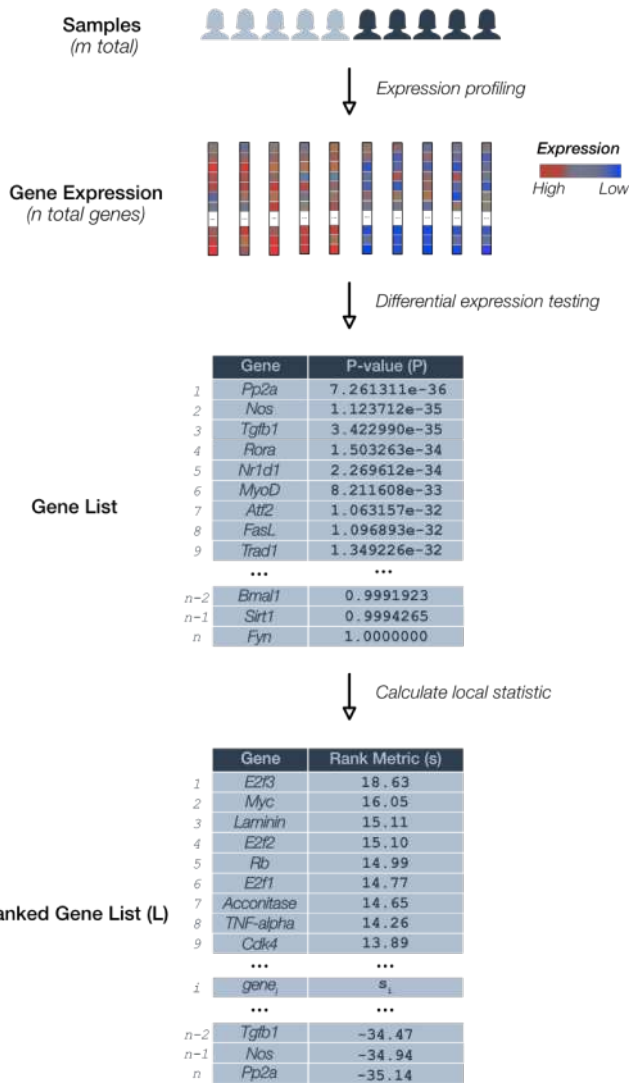
Files to start

Data File	Content	Format	Source
Expression dataset	Contains features (genes or probes), samples, and an expression value for each feature in each sample. Expression data can come from any source (Affymetrix, Stanford cDNA, and so on).	res, gct, pcl, or txt	You create the file.
Phenotype labels	Contains phenotype labels and associates each sample with a phenotype.	cls	You create the file or have GSEA create it for you.
Gene sets	Contains one or more gene sets. For each gene set, gives the gene set name and list of features (genes or probes) in that gene set.	gmx or gmt	You use the files on the Broad ftp site, export gene sets from the Molecular Signature Database (MSigDb) or create your own gene sets file.
Chip annotations	Lists each probe on a DNA chip and its matching HUGO gene symbol. Optional for the gene set enrichment analysis.	Chip	You use the files on the Broad ftp site, download the files from the GSEA web site, or create your own chip file.

Choose your database

- Gene set Databases.
 - a) Gene Ontology (GO).
 - b) Molecular Signatures Database (MSigDB).
- Detailed biochemical pathway databases.
 - a) Reactome.
 - b) Panther.
 - c) NetPath.
 - d) HumanCyc.
 - e) National Cancer Institute (NCI) Pathway Interaction Database (PID).
 - f) KEGG.

1. Local statistic



The rank file is a list of detected genes and a rank metric score.

- At the top of the list are genes with the "strongest" up-regulation.
- At the bottom of the list are the genes with the "strongest" down-regulation.
- The genes not changing are in the middle.

