ACM TEMPLATE

UESTC_Lasagne

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$\overline{\text{Contents}}$

1	注意	事项	2
2	字符	串处理	4
	2.1	*AC 自动机	4
		2.1.1 指针	4
		2.1.2 非指针	5
	2.2	后缀数组	6
		2.2.1 DC3	6
		2.2.2 DA	8
		2.2.3 调用	8
		2.2.4 最长公共前缀	9
		2.2.5 最长公共前缀大于等于某个值的区间	9
	2.3		9 10
	2.3	· · · · · · · · · · · · · · · · · · ·	10 14
	0.4		
	2.4		20
	2.5		20
	2.6		21
	2.7		22
	2.8		25
	2.9	带 * 通配符的匹配	25
	W 337		
3	数学		28
	3.1	** ** *	28
	3.2		28
	3.3		29
	3.4	康拓展开	30
	3.5	FFT	31
	3.6	爬山法计算器	34
	3.7	线性筛	36
	3.8	线性规划	37
	3.9	分解质因数	40
		3.9.1 米勒拉宾 + 分解因数	40
			13
	3.10		 43
	0.10	The state of the s	13
			14 14
	2 11		16
	3.12		17
	-		±ι 17
			-
	5.14		17
			17
	0.15	· · · · · · · · · · · · · · · · · · ·	47
		2 * 2 * 1 * 1 * 1 * 1 * 1 * 1 * 1 * 1 *	18
	3.16	1	19
	3.17		50
			51
	3.19	—	52
	3.20		53
	3.21	其它公式	55
		3.21.1 Polya	55

		3.21.2 拉格朗日插值法 55
		3.21.3 正多面体顶点着色
		3.21.4 求和公式
		3.21.5 几何公式
		· - · · · · ·
		3.21.6 小公式
		3.21.7 马步问题 57
4	数据	
4		
	4.1	*Splay
		4.1.1 节点定义
		4.1.2 维护序列
		4.1.3 维护括号序列
	4.2	动态树
		4.2.1 维护点权 70
		4.2.2 维护边权
	4.3	可持久化线段树
	4.4	treap 正式版
	4.5	树链剖分
		4.5.1 点权
		4.5.2 边权
	4.6	划分树
	4.7	树状数组
	1.1	TO STATE OF THE ST
5	图论	98
	5.1	优先队列优化的 dijkstra
	5.2	SAP 四版
	5.3	费用流
	0.0	5.3.1 三版
		5.3.2 dijkstra 加改点堆
	5.4	网络单纯形
	5.5	M3年元が、、、、、、、、、、、、、、、、、、、、、、、、、、、、、、、、、、、、
	5.5	5.5.1 新版, 隐式图可解
		5.5.2 邻接矩阵
		5.5.3 邻接表
	5.6	一般图最大加权匹配
	5.7	一般图匹配带花树117
	5.8	KM
		5.8.1 最大加权匹配
		5.8.2 自认为正确的 Kuhn_Munkras
	5.9	* 二维平面图的最大流
	5.10	强联通
	5.11	最大团以及相关知识
	5.12	双连通分量
	5.13	割点与桥
		LCA
		最优比例生成树
	5.16	生成树计数
	5.18	欧拉路
		5.18.1 有向图
		5.18.9 无向图 12.0

		-
		5.18.3 混合图
	5 19	K 短路
		稳定婚姻
		最小树形图
	0.21	ж у гулода т.
6	计算	几何 14
	6.1	注意事项
	6.2	基本函数
		6.2.1 Point 定义
		6.2.2 Line 定义
		6.2.3 距离: 点到直线距离
		6.2.4 距离: 点到线段距离
		6.2.5 面积: 多边形
		6.2.6 判断:线段相交14
		6.2.7 判断: 点在线段上
		6.2.8 判断: 点在多边形内
		6.2.9 判断:两凸包相交
		6.2.10 排序: 叉积极角排序
	6.3	三维几何
		6.3.1 Point 定义
		6.3.2 经度纬度转换
		6.3.3 判断: 直线相交
		6.3.4 判断:线段相交
		6.3.5 判断: 三维向量是否为 0
		6.3.6 判断: 点在直线上
		6.3.7 判断: 点在线段上
		6.3.8 距离: 点到直线
		6.3.9 夹角
	6.4	圆
		6.4.1 面积: 两圆相交
		6.4.2 三角形外接圆
		6.4.3 三角形内切圆
		6.4.4 点对圆的两个切点
		6.4.5 两圆公切点
		6.4.6 两圆交点
	6.5	三角形相关
	6.6	矩阵
		6.6.1 基本矩阵
	a =	6.6.2 刘汝佳的几何教室
	6.7	重心
	6.8	KD 树
	0.0	6.8.1 例题
	6.9	半平面交
		凸包
		直线与凸包求交点
		点对凸包的两切点
		三维凸包
	6.14	旋转卡壳
		6.14.1 单个凸包
		6.14.2 两个凸包
		6.14.3 外接矩形

	6.15	三角形内点个数	76
		5.15.1 无三点共线	76
		5.15.2 有三点共线且点有类别之分	78
	6.16	最近点对	.80
		3.16.1 类快排算法	80
		3.16.2 随机增量法	.80
	6.17	多圆面积并	
		 3.17.1 去重	
		5.17.2 圆并	
	6.18	一 个圆与多边形面积交	
	0.10	5.19.1 浮点数为啥会有精度问题	
		5.19.2 eps	
		5.19.3 eps 带来的函数越界	
		5.19.4 输出陷阱 I	
		5.19.5 输出陷阱 II	
		5.19.6 范围越界	
		5.19.7 关于 set	
		5.19.7 关)set	
		5.19.8 制入恒波切近入	
		0.19.9 一些建议	.00
7	搜索	1	89
•		Dancing Links	
	1.1	7.1.1 估价函数	
		7.1.2 DLX	
			.03
8	动态	[划]	93
	8.1	 	93
	8.2	RMQ 二版	
	8.3	二维 LIS	
	8.4	重头 DP	
9	杂物	2	01
	9.1	高精度数	201
	9.2	整数外挂	202
	9.3	Java	202
		D.3.1 文件操作	202
		D.3.2 优先队列	203
		0.3.3 Map	203
		1	203
	9.4		204
	9.5	T	205
	0.0		205
		_ , , ,	206
			206
		_	206
			200
	9.6	7	207 209
	9.0		209
		T. A. T.	209 209
	0.7		
	9.7		210
		0.7.1 对跑脚本	UL

1 注意事项

输入输出格式?调试信息?初始化?算术溢出?数组大小?

左右端点范围? acos/asin/sqrt 函数定义域? 精度问题?

二分答案?暴力?单调性?凸性?块状结构?函数式?对偶问题?

排序的时候注意一下是否需要记录排序前的位置!

使用 map 进行映射的时候,不要用下面这种不安全写法

```
1 if (mp.find(s) == mp.end())
2   mp[s] = mp.size()-1;//挂成狗
3 
4 if (mp.find(s) == mp.end())
5 {
6   int tmp = mp.size();
7   mp[s] = tmp;//正确
8 }
```

106 数量级慎用后缀数组

TLE 的时候要冷静哟。。

思考的时候结合具体步骤来的话会体会到一些不同的东西

C++ 与 G++ 是很不一样的。。。

map 套字符串是很慢的。。。

栈会被记录内存。。。

浮点数最短路要注意取 < 来判断更新。。。

注意 long long

不要相信.size()

重复利用数组时小心数组范围

先构思代码框架每当实际拍马框架变化时停手重新思考

有时候四边形不等式也是帮得上忙的 dp 优化是可以水的

结构体里面带数组会非常慢, 有时候 BFS 把数组压成数字会快很多。

```
1 void fun(int a[])
2 {
3  printf("%d\n",sizeof(a));
4 }
```

结果是 sizeof(a[0]), 如果传数组指针然后要清空的话不要用 sizeof。

sqrt 某些时候会出现 sqrt(-0.00) 的问题。

将 code::blocks 的默认终端改成 gnome-terminal

 $1 \mid gnome-terminal -t TITLE -x$

最小割割集找法在残量网络中从源点出发能到的点集记为 S 原图中 S 到 S' 的边即是最小割集

double 全局变量初始值可能不是 0

2 字符串处理

2.1 *AC 自动机

别忘记 Build

```
2.1.1 指针
```

```
1 const int CHAR=26;
   const int TOTLEN=500000;
   const int MAXLEN=1000000;
   struct Vertex
 5
   {
 6
     Vertex *fail,*next[CHAR];
 7
     Vertex(){}
 8
     Vertex(bool flag)//为什么要这样写?
 9
10
       fail=0;
       memset(next,0,sizeof(next));
11
12
   };
13
   int size;
14
15 | Vertex vertex[TOTLEN+1];
16 void init()
17
18
     vertex[0]=Vertex(0);
19
     size=1;
20
21
   void add(Vertex *pos,int cha)
22
23
     vertex[size]=Vertex(0);
24
     pos->next[cha]=&vertex[size++];
25
26
   void add(vector<int> s)
27
   {
28
     int l=s.size();
29
     Vertex *pos=&vertex[0];
30
     for (int i=0; i<1; i++)
31
       if (pos->next[s[i]]==NULL)
32
33
          add(pos,s[i]);
34
       pos=pos->next[s[i]];
35
36
37
   void bfs()
38
39
     queue<Vertex *> que;
40
     Vertex *u=&vertex[0];
41
     for (int i=0; i<CHAR; i++)
42
       if (u->next[i]!=NULL)
43
```

```
44
          que.push(u->next[i]);
45
          u->next[i]->fail=u;
        }
46
47
        else
48
          u->next[i]=u;
49
      u->fail=NULL;
50
      while (!que.empty())
51
      {
52
        u=que.front();
53
        que.pop();
54
        for (int i=0; i<CHAR; i++)
55
          if (u->next[i]!=NULL)
56
          {
57
            que.push(u->next[i]);
            u->next[i]->fail=u->fail->next[i];
58
          }
59
60
          else
61
            u->next[i]=u->fail->next[i];
62
      }
   }
63
   2.1.2 非指针
 1
   struct Trie
 2
   {
 3
      int next[50][10], fail[50];
 4
      bool end[50];
 5
      int L, root;
 6
 7
      int newNode()
 8
      {
 9
        for (int i = 0; i < 10; i++)
10
          next[L][i] = -1;
11
        end[L] = false;
12
        return L++;
      }
13
14
15
      void Init()
16
17
        L = 0;
18
        root = newNode();
19
      }
20
21
      void Insert(char s[])
22
      {
23
        int now = root;
24
        for (int i = 0; s[i] != 0; i++)
25
26
          if (next[now][s[i]-'0'] == -1)
27
            next[now][s[i]-'0'] = newNode();
28
          now = next[now][s[i]-'0'];
29
        }
```

```
30
        end[now] = true;
31
32
33
     void Build()
34
35
        queue<int> Q;
36
        for (int i = 0; i < 10; i++)
37
          if (next[root][i] == -1)
            next[root][i] = root;
38
39
          else
40
          {
41
            fail[next[root][i]] = root;
42
            Q.push(next[root][i]);
43
44
        while (!Q.empty())
45
46
          int now = Q.front();
47
          Q.pop();
48
          end[now] |= end[fail[now]];
49
          for (int i = 0; i < 10; i++)
50
            if (next[now][i] == -1)
51
              next[now][i] = next[fail[now]][i];
52
            else
53
            {
54
              fail[next[now][i]] = next[fail[now]][i];
55
              Q.push(next[now][i]);
56
57
       }
58
     }
59 \};
   2.2
        后缀数组
   2.2.1 DC3
   所有下标都是 0 \text{ n-1}, height[0] 无意义。
 1 //所有相关数组都要开三倍
   const int maxn = 300010;
   # define F(x) ((x)/3+((x)\%3==1?0:tb))
   # define G(x) ((x)<tb?(x)*3+1:((x)-tb)*3+2)
   int wa[maxn * 3], wb[maxn * 3], wv[maxn * 3], ws[maxn * 3];
   int c0(int *r, int a, int b)
 7
   {
 8
     return
 9
     r[a] == r[b] \&\& r[a + 1] == r[b + 1] \&\& r[a + 2] == r[b + 2];
10
11
   int c12(int k, int *r, int a, int b)
12
   {
13
     if (k == 2)
14
        return r[a] < r[b] \mid | r[a] == r[b] \&\& c12(1, r, a + 1, b + 1);
15
     else return r[a] < r[b] || r[a] == r[b] && wv[a + 1] < wv[b + 1];
16 }
```

```
void sort(int *r, int *a, int *b, int n, int m)
18
   {
19
     int i;
20
     for (i = 0; i < n; i++) wv[i] = r[a[i]];
21
     for (i = 0; i < m; i++) ws[i] = 0;
22
     for (i = 0; i < n; i++) ws[wv[i]]++;
23
     for (i = 1; i < m; i++) ws[i] += ws[i - 1];
24
     for (i = n - 1; i \ge 0; i - b[-ws[wv[i]]] = a[i];
25
     return;
26
27
   void dc3(int *r, int *sa, int n, int m)
28
29
     int i, j, *rn = r + n;
30
     int *san = sa + n, ta = 0, tb = (n + 1) / 3, tbc = 0, p;
31
     r[n] = r[n + 1] = 0;
     for (i = 0; i < n; i++) if (i % 3 != 0) wa[tbc++] = i;
32
33
     sort(r + 2, wa, wb, tbc, m);
34
     sort(r + 1, wb, wa, tbc, m);
35
     sort(r, wa, wb, tbc, m);
36
     for (p = 1, rn[F(wb[0])] = 0, i = 1; i < tbc; i++)
       rn[F(wb[i])] = c0(r, wb[i - 1], wb[i]) ? p - 1 : p++;
37
38
     if (p < tbc) dc3(rn, san, tbc, p);
     else for (i = 0; i < tbc; i++) san[rn[i]] = i;
39
     for (i = 0; i < tbc; i++) if (san[i] < tb) wb[ta++] = san[i] * 3;
40
41
     if (n \% 3 == 1) wb[ta++] = n - 1;
42
     sort(r, wb, wa, ta, m);
43
     for (i = 0; i < tbc; i++) wv[wb[i] = G(san[i])] = i;
     for (i = 0, j = 0, p = 0; i < ta && j < tbc; p++)
44
45
       sa[p] = c12(wb[j] % 3, r, wa[i], wb[j]) ? wa[i++] : wb[j++];
46
     for (; i < ta; p++) sa[p] = wa[i++];
47
     for (; j < tbc; p++) sa[p] = wb[j++];
48
   //str 和 sa 也要三倍
50
   void da(int str□,int sa□,int rank□,int height□,int n,int m)
51
   {
52
     for (int i = n; i < n * 3; i++)
53
       str[i] = 0;
54
     dc3 (str , sa , n + 1 , m);
55
     int i, j, k;
56
     for (i = 0; i < n; i++)
57
     {
58
       sa[i] = sa[i + 1];
59
       rank[sa[i]] = i;
60
     for (i = 0, j = 0, k = 0; i < n; height[rank[i ++]] = k)
61
       if (rank[i] > 0)
62
63
         for (k ? k - : 0 , j = sa[rank[i] - 1];
64
           i + k < n \& j + k < n \& str[i + k] == str[j + k];
65
           k++);
66 |}
```

2.2.2 DA

这份似乎就没啥要注意的了。 const int maxn = 200010; int wx[maxn],wy[maxn],*x,*y,wss[maxn],wv[maxn]; bool cmp(int *r,int n,int a,int b,int l) 5 { 6 return a+1< n && b+1< n && r[a]==r[b]&&r[a+1]==r[b+1];7 8 void da(int str[],int sa[],int rank[],int height[],int n,int m) 9 10 int *s = str; 11 int x=wx, y=wy, t, p; 12 int i,j; 13 for(i=0; i<m; i++)wss[i]=0; 14 for(i=0; i<n; i++)wss[x[i]=s[i]]++; 15 for(i=1; i<m; i++)wss[i]+=wss[i-1]; 16 for(i=n-1; i>=0; i--)sa[--wss[x[i]]]=i; 17 for(j=1,p=1; p<n && j<n; j*=2,m=p) 18 { 19 for(i=n-j, p=0; i < n; i++)y[p++]=i;20 for(i=0; i<n; i++)if(sa[i]-j>=0)y[p++]=sa[i]-j; for(i=0; i<n; i++)wv[i]=x[y[i]]; 21 22 for(i=0; i<m; i++)wss[i]=0; 23 for(i=0; i<n; i++)wss[wv[i]]++; 24 for(i=1; i < m; i++)wss[i]+=wss[i-1];25 for(i=n-1; i>=0; i--)sa[--wss[wv[i]]]=y[i]; 26 for($t=x,x=y,y=t,p=1,i=1,x\lceil sa\lceil 0\rceil \rceil=0;i < n;i++)$ 27 x[sa[i]] = cmp(y,n,sa[i-1],sa[i],j)?p-1:p++;28 29 for(int i=0; i<n; i++) rank[sa[i]]=i; 30 for(int i=0, j=0, k=0; i< n; height[rank[i++]]=k)31 if(rank[i]>0) 32 for(k?k-:0,j=sa[rank[i]-1];33 i+k < n && j+k < n && str[i+k]==str[j+k];34 k++);35 } 2.2.3 调用 注意几个数组的下标是不同的 char s[maxn]: int str[maxn],sa[maxn],rank[maxn],height[maxn]; 3 4 int main() 5 { 6 scanf("%s",s); 7 int len = strlen(s); 8 for (int i = 0; $i \le len$; i++) str[i] = s[i]; 9

```
10
      da(str,sa,rank,height,len,128);
11
12
      for (int i = 0; i < len; i++)
13
      {
14
        printf("sa=\lfloor \%d, height=\lfloor \%d, s=\lfloor \%s \setminus n", sa[i], height[i], s+sa[i]);
15
16
      return 0;
17 }
   2.2.4 最长公共前缀
   记得不要忘记调用 lcpinit!
 1 | int f[maxn][20];
   int lent[maxn];
   void lcpinit()
 4
   {
 5
      int i,j;
 6
      int n = len, k = 1, l = 0;
 7
     for (i = 0; i < n; i++)
 8
 9
        f[i][0] = height[i];
        if (i+1 > k*2)
10
11
12
          k *= 2;
13
          1++;
14
15
        lent[i+1] = l;
16
     for (j = 1; (1 << j) - 1 < n; j++)
17
18
        for (i = 0; i+(1<< j)-1< n; i++)
19
          f[i][j] = min(f[i][j-1], f[i+(1<<(j-1))][j-1]);
20
21
   int lcp(int x,int y)
22
   {
23
     if (x > y) swap(x,y);
24
      if (x == y)
25
        return x-sa[x];//自己和自己当然是自己的长度啦lcp
26
      X++;
27
      int k = lent[y-x+1];
28
      return min(f[x][k], f[y-(1<< k)+1][k]);
29 }
         最长公共前缀大于等于某个值的区间
   2.2.5
   |void getinterv(int pos,int comlen,int& pl,int& pr)
 2
   {
 3
      int l,r,mid,cp;
 4
      l = 0;
 5
      r = pos;
 6
      while (l < r)
```

```
7
     {
 8
        mid = l+r>>1;
        cp = lcp(mid,pos);
 9
        if (cp < comlen)</pre>
10
11
          l = mid+1;
        else
12
13
          r = mid;
14
     }
15
     pl = l;
16
17
     l = pos;
18
     r = len-1;
19
     while (l < r)
20
     {
21
        mid = 1+r+1>>1;
22
        cp = lcp(pos,mid);
23
        if (cp < comlen)</pre>
24
          r = mid-1;
25
        else
26
          l = mid;
27
     }
28
     pr = 1;
29 |}
        后缀三兄弟
   2.3
 1 |#include <cstdio>
   #include <cstring>
   |#include <algorithm>
   using namespace std;
   const int CHAR = 26;
   const int MAXN = 100000;
   struct SAM_Node
 8
   {
 9
     SAM_Node *fa,*next[CHAR];
10
     int len;
11
     int id, pos;
12
     SAM_Node() {}
13
     SAM_Node(int _len)
14
     {
15
        fa = 0;
16
        len = _len;
17
        memset(next,0,sizeof(next));
18
19
   SAM_Node SAM_node[MAXN * 2], *SAM_root, *SAM_last;
   int SAM_size;
22
   SAM_Node *newSAM_Node(int len)
23
   {
24
     SAM_node[SAM_size] = SAM_Node(len);
25
     SAM_node[SAM_size].id=SAM_size;
26
     return &SAM_node[SAM_size++];
```

```
27 |}
28 SAM_Node *newSAM_Node(SAM_Node *p)
29
30
      SAM_node[SAM_size] = *p;
31
      SAM_node[SAM_size].id=SAM_size;
32
      return &SAM_node[SAM_size++];
33
34
   void SAM_init()
35
   {
36
      SAM_size = 0;
37
      SAM_root = SAM_last = newSAM_Node(0);
38
      SAM_node[0].pos=0;
39
40
   void SAM_add(int x,int len)
41
   {
42
      SAM_Node *p = SAM_last, *np = newSAM_Node(p->len + 1);
43
      np->pos=len;
44
      SAM_last = np;
45
      for (; p && !p->next[x]; p = p->fa)
46
        p->next[x] = np;
47
      if (!p)
48
      {
49
        np->fa = SAM\_root;
50
        return ;
51
52
      SAM_Node *q = p -> next[x];
53
      if (q\rightarrow len == p\rightarrow len + 1)
54
      {
55
        np \rightarrow fa = q;
56
        return ;
57
58
      SAM_Node *nq = newSAM_Node(q);
59
      nq->len = p->len + 1;
60
      q\rightarrow fa = nq;
61
      np \rightarrow fa = nq;
62
      for (; p && p->next[x] == q; p = p->fa)
63
        p->next[x] = nq;
64
65
   void SAM_build(char *s)
66
67
      SAM_init();
68
      int l = strlen(s);
69
      for (int i = 0; i < 1; i++)
70
        SAM_add(s[i] - 'a', i+1);
71
   }
72
73
   SAM_Node * SAM_add(SAM_Node *p, int x, int len)
74
75
      SAM_Node *np = newSAM_Node(p->len + 1);
76
      np->pos = len;
77
      SAM_last = np;
```

```
78
       for (; p && !p->next[x]; p = p->fa)
 79
         p->next[x] = np;
       if (!p)
 80
 81
       {
 82
         np->fa = SAM\_root;
 83
         return np;
 84
 85
       SAM_Node *q = p->next[x];
 86
       if (q\rightarrow len == p\rightarrow len + 1)
 87
       {
 88
         np \rightarrow fa = q;
 89
         return np;
 90
 91
       SAM_Node *nq = newSAM_Node(q);
 92
       nq->len = p->len + 1;
 93
       q\rightarrow fa = nq;
 94
       np \rightarrow fa = nq;
 95
       for (; p && p->next[x] == q; p = p->fa)
 96
         p->next[x] = nq;
 97
       return np;
 98
 99
    void SAM_build(char *s)//多串建立 注意SAM_init()的调用
100
101
       int l = strlen(s);
102
       SAM_Node *p = SAM_root;
103
       for (int i = 0; i < l; i++)
104
       {
105
         if (!p->next[s[i] - 'a'] || !(p->next[s[i] - 'a']->len == i +
106
           p=SAM_add(p,s[i] - 'a', i + 1);
107
         else
108
           p = p \rightarrow next[s[i] - 'a'];
109
       }
    }
110
111
112
    struct ST_Node
113
114
       ST_Node *next[CHAR],*fa;
115
       int len, pos;
    }ST_node[MAXN*2],*ST_root;
116
    int Sufpos[MAXN];
117
    void ST_add(int u,int v,int chr,int len)
118
119
    {
120
       ST_node[u].next[chr]=&ST_node[v];
121
       ST_node[v].len=len;
122
123
    void init(int n)
124
125
       for (int i=0;i<n;i++)
126
       {
127
         ST_node[i].pos=-1;
```

```
128
         ST_node[i].fa=0;
129
         memset(ST_node[i].next,0,sizeof(ST_node[i].next));
130
      ST_node[0].pos=0;
131
132
      ST_root=&ST_node[0];
133
134
    void ST_build(char *s)
135
    {
136
      int n=strlen(s);
137
      reverse(s,s+n);
138
      SAM_build(s);
139
      init(SAM_size);
140
      for (int i=1;i<SAM_size;i++)</pre>
141
142
         ST_add(SAM_node[i].fa->id,
143
           SAM_node[i].id,
144
           s[SAM_node[i].pos-SAM_node[i].fa->len-1]-'a',
           SAM_node[i].len-SAM_node[i].fa->len);
145
         if (SAM_node[i].pos==SAM_node[i].len)
146
147
148
           Sufpos[n—SAM_node[i].pos+1]=i;
149
           ST_node[i].pos=n-SAM_node[i].pos+1;
150
        }
151
      }
    }
152
153
154
    int rank[MAXN],sa[MAXN+1];
155
    int height[MAXN];
156
    int L;
157
    void ST_dfs(ST_Node *p)
158
159
      if (p->pos!=-1)
160
         sa[L++]=p->pos;
      for (int i=0;i<CHAR;i++)</pre>
161
         if (p—>next[i])
162
163
           ST_dfs(p->next[i]);
164
165
    char s[MAXN+1];
166
    int main()
167
    {
168
      gets(s);
      ST_build(s);
169
      L=0;
170
171
      ST_dfs(ST_root);
172
      int n=strlen(s);
173
      for (int i=0; i<n; i++)
174
         sa[i]=sa[i+1]-1;
175
      for (int i=0; i<n; i++)
176
         rank[sa[i]]=i;
177
      reverse(s,s+n);
      for (int i=0, j=0, k=0; i< n; height[rank[i++]]=k)
178
```

```
179
        if (rank[i])
           for (k?k-:0,j=sa[rank[i]-1]; s[i+k]==s[j+k]; k++);
180
181 |}
    2.3.1
         例题
   |#include <iostream>
    #include <algorithm>
    #include <cstdio>
    #include <cstring>
    using namespace std;
  6
    const int CHAR = 26;
  8
    const int MAXN = 100000;
 9
10
    struct SAM_Node
11
    {
12
      SAM_Node *fa,*next[CHAR];
13
      int len;
14
      int id;
      int mat[9];
15
      SAM_Node() {}
16
17
      SAM_Node(int _len)
18
      {
19
        fa = 0;
20
        len = _len;
        memset(mat,0,sizeof(mat));
21
 22
        memset(next,0,sizeof(next));
 23
      }
    };
24
25
    SAM_Node SAM_node[MAXN*2],*SAM_root,*SAM_last;
    int SAM_size;
    SAM_Node *newSAM_Node(int len)
27
28
 29
      SAM_node[SAM_size] = SAM_Node(len);
30
      SAM_node[SAM_size].id = SAM_size;
 31
      return &SAM_node[SAM_size++];
 32
 33
    SAM_Node *newSAM_Node(SAM_Node *p)
 34
    {
 35
      SAM_node[SAM_size] = *p;
      SAM_node[SAM_size].id = SAM_size;
 36
 37
      return &SAM_node[SAM_size++];
 38
 39
    void SAM_init()
40
    {
41
      SAM_size = 0;
42
      SAM_root = SAM_last = newSAM_Node(0);
43
44
    void SAM_add(int x,int len)
45
46
      SAM_Node *p = SAM_last,*np = newSAM_Node(p->len+1);
```

```
47
      SAM_last = np;
      for (; p\&\&!p->next[x]; p=p->fa)
48
49
        p \rightarrow next[x] = np;
50
      if (!p)
51
52
        np->fa = SAM\_root;
53
        return;
54
55
      SAM_Node *q = p->next[x];
56
      if (q\rightarrow len == p\rightarrow len+1)
57
58
        np->fa = q;
59
        return;
60
61
      SAM_Node *nq = newSAM_Node(q);
      nq \rightarrow len = p \rightarrow len + 1;
62
63
      q\rightarrow fa = nq;
64
      np \rightarrow fa = nq;
65
      for (; p\&p->next[x] == q; p = p->fa)
66
        p->next[x] = nq;
67
68 int getid(char ch)
69
   {
70
      return ch-'a';
71
72 void SAM_build(char *s)
73
   {
74
      SAM_init();
75
      int l = strlen(s);
      for (int i = 0; i < 1; i++)
76
77
        SAM_add(getid(s[i]),i+1);
78
79
   |char s[10][MAXN+1];
80 | int ans;
81 | int head[MAXN*2];
82
   struct Edge
83
   {
84
      int to, next;
85
   |} edge[MAXN*2];
86 | int M;
87
   int n;
88
   void add_edge(int u,int v)
89
   {
90
      edge[M].to=v;
91
      edge[M].next=head[u];
92
      head[u]=M++;
93
   }
94 void dfs(int u)
95
      for (int i=head[u]; i!=-1; i=edge[i].next)
96
97
```

```
98
         int v=edge[i].to;
 99
         dfs(v);
         for (int j=0; j< n-1; j++)
100
101
         SAM_node[u].mat[j]=max(SAM_node[v].mat[j],SAM_node[u].mat[j]);
102
103
       int tmp=SAM_node[u].len;
104
       for (int i=0; i< n-1; i++)
105
         tmp=min(tmp,SAM_node[u].mat[i]);
106
       ans=max(ans,tmp);
107
    int main()
108
109
    {
110
111
       while (scanf("%s",s[n])!=EOF)
112
         n++;
113
       int L=strlen(s[0]);
114
       ans=M=0;
115
       SAM_build(s[0]);
116
       for (int j=1; j< n; j++)
117
         int l=strlen(s[j]),len=0;
118
119
         SAM_Node *p=SAM_root;
120
         for (int i=0; i<1; i++)
121
         {
122
           if (p->next[getid(s[j][i])])
123
           {
124
              p=p->next[getid(s[j][i])];
125
              p\rightarrow mat[j-1]=max(p\rightarrow mat[j-1],++len);
126
           }
127
           else
128
           {
129
             while (p && !p->next[getid(s[j][i])])
130
                p=p->fa;
131
              if (!p)
132
133
                p=SAM_root;
134
                len=0;
              }
135
              else
136
137
              {
138
                len=p->len+1;
                p=p->next[getid(s[j][i])];
139
140
141
             p\rightarrow mat[j-1]=max(p\rightarrow mat[j-1],len);
142
         }
143
144
       memset(head, -1, 4*SAM\_size);
145
       for (int i=1; i<SAM_size; i++)</pre>
146
147
         add_edge(SAM_node[i].fa—>id,i);
148
       dfs(0);
```

```
printf("%d\n",ans);
149
150
      return 0;
151 |}
    LCS2
  1 |#include <iostream>
    #include <algorithm>
    #include <cstdio>
    |#include <cstring>
    using namespace std;
  7
    const int CHAR = 26;
  8
    const int MAXN = 100000;
  9
    struct SAM_Node
 10
11
    {
12
      SAM_Node *fa,*next[CHAR];
13
      int len;
 14
      int id;
      int mat[9];
15
      SAM_Node() {}
16
17
      SAM_Node(int _len)
18
      {
 19
        fa = 0;
 20
        len = _len;
 21
        memset(mat,0,sizeof(mat));
 22
        memset(next,0,sizeof(next));
23
      }
24
    SAM_Node SAM_node[MAXN*2],*SAM_root,*SAM_last;
26
    int SAM_size;
27
    SAM_Node *newSAM_Node(int len)
 28
    {
 29
      SAM_node[SAM_size] = SAM_Node(len);
30
      SAM_node[SAM_size].id = SAM_size;
 31
      return &SAM_node[SAM_size++];
 32
 33
    SAM_Node *newSAM_Node(SAM_Node *p)
 34
 35
      SAM_node[SAM_size] = *p;
 36
      SAM_node[SAM_size].id = SAM_size;
 37
      return &SAM_node[SAM_size++];
 38
 39
    void SAM_init()
40
    {
41
      SAM_size = 0;
42
      SAM_root = SAM_last = newSAM_Node(0);
43
44
    void SAM_add(int x,int len)
45
46
      SAM_Node *p = SAM_last,*np = newSAM_Node(p->len+1);
```

```
47
      SAM_last = np;
      for (; p\&\&!p->next[x]; p=p->fa)
48
49
        p \rightarrow next[x] = np;
50
      if (!p)
51
52
        np->fa = SAM\_root;
53
        return;
54
55
      SAM_Node *q = p->next[x];
56
      if (q\rightarrow len == p\rightarrow len+1)
57
58
        np->fa = q;
59
        return;
60
61
      SAM_Node *nq = newSAM_Node(q);
      nq \rightarrow len = p \rightarrow len + 1;
62
63
      q\rightarrow fa = nq;
64
      np \rightarrow fa = nq;
65
      for (; p\&p->next[x] == q; p = p->fa)
66
        p->next[x] = nq;
67
68 int getid(char ch)
69
   {
70
      return ch-'a';
71
72 void SAM_build(char *s)
73
   {
74
      SAM_init();
75
      int l = strlen(s);
      for (int i = 0; i < 1; i++)
76
77
        SAM_add(getid(s[i]),i+1);
78
79 | char s[MAXN+1];
80 | int ans;
81 | int head[MAXN*2];
82
   struct Edge
83
   {
84
      int to, next;
85
   |} edge[MAXN*2];
86 | int M;
87
   int n;
88
   void add_edge(int u,int v)
89
    {
90
      edge[M].to=v;
91
      edge[M].next=head[u];
92
      head[u]=M++;
93
   }
94 void dfs(int u)
95
      for (int i=head[u]; i!=-1; i=edge[i].next)
96
97
```

```
98
         int v=edge[i].to;
 99
         dfs(v);
100
         for (int j=0; j<n; j++)
101
         SAM_node[u].mat[j]=max(SAM_node[v].mat[j],SAM_node[u].mat[j]);
102
103
       int tmp=SAM_node[u].len;
104
       for (int i=0; i<n; i++)
105
         tmp=min(tmp,SAM_node[u].mat[i]);
106
       ans=max(ans,tmp);
107
    int main()
108
109
     {
       //freopen("in.txt","r",stdin);
110
       //freopen("out.txt","w",stdout);
111
112
       n=0;
113
       gets(s);
114
       SAM_build(s);
115
       while (gets(s))
116
       {
117
         int l=strlen(s),len=0;
         SAM_Node *p=SAM_root;
118
119
         for (int i=0; i<1; i++)
120
121
           if (p->next[getid(s[i])])
122
           {
123
              p=p->next[getid(s[i])];
124
              p\rightarrow mat[n]=max(p\rightarrow mat[n],++len);
125
           }
126
           else
127
           {
128
             while (p && !p->next[getid(s[i])])
129
                p=p->fa;
130
              if (!p)
131
              {
132
                p=SAM_root;
133
                len=0;
134
              }
135
              else
136
137
                len=p->len+1;
138
                p=p->next[getid(s[i])];
139
140
             p\rightarrow mat[n]=max(p\rightarrow mat[n],len);
141
142
           //printf("%d %d %d\n",i,len,p->id);
143
         }
144
         n++;
145
146
       memset(head, -1, 4*SAM\_size);
147
       for (int i=1; i<SAM_size; i++)
         add_edge(SAM_node[i].fa->id,i);
148
```

```
149 | dfs(0);
150 | printf("%d\n",ans);
151 | return 0;
152 |}
```

2.4 KMP

求 A[0..i] 的一个后缀最多能匹配 B 的前缀多长。先对 B 进行自匹配然后与 A 匹配。KMP[i] 就是对应答案,p[i]+1 是 B[0..i] 的一个后缀最多能匹配 B 的前缀多长。

```
1 //自匹配过程
 2
   int j;
   p[0] = j = -1;
   for ( int i = 1; i < lb; i++)
 5
   {
     while (j \ge 0 \&\& b[j + 1] != b[i]) j = p[j];
 7
     if (b[j + 1] == b[i]) j ++;
 8
     p[i] = j;
   }
9
   //下面是匹配过程
10
11
   |j| = -1;
   for ( int i = 0; i < la; i++)
12
13
     while (j \ge 0 \& b[j + 1] != a[i]) j = p[j];
14
15
     if (b[j + 1] == a[i]) j ++;
16
     KMP[i] = j + 1;
17 |}
```

2.5 e-KMP

求 A[i..len-1] 和 B 的最长公共前缀有多长。先对 B 进行自匹配然后与 A 匹配。eKMP[i] 就是对应答案。p[i] 是 B[i..len-1] 和 B 的最长公共前缀有多长。

```
1 //自匹配过程
   int j = 0;
 3
   while (j < lb \& b[j] == b[j + 1])
     j++;
   p[0] = lb, p[1] = j;
   int k = 1;
 7
   for (int i = 2; i < lb; i++)
8
   {
9
     int Len = k + p[k] - 1, L = p[i - k];
     if (L < Len - i + 1)
10
11
       p[i] = L;
12
     else
13
     {
14
       j = max(0, Len - i + 1);
15
       while (i + j < lb \& b[i + j] == b[j])
16
          j++;
17
       p[i] = j, k = i;
     }
18
19
20 //下面是匹配过程
```

```
21 | j = 0;
22
   |while (j < la && j < lb && a[j] == b[j])
23
     j++;
24
   eKMP[0] = j;
25
   k = 0;
26
   for (int i = 1; i < la; i++)
27
28
     int Len = k + eKMP[k] - 1, L = p[i - k];
29
     if (L < Len - i + 1)
30
        eKMP[i] = L;
31
     else
32
     {
33
        j = max(0, Len - i + 1);
34
        while (i + j < la && j < lb && a[i + j] == b[j])
35
          j++;
36
        eKMP[i] = j, k = i;
37
38 |}
   2.6
        Manacher
   const int maxn = 110000;
 2
 3
   char Ma[maxn*2];
   int Mp[maxn*2];
 5
   void Manacher(char s□,int len)
```

```
6
   {
 7
      int l = 0;
     Ma[l++] = '.';
Ma[l++] = ',';
 8
 9
10
      for (int i = 0; i < len; i++)
11
12
        Ma[l++] = s[i];
13
        Ma[l++] = ',';
14
      }
15
      Ma[1] = 0;
16
      int pnow = 0,pid = 0;
17
      for (int i = 1; i < l; i++)
18
      {
19
        if (pnow > i)
20
          Mp[i] = min(Mp[2*pid-i],pnow-i);
21
        else
22
          Mp[i] = 1;
23
        for (;Ma[i-Mp[i]] == Ma[i+Mp[i]];Mp[i]++);
24
        if (i+Mp[i] > pnow)
25
26
          pnow = i+Mp[i];
27
          pid = i;
28
        }
29
      }
30 |}
```

```
31 | /*
32
   abaaba
33
                 b , a , a , b , a ,
4 1 2 7 2 1 4 1 2 1
             ,
1
       ,
1
           2
34
    0
35
   */
   2.7
       不同回文串
   往 hash 表中插入新东西的时候就说明找到了一个新回文字串
   一共 O(n) 个
  |typedef unsigned int uint;
 3
   const int maxn = 110000;
 4
 5
   char Ma[maxn*2];
   int Mp[maxn*2];
   void Manacher(char s[],int len)
 8
   {
 9
     int l = 0;
     Ma[l++] = '.';
10
     Ma[l++] = ','
11
12
     for (int i = 0; i < len; i++)
13
     {
14
       Ma[l++] = s[i];
15
       Ma[l++] = ',';
     }
16
17
     Ma[1] = 0;
     int pnow = 0, pid = 0;
18
19
     for (int i = 1; i < l; i++)
20
21
        if (pnow > i)
22
          Mp[i] = min(Mp[2*pid-i],pnow-i);
23
        else
24
          Mp[i] = 1;
25
        for (; Ma[i-Mp[i]] == Ma[i+Mp[i]]; Mp[i]++);
26
        if (i+Mp[i] > pnow)
27
        {
28
          pnow = i+Mp[i];
29
          pid = i;
30
       }
31
     }
   }
32
33
34
   char s[maxn*2];
35
   |int len;
36
   int p[maxn*2];
   const int muts = 129;
37
38
   |uint sum[maxn];
39
   uint mutpower[maxn];
40
41
   struct hash_map
42 | {
```

```
43
      const static int mod = 300007;
44
      int head[mod];
45
      struct hash_tables
46
      {
47
        uint key1;
48
        int key2;
49
        int next;
50
      } ele[maxn*10];
51
      int N;
52
      void init()
53
      {
        memset(head,-1,sizeof(head));
54
55
        N = 0;
56
57
      int totlen[mod];
58
      void clear()
59
60
        for (int i = 0; i < N; i++)
61
          head[ele[i].key1\%mod] = -1;
62
        N = 0;
63
     int find(uint x,int len)
64
65
66
        int hashcode = x%mod;
67
        for (int i = head[hashcode]; i != -1; i = ele[i].next)
68
          if (ele[i].key1 == x \& ele[i].key2 == len)
69
            return i;
70
        return -1;
71
      }
72
      void insert(uint x,int len)
73
74
        int tmp = x \mod;
75
        ele[N].key1 = x;
        ele[N].key2 = len;
76
77
        ele[N].next = head[tmp];
78
        head[tmp] = N++;
79
   };
80
81
82
   |hash_map hash;
83
84
   uint gethashcode(int l,int r)
85
86
     uint ret;
87
      ret = sum[r];
88
      if (l)
89
        ret -= sum[l-1]*mutpower[r-l+1];
90
      return ret;
   }
91
92
93
   |int calc(char s[])
```

```
94 |{
 95
      len = strlen(s);
 96
      Manacher(s,len);
 97
 98
      sum[0] = s[0];
 99
      for (int i = 1; i < len; i++)
100
         sum[i] = sum[i-1]*muts+s[i];
101
102
      int res = 0;
103
      uint tmp;
104
      int nt = 0;
      hash.clear();
105
106
      //odd
107
      for (int i = 0; i < len; i++)
         if (Mp[i*2+2]\%2 == 0)
108
109
           int pl = Mp[i*2+2]/2;
110
111
           if (i+pl < nt || pl == 0) continue;
112
           for (int j = i-pl+1; j <= i; j++)
113
114
             tmp = gethashcode(j,i);
115
             if (hash.find(tmp,i-j+1) != -1) break;
116
             hash.insert(tmp,i-j+1);
           }
117
118
           nt = i+pl;
119
         }
120
      res += hash.N;
121
122
      nt = 0;
      hash.clear();
123
124
      //even
125
      for (int i = 0; i < len; i++)
126
         if (Mp[i*2+3] > 1)
127
128
           int pl = Mp[i*2+3]/2;
129
           if (i+pl < nt || pl == 0) continue;
130
           for (int j = i-pl+1; j \le i; j++)
131
           {
132
             tmp = gethashcode(j,i);
133
             if (hash.find(tmp,i-j+1) != -1) break;
134
             hash.insert(tmp,i-j+1);
135
136
           nt = i+pl;
        }
137
138
      res += hash.N;
139
      return res;
    }
140
141
142
    int main()
143
    {
144
      mutpower[0] = 1;
```

```
145
      for (int i = 1; i < maxn; i++)
        mutpower[i] = mutpower[i-1]*muts;
146
147
      hash.init();
148
149
      int totcas;
      scanf("%d",&totcas);
150
151
      for (int cas = 1; cas <= totcas; cas++)
152
      {
153
        scanf("%s",s);
154
155
        printf("Case_#%d:_%d\n",cas,calc(s));
156
157
      return 0;
158 |}
        * 字符串最小表示法
    2.8
    |int Gao(char a[],int len)
  2
    {
  3
      int i = 0, j = 1, k = 0;
  4
      while (i < len && j < len && k < len)
  5
      {
  6
        int cmp = a[(j+k)\%len]-a[(i+k)\%len];
  7
        if (cmp == 0)
  8
          k++;
  9
        else
 10
         {
           if (cmp > 0)
 11
 12
             j += k+1;
 13
           else
 14
             i += k+1;
          if (i == j) j++;
 15
 16
          k = 0;
 17
        }
 18
 19
      return min(i,j);
 20 |}
         带 * 通配符的匹配
    2.9
  1 | #include <iostream>
  2 | #include <algorithm>
    #include <cstdio>
    #include <cstring>
    using namespace std;
  6
    char a[110],b[110],sp[110][110],tot,place[110];
  8
    |int n,la,lb,ll;
  9
 10 | bool check(int id, int pos)
 11 | {
```

```
12
      for (int i = 0; sp[id][i] != 0; i++)
        if (b[pos+i] != sp[id][i])
13
14
          return false;
15
      return true;
   }
16
17
18
   bool check()
19
   {
20
     lb = strlen(b);
21
      int pre = 0;
22
      for (int i = 0; i < tot; i++)
23
24
        bool find = false;
25
        for (int j = pre; j < lb; j++)
26
          if (check(i,j) == true)
27
          {
28
            place[i] = j;
29
            pre = place[i]+1;
30
            find = true;
31
            break;
32
33
        if (find == false)
                            return false;
34
35
     if (a[0] != '*')
36
        if (place[0] != 0)
37
          return false;
     if (a[la-1] != '*')
38
39
        if (check(tot-1,lb-ll) == false)
40
          return false;
41
     return true;
   }
42
43
44
   int main()
45
   {
     while (scanf("%s",a) != EOF)
46
47
      {
48
        tot = 0;
49
        for (int i = 0; a[i] != 0; i++)
          if (a[i] != '*')
50
51
          {
52
            int j;
            for (j = i; a[j] != 0 && a[j] != '*'; j++)
53
54
              sp[tot][j-i] = a[j];
55
            sp[tot++][j-i] = 0;
56
            i = j;
57
58
        la = strlen(a);
59
        ll = strlen(sp[tot-1]);
        scanf("%d",&n);
60
61
        for (int i = 0; i < n; i++)
62
```

```
scanf("%s",b);
63
         if (check() == true)
64
65
           puts(b);
66
       }
     }
67
68
     return 0;
   }
/*
69
70
71
   Sample Input 1
72
   *.*
   4
73
74 main.c
75 a.out
76 readme
77 yacc
78
79 Sample Input 2
80 |*a*a*a
81
   4
82
   aaa
83
   aaaaa
84
   aaaaax
85
   abababa
86
87
   Sample Output 1
88 main.c
89
   a.out
90
91 Sample Output 2
92
   aaa
93 aaaaa
94
   abababa
95 */
```

3 数学

3.1 扩展 GCD

```
 \bar{\mathbf{x}}   ax+by=gcd(a,b)  的一组解
   long long ex_gcd(long long a,long long b,long long &x,long long &y)
 2
   {
 3
      if (b)
 4
      {
 5
        long long ret = ex_gcd(b,a\%b,x,y), tmp = x;
 6
        x = y;
 7
        y = tmp-(a/b)*y;
 8
        return ret;
 9
      }
      else
10
11
      {
12
        x = 1;
13
        y = 0;
14
        return a;
15
16 }
```