Metric

- Signal-to-noise ratio (S2N; the default measure in GSEA)
- Absolute value of signal-to-noise ratio ($|S2N|$)
- Difference of expression means between classes (Ratio)
- Log₂ of Ratio ($\log_2(\text{Ratio})$)
- T-test statistic (T-test).

$$\frac{\mu_A - \mu_B}{\sigma_A + \sigma_B}$$

- **Signal2Noise** (default) uses the difference of means scaled by the standard deviation.

where μ is the mean and σ is the standard deviation; σ has a minimum value of $.2 * \text{absolute}(\mu)$, where $\mu=0$ is adjusted to $\mu=1$. The larger the signal-to-noise ratio, the larger the differences of the means (scaled by standard deviations);

$$\frac{\mu_A - \mu_B}{\sqrt{\frac{\sigma_A^2}{n_A} + \frac{\sigma_B^2}{n_B}}}$$

- **tTest** uses the difference of means scaled by the standard deviation and number of samples.

where μ is the mean, n is the number of samples, and σ is the standard deviation; σ has a minimum value of $.2 * \text{absolute}(\mu)$, where $\mu=0$ is adjusted to $\mu=1$. The larger the tTest ratio, the more distinct the gene expression is in each phenotype and the more the gene acts as a “class marker.”

$$\frac{\mu_A}{\mu_B}$$

- **Ratio_of_Classes** (also referred to as fold change) uses the ratio of class means to calculate fold change for natural scale data:

where μ is the mean. The larger the fold change, the more distinct the gene expression is in each phenotype and the more the gene acts as a “class marker.”

$$\mu_A - \mu_B$$

- **Diff_of_Classes** uses the difference of class means to calculate fold change for log scale data:

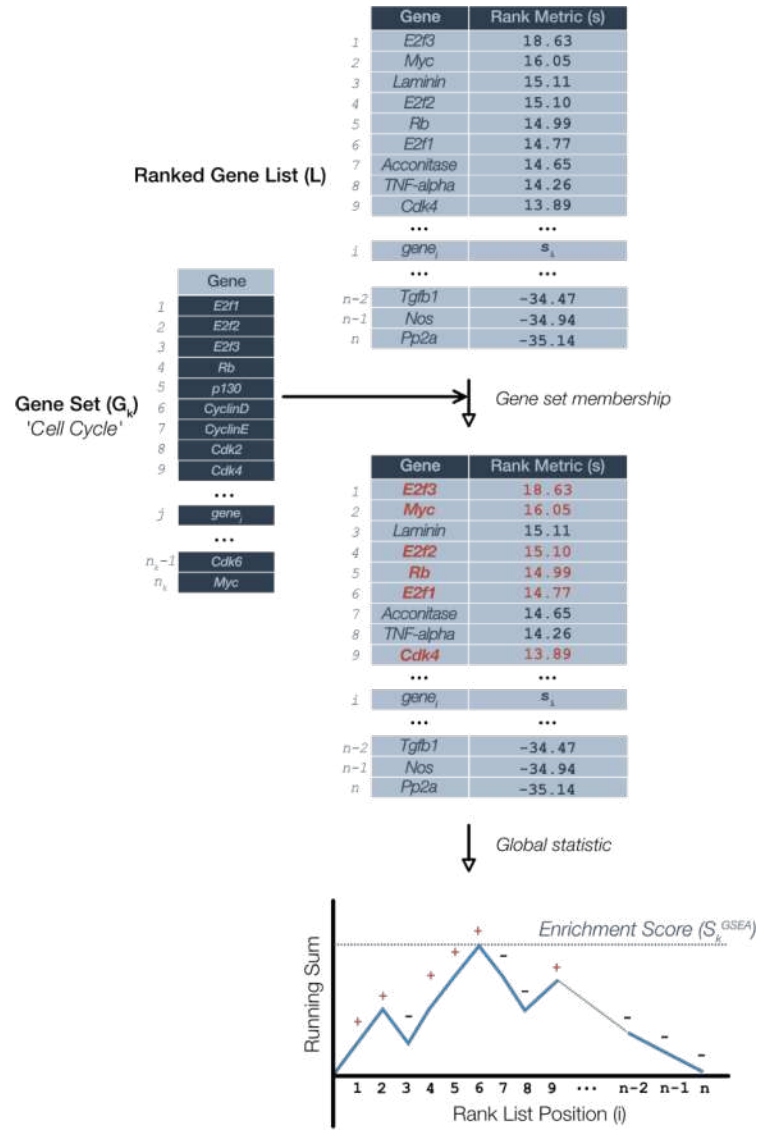
where μ is the mean. The larger the fold change, the more distinct the gene expression is in each phenotype and the more the gene acts as a “class marker.”

$$\log_2 \left(\frac{\mu_A}{\mu_B} \right)$$

- **log2_Ratio_of_Classes** uses the log2 ratio of class means to calculate fold change for natural scale data:

where μ is the mean. This is the recommended statistic for calculating fold change for natural scale data.

2. Global statistic



Enrichment Score (ES)

Reflects the degree to which a gene set is overrepresented at the top or bottom of a ranked list of genes.

GSEA calculates the ES by walking down the ranked list of genes, increasing a running-sum statistic when a gene is in the gene set and decreasing it when it is not.

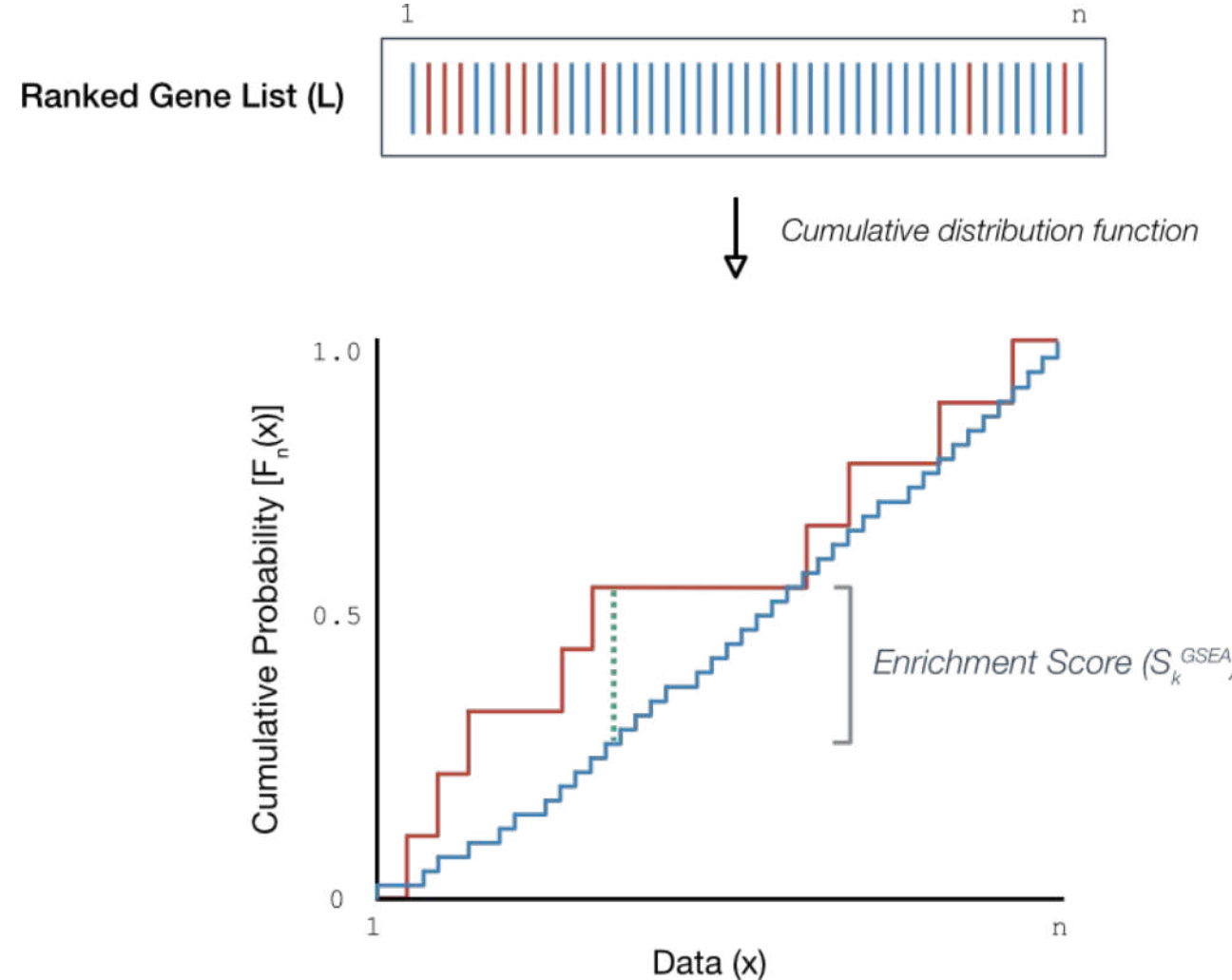
- The magnitude of the increment depends on the correlation of the gene with the phenotype.
- The ES is the maximum deviation from zero encountered in walking the list.
- A positive ES indicates gene set enrichment at the top of the ranked list; a negative
- ES indicates gene set enrichment at the bottom of the ranked list.