3.2 模线性方程组

```
1 // 有更新
   int m[10],a[10];//模数m 余数a
   bool solve(int &m0, int &a0, int m, int a)//模线性方程组
 4
   {
 5
     int y,x;
 6
     int g=ex\_gcd(m0,m,x,y);
 7
     if (abs(a-a0)\%g) return 0;
 8
     x*=(a-a0)/g;
 9
     x\%=m/g;
     a0=(x*m0+a0);
10
11
     m0*=m/g;
12
     a0\%=m0;
13
     if (a0<0) a0+=m0;
14
     return 1;
15
   }
16
   int MLES()
17
18
     bool flag=1;
19
     int m0=1, a0=0;
20
     for (int i=0; i<n; i++)
21
        if (!solve(m0,a0,m[i],a[i]))
22
        {
23
          flag=0;
24
          break;
25
     if (flag)
26
```

```
27
        return a0;
28
     else
29
        return -1;
30 |}
        矩阵
   3.3
   乘法的时候将 B 数组转置一下然后 C[i][j] = \sum A[i][k] \times B[j][k] 会有奇效。
   struct Matrix
 2
   {
 3
     int a[52][52];
 4
     void clear()
 5
 6
        memset(a,0,sizeof(a));
 7
 8
     int det(int n)//求行列式的值模上一个数,需要预处理逆元
 9
        for (int i = 0; i < n; i++)
10
11
          for (int j = 0; j < n; j++)
12
            a[i][j] = (a[i][j]%mod+mod)%mod;
13
        int res = 1;
14
        for (int i = 0; i < n; i++)
15
        {
16
          for (int j = i; j < n; j++)
17
            if (a[j][i] != 0)
18
            {
19
              for (int k = i; k < n; k++)
20
                swap(a[i][k],a[j][k]);
21
              if (i != j)
22
                res = (res+mod)%mod;
23
              break;
24
25
          if (a[i][i] == 0)
26
27
            res = -1;//不存在
28
            break;
29
30
          for (int j = i+1; j < n; j++)
31
32
            int mut = (a[j][i]*inv[a[i][i]])%mod;
33
            for (int k = i; k < n; k++)
34
              a[j][k] = (a[j][k]-(a[i][k]*mut)%mod+mod)%mod;
35
          }
36
          res = (res*a[i][i]) mod;
37
        }
38
        return res;
39
40
     Matrix operator * (const Matrix &b)const
41
     {
42
        Matrix res;
43
        for (int i = 0; i < 52; i++)
          for (int j = 0; j < 52; j++)
44
```

```
45
          {
46
            res.a[i][j] = 0;
47
            for (int k = 0; k < 52; k++)
48
              res.a[i][j] += a[i][k] * b.a[k][j];
49
50
       return res;
51
52
     Matrix operator ^ (int y)const
53
54
       Matrix res, x;
55
       for (int i = 0; i < 52; i++)
56
57
          for (int j = 0; j < 52; j++)
            res.a[i][j] = 0, x.a[i][j] = a[i][j];
58
59
          res.a[i][i] = 1;
60
61
       for (; y; y >>= 1, x = x * x)
         if (y & 1)
62
63
            res = res * x;
64
       return res;
65
66 | };
        康拓展开
   3.4
   |const int PermSize = 12;
   int factory[PermSize] =
   {1, 1, 2, 6, 24, 120, 720, 5040, 40320, 362880, 3628800, 39916800};
   int Cantor(int a[])
 5
   {
 6
     int i, j, counted;
 7
     int result = 0;
     for (i = 0; i < PermSize; ++i)
 8
 9
10
       counted = 0;
       for (j = i + 1; j < PermSize; ++j)
11
12
          if (a[i] > a[j])
13
            ++counted;
14
       result = result + counted * factory[PermSize - i - 1];
15
16
     return result;
   }
17
18
19
   bool h[13];
20
21
   void UnCantor(int x, int res[])
22
   {
23
     int i,j,l,t;
24
     for (i = 1; i \le 12; i++)
25
       h[i] = false;
26
     for (i = 1; i \le 12; i++)
```

```
{
27
28
        t = x / factory[12 - i];
        x = t * factory[12 - i];
29
        for (j = 1, l = 0; l \ll t; j++)
30
31
          if (!h[j])l++;
32
        h[j] = true;
33
34
        res[i - 1] = j;
35
     }
36 | }
        FFT
   3.5
   const double PI= acos(-1.0);
 2
   struct vir
 3
   {
 4
     double re,im; //实部和虚部
 5
     vir(double a=0,double b=0)
 6
 7
        re=a;
 8
        im=b;
 9
10
     vir operator +(const vir &b)
11
     {return vir(re+b.re,im+b.im);}
12
     vir operator –(const vir &b)
13
     {return vir(re-b.re, im-b.im);}
     vir operator *(const vir &b)
14
15
     {return vir(re*b.re-im*b.im , re*b.im+im*b.re);}
   };
16
17
   vir x1[200005],x2[200005];
   void change(vir *x,int len,int loglen)
19
   {
20
     int i,j,k,t;
21
     for(i=0;i<len;i++)</pre>
22
     {
23
        t=i:
24
        for(j=k=0; j<loglen; j++,t>>=1)
25
          k = (k << 1) | (t & 1);
26
        if(k<i)
27
            printf("%d %d\n",k,i);
28
29
          vir wt=x[k];
30
          x[k]=x[i];
31
          x[i]=wt;
32
        }
     }
33
34
35
   void fft(vir *x,int len,int loglen)
36
   {
37
     int i,j,t,s,e;
38
     change(x,len,loglen);
39
     t=1;
```

```
40
      for(i=0;i<loglen;i++,t<<=1)
41
      {
42
        s=0;
43
        e=s+t;
44
        while(s<len)</pre>
45
46
          vir a,b,wo(cos(PI/t),sin(PI/t)),wn(1,0);
47
           for(j=s;j<s+t;j++)
48
           {
49
             a=x[j];
50
             b=x[j+t]*wn;
51
             x[j]=a+b;
52
             x[j+t]=a-b;
53
             wn=wn*wo;
          }
54
55
           s=e+t;
56
           e=s+t;
57
        }
58
      }
   }
59
60
   void dit_fft(vir *x,int len,int loglen)
61
62
      int i,j,s,e,t=1<<loglen;</pre>
63
      for(i=0;i<loglen;i++)</pre>
64
      {
65
        t>>=1;
66
        s=0;
67
        e=s+t:
68
        while(s<len)</pre>
69
        {
70
          vir a,b,wn(1,0),wo(cos(PI/t),-sin(PI/t));
71
           for(j=s;j<s+t;j++)
72
           {
73
             a=x[j]+x[j+t];
74
             b=(x[j]-x[j+t])*wn;
75
             x[j]=a;
76
             x[j+t]=b;
77
             wn=wn*wo;
           }
78
79
           s=e+t;
80
           e=s+t;
        }
81
      }
82
83
      change(x,len,loglen);
84
      for(i=0;i<len;i++)</pre>
85
        x[i].re/=len;
86
   int main()
87
88
    {
89
      char a[100005],b[100005];
90
      int i,len1,len2,len,loglen;
```

```
91
       int t, over;
 92
       while(scanf("%s%s",a,b)!=E0F)
 93
 94
         len1=strlen(a)<<1;</pre>
 95
         len2=strlen(b)<<1;</pre>
         len=1;loglen=0;
 96
 97
         while(len<len1)</pre>
 98
         {
 99
           len<<=1;
                      loglen++;
         }
100
101
         while(len<len2)</pre>
102
103
           len<<=1; loglen++;</pre>
104
         }
         for(i=0;a[i];i++)
105
106
107
           x1[i].re=a[i]-'0';
108
           x1[i].im=0;
109
110
         for(;i<len;i++)</pre>
111
           x1[i].re=x1[i].im=0;
112
         for(i=0;b[i];i++)
113
           x2[i].re=b[i]-'0';
114
115
           x2[i].im=0;
116
         }
117
         for(;i<len;i++)</pre>
118
           x2[i].re=x2[i].im=0;
119
         fft(x1,len,loglen);
         fft(x2,len,loglen);
120
121
         for(i=0;i<len;i++)</pre>
122
           x1[i] = x1[i]*x2[i];
123
         dit_fft(x1,len,loglen);
124
         for(i=(len1+len2)/2-2, over=len=0; i>=0; i--)
125
         {
126
           t=(int)(x1[i].re+over+0.5);
127
           a[len++] = t%10;
128
           over = t/10;
129
         }
130
         while(over)
131
         {
132
           a[len++]=over%10;
133
           over=10;
         }
134
135
         for(len-;len>=0&&!a[len];len-);
136
           if(len<0)
137
           putchar('0');
138
           else
              for(;len>=0;len---)
139
140
                putchar(a[len]+'0');
141
         putchar('\n');
```

```
142
     }
143
      return 0;
144 |}
        爬山法计算器
    3.6
    注意灵活运用。
    双目运算符在 calc() 中,左结合单目运算符在 P() 中,右结合单目运算符在 calc\_exp 中。(但
    是还没遇到过。。)
  1 |#include <iostream>
  2 |#include <cstdio>
  3 |#include <cstring>
  4 | #include <algorithm>
  5 #include <string>
   using namespace std;
  6
  7
 8
    char s[100000];
    int n,cur;
 9
    const string OP = "+-*";
10
11
12
    char next_char()
13
    {
14
      if (cur >= n) return EOF;
15
      return s[cur];
    }
16
17
18 | int get_priority(char ch)
19
    {
20
      if (ch == '*') return 2;
21
      return 1;
    }
22
23
24
   int P();
25
26
    int calc(int a,char op,int b)
27
    {
28
      if (op == '+')
29
        return a+b;
 30
      if (op == '-')
 31
        return a-b;
      if (op == '*')
 32
 33
        return a*b;
    }
 34
 35
36
    int calc_exp(int p)
 37
 38
      int a = P();
      while ((OP.find(next_char()) != OP.npos) &&
39
40
        (get_priority(next_char()) >= p))
      {
41
42
        char op = next_char();
```

```
43
        cur++;
44
        a = calc(a,op,calc_exp(get_priority(op)+1));
45
46
      return a;
   }
47
48
49
   int totvar,m,var[26],varid[26];
50
51
   int P()
52
    {
53
      if (next_char() == '-')
54
55
        cur++;
56
        return -P();
57
      }
58
      else if (next_char() == '+')
59
60
        cur++;
61
        return P();
62
63
      else if (next_char() == '(')
64
65
        cur++;
66
        int res = calc_{exp}(0);
67
        cur++;
68
        return res;
69
      }
70
      else
71
      {
72
        cur++;
        return var[varid[s[cur-1]-'a']];
73
74
75
   }
76
77
   int id[26],minid;
78
79
   int main()
80
    {
81
      while (true)
82
83
        scanf("%d%d",&totvar,&var[0]);
84
        if (totvar == 0 && var[0] == 0)
                                             break;
85
        for (int i = 1; i < totvar; i++)
          scanf("%d",&var[i]);
86
        scanf("%d",&m);
scanf("%s",s);
87
88
89
        for (int i = 0; i < 26; i++)
90
          id[i] = -1;
91
        minid = 0;
92
        n = strlen(s);
93
        for (int i = 0; i < n; i++)
```

```
94
           if (s[i] >= 'a' \&\& s[i] <= 'z')
 95
 96
              if (id\lceil s\lceil i\rceil - 'a'\rceil == -1)
 97
              {
 98
                id[s[i]-'a'] = minid;
 99
                minid++;
100
101
              s[i] = 'a' + id[s[i] - 'a'];
           }
102
         for (int i = 0; i < totvar; i++)
103
104
           varid[i] = i;
105
         int res = 0;
106
         do
107
         {
108
           cur = 0;
109
           int tmp = calc_exp(0);
110
           if (tmp == m)
111
           {
112
              res++;
113
              break;
           }
114
115
116
         while (next_permutation(varid, varid+totvar));
117
         //puts(s);
118
         if (res > 0)
119
           puts("YES");
120
         else
121
           puts("N0");
122
       }
123
       return 0;
124 |}
          线性筛
    3.7
    |int N;
    bool isPrime[10001];
    int prime[10000];
    void getPrime(int n)
  5
    {
  6
       memset(isPrime,1,++n);
  7
       N=0;
  8
       isPrime[0]=isPrime[1]=0;
  9
       for (int i=2;i<n;i++)
 10
       {
 11
         if (isPrime[i])
 12
           prime[N++]=i;
 13
         for (int j=0; j<N && prime[j]*i<n; j++)
 14
 15
           isPrime[i*prime[j]]=0;
 16
           if (i%prime[j]==0)
 17
              break;
```

```
18
        }
19
      }
20 }
         线性规划
   3.8
   |#define MAXM 20 //max num of basic varibles
   #define INF 1E200
   double A[MAXM+5][MAXN+MAXM+5];
   double b[MAXM+5],c[MAXN+MAXM+5];
   int N[MAXN+5],B[MAXM+5];
 7
   double X[MAXN+MAXM+5],V;
   int n,m,R,C,nCnt,bCnt;
 9
   int v1\lceil MAXN\rceil, v2\lceil MAXN\rceil;
10
11
   int fcmp(double a,double b)
12
   {
13
      if(fabs(a–b)<1E-7) return 0;
14
      if(a>b) return 1;
15
      return -1;
   }
16
17
18
   void Pivot(int l,int e)
19
   {
20
      double t=A[l][e], p=c[e];
21
      b[l]=b[l]/t;
22
      for(int i=1;i<=C;i++)
23
        A[l][i]/=t;
24
      V=V-c[e]*b[l];
25
      for(int i=1;i<=R;i++)
26
      {
27
        if(i==1||fcmp(A[i][e],0.0)==0)
28
          continue;
29
        t=A[i][e];
30
        b\Gamma i = b\Gamma i - t \cdot b\Gamma i;
31
        for(int j=1;j<=C;j++)
32
          A[i][j]=A[i][j]-t*A[l][j];
33
34
      for(int i=1;i<=C;i++)
35
        c[i]=c[i]-p*A[l][i];
36
      for(int i=1;i<=nCnt;i++)</pre>
37
      {
38
        if(N[i]==e)
39
        {
40
          N[i]=B[l];
41
          break;
42
        }
43
44
      B[1]=e;
45
   }
46
```

```
47
   |bool Process(double P[])
48
   {
49
     while(true)
50
      {
51
        int e=-1;
52
        double mV=-INF;
        for(int i=1;i<=nCnt;i++)</pre>
53
54
          if(fcmp(P[N[i]], mV)==1)
55
            mV=P[N[i]],e=N[i];
56
57
        if(fcmp(mV, 0.0)<=0) break;
58
        int l=-1;
59
        mV=INF;
60
        for(int i=1;i<=bCnt;i++)</pre>
61
62
          if(fcmp(A[i][e], 0.0) == 1)
63
64
            double t=b[i]/A[i][e];
65
            if(fcmp(mV,t)==1||(fcmp(mV,t)==0\&\&(l==-1||B[l]>B[i])))
66
              mV=t,l=i;
          }
67
        }
68
69
        if(l==-1) return false;
70
        Pivot(l,e);
71
72
      return true;
   }
73
74
75
   bool initSimplex()
76
   {
77
      nCnt=bCnt=0;
78
      for(int i=1;i<=n;i++)
79
        N[++nCnt]=i;
80
      for(int i=1;i<=m;i++)
81
        B[++bCnt]=i+n,A[i][n+i]=1.0;
82
      R=bCnt, C=bCnt+nCnt;
83
      double minV=INF;
84
      int p=-1;
85
      for(int i=1;i<=m;i++)
86
        if(fcmp(minV,b[i])==1)
87
          minV=b[i],p=i;
      if(fcmp(minV, 0.0) >= 0)
88
89
        return true;
90
      N[++nCnt]=n+m+1;R++,C++;
91
      for(int i=0;i<=C;i++)
92
        A[R][i]=0.0;
93
      for(int i=1;i<=R;i++)
        A[i][n+m+1]=-1.0;
94
95
      Pivot(p,n+m+1);
96
      if(!Process(A[R])) return false;
97
      if(fcmp(b[R],0.0)!=0)
```

```
98
         return false;
 99
       p = -1;
100
       for(int i=1;i<=bCnt&&p==-1;i++)
101
         if(B[i]==n+m+1) p=i;
       if(p!=-1)
102
103
       {
104
         for(int i=1;i<=nCnt;i++)</pre>
105
           if(fcmp(A[p][N[i]],0.0)!=0)
106
107
            {
108
              Pivot(p,N[i]);
109
              break;
110
           }
         }
111
       }
112
       bool f=false;
113
       for(int i=1;i<=nCnt;i++)</pre>
114
115
       {
116
         if(N[i]==n+m+1) f=true;
117
         if(f&&i+1 \le nCnt)
           N[i]=N[i+1];
118
119
       }
120
       nCnt--;
121
       R---, C---;
122
       return true;
    }
123
124
125
    //-1: no solution 1: no bound 0: has a solution -V
126
    int Simplex()
127
     {
128
       if(!initSimplex())
129
         return -1;
130
       if(!Process(c))
131
         return 1;
132
       for(int i=1;i<=nCnt;i++)</pre>
133
         X[N[i]]=0.0;
134
       for(int i=1;i<=bCnt;i++)</pre>
135
         X[B[i]]=b[i];
136
       return 0;
    }
137
138
139
     int main()
140
     {
141
       //n = 1; m=1;
142
       //V = 0.0;
143
       //c[1] = 1.0;
144
       //A\Gamma1\Gamma\Gamma1 = 1.0;
145
       //b[1] = 5.0;
       //Simplex();
146
       //printf("V = %.3f\n",V);
147
148
```

```
149
      while(scanf("%d", &v1[1]) == 1)
150
         {
151
           for(int i = 2; i <= 6; i ++)
152
             scanf("%d",&v1[i]);
           n = 4; m = 6;
153
154
           for(int i = 0; i <= m+1; i++)
             for(int j=0; j<=n+m+2; j++)
155
156
               A[i][j] = c[j] = 0;
157
           memset(b,0,sizeof(b));
158
           V = 0.0;
           /*
159
160
           n 为未知数个数
161
           m 为约束个数
162
           目标: siama(c[i]*xi)
           约束: sigma(A[i][j]*xj) <=b[i]; j = 1 ... n
163
164
           解存在 X 里面
           */
165
           b[1] = v1[1]; A[1][1] = 1; A[1][4] = 1;
166
           b[2] = v1[2]; A[2][1] = 1; A[2][3] = 1;
167
168
           b[3] = v1[3]; A[3][3] = 1; A[3][4] = 1;
                         ; A[4][2] = 1; A[4][3] = 1;
169
           b\lceil 4 \rceil = v1\lceil 4 \rceil
           b[5] = v1[5]; A[5][2] = 1; A[5][4] = 1;
170
           b[6] = v1[6]; A[6][1] = 1; A[6][2] = 1;
171
172
           c[1] = 1; c[2] = 1; c[3] = 1; c[4] = 1;
173
           Simplex();
174
           //printf("V = \%.3f\n",V);
175
           printf("%.3f_{\perp}%.3f_{\perp}%.3f_{\perp}%.3f_{\perp}%.3f_{\parallel},X[1],X[2],X[3],X[4]);
176
         }
177
178
       return 0;
179 |}
          分解质因数
    3.9
    3.9.1 米勒拉宾 + 分解因数
  1 |#include<ctime>
    #include<iostream>
    #define bint long long
    using namespace std;
    const int TIME = 8;//测试次数,够了8~10
    int factor [100], fac_top = -1;
  7
  8
    //计算两个数的acd
  9
    bint acd(bint small,bint bia)
 10
    {
 11
      while(small)
 12
       {
 13
         swap(small,big);
 14
         small%=big;
 15
 16
       return abs(big);
```

```
17 |}
18
19
   //ret = (a*b)%n (n<2^62)
   bint muti_mod(bint a,bint b,bint n)
21
22
      bint exp = a\%n, res = 0;
23
      while(b)
24
      {
25
        if(b&1)
26
        {
27
          res += exp;
28
          if(res>n) res -= n;
29
        }
30
        exp <<= 1;
31
        if (exp>n) exp = n;
32
        b >> = 1;
33
34
      return res;
35
   }
36
37
   // \text{ ret = (a^b)} %n
38
   bint mod_exp(bint a,bint p,bint m)
39
40
      bint exp=a%m, res=1; //
41
      while(p>1)
42
      {
43
        if(p&1)
44
          res=muti_mod(res,exp,m);
45
        exp = muti_mod(exp,exp,m);
46
        p>>=1;
47
48
      return muti_mod(res,exp,m);
49
   }
50
51
   //miller-法测试素数rabin, time 测试次数
52
   bool miller_rabin(bint n, int times)
53
   {
54
      if(n==2) return 1;
55
      if(n<2||!(n&1))return 0;
      bint a, u=n-1, x, y;
56
57
      int t=0;
      while(u%2==0)
58
59
      {
60
        t++;
61
        u/=2;
62
63
      srand(time(0));
64
      for(int i=0; i<times; i++)</pre>
65
66
        a = rand() \% (n-1) + 1;
67
        x = mod_{exp}(a, u, n);
```

```
68
        for(int j=0; j<t; j++)
 69
 70
          y = muti_mod(x, x, n);
 71
           if (y == 1 \&\& x != 1 \&\& x != n-1)
 72
             return false; //must not
 73
          x = y;
 74
 75
        if( y!=1) return false;
 76
 77
      return true;
    }
 78
 79
 80
    |bint pollard_rho(bint n,int c)//找出一个因子
 81
 82
      bint x,y,d,i = 1,k = 2;
 83
      srand(time(0));
 84
      x = rand()%(n-1)+1;
      y = x;
 85
      while(true)
 86
 87
      {
 88
        i++;
 89
        x = (muti\_mod(x,x,n) + c) \% n;
        d = gcd(y-x, n);
90
 91
        if (1 < d \&\& d < n) return d;
 92
        if( y == x) return n;
 93
        if(i == k)
 94
        {
 95
          y = x;
 96
           k <<= 1;
 97
        }
 98
    }
 99
100
101
    void findFactor(bint n,int k)//二分找出所有质因子,存入factor
102
    {
103
      if(n==1)return;
      if(miller_rabin(n, TIME))
104
105
106
        factor[++fac_top] = n;
107
        return;
108
      }
109
      bint p = n;
110
      while(p >= n)
111
        p = pollard_rho(p,k--);//值变化,防止死循环k
112
      findFactor(p,k);
113
      findFactor(n/p,k);
114
    }
115
116
    int main()
117
    {
118
      bint cs,n,min;
```

```
119
       cin>>cs;
120
       while (cs—)
121
122
         cin>>n;
123
         fac_{top} = min = -1;
124
         if(miller_rabin(n,TIME)) cout<<"Prime"<<endl;</pre>
125
         else
126
         {
127
           findFactor(n,107);
128
           for(int i=0; i<=fac_top; i++)</pre>
129
130
              if(min<0||factor[i]<min)</pre>
131
                min = factor[i];
132
133
           cout<<min<<endl;</pre>
         }
134
135
136
       return 0;
137
    }
    3.9.2 暴力版本
  1
    |int N;
    int num[30],fac[30];
    void getFactor(int x)
  4
    {
  5
       N=0;
  6
       memset(num,0,sizeof(num));
  7
       for (int i=0; prime[i]*prime[i]<=x && i<L; i++)</pre>
  8
  9
         if (x%prime[i]==0)
 10
         {
 11
           while (x%prime[i]==0)
 12
           {
 13
             x/=prime[i];
 14
             num[N]++;
 15
 16
           fac[N++]=prime[i];
         }
 17
 18
       }
      if (x>1)
 19
 20
 21
         num[N]=1;
 22
         fac[N++]=x;
 23
 24 | }
           baby step giant step
    3.10
    3.10.1 BSGS
  1 | #define MOD 76543
    int hs[MOD], head[MOD], next[MOD], id[MOD], top;
```

```
void insert(int x, int y)
   {
 5
     int k = x\%MOD;
 6
     hs[top] = x, id[top] = y, next[top] = head[k], head[k] = top++;
8
   int find(int x)
9
   {
10
     int k = x\%MOD;
     for (int i = head[k]; i; i = next[i]) if (hs[i] == x)
11
12
       return id[i];
13
     return -1;
14
15
   int BSGS(int a, int b, int n)
16
17
     memset(head, 0, sizeof(head));
18
     top = 1;
19
     if (b==1) return 0;
20
     int m = sqrt(n+.0), j;
21
     long long x = 1, p = 1;
22
     for (int i = 0; i < m; ++i, p = p*a%n) insert(p*b%n, i);
23
     for (long long i = m; i += m)
24
     {
25
       if ((j = find(x=x*p%n)) != -1) return i-j;
26
       if (i > n) break;
27
28
     return -1;
29 }
   3.10.2 何老师的版
1 //离散对数
   #include <cstdio>
   |#include <cstring>
4 |#include <cmath>
 5
   |#include <algorithm>
   using namespace std;
   typedef long long LL;
8
   struct Hash
9
   {
10
       static const int MOD = 100007;
11
       static const int MaxN = 100005;
12
       struct Node
13
14
           LL k, v;//A^k = v
           Node *nxt;
15
16
       } buf[MaxN], *g[MaxN], *pt;
17
       void init()
18
       {
19
           memset(g,0,sizeof(g));
20
           pt = buf;
21
22
       LL find(LL v)
```

```
{
23
24
            for (Node *now = g[v\%MOD]; now; now = now->nxt)
25
                if (now->v == v)
26
                     return now->k;
27
            return -1;
28
        }
29
        void Ins(LL k, LL v)
30
            if ( find (v) !=-1)return;
31
32
            pt->k = k;
33
            pt->v = v;
34
            pt->nxt = g[v \% MOD];
35
            a[v \% MOD] = pt++;
36
37
   }hash;
38
   LL gcd(LL x, LL y)
39
40
        return y==0?x:gcd(y,x%y);
41
42
   LL e_gcd(LL a, LL b, LL &x, LL &y)
43
   {
44
        if (b==0)
45
        {
            x = 1;
46
47
            y = 0;
48
            return a;
49
        }
50
        LL ret = e_gcd(b, a\%b, y, x);
51
        y = y - a/b*x;
52
        return ret ;
53
   LL Baby(LL A, LL B, LL C)//A^x = B (mod C)
54
55
   {
56
        B %= C;
57
        A %= C;
58
        LL x = 1\%C, y;
        for (int i = 0; i <= 64; i++)
59
60
        {
61
            if (x==B)return i;
62
            x = x*A \% C;
63
        }
64
65
        LL D = 1\%C, g;
66
        int cnt = 0;
67
        while((g = gcd(A,C)) != 1)
68
        {
69
            if (B%q) return -1;
70
            cnt++;
            C /= g;
71
72
            B /= g;
73
            D = A/q * D % C;
```

```
74
         }
 75
         hash. init ();
 76
         int m = (int) sqrt(C);
 77
         LL Am = 1\%C;
 78
         hash.Ins(0,Am);
 79
         for (int i = 1; i <= m; i++)
 80
         {
 81
              Am = Am*A \% C;
              hash. Ins (i,Am);
 82
 83
         for (int i = 0; i <= m; i++)
 84
 85
 86
         //D*x = B \pmod{C}, D*x + C*y = B
              g = e_gcd(D,C,x,y);
 87
 88
              x = (x*B/g%C+C)%C;
 89
              LL k = hash.find(x)
              if (k != -1) return i*m+k+cnt;
 90
 91
              D = D*Am \% C;
 92
         }
 93
         return -1;
 94
 95
    int main()
96
     {
 97
         int A,B,C;
 98
         while(scanf("%d%d%d",&A,&C,&B) == 3 \& (A+B+C))
99
              if (B>=C)
100
101
              {
                  puts("Orz,I<sub>□</sub>' cant<sub>□</sub>find<sub>□</sub>D!");
102
103
                  continue;
104
105
              LL ret = Baby(A,B,C);
              if ( ret == -1)puts("0rz,I_{\square}' cant_{\square}find_{\square}D!");
106
              else printf ("%I64d\n",ret);
107
108
109
         return 0;
110 |}
           原根
    3.11
    |int getPriRoot(int p)
  1
  2
    {
  3
       if (p==2) return 1;
  4
       int phi = p - 1;
  5
       getFactor(phi);
       for (int g = 2; g < p; ++g)
  6
  7
  8
         bool flag=1;
  9
         for (int i = 0; flag && i < N; ++i)
            if (power(g, phi/fac[i], p) == 1)
 10
              flag=0;
 11
 12
         if (flag)
```

```
13
          return g;
14
     }
15 }
         逆元
   3.12
  |void getInv2(int x)
 2
   {
 3
     inv[1]=1;
 4
     for (int i=2; i<=x; i++)
       inv[i]=(mod-(mod/i)*inv[mod%i]%mod)%mod;
 7
   int getInv(int x)//为素数mod
 8
 9
     return power(x,mod-2);
   }
10
   3.13 卢卡斯
   卢卡斯,num[i] 阶乘也
   int comLucus(int n,int m,int p)
 2
   {
 3
     int ans=1;
 4
     for (; n && m && ans; n/=p,m/=p)
 5
 6
       if (n\%p > = m\%p)
         ans = ans*num[n%p]%p*getInv(num[m%p]%p)%p
 7
 8
            *getInv(num[n%p-m%p])%p;
 9
       else
10
         ans=0;
11
     }
12
     return ans;
13 |}
         欧拉函数
   3.14
   3.14.1 分解质因数
   |int getEuler(int x)
 2
   {
 3
     getFactor(x);
 4
     int ret=x;
 5
     for (int i=0; i<N; i++)
 6
       ret = ret/fac[i]*(fac[i]-1);
 7
     return ret;
 8 | }
   3.14.2 一次预处理
 1 |void getEuler2()
 2
     memset(euler,0,sizeof(euler));
 3
     euler[1] = 1;
```

```
5
      for (int i = 2; i \le 3000000; i++)
 6
 7
        if (!euler[i])
 8
        {
          for (int j = i; j \le 3000000; j += i)
 9
10
          {
11
             if (!euler[j])
12
               euler[j] = j;
13
            euler[j] = euler[j]/i*(i-1);
14
15
        }
16
      }
   }
17
          费马降阶法
   3.15
   分解素数 p 为 x^2+y^2 的费马降阶法,失败返回 -1,主程序调用 \operatorname{calcu}(\mathbf{p},\mathbf{x},\mathbf{y})
 1 |#include <stdio.h>
   #include <string.h>
   #include <stdlib.h>
   int p,expp,A,B,aa,ans,tt;
   long long M;
   long long exp(int a,int b,long long mod)
 7
    {
 8
       long long ans=1, num=a;
 9
       while (b!=0)
10
       {
11
           if (b&1)
12
           {
13
                ans=((ans%mod)*(num%mod))%mod;
14
15
           num=((num%mod)*(num%mod))%mod;
16
           b >> = 1;
17
       }
18
       return ans;
19
20
   int calcu(int p,int &x,int &y)
21
   {
22
          if (p\%4!=1) return -1;
23
          else
24
          {
25
            expp=(p-1)/4;
26
            A,B;
27
            while (1)
28
29
               aa=rand()%p;
30
               if (aa==0) continue;
31
               A=\exp(aa, \exp p, p);
32
               ans=(((long long)A%p)*((long long)A%p))%p;
33
               if (ans==p-1) break;
34
35
            B=1;
```

```
36
           M=((long long)A*(long long)A+(long long)B*(long long)B)/p;
37
            if (M!=1) B=p;
38
           while (M!=1)
39
            {
40
              if (B>A)
41
              {tt=A; A=B; B=tt;}
42
              tt=A;
43
              A=B;
44
              B=tt%B;
45
             M=((long long)A*(long long)A
46
                +(long long)B*(long long)B)/p;
47
48
            if (B \le A)
            {
49
50
                 x=B;
51
                 y=A;
52
            }
53
            else
54
55
            x=A;
56
            y=B;
57
         }
58
59
60
   int main()
61
   {
62
     while (scanf("%d",&p)!=EOF)
63
     {
64
         int x,y;
65
         if (calcu(p,x,y)!=-1)
66
67
     return 0;
   }
68
          自适应 simp
   3.16
   过了哈尔滨积分题,精度要求不高的时候可以考虑使用。
   暂时我只能用这个做做类似于凸函数或者凹函数的函数。
   double Simp(double l,double r)
 2
   {
 3
     double h = (r-1)/2.0;
 4
     return h*(calc(l)+4*calc((l+r)/2.0)+calc(r))/3.0;
   }
 5
 6
 7
   double rSimp(double l,double r)
 8
 9
     double mid = (1+r)/2.0;
10
     if (abs((Simp(l,r)-Simp(l,mid)-Simp(mid,r)))/15 < eps)
11
       return Simp(l,r);
12
     else
13
       return rSimp(l,mid)+rSimp(mid,r);
```