Kolmogorov–Smirnov test

The Kolmogorov–Smirnov statistic quantifies a distance between the empirical distribution function of the sample and the cumulative distribution function of the reference distribution.

...Or between the empirical distribution functions of two samples.

The null distribution of this statistic is calculated under the null hypothesis that the sample is drawn from the reference distribution.



3. “Significance” value

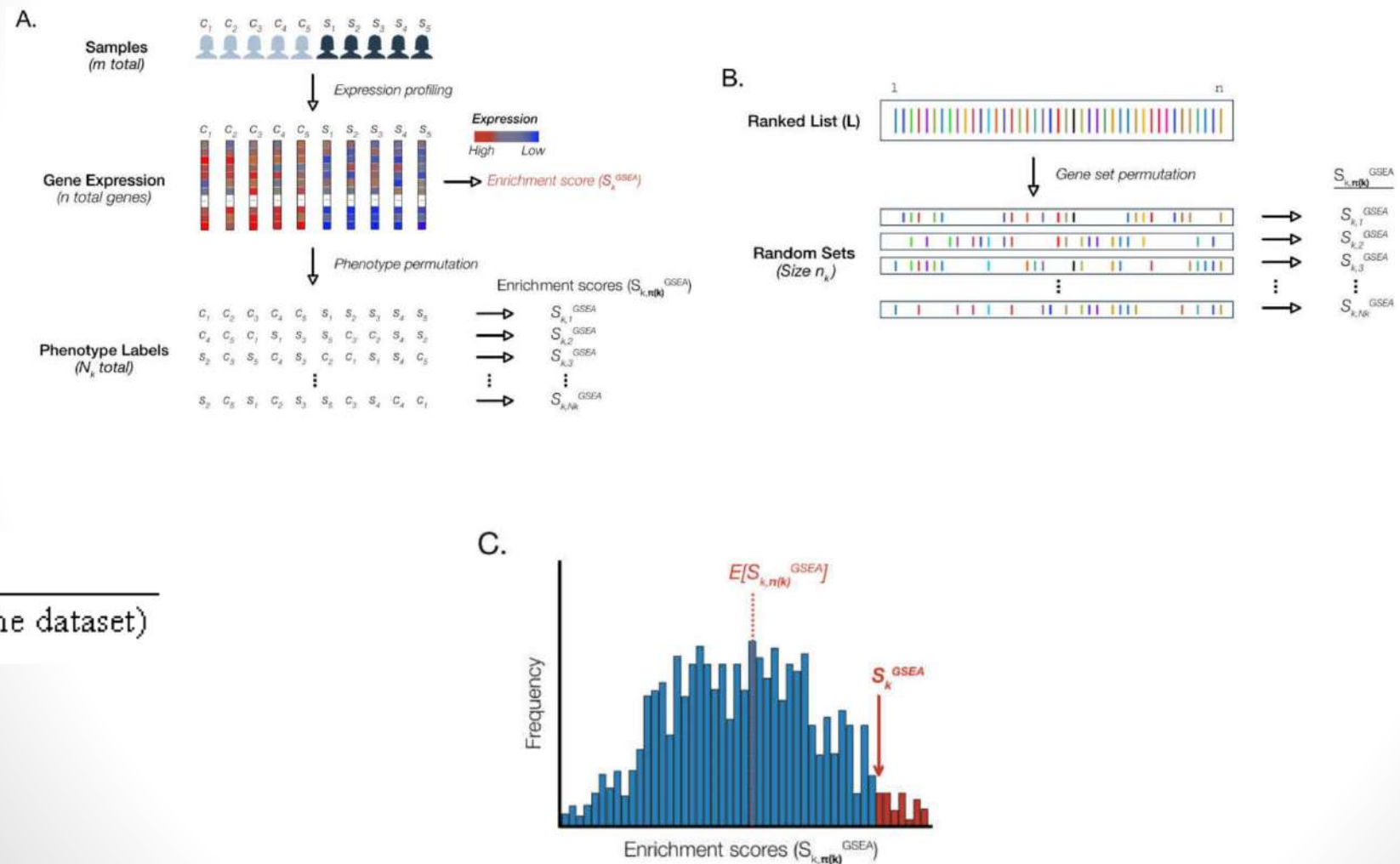
Normalized Enrichment Score (NES)

The normalized enrichment score (NES) is the primary statistic for examining gene set enrichment results.

By normalizing the enrichment score, GSEA accounts for differences in gene set size and in correlations between gene sets and the expression dataset.

Therefore, the normalized enrichment scores (NES) can be used to compare analysis results across gene sets.

$$NES = \frac{\text{actual ES}}{\text{mean(ESs against all permutations of the dataset)}}$$



4. Adjust for multiple comparisons.

False Discovery Rate (FDR)

The false discovery rate (FDR) is the estimated probability that a gene set with a given NES represents a false positive finding.

For example, an FDR of 25% indicates that the result is likely to be valid 3 out of 4 times.

When we test a family of hypotheses, the chance of observing a statistic with a small p-value increases.

When smaller than the significance level, they can be erroneously classified as discoveries or Type I errors.

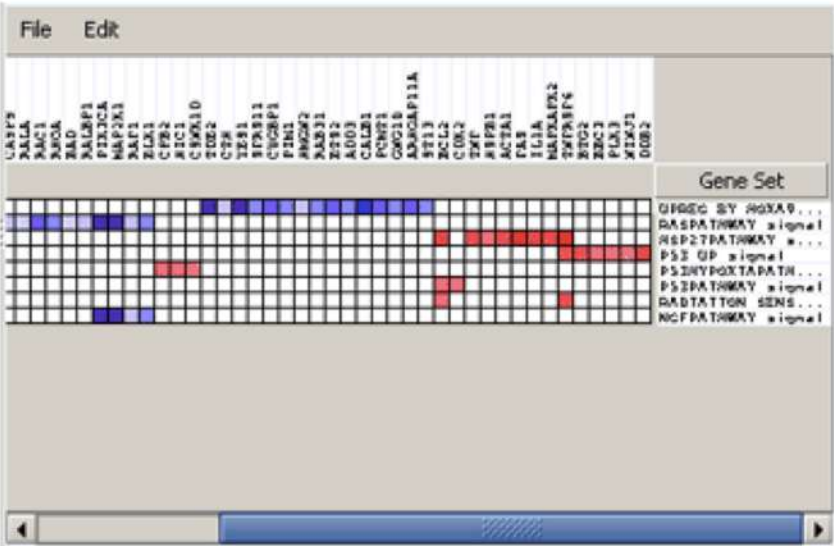
Multiple testing procedures attempt to quantify and control for these.