14 |}

3.17 组合数求模

```
模是质数
 1 |#include<cstdio>
 2 #include<cstring>
   #include<iostream>
   using namespace std;
 5
   int mod;
   long long num[100000];
 7
   int ni[100],mi[100];
 8
   int len;
 9
   void init(int p)
10
   {
11
     mod=p;
12
     num[0]=1;
13
     for (int i=1; i<p; i++)
14
        num[i]=i*num[i-1]%p;
15
16
   void get(int n,int ni[],int p)
17
18
     for (int i = 0; i < 100; i++)
19
        ni[i] = 0;
20
     int tlen = 0;
21
     while (n != 0)
22
     {
23
        ni[tlen++] = n%p;
24
        n \neq p;
25
26
     len = tlen;
27
28
   long long power(long long x,long long y)
29
   {
30
     long long ret=1;
31
     for (long long a=x \mod; y; y>>=1, a=a*a \mod)
        if (y&1)
32
33
          ret=ret*a%mod;
34
     return ret;
35
36
   long long getInv(long long x)//mod 为素数
37
38
     return power(x,mod-2);
39
40
   long long calc(int n,int m,int p)//C(n,m)%p
41
42
     init(p);
43
     long long ans=1;
44
     for (; n && m && ans; n/=p,m/=p)
45
     {
46
        if (n\%p > = m\%p)
```

```
47
          ans = ans*num[n%p]%p*getInv(num[m%p]%p)%p
48
            *getInv(num[n%p-m%p])%p;
49
        else
50
          ans=0;
51
      }
52
      return ans;
53
54
   int main()
55
   {
56
      int t;
57
      scanf("%d",&t);
58
     while (t—)
59
      {
60
        int n,m,p;
61
        scanf("%d%d%d",&n,&m,&p);
        printf("%I64d\n",calc(n+m,m,p));
62
63
64
      return 0;
65 |}
          高斯消元
   3.18
   |const double eps = 1e-8;
 2
 3
   void Guess(int n)
 4
   {
 5
      for (int i = 0; i < n; i++)
 6
      {
 7
        for (int j = i; j < n; j++)
 8
          if (fabs(a[j][i]) > eps)
 9
          {
            for (int k = i; k \le n; k++)
10
11
              swap(a[i][k],a[j][k]);
12
            break;
13
          }
14
15
        if (fabs(a[i][i]) < eps) continue;</pre>
16
        for (int j = 0; j < n; j++)
17
          if (i != j && fabs(a[j][i]) > eps)
18
19
          {
20
            double det = a[j][i]/a[i][i];
21
            for (int k = i; k \le n; k++)
22
              a[j][k] = a[i][k]*det;
23
          }
24
      }
25
26
      for (int i = 0; i < n; i++)
27
28
        if (fabs(a[i][i]) < eps)
29
        {
```

```
if (fabs(a[i][n]) > eps)
30
31
          {
32
            //无解
33
            puts("Fuck");
34
          }
35
          //否则 x_i 可以是任意解
        }
36
37
        else
38
        {
39
          a[i][n] /= a[i][i];
40
          if (fabs(a[i][n]) < eps)
            a[i][n] = 0;
41
        }
42
43
44
45 |}
   3.19
          整数拆分
 1 |#include <cstdio>
   #include <cmath>
   #include <cstring>
   #include <map>
   #include <algorithm>
   using namespace std;
   bool check(int x)
 8
   {
 9
      for (int i=2; i*i <= x; i++)
        if (x\%i==0)
10
11
          return 0;
12
      return 1;
   }
13
14
   int p[100000];
15
   inline int calc(int x)
16
   {
17
      return x*(x*3-1)/2;
18
19
   int main()
20
   {
     p[0]=1;
21
     for (int i=1; i<100000; i++)
22
23
24
        for (int j=1, k=1; calc(j) <= i; j++, k*=-1)
25
26
          p[i]+=k*p[i-calc(j)];
27
          if (p[i]<0)
28
            p[i]+=1000000;
29
          if (p[i] > = 1000000)
30
            p[i]-=1000000;
31
          if (calc(-j) <= i)
            p[i]+=k*p[i-calc(-j)];
32
33
          if (p[i]<0)
```

```
34
            p[i]+=1000000;
35
          if (p[i] > = 1000000)
36
            p[i]-=1000000;
37
       }
38
       if (!p[i])
         printf("%d\n",i);
39
40
41
     return 0;
42 |}
   3.20
         佩尔方程
   写的不好稍微收一下
 1
   import java.math.BigInteger;
   import java.util.*;
   public class Main
 4
   {
 5
     public static class Fraction
 6
 7
       public BigInteger num,den;
 8
       public Fraction()
 9
         num=BigInteger.ZERO;
10
11
          den=BigInteger.ONE;
12
13
       public Fraction(int _num,int _den)
14
15
          num=BigInteger.valueOf(_num);
          den=BigInteger.valueOf(_den);
16
17
18
       public Fraction(BigInteger _num, BigInteger _den)
19
        {
20
         num=_num;
21
          den=_den;
22
       }
23
       public Fraction gen()
24
        {
25
          BigInteger g=num.gcd(den);
26
          return new Fraction(num.divide(g),den.divide(g));
27
       }
28
       public Fraction add(Fraction x)
29
30
          return new Fraction(x.num.multiply(den).add(num.multiply(x.
            den)),x.den.multiply(den)).gen();
31
       }
32
       public Fraction reciprocal()
33
34
          return new Fraction(den,num);
35
36
       public void out()
37
        {
38
          System.out.println(num+"/"+den);
```

```
}
39
40
41
     public static BigInteger sqrt(BigInteger a)
42
43
        BigInteger b=a;
44
            while (a.compareTo(b.multiply(b))<0)</pre>
45
              b=b.multiply(b).add(a).divide(b.multiply(BigInteger.
                 value0f(2));
46
            return b;
47
48
      public static boolean check(Fraction x,int n)
49
50
        return x.num.multiply(x.num).add(x.den.multiply(x.den.multiply()
           BigInteger.valueOf(n))).negate()).compareTo(BigInteger.ONE)
           ==0;
51
      }
      static int p[]=new int[1000];
52
53
      static int 1;
54
      public static void main(String∏ args)
55
        BigInteger ans=BigInteger.ZERO;
56
57
        int idx=0:
58
        for (int n=2, r=2; n<=1000; n++)
59
60
          if (n==r*r)
61
          {
62
            r++;
63
            continue;
64
65
          int tmp=calc(n,0,1), a=tmp, b=n-tmp*tmp;
66
          p[0]=tmp;
67
          l=1;
68
          while (true)
69
          {
70
            tmp=calc(n,a,b);
71
            p[l++]=tmp;
72
            a=a-tmp*b;
73
            Fraction x=getFrac();
            if (check(x,n))
74
75
76
              if (ans.compareTo(x.num)<0)</pre>
77
78
                 ans=x.num;
79
                 idx=n;
80
81
              break;
82
            }
83
            a=-a;
84
            b=(n-a*a)/b;
85
          }
86
        }
```

```
87
        System.out.println(idx);
 88
      private static Fraction getFrac() {
 89
        Fraction ret=new Fraction(p[l-1],1);
 90
 91
        for (int i=l-2; i>=0; i---)
           ret=new Fraction(p[i],1).add(ret.reciprocal());
 92
 93
        return ret;
 94
 95
      private static int calc(int n, int a, int b) {
        for (long i=2;;i++)
 96
           if ((i*b-a)*(i*b-a)>n)
 97
 98
             return (int)i-1;
 99
      }
    }
100
```

3.21 其它公式

3.21.1 Polya

设 $G \neq p$ 个对象的一个置换群,用 k 种颜色去染这 p 个对象,若一种染色方案在群 G 的作用下变为另一种方案,则这两个方案当作是同一种方案,这样的不同染色方案数为:

$$L = \frac{1}{|G|} \times \Sigma(k^{C(f)}), f \in G$$

 $C(f)$ 为循环节, $|G|$ 表示群的置换方法数

对于有 n 个位置的手镯, 有 n 种旋转置换和 n 种翻转置换

对于旋转置换:

$$C(f_i) = \gcd(n,i)$$
 , i 表示一次转过 i 颗宝石, $i = 0$ 时 $c = n$;

对于翻转置换:

如果 n 为偶数: 则有 $\frac{n}{2}$ 个置换 $C(f) = \frac{n}{2}$,有 $\frac{n}{2}$ 个置换 $C(f) = \frac{n}{2} + 1$

如果 n 为奇数: $C(f) = \frac{n}{2} + 1$

3.21.2 拉格朗日插值法

已知 $y = a_0 + a_1 x + a_2 x^2 + \cdots + a_{n-1} x^{n-1}$ 曲线上的 n 个点 $(x_1, y_1), (x_2, y_2), (x_3, y_3) \cdots (x_n, y_n)$ 用拉格朗日插值法可以不求系数可知任意 x 对应的 y 值。

$$y = y_1 \frac{(x - x_2)(x - x_3) \cdots (x - x_n)}{(x_1 - x_2)(x_1 - x_3) \cdots (x_1 - x_n)}$$

$$+ y_2 \frac{(x - x_1)(x - x_3) \cdots (x - x_n)}{(x_2 - x_1)(x_2 - x_3) \cdots (x_2 - x_n)}$$

$$+ \cdots$$

$$+ y_n \frac{(x - x_1)(x - x_2) \cdots (x - x_{n-1})}{(x_n - x_1)(x_n - x_2) \cdots (x_n - x_{n-1})}$$

特别的,如果 $x_1 \sim x_n$ 为连续自然数,那么对于下一个自然数对应的 y 值为:

$$y_{n+1} = (-1)^{n-1}C_n^0y_1 + (-1)^{n-2}C_n^1y_2 + \dots + (-1)^0C_n^{n-1}y_n$$

这个组合系数可以通过高斯消元暴出来,前提是要猜到它满足递推关系。

3.21.3 正多面体顶点着色

正四面体:
$$N=\frac{(n^4+11\times n^2)}{12}$$
 正六面体: $N=\frac{(n^8+17\times n^4+6\times n^2)}{24}$ 正八面体: $N=\frac{(n^6+3\times n^4+12\times n^3+8\times n^2)}{24}$ 正十二面体: $N=\frac{(n^{20}+15\times n^{10}+20\times n^8+24\times n^4)}{60}$ 正二十面体: $N=\frac{(n^{12}+15\times n^6+44\times n^4)}{60}$

3.21.4 求和公式

$$\begin{array}{l} \sum k = \frac{n \times (n+1)}{2} \\ \sum 2k - 1 = n^2 \\ \sum k^2 = \frac{n \times (n+1) \times (2n+1)}{6} \\ \sum (2k-1)^2 = \frac{n \times (4n^2-1)}{3} \\ \sum k^3 = (\frac{n \times (n+1)}{2})^2 \\ \sum (2k-1)^3 = n^2 \times (2n^2-1) \\ \sum k^4 = \frac{n \times (n+1) \times (2n+1) \times (3n^2+3n-1)}{30} \\ \sum k^5 = \frac{n^2 \times (n+1)^2 \times (2n^2+2n-1)}{12} \\ \sum k \times (k+1) = \frac{n \times (n+1) \times (n+2)}{3} \\ \sum k \times (k+1) \times (k+2) = \frac{n \times (n+1) \times (n+2) \times (n+3)}{4} \\ \sum k \times (k+1) \times (k+2) \times (k+3) = \frac{n \times (n+1) \times (n+2) \times (n+3)}{5} \end{array}$$

3.21.5 几何公式

球扇形:

全面积: $T = \pi r (2h + r_0)$, h 为球冠高, r_0 为球冠底面半径体积: $V = \frac{2\pi r^2 h}{3}$

3.21.6 小公式

Pick 公式: $A = E \times 0.5 + I - 1$ (A 是多边形面积, E 是边界上的整点, I 是多边形内部的整点)海伦公式: $S = \sqrt{p(p-a)(p-b)(p-c)}$,其中 $p = \frac{(a+b+c)}{2}$,abc 为三角形的三条边长 求 $\binom{n}{k}$ 中素因子 P 的个数:

- 1. 把 n 转化为 P 进制,并记它每个位上的和为 S1
- 2. 把 n-k, k 做同样的处理, 得到 S2, S3

```
则 \binom{n}{k} 中素因子 P 的个数: \frac{S2+S3-S1}{P-1}
   部分错排公式:
   n+m 个数中 m 个数必须错排求排列数
 1 | dp[i] = n*dp[i-1]+(i-1)*(dp[i-1]+dp[i-2]);
   |dp[0] = n!;
 3 | dp[1] = n*n!;
   dp[m] 为所求解
   3.21.7 马步问题
   任意步长 (p,q) 无限棋盘可达性判定
 1 |bool check(int dx,int dy,int p,int q)
 2
   {
 3
     if (p < 0) p = -p;
     if (q < 0) q = -q;
     LL g = gcd(p,q);
     if (dx % g || dy % g) return false;
     dx /= g, dy /= g, p = (p / g) & 1, q = (q / g) & 1;
     return !(p == q \&\& ((dx \land dy) \& 1));
   }
 9
   拓展:
   若可选马步可以有 N 种 (p_i,q_i), 令 g=gcd(p_1,q_1,p_2,q_2\cdots p_N,q_N), 则不在 g 的整数倍点上
   的节点肯定不可达。 坐标除 2g,同时将可选马步除 g 之后放缩到 2 \times 2 之内,即 (\frac{p_i}{g} \mod 2, \frac{q_i}{g}
   mod 2)。若放缩后马步中有 (1,0) 或 (0,1), 则全放缩后全棋盘可达, 否则只可达偶点。
   (2,1) 马步无限棋盘最小距离
 1 | int dis(int dx,int dy)
 2
   {
 3
     if (dx < 0) dx = -dx;
 4
     if (dy < 0) dy = -dy;
     if (dx < dy) swap(dx,dy);
 5
 6
     if (dx & 1)
 7
 8
       if (dy \& 1) return dis(dx+1,dy-1);
       if (dx == 1 \&\& dy == 0) return 3;
 9
10
       return dis(dx+3,dy)-1;
11
     if (dy & 1)
12
13
14
       if (dx == 4 \&\& dy == 3) return 3;
15
       return dis(dx-2,dy-1)+1;
```

if (dx == 0 && dy == 0) return 0;

if (dx == 2 && dy == 2) return 4;

int c = (((dx-1) / 4)+1)*2;

if (dx & 2) dy = 2;

if (dy <= c) return c;

16 17

18

19

20

21

```
22 | dy -= c;
23 | return c+(dy-2) / 6*2+2;
24 |}
```

4 数据结构

4.1 *Splay

持续学习中。

注意节点的 size 值不一定是真实的值!如果有需要需要特别维护!

- 1. 旋转和 Splay 操作
- 2. rank 操作
- 3. insert 操作(。。很多题目都有)
- 4. del 操作(郁闷的出纳员)
- 5. 由数组建立 Splay
- 6. 前驱后继(营业额统计)
- 7. Pushdown Pushup 的位置
- 8. *。。。暂时想不起了

|const int MaxN = 50003;

4.1.1 节点定义

2

```
3
   struct Node
 4
   {
 5
      int size, key;
 6
 7
      Node *c[2];
 8
      Node *p;
 9 |} mem[MaxN], *cur, *nil;
    无内存池的几个初始化函数。
 1 | Node *newNode(int v, Node *p)
 2
 3
      cur\rightarrow c[0] = cur\rightarrow c[1] = nil, cur\rightarrow p = p;
 4
      cur->size = 1;
 5
      cur \rightarrow key = v;
 6
      return cur++;
   }
 7
 8
 9
   void Init()
10
11
      cur = mem;
12
      nil = newNode(0, cur);
13
      nil->size = 0;
14 |}
```

带内存池的几个函数。

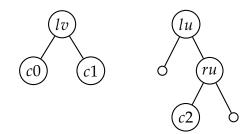
```
|int emp[MaxN], totemp;
 2
 3
   Node *newNode(int v, Node *p)
 4
    {
 5
      cur = mem + emp[--totemp];
 6
      cur\rightarrow c[0] = cur\rightarrow c[1] = nil, cur\rightarrow p = p;
 7
      cur->size = 1;
 8
      cur -> key = v;
 9
      return cur;
   }
10
11
12
   |void Init()
13
   {
14
      for (int i = 0; i < MaxN; ++i)
15
         emp[i] = i;
16
      totemp = MaxN;
17
      cur = mem + emp[--totemp];
18
      nil = newNode(0, cur);
19
      nil->size = 0;
20 }
21
22
   void Recycle(Node *p)
23
24
      if (p == nil) return;
25
      Recycle(p\rightarrow c[0]), Recycle(p\rightarrow c[1]);
26
      emp[totemp++] = p - mem;
27 }
    4.1.2 维护序列
    一切下标从①开始。
 1 | struct SplayTree
 2
    {
 3
      Node *root;
 4
      void Init()
 5
      {
 6
         root = nil;
 7
 8
      void Pushup(Node *x)
 9
10
         if (x == nil)
                            return;
         Pushdown(x); Pushdown(x\rightarrowc[0]); Pushdown(x\rightarrowc[1]);
11
12
         x\rightarrow size = x\rightarrow c[0]\rightarrow size + x\rightarrow c[1]\rightarrow size + 1;
13
      }
14
      void Pushdown(Node *x)
15
16
         if (x == nil)
                            return;
17
         //do something
18
19
      void Rotate(Node *x, int f)
20
      {
```

```
21
        if (x == nil)
                           return;
22
        Node *y = x \rightarrow p;
        y -> c[f \land 1] = x -> c[f], x -> p = y -> p;
23
        if (\bar{x} \rightarrow c[f] != nil)
24
           x\rightarrow c[f]\rightarrow p = y;
25
26
        if (y->p != nil)
27
           y->p->c[y->p->c[1] == y] = x;
28
        x - c[f] = y, y - p = x;
29
        Pushup(y);
30
31
      void Splay(Node *x, Node *f)
32
33
        static Node *stack[maxn];
34
        int top = 0;
35
        stack[top++] = x;
        for (Node *y = x; y != f; y = y -> p)
36
37
           stack[top++] = y->p;
38
        while (top)
39
           Pushdown(stack[—top]);
40
41
        while (x->p != f)
42
        {
43
           Node *y = x \rightarrow p;
44
           if (y->p == f)
45
             Rotate(x, x == y -> c[0]);
46
           else
47
           {
48
             int fd = y-p-c[0] == y;
49
             if (y\rightarrow c[fd] == x)
50
                Rotate(x, fd ^1), Rotate(x, fd);
51
             else
                Rotate(y, fd), Rotate(x, fd);
52
           }
53
54
55
        Pushup(x);
        if (f == nil)
56
57
           root = x;
58
59
      void Select(int k, Node *f)
60
61
        Node *x = root;
62
        Pushdown(x);
63
        int tmp;
64
        while ((tmp = x->c[0]->size) != k)
65
           if (k < tmp) x = x -> c[0];
66
67
           else
68
             x = x - c[1], k - tmp + 1;
69
           Pushdown(x);
70
71
        Splay(x, f);
```

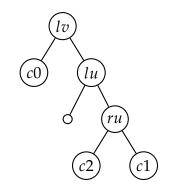
```
72
        }
 73
        void Select(int 1, int r)
 74
 75
          Select(l, nil), Select(r + 2, root);
 76
        Node *Make_tree(int a[], int l, int r, Node *p)
 77
 78
        {
 79
          if (l > r) return nil;
          int mid = l + r \gg 1;
 80
          Node *x = newNode(a[mid], p);
 81
 82
          x\rightarrow c[0] = Make\_tree(a, l, mid - 1, x);
 83
          x\rightarrow c[1] = Make\_tree(a, mid + 1, r, x);
 84
          Pushup(x);
 85
          return x;
 86
        }
 87
        void Insert(int pos, int a□, int n)
 88
 89
          Select(pos, nil), Select(pos + 1, root);
 90
          root \rightarrow c[1] \rightarrow c[0] = Make\_tree(a, 0, n - 1, root \rightarrow c[1]);
 91
          Splay(root \rightarrow c[1] \rightarrow c[0], nil);
 92
 93
        void Insert(int v)
 94
 95
          Node *x = root, *y = nil;
 96
          while (x != nil)
 97
           {
 98
             y = x;
 99
             v->size++;
100
             x = x \rightarrow c[v >= x \rightarrow key];
101
102
          y \rightarrow c[v >= y \rightarrow key] = x = newNode(v, y);
          Splay(x, nil);
103
104
        void Remove(int 1, int r)
105
106
        {
107
          Select(l, r);
          //Recycle(root->c[1]->c[0]);
108
109
          root \rightarrow c[1] \rightarrow c[0] = nil;
110
          Splay(root->c[1], nil);
        }
111
112 | };
     例题:旋转区间赋值求和求最大子序列。
     注意打上懒标记后立即 Pushup。Pushup(root-c[1]-c[0]),Pushup(root-c[1]),Pushup(root);
  1
        void Pushup(Node *x)
  2
  3
          if (x == nil) return;
          Pushdown(x); Pushdown(x\rightarrowc[0]); Pushdown(x\rightarrowc[1]);
  4
  5
          x\rightarrow size = x\rightarrow c[0]\rightarrow size+x\rightarrow c[1]\rightarrow size+1;
  6
  7
          x\rightarrow sum = x\rightarrow c[0]\rightarrow sum+x\rightarrow c[1]\rightarrow sum+x\rightarrow key;
```

```
8
           x\rightarrow lsum = max(x\rightarrow c[0]\rightarrow lsum,
 9
              x \rightarrow c[0] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow lsum));
10
           x \rightarrow rsum = max(x \rightarrow c[1] \rightarrow rsum,
11
              x \rightarrow c[1] - sum + x - key + max(0, x - c[0] - rsum));
           x\rightarrow \max = \max(\max(x\rightarrow c[0]-\max ,x\rightarrow c[1]-\max ),
12
13
              x \rightarrow key + max(0, x \rightarrow c[0] \rightarrow rsum) + max(0, x \rightarrow c[1] \rightarrow lsum));
14
15
        void Pushdown(Node *x)
16
17
           if (x == nil) return;
18
           if (x->rev)
19
           {
20
              x\rightarrow rev = 0;
              x\rightarrow c[0]->rev \land = 1;
21
              x\rightarrow c[1]\rightarrow rev ^= 1;
22
23
              swap(x->c[0],x->c[1]);
24
25
              swap(x->lsum,x->rsum);
           }
26
27
           if (x->same)
28
           {
29
              x\rightarrow same = false;
              x\rightarrow key = x\rightarrow lazy;
30
31
              x \rightarrow sum = x \rightarrow key*x \rightarrow size;
32
              x\rightarrow 1sum = x\rightarrow rsum = x\rightarrow maxsum = max(x\rightarrow key, x\rightarrow sum);
              x\rightarrow c[0]->same = true, x\rightarrow c[0]->lazy = x\rightarrow key;
33
34
              x\rightarrow c[1]-same = true, x\rightarrow c[1]-slazy = x\rightarrow key;
35
           }
        }
36
37
38
    int main()
39
     {
40
        int totcas;
41
        scanf("%d",&totcas);
42
        for (int cas = 1;cas <= totcas;cas++)</pre>
43
        {
44
           Init();
45
           sp.Init();
46
           nil->lsum = nil->rsum = nil->maxsum = -Inf;
47
           sp.Insert(0);
48
           sp.Insert(0);
49
50
           int n,m;
51
           scanf("%d%d",&n,&m);
52
           for (int i = 0; i < n; i++)
53
              scanf("%d",&a[i]);
54
           sp.Insert(0,a,n);
55
56
           for (int i = 0; i < m; i++)
57
           {
58
              int pos, tot, c;
```

```
59
            scanf("%s",buf);
            if (strcmp(buf, "MAKE-SAME") == 0)
 60
 61
 62
              scanf("%d%d%d",&pos,&tot,&c);
 63
              sp.Select(pos-1,pos+tot-2);
 64
              sp.root \rightarrow c[1] \rightarrow c[0] \rightarrow same = true;
              sp.root \rightarrow c[1] \rightarrow c[0] \rightarrow lazy = c;
 65
 66
              sp.Pushup(sp.root->c[1]), sp.Pushup(sp.root);
            }
 67
            else if (strcmp(buf, "INSERT") == 0)
 68
 69
              scanf("%d%d",&pos,&tot);
 70
 71
              for (int i = 0; i < tot; i++)
                scanf("%d",&a[i]);
 72
 73
              sp.Insert(pos,a,tot);
 74
            }
 75
            else if (strcmp(buf, "DELETE") == 0)
 76
            {
 77
              scanf("%d%d",&pos,&tot);
 78
              sp.Remove(pos-1,pos+tot-2);
 79
            }
            else if (strcmp(buf, "REVERSE") == 0)
 80
 81
              scanf("%d%d",&pos,&tot);
 82
 83
              sp.Select(pos-1,pos+tot-2);
 84
              sp.root \rightarrow c[1] \rightarrow c[0] \rightarrow rev \land = 1;
 85
              sp.Pushup(sp.root->c[1]), sp.Pushup(sp.root);
 86
            else if (strcmp(buf, "GET-SUM") == 0)
 87
 88
            {
 89
              scanf("%d%d",&pos,&tot);
 90
              sp.Select(pos-1,pos+tot-2);
 91
              printf("%d\n", sp.root->c[1]->c[0]->sum);
 92
 93
            else if (strcmp(buf, "MAX—SUM") == 0)
 94
 95
              sp.Select(0,sp.root->size-3);
 96
              printf("%d\n", sp.root->c[1]->c[0]->maxsum);
 97
         }
 98
 99
100
       return 0;
101
    |}
     4.1.3 维护括号序列
     不需要哨兵。
     合并操作:
     先转成下面的样子:
```

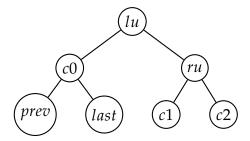


再链接成这样:

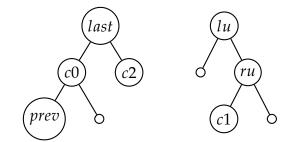


分离操作:

先把 lu 和 ru 转上去:



把 c0 和 c2 从原来的位置断开 然后接上:



```
1 #include <iostream>
2 #include <cstdio>
3 #include <cstring>
4 using namespace std;
5
6 const int maxn = 500000;
7 const int mod = 99990001;
8 struct Node
9 {
10 int size,key;
11
```

```
12
       int a,b;
13
       int minid, id;
14
15
      Node *c[2];
16
      Node *p;
    }mem[maxn],*cur,*nil;
17
    Node *l[maxn],*r[maxn];//左括号右括号定义在前面
18
19
20
    |int emp[maxn],totemp;
21
    Node *newNode(int v,Node *p)
22
23
       cur\rightarrow c[0] = cur\rightarrow c[1] = nil, cur\rightarrow p = p;
24
       cur->size = 1;
25
       cur \rightarrow key = v;
26
27
       cur->a=1;
28
       cur -> b = 0;
29
       cur->minid = cur->id = maxn;
30
31
       return cur++;
32
33
    void Init()
34
    {
35
      cur = mem;
36
       nil = newNode(0,cur);
37
       nil->size = 0;
    }
38
39
40
    struct SplayTree
41
    {
42
      Node *root;
43
      void Init()
44
       {
45
         root = nil;
46
47
      void Pushup(Node *x)
48
49
         if (x == nil) return;
         Pushdown(x);
50
51
         Pushdown(x \rightarrow c[0]);
52
         Pushdown(x \rightarrow c[1]);
53
         x\rightarrow size = x\rightarrow c[0]\rightarrow size+x\rightarrow c[1]\rightarrow size+1;
54
55
         x->minid = x->id;
56
         for (int i = 0; i < 2; i++)
57
           if (x->c[i] != nil)
58
              x \rightarrow minid = min(x \rightarrow minid, x \rightarrow c[i] \rightarrow minid);
59
      void Pushdown(Node *x)
60
61
       {
62
         if (x == nil) return;
```

```
63
 64
            x\rightarrow key = ((long long)x\rightarrow key*x\rightarrow a\%mod+x\rightarrow b)\%mod;
 65
            for (int i = 0; i < 2; i++)
              if (x\rightarrow c[i] != nil)
 66
 67
               {
 68
                 x\rightarrow c[i]\rightarrow a = (long long)x\rightarrow c[i]\rightarrow a*x\rightarrow a%mod;
 69
                 x \rightarrow c[i] \rightarrow b = ((long long)x \rightarrow c[i] \rightarrow b*x \rightarrow a\%mod+x \rightarrow b)\%mod;
 70
 71
            x\rightarrow a = 1;
 72
            x \rightarrow b = 0;
 73
 74
         void Rotate(Node *x,int f)
 75
         {
 76
            if (x == nil) return;
            Node *y = x \rightarrow p;
 77
           y \rightarrow c[f^1] = x \rightarrow c[f], x \rightarrow p = y \rightarrow p;
 78
 79
            if (x\rightarrow c[f] != nil)
 80
              x\rightarrow c[f]\rightarrow p = y;
 81
            if (y->p != nil)
 82
              y->p->c[y->p->c[1] == y] = x;
 83
            x\rightarrow c[f] = y, y\rightarrow p = x;
 84
            Pushup(y);
         }
 85
         void Splay(Node *x,Node *f)
 86
 87
 88
            static Node *stack[maxn];
 89
            int top = 0;
 90
            stack[top++] = x;
 91
            for (Node *y = x; y != f; y = y \rightarrow p)
 92
               stack[top++] = y->p;
 93
            while (top)
 94
              Pushdown(stack[—top]);
 95
 96
            while (x->p != f)
 97
            {
              Node *y = x \rightarrow p;
 98
 99
              if (y->p == f)
100
                 Rotate(x,x == y\rightarrowc[0]);
              else
101
102
               {
103
                 int fd = y-p-c[0] == y;
                 if (y\rightarrow c[fd] == x)
104
105
                    Rotate(x, fd^1), Rotate(x, fd);
106
                 else
107
                    Rotate(y,fd), Rotate(x,fd);
              }
108
109
110
            Pushup(x);
111
            if (f == nil)
112
              root = x;
113
         }
```

```
114
       Node *Last(Node *now)
115
       {
116
         Splay(now,nil);
         while (now->c[1] != nil)
117
           now = now \rightarrow c[1];
118
119
         return now;
120
       //把 u 接到 v 下面去,边权为 w
121
122
       //需要保证 u 是某棵树的根
123
       void Link(int u,int v,int w)
124
       {
125
         Splay(l[v],nil);
126
127
         Splay(l[u],nil);
128
         l[u]->key = w;
129
         Pushup(l[u]);
130
         Splay(r[u],l[u]);
131
132
         Node *c1 = l[v] \rightarrow c[1];
133
         l[v] -> c[1] = l[u];
134
         r[u] - c[1] = c1;
135
         l[u]->p = l[v];
         c1 \rightarrow p = r[u];
136
         Pushup(r[u]);
137
138
         Pushup(l[u]);
139
         Pushup(l[v]);
140
         Splay(l[u],nil);
141
       //把 u 为根的子树分离开
142
143
       int Split(int u)
144
145
         Splay(l[u],nil);
146
147
         int ret = l[u]->key;
148
         Splay(r[u],l[u]);
         Node *c0 = l[u] -> c[0], *c2 = r[u] -> c[1];
149
150
         l[u]->key = 0;//去掉边权
151
152
         l[u] \rightarrow c[0] = r[u] \rightarrow c[1] = c0 \rightarrow p = c2 \rightarrow p = nil;
153
         Pushup(r[u]);
154
         Pushup(l[u]);
155
         Node *last = Last(c0);
156
157
         Splay(last,nil);
158
         last \rightarrow c[1] = c2;
159
         c2 \rightarrow p = last;
160
         Pushup(last):
161
162
         //对拆分后的两部份进行处理
163
         Node *nu = last;
164
         Node *nv = l[u];
```

```
165
         if (nu->size > nv->size || (nu->size == nv->size && nu->minid >
             nv->minid))
           swap(nu,nv);
166
         nu->a = (long long)nu->a*ret%mod;
167
         nu->b = (long long)nu->b*ret%mod;
168
         nv \rightarrow b = (nv \rightarrow b + ret) \mod;
169
170
171
         return ret;//返回原边权
172
      }
    };
173
174
175
    SplayTree sp;
176
    int n;
177
    struct Edge
178
    {
179
      int to, next, w, id;
180
181
    Edge edge[maxn];
    int head[maxn],L;
182
183
    int eid[maxn],toid[maxn];
184
185
    void addedge(int u,int v,int w,int id)
186
    {
187
      edge[L].to = v;
188
      edge[L].w = w;
189
      edge[L].id = id;
190
      edge[L].next = head[u];
191
      head[u] = L++;
    }
192
193
194
    void DFS(int now,int fa)
195
    {
196
      for (int i = head[now]; i != -1; i = edge[i].next)
197
         if (edge[i].to != fa)
         {
198
199
           sp.Link(edge[i].to,now,edge[i].w);
200
           eid[edge[i].id] = edge[i].to;
201
           toid[edge[i].id] = now;
202
203
           DFS(edge[i].to,now);
         }
204
    }
205
206
    int main()
207
208
209
      Init();
210
      sp.Init();
211
      scanf("%d",&n);
212
213
      for (int i = 0; i < n; i++)
214
```

```
{
215
         l[i] = newNode(0,nil);
216
217
         r[i] = newNode(0,nil);
         l[i]\rightarrow id = r[i]\rightarrow id = i;
218
219
         l[i]->c[1] = r[i], r[i]->p = l[i];
220
         sp.Pushup(l[i]);
221
222
         head[i] = -1;
       }
223
224
      L = 0;
225
226
       for (int i = 0; i < n-1; i++)
227
       {
228
         int u,v,w;
         scanf("%d%d%d",&u,&v,&w);
229
230
         u--,v--;
231
232
         addedge(u,v,w,i);
233
         addedge(v,u,w,i);
       }
234
235
236
       DFS(0,-1);
237
       for (int i = 0; i < n-1; i++)
238
239
       {
240
         fflush(stdout);
241
242
         int id;
         scanf("%d",&id);
243
244
         id—;
245
246
         int ret = sp.Split(eid[id]);
247
         printf("%d\n",ret);
248
       }
249
250
       return 0;
251 }
    4.2
          动态树
    懒标记是否及时 Pushdown 了?
    修改之后有没有及时 Pushup?
          维护点权
    4.2.1
    查询链上的最长字段和
    GetRoute 是用换根写的
  1
    const int MaxN = 110000;
  2
```

```
3
    struct Node
 4
    {
 5
       int size, key;
 6
       bool rev;
 7
 8
    // bool same;
 9
    // int lsum, rsum, sum, maxsum, sa;
10
11
       Node *c[2];
12
       Node *p;
13
    14
15 Node *newNode(int v, Node *p)
16
17
       cur\rightarrow c[0] = cur\rightarrow c[1] = nil, cur\rightarrow p = p;
18
       cur \rightarrow size = 1;
       cur -> key = v;
19
       cur->rev = false;
20
21
22
    // cur->same = false;
23
    //
          cur \rightarrow sa = 0;
24
    // cur->lsum = cur->rsum = cur->maxsum = 0;
25
    // cur\rightarrowsum = v;
26
27
       return cur++;
28
    }
29
30
    void Init()
31
    {
32
       cur = mem;
33
       nil = newNode(0, cur);
34
       nil->size = 0;
35
    }
36
37
    struct SplayTree
38
39
       void Pushup(Node *x)
40
41
          if (x == nil)
                                return;
42
          Pushdown(x); Pushdown(x\rightarrowc[0]); Pushdown(x\rightarrowc[1]);
43
          x\rightarrow size = x\rightarrow c[0]\rightarrow size + x\rightarrow c[1]\rightarrow size + 1;
44
45 //
             x \rightarrow sum = x \rightarrow c[0] \rightarrow sum + x \rightarrow c[1] \rightarrow sum + x \rightarrow key;
46 //
             x\rightarrow lsum = max(x\rightarrow c[0]\rightarrow lsum,
47 //
                x \rightarrow c[0] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow lsum));
48 //
             x\rightarrow rsum = max(x\rightarrow c[1]\rightarrow rsum,
49 //
                x\rightarrow c[1]-sum + x\rightarrow key + max(0, x\rightarrow c[0]-srsum));
50 //
             x \rightarrow \max = \max(\max(x \rightarrow c[0] \rightarrow \max , x \rightarrow c[1] \rightarrow \max ),
51 //
                x \rightarrow key + max(0, x \rightarrow c[0] \rightarrow rsum) + max(0, x \rightarrow c[1] \rightarrow lsum));
52
53
       }
```

```
54
        void Pushdown(Node *x)
 55
 56
           if (x == nil)
                                 return;
 57
           if (x->rev)
 58
 59
              x\rightarrow rev = 0;
 60
              x->c[0]->rev ^= 1;
 61
              x \rightarrow c[1] \rightarrow rev ^= 1;
 62
              swap(x->c[0], x->c[1]);
 63
     //注意修改与位置有关的量
 64
     //
                swap(x\rightarrow lsum, x\rightarrow rsum);
           }
 65
 66
 67
     //
              if (x->same)
 68 //
 69 //
                x\rightarrow same = false;
 70 |//
                x\rightarrow key = x\rightarrow sa;
 71 //
                x\rightarrow sum = x\rightarrow sa * x\rightarrow size;
 72 //
                x\rightarrow 1sum = x\rightarrow rsum = x\rightarrow maxsum = max(0, x\rightarrow sum);
 73 //
                if (x\rightarrow c[0] != nil)
 74 //
                   x\rightarrow c[0]->same = true, x\rightarrow c[0]->sa = x\rightarrow sa;
 75
     //
                if (x\rightarrow c[1] != nil)
 76
     //
                   x \to c[1] \to same = true, x \to c[1] \to sa = x \to sa;
 77
     //
              }
 78
 79
        bool isRoot(Node *x)
 80
        {
 81
           return (x == nil) || (x->p->c[0] != x && x->p->c[1] != x);
 82
 83
        void Rotate(Node *x, int f)
 84
 85
           if (isRoot(x))
                                  return;
           Node *y = x \rightarrow p;
 86
           y -> c[f \land 1] = x -> c[f], x -> p = y -> p;
 87
           if (\bar{x} \rightarrow c[f] != nil)
 88
 89
              x\rightarrow c[f]\rightarrow p = y;
 90
           if (y != nil)
 91
           {
 92
              if (y == y -> p -> c[1])
 93
                y - p - c[1] = x;
 94
              else if (y == y -> p -> c[0])
 95
                y \rightarrow p \rightarrow c[0] = x;
           }
 96
 97
           x->c[f] = y, y->p = x;
 98
           Pushup(y);
 99
        }
        void Splay(Node *x)
100
101
102
           static Node *stack[MaxN];
103
           int top = 0;
           stack[top++] = x;
104
```

```
105
         for (Node *y = x; !isRoot(y); y = y - p)
106
            stack[top++] = y->p;
107
         while (top)
108
            Pushdown(stack[—top]);
109
110
         while (!isRoot(x))
111
         {
            Node *y = x \rightarrow p;
112
            if (isRoot(y))
113
114
              Rotate(x, x == y \rightarrow c[0]);
115
            else
116
            {
117
              int fd = y-p-c[0] == y;
118
              if (y\rightarrow c[fd] == x)
119
                 Rotate(x, fd ^1), Rotate(x, fd);
120
              else
121
                 Rotate(y, fd), Rotate(x, fd);
            }
122
123
124
         Pushup(x);
125
126
       Node *Access(Node *u)
127
         Node *v = nil;
128
129
         while (u != nil)
130
131
            Splay(u);
132
            V \rightarrow p = u;
133
            u \rightarrow c[1] = v;
134
            Pushup(u);
135
            u = (v = u) - p;
136
            if (u == nil)
137
              return v;
138
         }
139
140
       Node *LCA(Node *u, Node *v)
141
142
         Access(u);
143
         return Access(v);
144
145
       Node *Link(Node *u, Node *v)
146
       {
147
         Access(u);
148
         Splay(u);
149
         u->rev = true;
150
         u \rightarrow p = v;
151
152
       void ChangeRoot(Node *u)
153
       {
154
         Access(u) \rightarrow rev ^= 1;
155
       }
```

```
156
      Node *GetRoute(Node *u, Node *v)
157
      {
158
         ChangeRoot(u);
159
         return Access(v);
160
    };
161
162
163
    int n, m;
164
    SplayTree sp;
165
166
    int main(int argc, char const *argv[])
167
168
      while (scanf("%d", &n) != EOF)
169
      {
170
         Init();
171
         for (int i = 0; i < n; i++)
172
173
           int v;
174
           scanf("%d", &v);
175
           pos[i] = newNode(v, nil);
176
         for (int i = 0; i < n - 1; i++)
177
178
179
           int u, v;
180
           scanf("%d%d", &u, &v);
181
           u--, v--;
182
           sp.Link(pos[u], pos[v]);
183
         }
184
185 |//
           scanf("%d", &m);
186
    //
           for (int i = 0; i < m; i++)
187
    //
           {
188
    //
             int typ, u, v, c;
189 //
             scanf("%d%d%d", &typ, &u, &v);
190 //
             u--, v--;
191 //
             if (typ == 1)
               printf("%d\n", sp.GetRoute(pos[u], pos[v])->maxsum);
192 //
193 //
             else
194 //
             {
195 //
               scanf("%d", &c);
196 //
               Node *p = sp.GetRoute(pos[u], pos[v]);
197
    //
               p—>same = true;
198 //
               p \rightarrow sa = c;
199
    //
             }
200
    //
           }
201
      }
202
      return 0;
203 }
```