$$\hat{FDR} = \frac{s_{null}}{s_{obs}} \cdot \frac{n_{obs}}{n_{null}}$$

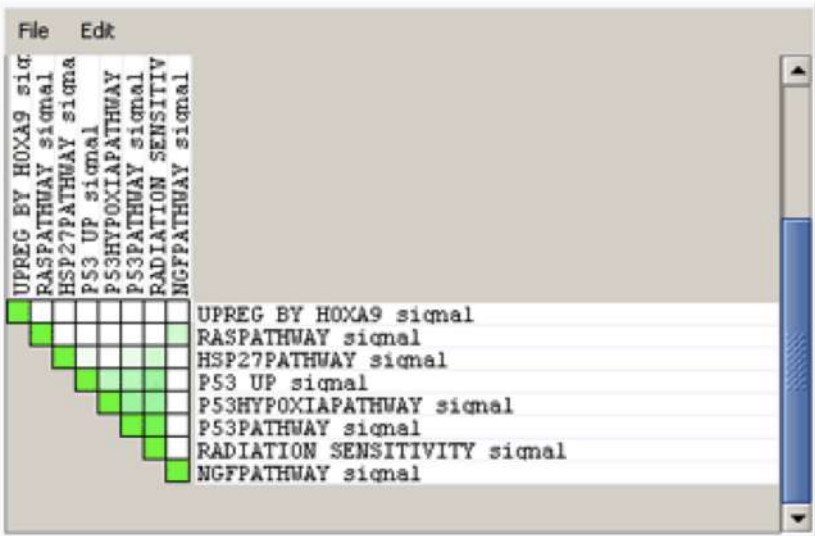
In GSEA, the collection of gene sets interrogated against the observed data are a family of hypotheses.

The recommended procedure for quantifying Type I errors is the false discovery rate (FDR). The FDR is defined as the expected value of the fraction of rejected null hypotheses that are in fact true. In practice, GSEA establishes this proportion empirically.