4.2.2 维护边权

```
刘汝佳的 Happy Painting!
查询链上边的不同颜色数量
不能换根,但是可以 Link 和 Cut
```

```
const int MaxN = 60000;
 2
 3
    struct Node
 4
    {
 5
       int size, key;
 6
 7
       int msk, lazy;
 8
 9
       Node *c[2];
10
       Node *p;
    } mem[MaxN], *cur, *nil, *pos[MaxN];
11
12
13 | Node *newNode(int v, Node *p)
14
    {
15
       cur\rightarrow c[0] = cur\rightarrow c[1] = nil, cur\rightarrow p = p;
16
       cur->size = 1;
17
       cur -> key = v;
18
19
       cur \rightarrow msk = 0;
20
       cur \rightarrow lazy = -1;
21
22
       return cur++;
    }
23
24
25
    void Init()
26
27
       cur = mem;
28
       nil = newNode(0, cur);
29
       nil->size = 0;
    }
30
31
32
    struct SplayTree
33
34
       void Pushup(Node *x)
35
       {
36
         if (x == nil) return;
         Pushdown(x);
37
38
         Pushdown(x \rightarrow c[0]);
         Pushdown(x \rightarrow c[1]);
39
40
         x \rightarrow size = x \rightarrow c[0] \rightarrow size + x \rightarrow c[1] \rightarrow size + 1;
41
42
         x \to msk = x \to c[0] \to msk \mid x \to c[1] \to msk \mid (1 << x \to key);
43
44
       void Pushdown(Node *x)
45
       {
```

```
46
                          if (x == nil) return;
47
                          if (x\rightarrow lazy != -1)
48
49
                          {
50
                                x\rightarrow key = x\rightarrow lazy;
                                 x \rightarrow msk = (1 << x \rightarrow key);
51
52
                                x \to c[0] \to lazy = x \to c[1] \to lazy = x \to lazy;
53
                                x\rightarrow lazy = -1;
                         }
54
55
56
                   bool isRoot(Node *x)
57
58
                          return (x == nil) \mid (x -> p -> c[0] \mid = x \& x -> p -> c[1] \mid = x);
59
60
                  void Rotate(Node *x, int f)
61
62
                          if (isRoot(x)) return;
63
                          Node *y = x \rightarrow p;
64
                          y - x = x - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - x = y - 
                          if (x\rightarrow c[f] != nil)
65
66
                                 x\rightarrow c[f]\rightarrow p = y;
                          if (y != nil)
67
68
                          {
69
                                 if (y == y -> p -> c[1])
70
                                       y \rightarrow p \rightarrow c[1] = x;
71
                                 else if (y == y \rightarrow p \rightarrow c[0])
72
                                       y \rightarrow p \rightarrow c[0] = x;
73
74
                          x - c[f] = y, y - p = x;
75
                          Pushup(y);
76
77
                  void Splay(Node *x)
78
79
                          static Node *stack[MaxN];
80
                          int top = 0;
                          stack[top++] = x;
81
82
                          for (Node *y = x; !isRoot(y); y = y - p)
83
                                 stack[top++] = y->p;
84
                          while (top)
85
                                Pushdown(stack[—top]);
86
87
                          while (!isRoot(x))
88
                          {
                                Node *y = x \rightarrow p;
89
                                 if (isRoot(y))
90
91
                                        Rotate(x, x == y -> c[0]);
92
                                 else
93
                                  {
94
                                        int fd = y->p->c[0] == y;
95
                                        if (y\rightarrow c[fd] == x)
96
                                               Rotate(x, fd ^1), Rotate(x, fd);
```

```
97
               else
 98
                 Rotate(y, fd), Rotate(x, fd);
            }
 99
100
101
          Pushup(x);
102
103
       Node *Access(Node *u)
104
105
          Node *v = nil;
106
          while (u != nil)
107
108
            Splay(u);
109
            v \rightarrow p = u;
110
            u\rightarrow c[1] = v;
111
            Pushup(u);
112
            u = (v = u) - p;
113
            if (u == nil) return v;
          }
114
115
116
       Node *Root(Node *u)
117
       {
118
          Access(u);
119
          Splay(u);
          for (Pushdown(u); u\rightarrow c[0] != nil; u = u\rightarrow c[0])
120
121
            Pushdown(u);
122
          Splay(u);
123
          return u;
124
125
       Node *LCA(Node *u, Node *v)
126
       {
127
          if (Root(u) != Root(v))
128
            return nil;
129
          Access(u);
130
          return Access(v);
131
       }
132
       void Cut(Node *u)
133
134
          Access(u);
135
          Splay(u);
136
          u \rightarrow c[0] = u \rightarrow c[0] \rightarrow p = nil;
137
          Pushup(u);
138
139
       void Link(Node *u, Node *v, int val)
140
       {
          Access(u);
141
142
          Splay(u);
143
          u \rightarrow p = v;
144
          u\rightarrow key = val;
145
          Pushup(u);
146
       }
    |};
147
```

```
148
149
    int cntbit(int x)
150
151
       x = (x \& 0x55555555) + ((x >> 1) \& 0x55555555);
152
       x = (x \& 0x33333333) + ((x >> 2) \& 0x33333333);
       x = (x \& 0x0F0F0F0F) + ((x >> 4) \& 0x0F0F0F0F);
153
154
       x = (x \& 0x00FF00FF) + ((x >> 8) \& 0x00FF00FF);
155
       x = (x \& 0x0000FFFF) + ((x >> 16) \& 0x0000FFFF);
156
       return x;
    }
157
158
159
    SplayTree sp;
160
    int n, 0, f[MaxN];
161
162
    int main(int argc, char const *argv[])
163
       while (scanf("%d%d",&n,&Q) != EOF)
164
165
       {
166
         Init();
167
         for (int i = 0; i < n; i++)
168
           scanf("%d",&f[i]);
169
170
           pos[i] = newNode(0, nil);
171
172
         for (int i = 0; i < n; i++)
173
174
           int col;
           scanf("%d",&col);
175
176
           if (f[i] > 0)
             sp.Link(pos[i],pos[f[i]-1],col-1);
177
178
179
         for (int q = 0; q < 0; q++)
180
181
           int typ,x,y,c;
           scanf("%d%d%d",&typ,&x,&y);
182
183
           x---,y---;
184
           if (typ == 3)
185
           {
186
             Node *lca = sp.LCA(pos[x],pos[y]);
187
             if (lca == nil \mid | x == y)
188
             {
                printf("0<sub>□</sub>0\n");
189
190
               continue;
             }
191
192
             int totedge = lca \rightarrow c[1] \rightarrow size;
             int msk = lca -> c[1] -> msk;
193
194
             if (pos[x] != lca)
195
196
197
                sp.Splay(pos[x]);
                totedge += pos[x]->size;
198
```

```
199
                msk l= pos[x]->msk;
             }
200
201
202
             printf("%d<sub>\\\\</sub>%d\n",totedge,cntbit(msk));
           }
203
           else
204
205
           {
             scanf("%d",&c);
206
207
             if (typ == 1)
208
209
                if (x == y) continue;
210
211
                Node *lca = sp.LCA(pos[x],pos[y]);
212
                if (pos[x] == lca) continue;
213
214
215
                sp.Cut(pos[x]);
216
                sp.Link(pos[x],pos[y],c);
217
             }
218
219
             else
220
              {
221
                Node *lca = sp.LCA(pos[x],pos[y]);
222
223
                if (lca == nil \mid \mid x == y)
224
                  continue;
225
                lca \rightarrow c[1] \rightarrow lazy = c;
226
227
                sp.Pushup(lca->c[1]);
                sp.Pushup(lca);
228
229
                if (pos[x] != lca)
230
231
                  sp.Splay(pos[x]);
232
                  pos[x] -> lazy = c;
233
                  sp.Pushup(pos[x]);
234
                }
             }
235
           }
236
         }
237
238
       }
239
       return 0;
240 }
    4.3
          可持久化线段树
     区间第 k 小数,内存压缩版,POJ2014。
  1 |#include <cstdio>
    #include <algorithm>
  3
    using namespace std;
  4
    const int MAXN=100000, MAXM=100000;
```

```
6
 7
   struct node
 8
    {
      node *1,*r;
 9
10
      int sum;
   }tree[MAXN*4+MAXM*20];
11
12
13
   int N;
14
   node *newnode()
15
16
      tree[N].l=tree[N].r=NULL;
17
      tree[N].sum=0;
18
      return &tree[N++];
19
20 | node *newnode(node *x)
21
   {
22
      tree[N].l=x->l;
23
      tree[N].r=x->r;
24
      tree[N].sum=x->sum;
25
      return &tree[N++];
26
27
   node *build(int l,int r)
28
   {
29
      node *x=newnode();
30
      if (l<r)
31
      {
32
        int mid=l+r>>1;
33
        x->l=build(l,mid);
34
        x->r=build(mid+1,r);
35
        x\rightarrow sum=x\rightarrow l\rightarrow sum+x\rightarrow r\rightarrow sum;
36
      }
37
      else
38
        x \rightarrow sum = 0;
39
      return x;
40
41
   node *update(node *x,int l,int r,int p,int v)
42
    {
43
      if (l<r)
44
      {
45
        int mid=l+r>>1;
46
        node *nx=newnode(x);
47
        if (p<=mid)</pre>
48
        {
49
           node *ret=update(x->1,1,mid,p,v);
50
           nx->l=ret;
51
        }
52
        else
53
        {
54
           node *ret=update(x->r,mid+1,r,p,v);
55
           nx->r=ret;
56
        }
```

```
57
         nx->sum=nx->l->sum+nx->r->sum;
 58
         return nx;
       }
 59
 60
      else
 61
 62
         node *nx=newnode(x);
 63
         nx->sum+=v;
 64
         return nx;
       }
 65
 66
    int query(node *x1,node *x2,int l,int r,int k)
 67
 68
 69
       if (l<r)
 70
       {
 71
         int mid=l+r>>1;
 72
         int lsum=x2->l->sum-x1->l->sum;
 73
         if (lsum>=k)
 74
           return query(x1->1,x2->1,1,mid,k);
 75
         else
 76
           return query(x1->r,x2->r,mid+1,r,k-lsum);
      }
 77
 78
      else
 79
         return 1;
    }
 80
 81
    char s[10];
    node *root[MAXM+1];
 82
    int a[MAXN],b[MAXN];
    int init(int n)
 84
 85
    {
       for (int i=0;i<n;i++)
 86
 87
         b[i]=a[i];
 88
       sort(b,b+n);
 89
       int tn=unique(b,b+n)-b;
 90
       for (int i=0;i< n;i++)
 91
       {
 92
         int l=0, r=tn-1;
         while (l<r)
 93
 94
         {
 95
           int mid=l+r>>1;
 96
           if (b[mid]>=a[i])
 97
             r=mid;
 98
           else
 99
             l=mid+1;
         }
100
101
         a[i]=l;
102
103
       return tn;
104
105
    int main()
106
    {
107
       int cas=1,n;
```

```
108
      while (scanf("%d",&n)!=EOF)
109
      {
110
        printf("Case %d:\n",cas++);
111
        for (int i=0;i< n;i++)
112
           scanf("%d",&a[i]);
113
        int tn=init(n);
114
        N=0;
        root[0]=build(0,tn-1);
115
116
        for (int i=1;i<=n;i++)
           root[i]=update(root[i-1],0,tn-1,a[i-1],1);
117
118
        int m;
        scanf("%d",&m);
119
120
        for (int i=0; i< m; i++)
121
122
           int s,t;
           scanf("%d%d",&s,&t);
123
           printf("%d\n",b[query(root[s-1],root[t],0,tn-1,t-s+2>>1)]);
124
        }
125
126
127
      return 0;
128 |}
    4.4 treap 正式版
    支持翻转。
  1 |#include <cstdio>
    |#include <cstdlib>
    |#include <algorithm>
    using namespace std;
  5
  6
    const int MAXN = 100000;
    const int MAXM = 100000;
    const int inf = 0x7ffffffff;
  9
    int a[MAXN];
    struct Treap
 10
 11
    {
 12
      int N;
 13
      Treap()
 14
      {
 15
        N = 0;
 16
        root = NULL;
 17
      }
 18
      void init()
 19
 20
        N = 0;
 21
        root = NULL;
 22
      }
 23
      struct Treap_Node
 24
 25
        Treap_Node *son[2];//left & right
 26
        int value, fix;
```

```
27
         bool lazy;
28
         int size;
29
         Treap_Node() {}
30
         Treap_Node(int _value)
31
         {
32
            son[0] = son[1] = NULL;
           value = _value;
33
34
            fix = rand() * rand();
35
            lazy = 0;
36
            size = 1;
37
         }
38
         int sonSize(bool flag)
39
         {
40
            if (son[flag] == NULL)
41
              return 0;
42
            else
43
              return son[flag]->size;
44
         }
45
      } node[MAXN], *root, *pos[MAXN];
46
      void up(Treap_Node *p)
47
      {
         p\rightarrow size = p\rightarrow sonSize(0) + p\rightarrow sonSize(1) + 1;
48
49
50
      void down(Treap_Node *p)
51
      {
52
         if (!p->lazy)
53
            return ;
         for (int i = 0; i < 2; i++)
54
55
            if (p->son[i])
56
              p \rightarrow son[i] \rightarrow lazy = !p \rightarrow son[i] \rightarrow lazy;
57
         swap(p\rightarrow son[0], p\rightarrow son[1]);
58
         p\rightarrow lazy = 0;
59
60
      Treap_Node *merge(Treap_Node *p, Treap_Node *q)
61
      {
62
         if (p == NULL)
            return q;
63
64
         else if (q == NULL)
65
            return p;
66
         if (p\rightarrow fix \ll q\rightarrow fix)
67
         {
68
            down(p);
69
           p\rightarrow son[1] = merge(p\rightarrow son[1], q);
70
           up(p);
71
            return p;
72
         }
73
         else
74
         {
75
            down(q);
76
            q \rightarrow son[0] = merge(p, q \rightarrow son[0]);
77
            up(q);
```

```
78
           return q;
        }
 79
 80
 81
      pair<Treap_Node *, Treap_Node *> split(Treap_Node *p, int n)
 82
 83
         if (p == NULL)
 84
           return make_pair((Treap_Node *)NULL, (Treap_Node *)NULL);
 85
         if (!n)
 86
           return make_pair((Treap_Node *)NULL, p);
 87
         if (n == p \rightarrow size)
 88
           return make_pair(p, (Treap_Node *)NULL);
 89
         down(p);
 90
         if (p\rightarrow sonSize(0) >= n)
 91
 92
           pair<Treap_Node *, Treap_Node *> ret = split(p->son[0], n);
 93
           p \rightarrow son[0] = ret.second;
 94
           up(p);
 95
           return make_pair(ret.first, p);
 96
         }
 97
         else
 98
         {
           pair<Treap_Node *, Treap_Node *>
 99
             ret = split(p->son[1], n - p->sonSize(0) - 1);
100
           p->son[1] = ret.first;
101
102
           up(p);
103
           return make_pair(p, ret.second);
        }
104
105
106
      int smalls(Treap_Node *p,int value)
107
      {
108
         if (p==NULL)
109
           return 0;
110
         if (p->value<=value)
111
           return 1+p->sonSize(0)+smalls(p->son[1],value);
112
         else
113
           return smalls(p->son[0], value);
114
      }
115
      void insert(int value)
116
117
         Treap_Node *p = node[N++];
118
         *p = Treap_Node(value);
119
        pair<Treap_Node *, Treap_Node *>
           ret = split(root, smalls(root, value));
120
121
         root = merge(merge(ret.first, p), ret.second);
122
123
      void remove(int value)
124
125
         pair<Treap_Node *, Treap_Node *> ret = split(root, smalls(root,
             value) - 1);
         root = merge(ret.first, split(ret.second, 1).second);
126
127
      }
```

```
128
      Treap_Node *build(int s, int t)
129
      {
130
        int idx = t + s \gg 1;
131
        Treap_Node *p = node[N++];
132
        *p = Treap_Node(a[idx]);
133
        pos[a[idx]] = p;
134
        if (idx > s)
135
          p = merge(build(s, idx - 1), p);
136
        if (idx < t)
          p = merge(p, build(idx + 1, t));
137
138
        up(p);
139
        return p;
140
      }
141
      void build(int n)
142
      {
143
        root = build(0, n - 1);
144
145
      void *reverse(int s, int t)
146
147
        pair<Treap_Node *, Treap_Node *> tmp1, tmp2;
        tmp1 = split(root, s - 1);
148
149
        tmp2 = split(tmp1.second, t - s + 1);
        tmp2.first->lazy = !tmp2.first->lazy;
150
151
        root = merge(tmp1.first, merge(tmp2.first, tmp2.second));
152
      }
153
    };
154
    Treap treap;
155
    int main()
156
    {
157
      treap.init();
158
      int n;
      scanf("%d", &n);
159
      for (int i = 0; i < n; i++)
160
        scanf("%d", &a[i]);
161
162
      treap.build(n);
163 |}
    4.5
         树链剖分
    4.5.1 点权
  1 |#include <cstdio>
    #include <cstrina>
    #include <cstdlib>
    |#include <algorithm>
    using namespace std;
    const int MAX = 12000;
  7
    const int LOG = 15;
    const int oo = 0x3f3f3f3f;
 9
    struct Edge
10 | {
```

```
11
        int to, w, id;
        Edge* next;
12
   } memo[MAX<<1],*cur,*g[MAX],*pree[MAX],*solid[MAX],*valid[MAX];</pre>
13
   int dp[MAX][LOG], pos[MAX], lst[MAX], dep[MAX], cnt[MAX], h[MAX], K
15
   void init()
16
17
      for (int i = 1; i <= n; i++)
18
19
        g[i] = NULL;
20
        valid[i] = NULL;
21
        solid[i] = NULL;
22
        pree[i] = NULL;
23
24
      for (int i = 0; i < LOG; i++)
25
      {
26
        dp[1][i] = 1;
27
28
      cur = memo;
29
      K = 0;
30
31
   void add(int u, int v, int w, int id)
32
33
      cur \rightarrow to = v;
34
      cur -> w = w;
35
      cur->id = id;
36
      cur \rightarrow next = g[u];
37
      g[u] = cur++;
38
   }
39
   void dfsLCA(int d, int u, int f)
40
41
      dep[u] = d;
42
      dp[u][0] = f;
43
      cnt[u] = 1;
44
      for (int i = 1; i < LOG; i++)
45
      {
46
        dp[u][i] = dp[dp[u][i - 1]][i - 1];
47
48
      for (Edge* it = g[u]; it; it = it->next)
49
50
        int v = it -> to;
51
        if (v != f)
52
        {
53
          pree[v] = it;
54
          valid[it->id] = it;
55
          dfsLCA(d + 1, v, u); //RE
56
          cnt[u] += cnt[v];
          if (solid[u] == NULL || cnt[solid[u]->to] < cnt[v])</pre>
57
58
          {
59
            solid[u] = it;
          }
60
```

```
61
        }
      }
 62
 63
 64
    void dfsChain(int u, int head)
 65
 66
      h[u] = head;
 67
      if (solid[u])
 68
 69
         lst[pos[u] = K++] = u;
 70
         dfsChain(solid[u]->to, head);
      }
 71
 72
      else
 73
      for (Edge* it = g[u]; it; it = it->next)
 74
 75
         int v = it -> to;
 76
         if (it != solid[u] && v != dp[u][0])
 77
 78
           dfsChain(v, v);
 79
         }
 80
      }
 81
 82
    int getLCA(int u, int v)
 83
 84
      if (dep[u] < dep[v])
 85
         swap(u, v);
 86
      for (int st = 1 << (LOG - 1), i = LOG - 1; i >= 0; i--, st >>= 1)
 87
 88
         if (st \leftarrow dep[u] – dep[v])
 89
 90
           u = dp[u][i];
 91
 92
 93
      if (u == v)
 94
         return u;
 95
      for (int i = LOG - 1; i >= 0; i--)
 96
         if (dp[u][i] != dp[v][i])
97
 98
 99
           u = dp[u][i];
           v = dp[v][i];
100
101
         }
102
103
      return dp[u][0];
    }
104
105
    struct Node
106
    {
107
         int l, r, ma, mi;
108
         bool rev;
109
    } seg[MAX << 2];
110
    void reverse(int k)
111 | {
```

```
seg[k].mi *= -1;
112
      seg[k].ma *= -1;
113
      seg[k].rev ^= 1;
114
115
      swap(seg[k].mi, seg[k].ma);
116
117
    void pushdown(int k)
118
    {
119
      if (seg[k].rev)
120
121
         reverse(k << 1);
122
         reverse(k \ll 1 \mid 1);
123
         seg[k].rev = false;
      }
124
125
126
    void update(int k)
127
    {
128
      seg[k].mi = min(seg[k << 1].mi, seg[k << 1 | 1].mi);
129
      seg[k].ma = max(seg[k << 1].ma, seg[k << 1 | 1].ma);
130
131
    void init(int k, int l, int r)
132
    {
133
      seq[k].l = l;
134
      seg[k].r = r;
135
      seg[k].rev = false;
136
      if (l == r)
137
      {
138
         seg[k].mi = seg[k].ma = solid[lst[l]]->w; //solid WA
139
         return;
      }
140
      int mid = l + r \gg 1;
141
142
      init(k << 1, l, mid);
143
      init(k \ll 1 \mid 1, mid + 1, r);
144
      update(k);
145
    void update(int k, int id, int v)
146
147
148
      if (seg[k].l == seg[k].r)
149
150
         seg[k].mi = seg[k].ma = solid[lst[id]]->w = v;
151
         return;
152
      }
153
      pushdown(k);
154
      int mid = seg[k].l + seg[k].r >> 1;
155
      if (id <= mid)
156
         update(k \ll 1, id, v);
157
      else
158
         update(k \ll 1 \mid 1, id, v);
159
      update(k);
160
161
    void reverse(int k, int l, int r)
162 | {
```

```
163
       if (seg[k].l > r | l seg[k].r < l)
164
         return;
165
       if (seq[k].l >= l \&\& seq[k].r <= r)
166
167
         reverse(k);
168
         return;
169
170
      pushdown(k);
      reverse(k << 1, 1, r);
171
172
       reverse(k \ll 1 \mid 1, l, r);
173
       update(k);
174
175
    int read(int k, int l, int r)
176
177
       if (seg[k].l > r | l seg[k].r < l)
178
         return -oo;
179
       if (seg[k].l >= l \& seg[k].r <= r)
180
         return seg[k].ma;
181
      pushdown(k);
182
       return max(read(k \ll 1, l, r), read(k \ll 1 l 1, l, r));
183
184
    void setEdge(int id, int v)
185
    {
       Edge* it = valid[id];
186
187
       if (h[it\rightarrow to] != it\rightarrow to)
188
189
         update(1, pos[dp[it->to][0]], v);
190
       }
      else
191
192
       {
193
         it->w = v;
194
195
196
    void negateLCA(int t, int u)
197
      while (t != u)
198
199
200
         int tmp = h[u];
201
         if (dep[tmp] < dep[t])</pre>
202
           tmp = t;
203
         if (h[u] == u)
204
           pree[u]->w *= -1;
205
206
           u = dp[u][0];
207
         }
         else
208
209
210
           reverse(1, pos[tmp], pos[dp[u][0]]);
211
           u = tmp;
212
         }
213
       }
```

```
214 |}
215
    void negate(int u, int v)
216
217
       int t = getLCA(u, v);
218
       negateLCA(t, u);
219
       negateLCA(t, v);
220
221
    int maxLCA(int t, int u)
222
    {
223
       int ret = -00;
224
       while (t != u)
225
       {
226
         int tmp = h[u];
227
         if (dep[tmp] < dep[t])</pre>
228
           tmp = t;
229
         if (h[u] == u)
230
231
           ret = max(ret, pree[u]->w);
232
           u = dp[u][0];
233
         }
234
         else
235
236
           ret = max(ret, read(1, pos[tmp], pos[dp[u][0]]));
237
           u = tmp;
238
         }
239
       }
240
       return ret;
241
242
    int query(int u, int v)
243
    {
244
       int t = getLCA(u, v);
245
       return max(maxLCA(t, u), maxLCA(t, v));
246
247
    int main()
248
    {
249
       int T;
250
       int u, v, w;
251
       char op\lceil 15 \rceil;
       scanf("%d", &T);
252
253
       while (T—)
254
       {
         scanf("%d", &n);
255
256
         init();
257
         for (int i = 1; i < n; i++)
258
259
           scanf("%d%d%d", &u, &v, &w);
260
           add(u, v, w, i);
261
           add(v, u, w, i);
262
         }
263
         dfsLCA(0, 1, 1);
264
         dfsChain(1, 1);
```

```
init(1, 0, K - 1);
265
        while (scanf("%s", op), op[0] != 'D')
266
267
           scanf("%d%d", &u, &v);
268
269
           if (op[0] == 'C')
270
           {
271
             setEdge(u, v);
272
273
           else if (op[0] == 'N')
274
           {
275
             negate(u, v);
276
           }
277
           else
278
279
             printf("%d\n", query(u, v));
           }
280
         }
281
282
283
      return 0;
284 |}
    4.5.2 边权
  1 |#include <cstdio>
    #include <iostream>
    #include <cstdlib>
  4 | #include <algorithm>
  5 #include <cmath>
  6 #include <cstring>
    using namespace std;
  8
    int n,m,sum,pos;
    int head[50005],e;
    int s[50005],from[50005];
    int fa[50005][20],deep[50005],num[50005];
    int solid[50005],p[50005],fp[50005];
 12
 13
    struct N
 14
    {
 15
      int l,r,mid;
 16
      int add,w;
    }nod[50005*4];
 17
 18
    struct M
 19
    {
 20
      int v,next;
 21
    }edge[100005];
    void addedge(int u,int v)
 22
 23
    {
 24
      edge[e].v=v;
      edge[e].next=head[u];
 25
 26
      head[u]=e++;
 27
 28
      edge[e].v=u;
 29
      edge[e].next=head[v];
```

```
30
      head[v]=e++;
   }
31
32
   void LCA(int st,int f,int d)
33
   {
34
      deep[st]=d;
35
      fa[st][0]=f;
36
      num[st]=1;
37
      int i,v;
38
      for(i=1;i<20;i++)
39
        fa[st][i]=fa[fa[st][i-1]][i-1];
40
      for(i=head[st];i!=-1;i=edge[i].next)
41
      {
42
        v=edge[i].v;
43
        if(v!=f)
44
        {
45
          LCA(v, st, d+1);
46
          num[st]+=num[v];
          if(solid[st]==-1||num[v]>num[solid[st]])
47
48
            solid[st]=v;
        }
49
50
      }
51
52
   void getpos(int st,int sp)
53
   {
54
      from[st]=sp;
55
      if(solid[st]!=-1)
56
      {
57
        p[st]=pos++;
58
        fp[p[st]]=st;
59
        getpos(solid[st],sp);
      }
60
61
      else
62
63
        p[st]=pos++;
64
        fp[p[st]]=st;
65
        return;
      }
66
      int i,v;
67
68
      for(i=head[st];i!=-1;i=edge[i].next)
69
70
        v=edge[i].v;
71
        if(v!=solid[st]&&v!=fa[st][0])
72
          getpos(v,v);
      }
73
74
75
   int getLCA(int u,int v)
76
   {
77
      if(deep[u]<deep[v])</pre>
78
        swap(u,v);
79
      int d=1<<19,i;
80
      for(i=19;i>=0;i—)
```

```
81
       {
 82
         if(d<=deep[u]-deep[v])
 83
           u=fa[u][i];
 84
         d>>=1;
 85
       if(u==v)
 86
 87
         return u;
 88
       for(i=19;i>=0;i---)
 89
         if(fa[u][i]!=fa[v][i])
 90
         {
 91
           u=fa[u][i];
 92
           v=fa[v][i];
 93
 94
       return fa[u][0];
 95
96
    void init(int p,int l,int r)
 97
 98
       nod[p].l=l;
99
       nod[p].r=r;
100
       nod[p].mid=(l+r)>>1;
101
       nod[p].add=0;
102
       if(l==r)
103
         nod[p].w=s[fp[l]];
104
       else
105
       {
106
         init(p<<1,l,nod[p].mid);</pre>
107
         init(p<<1|1,nod[p].mid+1,r);
108
109
    }
    void lazy(int p)
110
111
112
       if(nod[p].add!=0)
113
114
         nod[p << 1].add+=nod[p].add;
115
         nod[p << 1|1].add+=nod[p].add;
116
         nod[p].add=0;
       }
117
118
119
    void update(int p,int l,int r,int v)
120
121
       if(nod[p].l==l&&nod[p].r==r)
122
123
         nod[p].add+=v;
124
         return;
125
126
       lazy(p);
127
       if(nod[p].mid<l)</pre>
128
         update(p<<1|1,1,r,v);
129
       else if(nod[p].mid>=r)
130
         update(p << 1, l, r, v);
131
       else
```

```
132
       {
133
         update(p<<1,l,nod[p].mid,v);</pre>
134
         update(p << 1 \mid 1, nod \lceil p \rceil .mid+1, r, v);
135
136
137
    int read(int p,int l,int r)
138
    {
139
       if(nod[p].l==l&&nod[p].r==r)
140
         return nod[p].w+nod[p].add;
141
       lazy(p);
       if(nod[p].mid<l)</pre>
142
143
         return read(p << 1 | 1, 1, r);
144
       else if(nod[p].mid>=r)
145
         return read(p<<1,1,r);</pre>
146
147
    void jump(int st,int ed,int val)
148
       while(deep[st]>=deep[ed])
149
150
151
         int tmp=from[st];
152
         if(deep[tmp]<deep[ed])</pre>
153
           tmp=ed:
         update(1,p[tmp],p[st],val);
154
         st=fa[tmp][0];
155
156
       }
157
    }
158
    void change(int st,int ed,int val)
159
160
       int lca=getLCA(st,ed);
       jump(st,lca,val);
161
162
       jump(ed,lca,val);
163
       jump(lca,lca,-val);
164
165
    int main()
166
    {
       while(scanf("%d%d%d",&n,&m,&sum)==3)
167
168
169
         int i;
170
         s[0]=0;pos=0;deep[0]=-1;
171
         memset(fa,0,sizeof(fa));
172
         for(i=1;i<=n;i++)
173
         {
174
           solid[i]=-1;
175
           scanf("%d",&s[i]);
176
177
         memset(head, -1, sizeof(head));
178
         e=0:
         for(i=0;i<m;i++)
179
180
         {
181
           int a,b;
           scanf("%d%d",&a,&b);
182
```

```
183
           addedge(a,b);
         }
184
         LCA(1,0,0);
185
186
         getpos(1,1);
         init(1,0,pos-1);
187
188
         for(i=0;i<sum;i++)
189
         {
190
           char que[5];
           scanf("%s",que);
191
           if(que[0]!='Q')
192
193
194
             int a,b,c;
195
             scanf("%d%d%d",&a,&b,&c);
             if(que[0]=='D')
196
197
               C=-C;
198
             change(a,b,c);
199
200
           else
201
           {
202
             int a;
             scanf("%d",&a);
203
             printf("%d\n", read(1,p[a],p[a]));
204
           }
205
         }
206
207
208
       return 0;
209 |}
          划分树
    4.6
    |int n,m|
  2
    struct elem
  3
  4
       int v, index;
    }a[120000];
    int d[30][120000];
  7
    int s[30][120000];
  8
  9
    bool cmp(elem a,elem b)
 10
    {
 11
       if (a.v == b.v)
 12
         return a.index <= b.index;</pre>
 13
       return a.v < b.v;
    }
 14
 15
 16
    void build(int depth,int l,int r)
 17
 18
       if (l == r)
 19
         return;
 20
       int mid = (1+r)/2;
 21
       int tl,tr;
 22
       tl = tr = 0;
```

```
23
      for (int i = 1; i <= r; i++)
24
25
        if (cmp(a[d[depth][i]],a[mid]))
26
        {
27
          d[depth+1][l+tl] = d[depth][i];
28
          tl++;
        }
29
30
        else
31
        {
32
          d\lceil depth+1\rceil\lceil mid+1+tr\rceil = d\lceil depth\rceil\lceil i\rceil;
33
          tr++;
34
        }
35
        s[depth][i] = tl;
36
37
     build(depth+1,1,mid);
     build(depth+1,mid+1,r);
38
   }
39
40
41
   int find(int depth, int dl, int dr, int fl, int fr, int k)
42
43
      if (fl == fr)
44
        return a[d[depth][fl]].v;
45
      int ls,rs;
      int mid = (dl+dr)/2;
46
     ls = (fl == dl)? 0 : s[depth][fl-1];
47
48
      rs = s\lceil depth\rceil\lceil fr\rceil;
49
      return (rs-ls < k)?
        50
51
        : find(depth+1,dl,mid,dl+ls,dl+rs-1,k);
52
   }
53
54
   int main()
55
56
     while (scanf("%d%d",&n,&m) != EOF)
57
      {
58
        for (int i = 1; i <= n; i++)
59
60
          scanf("%d",&a[i].v);
61
          a[i].index = i;
62
        }
63
        sort(a+1,a+n+1,cmp);
64
        for (int i = 1; i <= n; i++)
65
          d[0][a[i].index] = i;
66
        build(0,1,n);
67
        int l,r,k;
68
        for (int i = 1; i <= m; i++)
69
        {
70
          scanf("%d%d%d",&l,&r,&k);
71
          printf("%d\n",find(0,1,n,l,r,k));
        }
72
73
      }
```

```
74
     return 0;
75 }
   4.7 树状数组
  |int read(int k)
 2
   {
 3
     int sum = 0;
     for (; k; k^{-k}-k)
 4
 5
       sum+=tree[k];
 6
     return sum;
   void update(int k, int v)
 8
 9
     for (; k \le MaxN; k = k - k)
10
11
       tree[k]+=v;
   }
int find_Kth(int k)
12
13
14
15
     int idx = 0;
16
     for(int i=20; i>=0; i--)
17
18
       idx = 1 << i;
       if(idx <= MaxN && tree[idx] < k)</pre>
19
20
          k -= tree[idx];
21
       else idx ^= 1 << i;
22
23
     return idx + 1;
24 }
```

5 图论

5.1 优先队列优化的 dijkstra

```
1 |#include<cstdio>
   #include<cstring>
 3 |#include<iostream>
 4 | #include < algorithm >
 5 #include<queue>
 6 #include<vector>
   using namespace std;
   const int MAXN=100;
   const int MAXM=1000;
10 | int N,L;
11 | int head[MAXN];
12
   struct edges
13
14
     int to,next,cost;
   } edge[MAXM];
15
16 | int dist[MAXN];
17
   class states
18
   {
19
   public:
20
     int cost, id;
21 | };
22
   class cmp
23
   {
24
   public:
25
     bool operator ()(const states &i,const states &j)
26
27
        return i.cost>j.cost;
28
     }
   };
29
30
   void init(int n)
31
   {
32
     N=n;
33
     L=0;
     for (int i=0; i<n; i++)
34
35
       head[i]=-1;
36
   void add_edge(int x,int y,int cost)
37
38
   {
39
     edge[L].to=y;
40
     edge[L].cost=cost;
41
     edge[L].next=head[x];
42
     head[x]=L++;
43
44 | int dijkstra(int s,int t)
45
46
     memset(dist,63,sizeof(dist));
47
     states u;
```

```
48
     u.id=s;
49
     u.cost=0;
50
     dist[s]=0;
51
     priority_queue<states, vector<states>, cmp> q;
52
     q.push(u);
53
     while (!q.empty())
54
     {
55
        u=q.top();
56
        q.pop();
57
        if (u.id==t) return dist[t];
        if (u.cost!=dist[u.id]) continue;
58
59
        for (int i=head[u.id]; i!=-1; i=edge[i].next)
60
        {
61
          states v=u;
62
          v.id=edge[i].to;
63
          if (dist[v.id]>dist[u.id]+edge[i].cost)
64
65
            v.cost=dist[v.id]=dist[u.id]+edge[i].cost;
66
            q.push(v);
67
68
        }
69
     }
70
     return -1;
71
72
   int main()
73
   {
74
     int n,m;
75
     scanf("%d%d",&n,&m);
76
     init(n);
77
     for (int i=0; i<m; i++)
78
79
        int x,y,z;
80
        scanf("%d%d%d",&x,&y,&z);
81
        add_edge(x,y,z);
82
        add_edge(y,x,z);
     }
83
84
     int s,t;
85
     scanf("%d%d",&s,&t);
86
     printf("%d\n",dijkstra(s,t));
87
     return 0;
88 |}
        SAP 四版
 1 | const int MAXEDGE=20400;
   const int MAXN=400;
   const int inf=0x3fffffff;
 4
   struct edges
 5
   {
     int cap, to, next, flow;
   } edge[MAXEDGE+100];
 7
 8 struct nodes
```

```
9
   {
10
      int head, label, pre, cur;
11
   } node[MAXN+100];
12
   int L,N;
13
   int gap[MAXN+100];
14
   void init(int n)
15
   {
16
      L=0;
17
     N=n;
18
      for (int i=0; i<N; i++)
19
        node[i].head=-1;
20 |}
21
   void add_edge(int x,int y,int z,int w)
22
23
      edge[L].cap=z;
24
      edge[L].flow=0;
25
      edge[L].to=y;
26
      edge[L].next=node[x].head;
27
      node[x].head=L++;
28
      edge[L].cap=w;
29
      edge[L].flow=0;
30
      edge[L].to=x;
31
      edge[L].next=node[y].head;
32
      node[y].head=L++;
33
34
   int maxflow(int s,int t)
35
   {
36
      memset(gap,0,sizeof(gap));
37
      gap[0]=N;
38
      int u,ans=0;
39
      for (int i=0; i<N; i++)
40
      {
41
        node[i].cur=node[i].head;
42
        node[i].label=0;
43
      }
44
      u=s;
45
      node[u].pre=-1;
46
      while (node[s].label<N)</pre>
47
      {
        if (u==t)
48
49
        {
50
          int min=inf;
51
          for (int i=node[u].pre; i!=-1; i=node[edge[i^1].to].pre)
52
            if (min>edge[i].cap—edge[i].flow)
53
              min=edge[i].cap-edge[i].flow;
54
          for (int i=node[u].pre; i!=-1; i=node[edge[i^1].to].pre)
55
          {
56
            edge[i].flow+=min;
57
            edge[i^1].flow—≠min;
58
          }
59
          u=s;
```

```
60
          ans+=min;
61
          continue;
       }
62
63
       bool flaa=false;
64
       int v;
       for (int i=node[u].cur; i!=-1; i=edge[i].next)
65
66
67
         v=edge[i].to;
68
          if (edge[i].cap-edge[i].flow &&
69
            node[v].label+1==node[u].label)
70
          {
71
            flag=true;
72
            node[u].cur=node[v].pre=i;
73
            break;
         }
74
75
       if (flag)
76
77
        {
78
          u=v;
79
          continue;
80
81
       node[u].cur=node[u].head;
82
       int min=N;
83
       for (int i=node[u].head; i!=-1; i=edge[i].next)
84
          if (edge[i].cap-edge[i].flow && node[edge[i].to].label<min)
85
            min=node[edge[i].to].label;
86
       gap[node[u].label]--;
87
       if (!gap[node[u].label]) return ans;
       node[u].label=min+1;
88
       gap[node[u].label]++;
89
90
       if (u!=s) u=edge[node[u].pre^1].to;
91
92
     return ans;
93 |}
        费用流
   5.3
   5.3.1 三版
   T 了可以改成栈。
  const int MAXM=60000;
   const int MAXN=400;
   const int inf=0x3fffffff;
   int L,N;
 5
   int K;
 6
   struct edges
 7
   {
     int to,next,cap,flow,cost;
   } edge[MAXM];
 9
   struct nodes
10
11
  |{
```

```
12
     int dis, pre, head;
13
     bool visit;
   } node[MAXN];
14
15
   void init(int n)
16
   {
17
     N=n;
18
     L=0;
19
     for (int i=0; i<N; i++)
20
       node[i].head=-1;
21
22
   void add_edge(int x,int y,int cap,int cost)
23
24
     edge[L].to=y;
25
     edge[L].cap=cap;
26
     edge[L].cost=cost;
27
     edge[L].flow=0;
28
     edge[L].next=node[x].head;
29
     node[x].head=L++;
30
     edge[L].to=x;
31
     edge[L].cap=0;
32
     edge[L].cost=-cost;
33
     edge[L].flow=0;
34
     edge[L].next=node[y].head;
35
     node[y].head=L++;
36
37
   bool spfa(int s,int t)
38
   {
39
     queue <int> q;
40
     for (int i=0; i<N; i++)
41
42
       node[i].dis=0x3fffffff;
43
       node[i].pre=-1;
       node[i].visit=0;
44
45
46
     node[s].dis=0;
47
     node[s].visit=1;
48
     q.push(s);
49
     while (!q.empty())
50
     {
51
       int u=q.front();
52
       node[u].visit=0;
53
       for (int i=node[u].head; i!=-1; i=edge[i].next)
54
        {
55
          int v=edge[i].to;
56
          if (edge[i].cap>edge[i].flow &&
57
              node[v].dis>node[u].dis+edge[i].cost)
58
          {
59
            node[v].dis=node[u].dis+edge[i].cost;
            node[v].pre=i;
60
61
            if (!node[v].visit)
62
```

```
63
              node[v].visit=1;
64
              q.push(v);
65
            }
          }
66
        }
67
68
        q.pop();
69
70
     if (node[t].pre==-1)
71
        return 0;
72
     else
73
        return 1;
74
75
   int mcmf(int s,int t,int &cost)
76
77
     int flow=0;
78
     while (spfa(s,t))
79
80
        int max=inf;
81
        for (int i=node[t].pre; i!=-1; i=node[edge[i^1].to].pre)
82
83
          if (max>edge[i].cap-edge[i].flow)
84
            max=edge[i].cap-edge[i].flow;
85
        for (int i=node[t].pre; i!=-1; i=node[edge[i^1].to].pre)
86
87
88
          edge[i].flow+=max;
89
          edge[i^1].flow—=max;
90
          cost+=edge[i].cost*max;
91
        }
92
        flow+=max;
93
94
     return flow;
95 |}
   5.3.2 dijkstra 加改点堆
 1 |#include <cstdio>
 2 | #include <cstring>
   #include <algorithm>
   #include <queue>
 5 |#include <stack>
   using namespace std;
   int N, L;
 8
   |int head[2003];
 9
   struct Edge
10
11
        int to, next, flow, cost;
12
   } edge[2000 * 1999 / 2 + 2000 * 3 << 1];
   int h[2003], dis[2003], pre[2003];
13
14
   struct Heap
15 |{
```

```
16
        int value[2004], id[2004];
17
        int pos[2003];
18
        int size;
19
        void init()
20
        {
21
            size = 1;
22
23
        void swap2(int p, int q)
24
25
            swap(value[p], value[q]);
26
            swap(id[p], id[q]);
            pos[id[p]] = p;
27
28
            pos[id[q]] = q;
29
30
        void push_up(int p)
31
            while (p > 1 \& value[p / 2] > value[p])
32
33
            {
34
                 swap2(p, p / 2);
35
                 p /= 2;
36
37
        }
38
        void push_down(int p)
39
40
            while (p * 2 < size)
41
42
                 int best = p;
                 if (p * 2 < size && value[p] > value[p * 2])
43
                 best = p * 2;
if (p * 2 + 1 < size && value[best] > value[p * 2 + 1])
44
45
46
                     best = p * 2 + 1;
47
                 if (p == best)
48
                     break;
49
                 swap2(p, best);
50
                 p = best;
51
            }
52
53
        void push(int _value, int _id)
54
55
            value[size] = _value;
56
            id\Gamma size = _id;
            pos[_id] = size;
57
58
            push_up(size++);
59
        }
60
        int top()
61
        {
62
            return id[1];
63
64
        void pop()
65
        {
            value[1] = value[size - 1];
66
```

```
id[1] = id[--size];
 67
             pos[id[1]] = 1;
 68
 69
             push_down(1);
 70
        }
 71
        void update(int _value, int _id)
 72
 73
             int p = pos[_id];
 74
             value[p] = _value;
 75
             push_up(p);
 76
        }
    } heap;
 77
    bool inque[2003];
 79
    void init(int n)
 80
    {
 81
        N = n;
 82
        L = 0;
 83
        memset(head, -1, 4 * n);
 84
 85
    void add_edge(int u, int v, int flow, int cost)
 86
    {
 87
        edge[L].to = v;
 88
        edge[L].flow = flow;
 89
        edge[L].cost = cost;
 90
        edge[L].next = head[u];
 91
        head[u] = L++;
 92
        edge[L].to = u;
 93
        edge[L].flow = 0;
 94
        edge[L].cost = -cost;
 95
        edge[L].next = head[v];
96
        head[v] = L++;
 97
 98
    void spfa(int s)
 99
    {
100
        memset(dis, 63, 4 * N);
101
        memset(inque, 0, N);
102
        memset(pre, -1, 4 * N);
103
        dis[s] = 0;
        stack <int> que;
104
105
        que.push(s);
106
        while (!que.empty())
107
        {
108
             int u = que.top();
109
             inque[u] = 0;
             que.pop();
110
111
             for (int i = head[u]; i != -1; i = edge[i].next)
112
                 if (edge[i].flow)
113
                 {
114
                     int v = edge[i].to;
                     if (dis[v] > dis[u] + edge[i].cost)
115
116
                     {
                          dis[v] = dis[u] + edge[i].cost;
117
```

```
118
                          pre[v] = i;
119
                          if (!inque[v])
120
                          {
121
                              inque[v] = 1;
122
                              que.push(v);
123
                          }
                     }
124
                 }
125
        }
126
127
128
    void dijkstra(int s)
129
130
         for (int i = 0; i < N; ++i)
             h[i] += dis[i];
131
132
         memset(dis, 63, 4 * N);
        memset(pre, -1, 4 * N);
133
134
         memset(inque, 0, N);
135
         dis[s] = 0;
136
         inque[s] = 1;
137
         heap.init();
138
         heap.push(0, s);
139
         while (heap.size > 1)
140
141
             int u = heap.top();
142
             heap.pop();
143
             for (int i = head[u]; i != -1; i = edge[i].next)
144
                 if (edge[i].flow)
145
146
                     int v = edge[i].to;
147
                     if (dis[v] > dis[u] + edge[i].cost + h[u] - h[v])
148
149
                          dis[v] = dis[u] + edge[i].cost + h[u] - h[v];
150
                          pre[v] = i;
151
                          if (!inque[v])
152
                          {
153
                              heap.push(dis[v], v);
154
                              inque[v] = 1;
155
                          }
156
                          else
157
                              heap.update(dis[v], v);
                     }
158
159
                 }
        }
160
161
162
    int mcmf(int s, int t, int &cost)
163
164
         int flow = 0;
165
         memset(h, 0, 4 * N);
        for (spfa(s); pre[t] != -1; dijkstra(s))
166
      {
167
         int maxs = edge[pre[t]].flow;
168
```

```
169
        for (int i = pre[t]; i != -1; i = pre[edge[i \land 1].to])
170
           maxs = min(maxs, edge[i].flow);
             for (int i = pre[t]; i != -1; i = pre[edge[i \land 1].to])
171
172
             {
173
                 edge[i].flow -= maxs;
174
                 edge[i ^1].flow += maxs;
                 cost += edge[i].cost * maxs;
175
176
177
        flow += maxs;
178
      }
179
        return flow;
180
181
    int a[1000];
182
    int main()
183
    {
184
        int t;
        scanf("%d", &t);
185
186
        for (int cas = 1; cas <= t; ++cas)
187
         {
188
             int n;
             scanf("%d", &n);
189
             init(n * 2 + 3);
190
191
             for (int i = 0; i < n; ++i)
192
             {
193
                 int x;
194
                 scanf("%d", &x);
195
                 a[i] = x;
                 add_edge(i * 2, i * 2 + 1, 1, -1);
196
                 add_edge(i * 2 + 1, n * 2 + 1, 1, 0);
197
                 add_{edge}(n * 2 + 2, i * 2, 1, 0);
198
199
200
             for (int i = 0; i < n; ++i)
201
                 for (int j = i + 1; j < n; ++j)
                     if (a[i] < a[j])
202
                         add_edge(i * 2 + 1, j * 2, 1, 0);
203
             add_{edge}(n * 2, n * 2 + 2, 2, 0);
204
205
             int ans = 0;
             mcmf(n * 2, n * 2 + 1, ans);
206
207
             printf("Case_#%d:_%d\n", cas, -ans);
208
        }
209
        return 0;
210 |}
    5.4
         网络单纯形
    返回 pair(流量,费用)
  1 | #include <iostream>
    #include <cstdio>
    #include <cstring>
    #include <algorithm>
  5
    using namespace std;
  6
```

```
7 | const int N = 1100;
   const int M = 50000*2*5+2;
   struct Node
   {
10
11
      int depth, pot, id;
12
      Node *parent, *thread, *prev, *last;
13
   };
14 | struct Arc
15
   {
16
     int tail,head,u,c;
   };
17
18 | Arc arc[M];
19 | int cnt_arc;
Node nnode[N],*rec[N];
21 | int cr;
   const int inf = 0x222222222;
22
23
   void dfs(Node *n)
24
   {
25
     cr=0;
26
      rec[cr++]=n;
27
      while(cr)
28
      {
29
        Node *nn=n->thread;
30
        nn->prev=n;
31
        n=nn;
32
        int d=n->depth;
33
        if(d<=rec[cr-1]->depth)
34
35
          Node *l=rec[cr−1];
36
          while(cr&&d<=rec[cr-1]->depth)
37
38
            rec[--cr]->last=l;
          }
39
40
41
        if(cr) rec[cr++]=n;
42
      }
43
   Node*pivot(Node*n1, Node*n2, Node*n3, Node*n4)
45
   {
46
      dfs(n1);
47
      Node *n1l=n1->last,*n3l,*n3p,*end;
      if(n11->thread==n2)
48
49
      {
50
        n2->parent=n1;
51
        dfs(n3);
52
        return n3->last->thread;
53
54
      if(n1l->thread!=n3)
55
      {
56
        dfs(n4);
57
        n3p=n3->prev;
```

```
58
         n3l=n3\rightarrow last;
 59
         n3p->thread=n3l->thread;
 60
         if(n3l==n1l)
 61
           n3l->thread=n1->thread,n1->thread=n2;
 62
         else
 63
           n3l->thread=n1l->thread,n1l->thread=n2;
 64
       }
 65
       else
 66
       {
         dfs(n3);
 67
 68
         n3l=n3->last;
 69
         n11->thread=n2;
 70
       }
 71
       end=n3l->thread;
 72
       Node *n2l=n2->last,*n2lp=NULL,*p2=n1,*pp=NULL;
 73
       int pid;
       int first=0;
 74
 75
       while(n2!=n3)
 76
       {
 77
         n2l=n2\rightarrow last;
 78
         Node *xp=pp;
 79
         if(n2l!=n2lp) xp=n2l,n2lp=n2l;
 80
         pp=n2->prev;
 81
         pp->thread=xp->thread;
 82
         xp->thread=n2->parent;
 83
         Node *n2n=n2->parent;
 84
         int ppid=n2->id;
         if(first) n2->id=pid^1;
 85
 86
         pid=ppid;
 87
         first++;
 88
         n2->parent=p2;
 89
         p2=n2;
 90
         n2=n2n;
 91
      if(first) n2->id=pid^1;
 92
 93
       n2->parent=p2;
 94
       return end;
 95
 96
    void update(Node *n1,Node *n2)
 97
 98
       n1=n1->thread;
 99
       while(n1!=n2)
100
       {
         Node *n1p=n1->parent;
101
102
         n1->depth=n1p->depth+1;
103
         n1->pot = n1p->pot - arc[n1->id].c;
104
         n1=n1->thread;
105
       }
106
    void pivot(int id)
107
108 | {
```

```
int tail=arc[id].tail,head=arc[id].head;
109
110
      int u=arc[id].u,c=arc[id].c;
      Node *uu=nnode+tail,*vv=nnode+head;
111
      Node *mu=0,*mv=0;
112
113
      int mn_f = u;
114
      while(uu!=vv)
115
      {
116
         int nid;
117
         if(uu->depth>vv->depth)
118
           nid=uu->id,uu=uu->parent;
119
         else nid=vv->id^1,vv=vv->parent;
120
         if(arc[nid].u<mn_f) mn_f=arc[nid].u;</pre>
121
      uu=nnode+tail,vv=nnode+head;
122
123
      arc[id].u—=mn_f;
124
      arc[id^1].u+=mn_f;
125
      while(uu!=vv)
126
      {
127
         int nid;
128
         if(uu->depth>vv->depth)
129
130
           nid=uu->id:
131
           arc[nid].u—=mn_f;
132
           arc[nid^1].u+=mn_f;
133
           if(arc[nid].u==0\&\&mu==0)
134
             mu=uu, mv=0;
135
           uu=uu->parent;
136
         }
         else
137
138
         {
139
           nid=vv->id^1;
140
           arc[nid].u—=mn_f;
           arc[nid^1].u+=mn_f;
141
142
           if(arc[nid].u==0\&\&mu==0)
143
             mv=vv;
144
           vv=vv->parent;
        }
145
146
147
      if(arc[id].u)
148
149
         if(mv)
150
151
           int n3=mv-nnode,n4=mv->parent-nnode;
152
           Node *nx=pivot(nnode+tail,nnode+head,mv,mv->parent);
153
           nnode[head].id=id;
154
           update(nnode+tail,nx);
        }
155
156
         else
157
         {
158
           int n3=mu-nnode,n4=mu->parent-nnode;
159
           Node *nx=pivot(nnode+head,nnode+tail,mu,mu->parent);
```

```
nnode[tail].id=id^1;
160
161
           update(nnode+head,nx);
162
        }
      }
163
164
165
    struct List
166
    {
167
      int v;
      List *R;
168
169
170
    |List lst[M],*cl,*hd;
    pair<int,int> cost(int s,int t,int cnt_node)
171
172
    {
173
      int tmp_arc=cnt_arc;
174
      int i;
175
      int sid=-1;
176
      nnode[cnt_node].depth=0;
177
      nnode[cnt_node].parent=nnode+cnt_node;
178
      nnode[cnt_node].pot=0;
179
      nnode[cnt_node].thread=nnode;
180
      for(i=0; i<cnt_node; i++)</pre>
181
      {
182
         nnode[i].depth=1;
183
         nnode[i].parent=nnode+cnt_node;
184
         nnode[i].thread=nnode+(i+1);
185
         nnode[i].id=tmp_arc;
186
         int pot=-inf,u=0,tot=0;
187
         if(i==s)
188
           pot=-pot,tot=inf,u=inf,sid=tmp_arc+1;
189
         if(i==t) tot=inf;
190
         nnode[i].pot=pot;
191
         arc[tmp_arc].tail=cnt_node;
192
         arc[tmp_arc].head=i;
193
         arc[tmp_arc].u=u;
194
         arc[tmp_arc].c=-pot;
195
         tmp_arc++;
         arc[tmp_arc].tail=i;
196
197
         arc[tmp_arc].head=cnt_node;
198
         arc[tmp_arc].u=tot-u;
199
         arc[tmp_arc].c=pot;
200
         tmp_arc++;
201
      }
      while(1)
202
203
      {
204
         bool fd=false;
205
         int i,tot=0;
206
         hd=cl=lst:
207
         cl->R=cl++;
         int tail,head,c,cc;
208
         const int MAXQ = cnt_node/4+5;
209
         const int MINQ = cnt_node/10+2;
210
```

```
211
         for(i=0; i<cnt_arc; i++)</pre>
212
213
            if(arc[i].u==0) continue;
214
            tail=arc[i].tail;
            head=arc[i].head,c=arc[i].c;
215
216
            cc=c-nnode[tail].pot+nnode[head].pot;
217
            if(cc<0)
218
            {
219
              fd=true;
220
              cl->v=i:
221
              cl \rightarrow R = hd \rightarrow R;
222
              hd \rightarrow R = cl;
223
              cl++;
224
              tot++;
225
              if(tot>=MAXQ)
226
              {
227
                 while(tot>MINQ)
228
229
                   List *mj=NULL, *mjp, *it=hd->R, *itp=hd;
230
                   int mp=0;
231
                   while(it!=hd)
232
                   {
233
                     int id=it->v;
                     tail=arc[id].tail,head=arc[id].head,c=arc[id].c;
234
235
                     cc=c-nnode[tail].pot+nnode[head].pot;
236
                     if(cc >= 0)
237
                     {
238
                        itp->R=it->R;
239
                        tot--;
                     }
240
241
                     else if(cc<mp)</pre>
242
                        mp=cc,mj=it,mjp=itp;
243
                     if(itp->R==it) itp=it;
244
                     it=it->R;
245
246
                   if(mj==NULL) break;
                   pivot(mj->v);
247
248
                   mjp \rightarrow R = mj \rightarrow R;
249
                   tot--;
250
                }
              }
251
            }
252
253
         }
254
         while(tot)
255
256
            List *it=hd—>R,*itp=hd;
257
            while(it!=hd)
258
259
              int id=it->v;
              tail=arc[id].tail,head=arc[id].head;
260
              c=arc[id].c;
261
```

```
cc=c-nnode[tail].pot+nnode[head].pot;
262
263
             if(cc<0) pivot(id);</pre>
264
             itp->R=it->R;
             tot--;
265
266
             it=it->R;
           }
267
268
         if(!fd) break;
269
      }
270
271
       int sum=0:
272
      for(i=0; i<cnt_arc; i+=2)
273
         sum+=arc[i].c*arc[i^1].u;
274
275
276
       return pair<int,int>(arc[sid].u,sum);
277
278
    void add_arc(int tail,int head,int u,int c)
279
    {
280
       arc[cnt_arc].tail=tail;
281
       arc[cnt_arc].head=head;
282
       arc[cnt_arc].u=u;
283
       arc[cnt_arc].c=c;
284
       cnt_arc++;
    }
285
286
287
    void init()
288
    {
289
       cnt_arc = 0;
    }
290
291
292
    void add_edge(int x,int y,int cap,int cost)
293
    {
294
       add_arc(x,y,cap,cost);
295
       add_arc(y,x,0,-cost);
    }
296
297
298
    int main()
299
     {
300
       int n,m,k;
301
       while (scanf("%d%d%d",&n,&m,&k)!=EOF)
302
       {
303
         init();
304
         add_edge(0,1,k,0);
305
         for (int i=0; i < m; i++)
306
307
           int u, v, a, c;
           scanf("%d%d%d%d",&u,&v,&a,&c);
308
309
           for (int j=0; j<c; j++)
310
             add_{edge}(u,v,1,a*(j*2+1));
311
312
         pair<int, int> ret = cost(0,n,n+1);
```

```
313
         if (ret.first == k)
           printf("%d\n",ret.second);
314
315
         else
316
           puts("-1");
       }
317
318
       return 0;
319 }
          匈牙利
    5.5
          新版, 隐式图可解
    5.5.1
    |bool check(int u)
  2
    {
  3
       for (int i=head[u]; i!=-1; i=edge[i].next)
  4
       {
  5
         int v=edge[i].to;
  6
         if (matc[v]==u) continue;
  7
         if (!use[v])
  8
  9
           use \lceil v \rceil = 1;
           if (matc[v]==-1 || check(matc[v]))
 10
 11
 12
             matc[v]=u;
 13
             matc[u]=v;
 14
             return 1;
 15
           }
         }
 16
 17
 18
       return 0;
 19
 20
    int match()
 21
    {
 22
       int ret=0;
      memset(matc,-1,sizeof(matc));
 23
 24
       for (int u=0; u<N; u++)
 25
 26
         if (matc[u]!=-1) continue;
 27
         memset(use,0,sizeof(use));
 28
         if (check(u))
 29
           ret++;
 30
       }
 31
       return ret;
 32 |}
    5.5.2
          邻接矩阵
    |bool check(int u)
  2
    {
  3
       for (int v=0; v<N; v++)
  4
         if (am[u][v] && !use[v])
  5
         {
```

```
6
          use[v]=1;
 7
          if (pre[v]=-1 \mid l \cdot check(pre[v]))
 8
 9
            pre[v]=u;
10
            return 1;
          }
11
12
13
      return 0;
14
15
   int match()
16
17
      int ret=0;
18
      memset(pre,-1,sizeof(pre));
19
      for (int u=0; u<N; u++)
20
      {
21
        memset(use,0,sizeof(use));
22
        if (check(u))
23
          ret++;
24
25
      return ret;
26 |}
   5.5.3
         邻接表
   |bool check(int u)
 2
   {
 3
      for (int i=head[u]; i!=-1; i=edge[i].next)
 4
 5
        int v=edge[i].to;
 6
        if (!use[v])
 7
        {
 8
          use[v]=1;
 9
          if (pre[v]=-1 \mid l check(pre[v]))
10
11
            pre[v]=u;
12
            return 1;
13
          }
14
        }
15
      }
16
      return 0;
17
18
   int match()
19
   {
20
      int ret=0;
21
      memset(pre,-1,sizeof(pre));
22
      for (int u=1; u<=N; u++)
23
24
        memset(use,0,sizeof(use));
25
        if (check(u))
26
          ret++;
27
      }
28
      return ret;
```