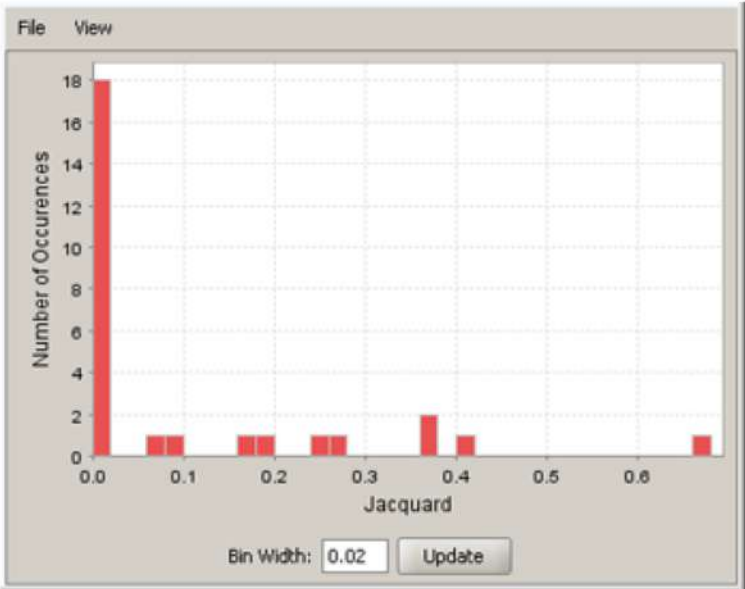
Graphs



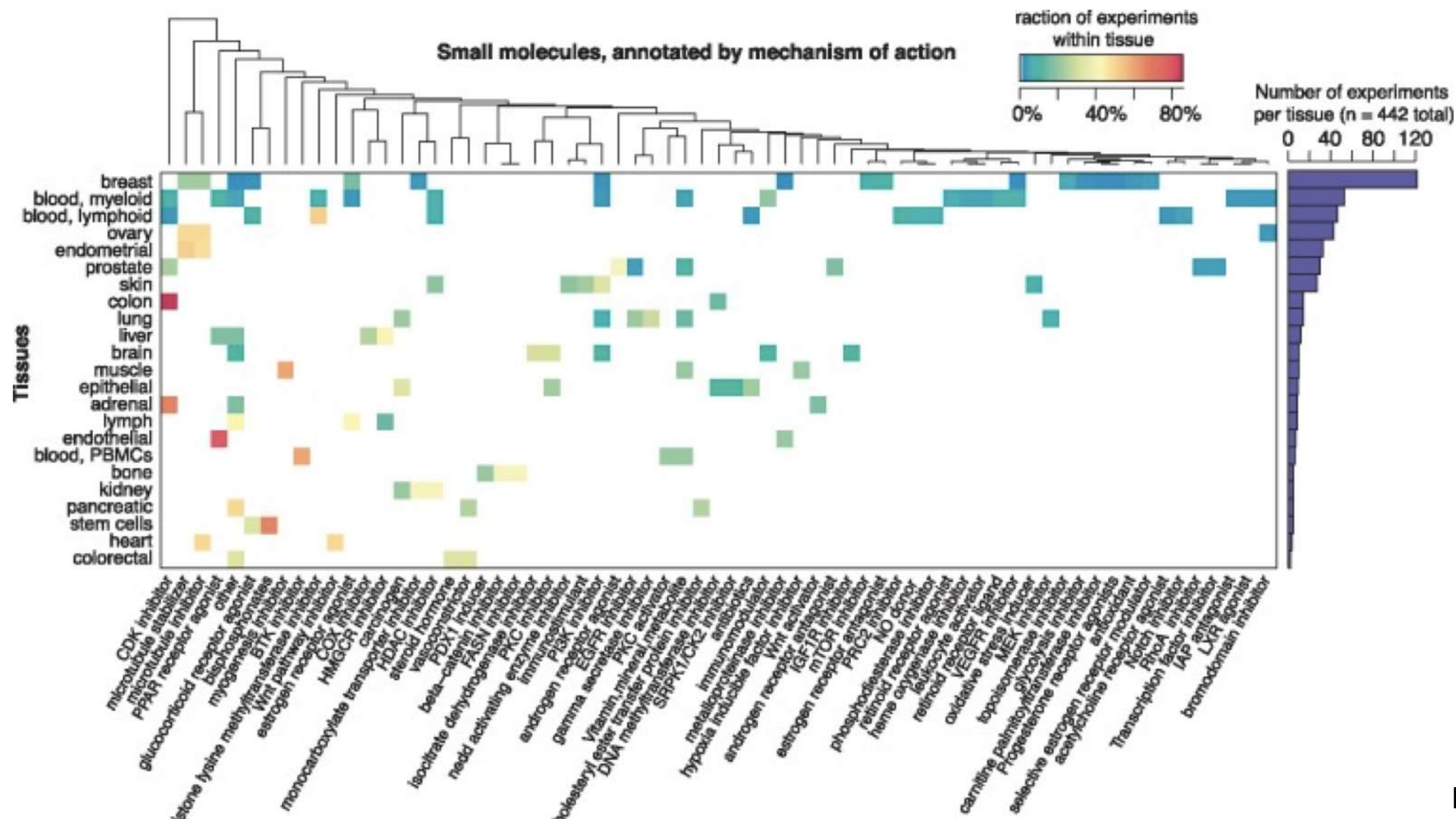
HEATMAP



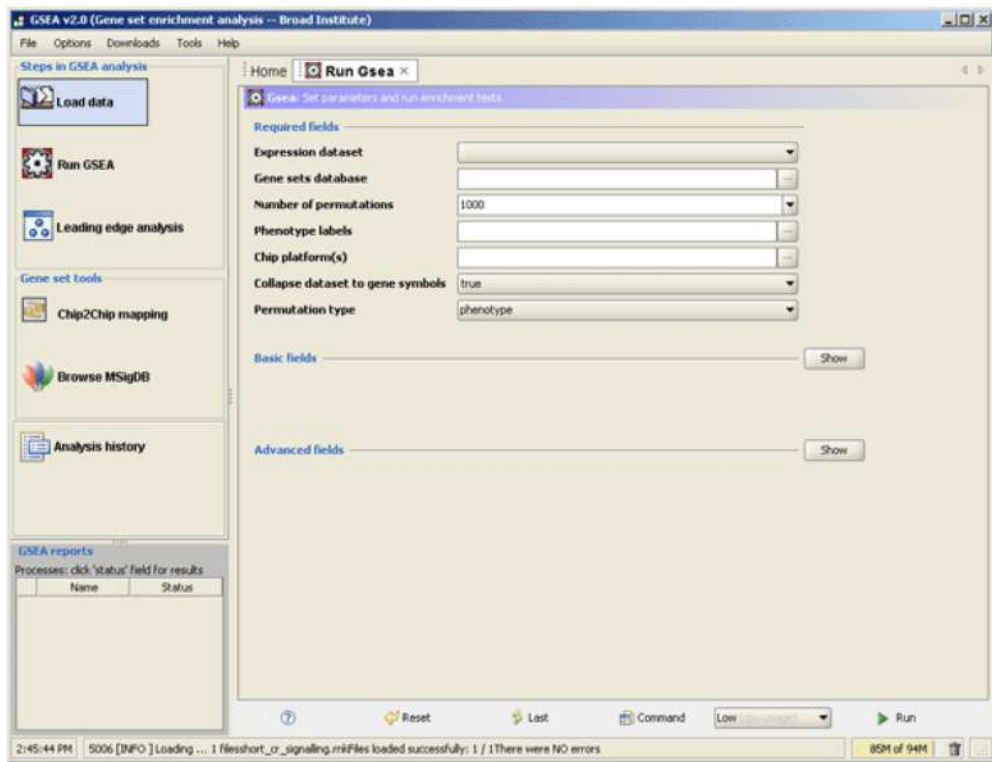
SET TO SET



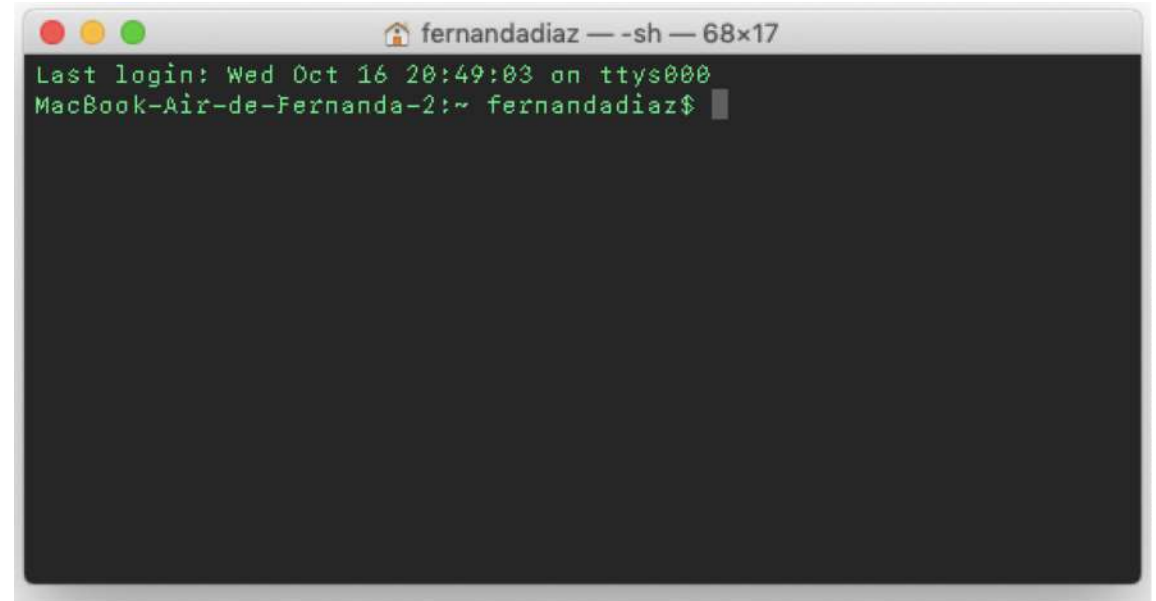
Histograms



Where to run



Java desktop app



Command line



R package

Alternatives



WEB-based GEne SeT AnaLysis Toolkit

Translating gene lists into biological insights...

Subramanian, A., Tamayo, P., Mootha, V. K., Mukherjee, S., Ebert, B. L., Gillette, M. A., ... & Mesirov, J. P. (2005). Gene set enrichment analysis: a knowledge-based approach for interpreting genome-wide expression profiles. *Proceedings of the National Academy of Sciences*, 102(43), 15545-15550.

https://www.pathwaycommons.org/guide/primers/data_analysis/gsea/