29 |} 一般图最大加权匹配 注意 G 初始化 1 |#define N 229 2 int G[N][N]; int cnt_node; int dist[N]; int rec $[\overline{N}]$, cr, M[N], P[N]; bool vst[N]; const int inf = 0x3f3f3f3f; 7 bool spfa(int u) 9 { 10 rec[cr++]=u; 11 if(vst[u]) return true; 12 vst[u]=true; int v; 13 14 for(v=0; v<cnt_node; v++)</pre> 15 16 if(v!=u&&M[u]!=v&&!vst[v])17 { 18 int w=M[v]; 19 if(dist[w]<dist[u]+G[u][v]-G[v][w]) 20 { 21 dist[w]=dist[u]+G[u][v]-G[v][w]; 22 if(spfa(w)) 23 { 24 return true; 25 } 26 } 27 28 } 29 cr--; 30 vst[u]=false: 31 return false; 32 33 int match() 34 35 int i; 36 for(i=0; i<cnt_node; i++) P[i]=i;</pre> 37 for(i=0; $i<cnt_node$; i+=2) M[i]=i+1, M[i+1]=i; 38 int cnt=0; while(1) 39 40 { 41 memset(dist,0,sizeof(dist)); 42 cr=0; 43 int i; 44 bool fd=false; 45 memset(vst,0,sizeof(vst)); 46 for(i=0; i<cnt_node; i++)</pre>

```
{
47
            if(spfa(P[i]))
48
49
50
               fd=true;
51
               int j;
52
               int nx=M[rec[cr-1]];
53
               for(j=cr-2; rec[j]!=rec[cr-1]; j--)
54
55
                  M[nx]=rec[j];
56
                  int tmp=nx;
                  nx=M[rec[j]];
57
58
                  M[rec[j]]=tmp;
59
60
               M[nx]=rec[j];
61
               M[rec[j]]=nx;
62
               break;
63
            }
64
65
          if(!fd)
66
          {
67
            cnt++;
68
            if(cnt>=3) break;
69
            random_shuffle(P,P+cnt_node);
          }
70
71
72
      int sum=0;
73
      for(i=0; i<cnt_node; i++)</pre>
74
75
          int v=M[i];
76
          if(i<v)
77
78
            sum+=G[i][v];
79
          }
80
81
       return sum;
82 }
       一般图匹配带花树
  |const int MaxN = 222;
 1
 2
   int N;
   bool Graph[MaxN+1][MaxN+1];
   int Match[MaxN+1];
   |bool InQueue[MaxN+1],InPath[MaxN+1],InBlossom[MaxN+1];
   int Head, Tail;
   int Queue[MaxN+1];
   int Start,Finish;
   int NewBase;
   int Father[MaxN+1],Base[MaxN+1];
11
   int Count;
12 void CreateGraph()
```

```
13 | {
14
     int u,v;
15
     memset(Graph, false, sizeof(Graph));
     scanf("%d",&N);
16
     while (scanf("%d%d",&u,&v) != EOF)
17
18
        Graph[u][v] = Graph[v][u] = true;
19
20
   void Push(int u)
21
   {
22
     Queue[Tail] = u;
23
     Tail++;
     InQueue[u] = true;
24
25
26
   int Pop()
27
   {
28
     int res = Queue[Head];
29
     Head++;
30
     return res;
31
32
   int FindCommonAncestor(int u,int v)
33
   {
34
     memset(InPath,false,sizeof(InPath));
35
     while (true)
36
     {
37
        u = Base[u];
38
        InPath[u] = true;
        if (u == Start) break;
39
40
        u = Father[Match[u]];
41
     }
42
     while (true)
43
44
        v = Base[v];
45
        if (InPath[v]) break;
46
        v = Father[Match[v]];
47
48
     return v;
   }
49
50
   void ResetTrace(int u)
51
   {
52
     int v;
53
     while (Base[u] != NewBase)
54
     {
55
        v = Match[u];
56
        InBlossom[Base[u]] = InBlossom[Base[v]] = true;
57
        u = Father[v];
58
        if (Base[u] != NewBase) Father[u] = v;
     }
59
60
61
   void BlossomContract(int u,int v)
62
   {
63
     NewBase = FindCommonAncestor(u,v);
```

```
64
      memset(InBlossom, false, sizeof(InBlossom));
 65
      ResetTrace(u);
      ResetTrace(v);
 66
 67
      if (Base[u] != NewBase) Father[u] = v;
 68
      if (Base[v] != NewBase) Father[v] = u;
      for (int tu = 1; tu <= N; tu++)
 69
         if (InBlossom[Base[tu]])
 70
 71
 72
           Base[tu] = NewBase;
 73
           if (!InQueue[tu]) Push(tu);
 74
 75 |}
 76
    void FindAugmentingPath()
 77
 78
      memset(InQueue, false, sizeof(InQueue));
 79
      memset(Father,0,sizeof(Father));
 80
      for (int i = 1; i <= N; i++)
 81
         Base[i] = i;
 82
      Head = Tail = 1;
 83
      Push(Start);
 84
      Finish = 0:
 85
      while (Head < Tail)
 86
      {
 87
         int u = Pop();
         for (int v = 1; v <= N; v++)
 88
 89
           if (Graph[u][v] && (Base[u] != Base[v]) && (Match[u] != v))
 90
           {
 91
             if ((v == Start) | I
 92
               ((Match[v] > 0) \&\& (Father[Match[v]] > 0)))
 93
               BlossomContract(u,v);
 94
             else if (Father[v] == 0)
 95
             {
 96
               Father[v] = u;
 97
               if (Match[v] > 0)
 98
                 Push(Match[v]);
 99
               else
100
101
                 Finish = v;
102
                 return;
103
            }
104
           }
105
      }
106
107
108
    void AugmentPath()
109
110
      int u,v,w;
111
      u = Finish;
112
      while (u > 0)
113
      {
114
         v = Father[u];
```

```
115
        w = Match[v];
116
        Match[v] = u;
117
        Match[u] = v;
118
        u = w;
      }
119
    }
120
121
    void Edmonds()
122
123
      memset(Match,0,sizeof(Match));
124
      for (int u = 1; u <= N; u++)
        if (Match[u] == 0)
125
126
         {
127
           Start = u;
128
           FindAugmentingPath();
           if (Finish > 0) AugmentPath();
129
130
         }
131
132
    void PrintMatch()
133
134
      for (int u = 1; u <= N; u++)
135
         if (Match[u] > 0)
136
           Count++;
      printf("%d\n",Count);
137
138
      for (int u = 1; u <= N; u++)
139
         if (u < Match \lceil u \rceil)
140
           printf("%d<sub>\\\\</sub>%d\n",u,Match[u]);
141 |}
    int main()
142
143
    {
144
      CreateGraph();
145
      Edmonds();
146
      PrintMatch();
147 }
    5.8
        KM
    5.8.1 最大加权匹配
  1 |bool visx[N], visy[N]; //x,y 中的点是否被访问
    int lx[N],ly[N];//x,y 中的点的标号
    int matchy[N];//y 中各点匹配状态
    int map[N][N];//二分图描述 [x][y]
  5
    bool find(int x)
  6
    {
  7
      visx[x]=true;
  8
      int t;
  9
      for (int y=0;y<ycnt;y++)</pre>
 10
      {
         if (!visy[y])
 11
 12
         {
 13
           t=lx[x]+ly[y]-map[x][y];
 14
           if (t==0)
```

```
15
          {
16
            visy[y]=true;
            if (matchy[y]=-1 | l find(matchy[y]))
17
18
            {
19
              matchy[y]=x;
20
              return true;
21
22
23
          else if (lack>t) lack=t;
24
        }
25
26
      return false;
27
28
   void KM()
29
   {
30
      memset(lx,0,sizeof(lx));
31
      memset(ly,0,sizeof(ly));
32
      memset(matchy,-1,sizeof(matchy));
33
      for (int i=0;i<xcnt;i++)</pre>
34
        for (int j=0;j<ycnt;j++)</pre>
          if (map[i][j]>lx[i])
35
36
            lx[i]=map[i][j];
37
      for (int x=0;x<xcnt;x++)
38
      {
39
        while (true)
40
41
          memset(visx,false,sizeof(visx));
42
          memset(visy, false, sizeof(visy));
43
          lack=INFI;
44
          if (find(x)) break;
45
          for (int i=0;i<xcnt;i++)</pre>
46
          {
47
            if (visx[i]) lx[i]—=lack;
48
            if (visy[i]) ly[i]+=lack;
49
        }
50
      }
51
52
      int cost=0;
53
      for (int i=0;i<ycnt;i++)</pre>
54
        cost+=map[matchy[i]][i];
55 |}
         自认为正确的 Kuhn_Munkras
   未验证
 1 |#include<cstdio>
 2 | #include < cstring >
   |#include<algorithm>
 4 using namespace std;
   const int MAXN=100;
   const int inf=0x3f3f3f3f;
   |bool visitx[MAXN], visity[MAXN];
```

```
|int labx[MAXN],laby[MAXN],matx[MAXN],maty[MAXN],slack[MAXN];
   int ma[MAXN][MAXN];
10
   bool check(int x,int n)
11
   {
12
     visitx[x]=1;
13
     for (int i=0; i<n; i++)
14
        if (!visity[i])
15
          if (labx[x]+laby[i]==ma[x][i])
16
17
            visity[i]=1;
18
            if (maty[i]=-1 | l check(maty[i],n))
19
20
              matx[x]=i;
21
              maty[i]=x;
22
              return 1;
23
            }
          }
24
25
          else
26
            slack[i]=min(slack[i],labx[x]+laby[i]-ma[x][i]);
27
28
     return 0;
29
30
   void maintain(int n)
31
   {
32
     int diff=inf;
33
     for (int i=0; i<n; i++)
34
        if (!visity[i])
          diff=min(diff,slack[i]);
35
36
     for (int i=0; i<n; i++)
37
     {
38
        if (visitx[i])
39
          labx[i]—=diff;
40
        if (visity[i])
41
          laby[i]+=diff;
42
        else
43
          slack[i]-=diff;
44
     }
45
46
   int Kuhn_Munkras(int n)
47
48
     for (int i=0; i<n; i++)
49
     {
50
        labx[i]=-inf;
51
        for (int j=0; j<n; j++)
52
          labx[i]=max(labx[i],ma[i][j]);
53
54
     memset(laby,0,4*n);
55
     memset(matx, -1, 4*n);
56
     memset(maty, -1, 4*n);
57
     for (int i=0; i< n; i++)
58
     {
```

```
59
       memset(visitx,0,n);
       memset(visity,0,n);
60
61
       memset(slack, 63, 4*n);
62
       while (!check(i,n))
63
        {
64
         maintain(n);
65
         memset(visitx,0,n);
66
         memset(visity,0,n);
       }
67
68
69
     int ret=0;
70
     for (int i=0;i< n;i++)
71
       ret+=labx[i]+laby[i];
72
     return ret;
73
   }
74
   int main()
75
   {
76
     int n,m;
77
     scanf("%d%d",&m,&n);
78
     for (int i=m; i<n; i++)
       for (int j=0; j<n; j++)
79
         ma[i][j]=0;
80
     for (int i=0; i<m; i++)
81
82
       for (int j=0; j<n; j++)
          scanf("%d",&ma[i][j]);
83
     printf("%d\n",Kuhn_Munkras(n));
84
85
     printf("%d",matx[0]+1);
86
     for (int i=1; i < m; i++)
       printf("\d",matx[i]+1);
87
     puts("");
88
89
     return 0;
90 }
       * 二维平面图的最大流
   5.9
   待整理
 1 | #include < iostream>
   #include <algorithm>
   #include <cstdio>
 4 | #include <cstring>
   #include <vector>
 6 | #include < cmath>
 7
   |#include <map>
   |#include <queue>
 9
   using namespace std;
10
11 | const int maxn = 100100;
12
   const int inf = 0x3f3f3f3f;
13
   struct Point
14 | {
```

```
15
      int x,y,id;
      double theta;
16
17
      Point() {}
18
      Point(int _x,int _y)
19
      {
20
        X = _X;
21
        y = _y;
22
23
      Point(Point _s,Point _e,int _id)
24
      {
25
        id = _id;
26
        x = _s.x-_e.x;
27
        y = _s.y-_e.y;
28
        theta = atan2(y,x);
29
      }
30
     bool operator < (const Point &b)const
31
32
        return theta < b.theta;
33
   };
34
35
36 |map<pair<int,int>,int > idmap;
37
   struct Edge
38
39
      int from, to, next, cap, near, mark;
40 };
41 | Edge edge[maxn*2];
42
   int head[maxn],L;
43 | int cntd[maxn];
   void addedge(int u,int v,int cap)
44
45
46
      cntd[u]++;
47
      cntd[v]++;
48
      idmap[make_pair(u,v)] = L;
49
      edge[L].from = u;
50
      edge[L].to = v;
51
      edge[L].cap = cap;
52
      edge[L].next = head[u];
53
      edge[L].mark = -1;
54
      head[u] = L++;
   }
55
56
57
   int rtp[maxn];
58 | Point p[maxn], tp[maxn];
59
   int n,m,S,T;
60
   int vid;
61
62
   struct Edge2
63
64
      int to, next, dis;
   |} edge2[maxn*2];
```

```
66 | int head2[maxn],L2;
 67
 68
    void addedge2(int u,int v,int dis)
 69
    {
 70
      edge2[L2].to = v;
 71
      edge2[L2].dis = dis;
 72
      edge2[L2].next = head2[u];
 73
      head2[u] = L2++;
 74
    }
 75
 76
    |int dist[maxn];
 77 bool ina[maxn];
 78
    int SPFA(int s,int t)
 79
    {
 80
      queue<int> Q;
 81
      memset(inq,false,sizeof(inq));
 82
      memset(dist,63,sizeof(dist));
 83
      Q.push(s);
 84
      dist[s] = 0;
 85
      while (!Q.empty())
 86
      {
 87
         int now = Q.front();
 88
         Q.pop();
         for (int i = head2[now]; i != -1; i = edge2[i].next)
 89
 90
           if (dist[edge2[i].to] > dist[now]+edge2[i].dis)
 91
           {
 92
             dist[edge2[i].to] = dist[now]+edge2[i].dis;
 93
             if (ing[edge2[i].to] == false)
 94
             {
95
               inq[edge2[i].to] = true;
 96
               Q.push(edge2[i].to);
 97
 98
           }
 99
         inq[now] = false;
100
      return dist[t];
101
    }
102
103
    int main()
104
105
    {
106
      int totcas;
      scanf("%d",&totcas);
107
      for (int cas = 1; cas <= totcas; cas++)</pre>
108
109
      {
         idmap.clear();
110
111
         L = 0;
        scanf("%d%d",&n,&m);
112
113
         S = T = 0;
114
         for (int i = 0; i < n; i++)
115
         {
116
           head[i] = -1;
```

```
117
           scanf("%d%d",&p[i].x,&p[i].y);
118
           if (p[S].x > p[i].x)
119
             S = i;
120
          if (p[T].x < p[i].x)
121
            T = i;
122
          cntd[i] = 0;
123
        }
124
        //源汇中间加入一个特殊节点
125
        head[n] = -1;
126
        n ++;
        addedge(S, n-1, inf);
127
128
        addedge(n-1,S,inf);
129
        addedge(T, n-1, inf);
130
        addedge(n-1,T,inf);
131
132
        for (int i = 0; i < m; i++)
133
        {
134
          int u,v,cap;
135
          scanf("%d%d%d",&u,&v,&cap);
136
137
          V--;
138
          addedge(u,v,cap);
139
          addedge(v,u,cap);
        }
140
141
142
        for (int i = 0; i < n; i++)
143
        {
144
          int tot = 0:
145
          //源点汇点连到特殊点的方向需要特别考虑一下
146
          if (i == S)
147
            tp[tot++] = Point(Point(0,0), Point(-1,0), n-1);
148
          else if (i == T)
149
            tp[tot++] = Point(Point(0,0), Point(1,0), n-1);
150
          else if (i == n-1)
151
           {
            tp[tot++] = Point(Point(0,0),Point(1,0),S);
152
153
            tp[tot++] = Point(Point(0,0), Point(-1,0), T);
154
          if (i < n-1)
155
156
           {
157
            for (int j = head[i]; j != -1; j = edge[j].next)
158
               if (i == S \&\& edge[j].to == n-1)
159
                                                  continue:
               if (i == T \& edge[j].to == n-1)
160
                                                  continue:
161
               tp[tot++] = Point(p[i],p[edge[j].to],edge[j].to);
162
163
          }
164
           sort(tp,tp+tot);
165
           for (int j = 0; j < tot; j++)
166
             rtp[tp[j].id] = j;
           for (int j = head[i]; j != -1; j = edge[j].next)
167
```

```
168
             edge[j].near = tp[(rtp[edge[j].to]+1)%tot].id;
        }
169
170
171
         vid = 0;
172
         for (int i = 0; i < L; i++)
173
           if (edge[i].mark == -1)
174
175
             int now = edge[i].from;
176
             int eid = i;
177
             int to = edge[i].to;
             while (true)
178
179
             {
180
               edge[eid].mark = vid;
181
               eid ^= 1;
182
               now = to;
               to = edge[eid].near;
183
184
               eid = idmap[make_pair(now,to)];
185
186
               if (now == edge[i].from) break;
187
188
             vid++;
           }
189
190
191
         L2 = 0;
192
         for (int i = 0; i < vid; i++)
193
           head2[i] = -1;
194
         for (int i = 0; i < L; i++)
           addedge2(edge[i].mark,edge[i^1].mark,edge[i].cap);
195
196
         printf("%d\n",SPFA(edge[0].mark,edge[1].mark));
197
198
      return 0;
199 |}
    5.10
           强联通
   |int dfsnum[2000];
    int low[2000];
  3
    int stack[2000];
    int top;
  5
    int ans;
  6
    int an;
    int be \lceil 2000 \rceil;
    int flag[2000];
  9
    void dfs(int x)
 10
    {
 11
      dfsnum[x] = low[x] = ans++;
 12
      stack[++top] = x;
 13
      flaq[x] = 1;
 14
      for (int i = head[x]; i != -1; i = edge[i].next)
 15
 16
         int y = edge[i].to;
```

```
if (dfsnum[y] == -1)
17
18
        {
          dfs(y);
19
          low[x] = min(low[x], low[y]);
20
21
22
        else if (flag[y] == 1)
23
          low[x] = min(low[x], dfsnum[y]);
24
25
      if (dfsnum[x] == low[x])
26
      {
27
        while (stack[top] != x)
28
29
          flag[stack[top]] = 0;
30
          be[stack[top]] = an;
31
          top--;
32
        }
33
        flaq[x] = 0;
        be[x] = an++;
34
35
        top--;
36
      }
37 |}
   调用:
 1 |void SC()
 2
   {
 3
     memset(dfsnum,-1,sizeof(dfsnum));
 4
     memset(flaq,0,sizeof(flaq));
 5
      top = 0;
 6
     an = 0;
 7
     ans = 0:
 8
      for (int i = 0; i < n; i++)
 9
        if (dfsnum[i] == -1)
          dfs(i);
10
11 |}
```

5.11 最大团以及相关知识

- 独立集: 独立集是指图的顶点集的一个子集,该子集的导出子图不含边.如果一个独立集不是任何一个独立集的子集,那么称这个独立集是一个极大独立集.一个图中包含顶点数目最多的独立集称为最大独立集。最大独立集一定是极大独立集,但是极大独立集不一定是最大的独立集。
- 支配集: 与独立集相对应的就是支配集,支配集也是图顶点集的一个子集,设 S 是图 G 的一个支配集,则对于图中的任意一个顶点 u,要么属于集合 s,要么与 s 中的顶点相邻。在 s 中除去任何元素后 s 不再是支配集,则支配集 s 是极小支配集。称 s 的所有支配集中顶点个数最少的支配集为最小支配集,最小支配集中的顶点个数成为支配数。
- 最小点的覆盖: 最小点的覆盖也是图的顶点集的一个子集,如果我们选中一个点,则称这个 点将以他为端点的所有边都覆盖了。将图中所有的边都覆盖所用顶点数最少,这个集合 就是最小的点的覆盖。
- 最大团: 图 G 的顶点的子集,设 D 是最大团,则 D 中任意两点相邻。若 u, v 是最大团,则 u,v 有边相连,其补图 u,v 没有边相连,所以图 G 的最大团 = 其补图的最大独立集。

给定无向图 G = (V, E),如果 U 属于 V,并且对于任意 u,v 包含于 U 有 < u,v > 包含于 E,则称 U 是 G 的完全子图,G 的完全子图 U 是 G 的团,当且仅当 U 不包含在 G 的更大的完全子图中,G 的最大团是指 G 中所含顶点数目最多的团。如果 U 属于 V,并且对于任意 u,v 包含于 U 有 < u,v > 不包含于 E,则称 U 是 G 的空子图,G 的空子图 G 的空子图 G 是 G 的独立集,当且仅当 G 不包含在 G 的更大的独立集,G 的最大团是指 G 中所含顶点数目最多的独立集。

一些性质: 最大独立集 + 最小覆盖集 = V,最大团 = 补图的最大独立集,最小覆盖集 = 最大匹配

```
1 |#include <cstdio>
   bool am[100][100];
 3
   int ans;
   int c[100];
   int U[100][100];
   int n;
 7
   bool dfs(int rest,int num)
 8
   {
 9
     if (!rest)
10
     {
11
        if (num>=ans)
12
          return 1;
13
        else
14
          return 0;
     }
15
     int pre=-1;
16
17
     for (int i=0;i<rest && rest-i+num>=ans;i++)
18
19
        int idx=U[num][i];
20
        if (num+c[idx]<ans)</pre>
21
          return 0;
22
        int nrest=0;
        for (int j=i+1; j<rest; j++)
23
          if (am[idx][U[num][j]])
24
25
            U[num+1][nrest++]=U[num][j];
26
        if (dfs(nrest,num+1))
27
          return 1;
28
     }
29
     return 0;
30
31
   int main()
32
   {
33
     while (scanf("%d",&n),n)
34
35
        for (int i=0;i<n;i++)
36
          for (int j=0; j< n; j++)
            scanf("%d",&am[i][j]);
37
38
        ans=0;
39
        for (int i=n-1; i>=0; i--)
40
        {
41
          int rest=0;
42
          for (int j=i+1; j<n; j++)
```

```
43
            if (am[i][j])
              U[0][rest++]=j;
44
45
          ans+=dfs(rest,0);
46
          c[i]=ans;
47
       }
       printf("%d\n",ans);
48
49
50
     return 0;
51 |}
   5.12
          双连通分量
   标号从 0 起
 1 |#include<cstdio>
   #include<cstring>
 3 |#include<stack>
   #include<queue>
 5 | #include < algorithm >
 6 using namespace std;
   const int MAXN=100000*2;
   const int MAXM=200000;
 9
   struct edges
10
   {
11
     int to, next;
12
     bool cut, visit;
13
   |} edge[MAXM<<1];
   int head[MAXN],low[MAXN],dpt[MAXN],L;
   |bool visit[MAXN],cut[MAXN];
16
   void init(int n)
17
   {
18
     L=0;
19
     memset(head, -1,4*n);
20
     memset(visit,0,n);
   }
21
22
   void add_edge(int u,int v)
23
24
     edge[L].cut=edge[L].visit=0;
25
     edge[L].to=v;
26
     edge[L].next=head[u];
27
     head[u]=L++;
   }
28
29
   int idx;
30
   stack<int> st;
31
   |int bcc[MAXM];
32
   void dfs(int u,int fu,int deg)
33
   {
34
     cut[u]=0;
35
     visit[u]=1;
36
     low[u]=dpt[u]=deg;
37
     int tot=0;
     for (int i=head[u]; i!=-1; i=edge[i].next)
38
```

```
39
      {
40
        int v=edge[i].to;
41
        if (edge[i].visit)
42
          continue;
43
        st.push(i/2);
44
        edge[i].visit=edge[i^1].visit=1;
45
        if (visit[v])
46
        {
          low[u]=dpt[v]>low[u]?low[u]:dpt[v];
47
48
          continue;
49
        }
50
        dfs(v,u,deg+1);
51
        edge[i].cut=edge[i^1].cut=(low[v]>dpt[u] || edge[i].cut);
52
        if (u!=fu) cut[u]=low[v]>=dpt[u]?1:cut[u];
53
        if (low[v] > = dpt[u] \mid | u = = fu)
54
55
          while (st.top()!=i/2)
56
          {
57
            int x=st.top()*2,y=st.top()*2+1;
58
            bcc[st.top()]=idx;
59
            st.pop();
60
61
          bcc[i/2]=idx++;
62
          st.pop();
63
64
        low[u]=low[v]>low[u]?low[u]:low[v];
65
        tot++;
66
67
      if (u==fu \&\& tot>1) cut[u]=1;
68
69
   int main()
70
   {
71
      int n,m;
72
      while (scanf("%d%d",&n,&m)!=EOF)
73
      {
74
        init(n);
75
        for (int i=0; i<m; i++)
76
        {
77
          int u,v;
78
          scanf("%d%d",&u,&v);
79
          add_edge(u,v);
80
          add_edge(v,u);
        }
81
82
        idx=0;
83
        for (int i=0; i<n; i++)
84
          if (!visit[i])
85
            dfs(i,i,0);
86
87
      return 0;
88 |}
```

5.13 割点与桥

```
1 |#include<cstdio>
   |#include<cstring>
   const int MAXN=10000;
   struct edges
 5
   {
 6
     int to, next;
 7
     bool cut, visit;
     int from;
   } edge[MAXN-1<<1];</pre>
10 | int head[MAXN],low[MAXN],dfn[MAXN],L;
11 |bool visit[MAXN], cut[MAXN];
12
   void init(int n)
13
   {
14
     L=0;
15
     memset(head, -1,4*n);
     memset(cut,0,4*n);
16
17
     memset(visit,0,4*n);
18
19
   void add_edge(int u,int v)
20
   {
     edge[L].from=u;
21
22
     edge[L].cut=edge[L].visit=0;
23
     edge[L].to=v;
24
     edge[L].next=head[u];
25
     head[u]=L++;
26
27
   int idx;
28
   void dfs(int u,int fu)
29
30
     visit[u]=1;
     low[u]=dfn[u]=idx++;
31
32
     int tot=0;
33
     for (int i=head[u]; i!=-1; i=edge[i].next)
34
     {
35
       int v=edge[i].to:
       if (edge[i].visit)
36
37
          continue;
38
       edge[i].visit=edge[i^1].visit=1;
39
       if (visit[v])
40
41
          low[u]=dfn[v]>low[u]?low[u]:dfn[v];
42
          continue:
       }
43
44
       dfs(v,u);
45
       edge[i].cut=edge[i^1].cut=low[v]>dfn[u] || edge[i].cut;
46
       if (u!=fu) cut[u]=low[v]>=dfn[u]?1:cut[u];
47
       low[u]=low[v]>low[u]?low[u]:low[v];
48
       tot++;
     }
49
```

```
50
     if (u==fu && tot>1) cut[u]=1;
   }
51
52
   |int main()
53
   {
54
      int t;
55
      scanf("%d",&t);
56
      while (t—)
57
      {
58
        int n,m;
59
        scanf("%d%d",&n,&m);
60
        init(n);
61
        for (int i=0; i<m; i++)
62
        {
63
          int u,v;
          scanf("%d%d",&u,&v);
64
65
          add_edge(--u,--v);
66
          add_edge(v,u);
67
        }
68
        for (int i=0; i<n; i++)
69
          if (!visit[i])
70
          {
71
            idx=0;
72
            dfs(i,i);
73
74
75
      return 0;
76 |}
   5.14 LCA
   在线 LCA, bfs
 1 |#include<cstdio>
   #include<cstring>
 3 |#include<queue>
   using namespace std;
   const int NSIZE = 50000;
   const int DEG = 20;
 7
   struct trees
 8
   {
 9
10
      int fa[DEG];
11
      int head, deg;
   } tree[NSIZE];
13
   struct edges
14
   {
15
      int to , next;
   } edge[NSIZE];
16
17
   struct states
18
19
     int u,fu,deg;
   };
20
21 | int L;
```

```
22 | void add_edge(int x, int y)
23
   {
24
     edge[L].to = y;
25
     edge[L].next = tree[x].head;
26
     tree[x].head = L++;
27
28
   int Root:
29
   void BFS(int s)
30
   {
31
     queue<states> que;
32
     states st;
33
     st.deg=0;
34
     st.fu=st.u=s;
35
     que.push(st);
36
     while(!que.empty())
37
     {
38
       states st=que.front();
39
       que.pop();
40
       tree[st.u].deg = st.deg;
41
       tree[st.u].fa[0] = st.fu;
       for (int i=1;i<DEG;i++)</pre>
42
43
          tree[st.u].fa[i]=s;
44
       for (int tmp=st.fu,num=1;tree[tmp].deg;tmp=tree[st.u].fa[num
          ++])
45
          tree[st.u].fa[num]=tree[tmp].fa[num-1];
46
       for(int i = tree[st.u].head; i != -1; i = edge[i].next)
47
       {
48
          int v = edge[i].to;
49
          if (v == st.fu) continue;
50
          states nst;
51
         nst.u=v;
52
          nst.fu=st.u;
53
          nst.deq=st.deq+1;
54
          que.push(nst);
55
       }
56
     }
57
58
   int LCA(int x, int y)
59
60
     if(tree[x].deg > tree[y].deg) swap(x,y);
61
     int hx=tree[x].deg,hy=tree[y].deg;
62
     int tx=x,ty=y;
63
     for (int det=hy-hx, i=0; det; det>>=1, i++)
64
       if (det&1)
65
          ty=tree[ty].fa[i];
66
     if(tx == ty) return tx;
67
     for (int i=DEG-1; i>=0; i---)
68
       if(tree[tx].fa[i] == tree[ty].fa[i])
69
70
          continue;
71
       tx = tree[tx].fa[i];
```

```
72
        ty = tree[ty].fa[i];
 73
 74
      return tree[tx].fa[0];
 75
 76
    int main()
 77
    {
 78
      int t;
      scanf("%d",&t);
 79
 80
      while(t—)
 81
      {
 82
        int n;
 83
        scanf("%d",&n);
 84
        L = 0;
 85
        for(int i = 0; i < n; i++)
 86
           tree[i].head = -1;
 87
        for(int i = 0; i < n-1; i++)
 88
         {
 89
           int a,b;
          scanf("%d%d",&a ,&b);
 90
 91
           add_edge(a-1,b-1);
 92
           add_edge(b-1,a-1);
        }
 93
94
        Root=0;
 95
        BFS(Root);
 96
        int a,b;
 97
        scanf("%d%d",&a,&b);
 98
        int lca=LCA(a-1,b-1)+1;
        printf("%d\n",lca);
 99
      }
100
101
      return 0;
102 |}
          最优比例生成树
    5.15
  1 |#include<stdio.h>
    |#include<string.h>
    |#include<math.h>
  4
    struct
  5
    {
  6
      int x,y;
      double z;
  7
    } node[1100];
  9
    struct
 10
    {
 11
      double l,c;
    } map[1100][1100];
 12
    |int n,l,f[1100],pre[1100];
    double dis[1100];
 15
    double mst(double x)
 16
```

int i,j,tmp;

17

```
18
     double min, s=0, t=0;
19
     memset(f,0,sizeof(f));
20
     f[1]=1;
21
     for (i=2; i<=n; i++)
22
23
        dis[i]=map[1][i].c-map[1][i].l*x;
24
        pre[i]=1;
25
26
     for (i=1; i<n; i++)
27
     {
28
        min=1e10;
29
        for (j=1; j<=n; j++)
30
          if (!f[j] && min>dis[j])
31
32
            min=dis[j];
33
            tmp=j;
34
35
        f[tmp]=1;
36
        t+=map[pre[tmp]][tmp].1;
37
        s+=map[pre[tmp]][tmp].c;
        for (j=1; j<=n; j++)
38
39
          if (!f[j] && map[tmp][j].c-map[tmp][j].l*x<dis[j])</pre>
40
          {
41
            dis[j]=map[tmp][j].c-map[tmp][j].l*x;
42
            pre[j]=tmp;
43
          }
44
45
     return s/t;
46
   int main()
47
48
49
     int i,j;
50
     double a,b;
     scanf("%d",&n);
51
52
     while (n)
53
     {
54
        for (i=1; i<=n; i++)
55
          scanf("%d%d%lf",&node[i].x,&node[i].y,&node[i].z);
56
        for (i=1; i<=n; i++)
57
          for (j=i+1; j<=n; j++)
58
          {
59
            map[j][i].l=map[i][j].l=sqrt(1.0*(node[i].x-node[j].x)*(
               node[i].x-node[j].x)+(node[i].y-node[j].y)*(node[i].y-
               node[j].y));
60
            map[j][i].c=map[i][j].c=fabs(node[i].z-node[j].z);
61
62
        a=0,b=mst(a);
63
        while (fabs(b-a)>1e-8)
64
        {
65
          a=b;
66
          b=mst(a);
```

```
}
67
68
       printf("%.3f\n",b);
69
       scanf("%d",&n);
70
71 |}
        生成树计数
   5.16
   根据邻接矩阵构造 Laplacian matrix。
 1 | Matrix laplacian;
 2
   laplacian.clear();
   for (int i = 0; i < n; i++)
 4
     for (int j = 0; j < n; j++)
 5
     if (i != j && G[i][j])
 6
     {
 7
       laplacian.a[i][j] = -1;
       laplacian.a[i][i]++;
 8
 9
10 | printf("%d\n", laplacian.det(n-1));
         全局最小割
   5.17
 1 | #include < iostream>
   using namespace std;
   const int maxn=510;
   |int map[maxn][maxn];
 5
   int n;
 6
   void contract(int x,int y)
 7
   {
 8
     int i,j;
 9
     for (i=0; i<n; i++)
       if (i!=x) map[x][i]+=map[y][i], map[i][x]+=map[i][y];
10
11
     for (i=y+1; i<n; i++) for (j=0; j<n; j++)
12
       {
13
         map[i-1][j]=map[i][j];
14
         map[j][i-1]=map[j][i];
15
16
     n--;
17
   int w[maxn],c[maxn];
18
   int sx,tx;
19
20
   int mincut()
21
   {
22
     int i,j,k,t;
23
     memset(c,0,sizeof(c));
24
     c[0]=1;
25
     for (i=0; i<n; i++) w[i]=map[0][i];
26
     for (i=1; i+1<n; i++)
27
28
       t=k=-1;
29
       for (j=0; j<n; j++) if (c[j]==0\&w[j]>k)
```

```
30
            k=w[t=j];
31
        c[sx=t]=1;
32
        for (j=0; j< n; j++) w[j]+=map[t][j];
33
34
      for (i=0; i<n; i++) if (c[i]==0) return w[tx=i];
35
36
   int main()
37
    {
38
      int i,j,k,m;
     while (scanf("%d%d",&n,&m)!=EOF)
39
40
41
        memset(map,0,sizeof(map));
42
        while (m——)
43
44
          scanf("%d%d%d",&i,&j,&k);
          map[i][j]+=k;
45
46
          map[j][i]+=k;
        }
47
48
        int mint=999999999;
49
        while (n>1)
50
        {
51
          k=mincut();
52
          if (k<mint) mint=k;</pre>
53
          contract(sx,tx);
54
55
        printf("%d\n",mint);
56
57
      return 0;
58 }
   5.18
          欧拉路
   5.18.1 有向图
   void solve(int x)
 2
   {
 3
      int i;
 4
     if (!match[x])
 5
 6
        path[++1]=x;
 7
        return ;
 8
 9
      for (i=1; i<=n; i++)
10
        if (b[x][i])
11
        {
12
          b[x][i]--;
13
          match[x]--;
14
          solve(i);
15
16
      path[++1]=x;
   }
17
```

5.18.2 无向图

```
void solve(int x)
 2
   {
 3
      int i;
 4
      if (!match[x])
 5
 6
        path[++l]=x;
 7
        return ;
 8
 9
      for (i=1; i<=n; i++)
        if (b[x][i])
10
11
        {
          b[x][i]--;
12
          b[i][x]--;
13
          match[x]--;
14
15
          match[i]--;
16
          solve(i);
17
        }
18
      path[++1]=x;
19 |}
   5.18.3 混合图
   zju1992
   int in[MAXN+100],out[MAXN+100];
   int main()
 3
   {
 4
      int t;
 5
      scanf("%d",&t);
 6
      while (t—)
 7
      {
 8
        int n,m;
        scanf("%d%d",&n,&m);
 9
10
        N=n+2; L=-1;
11
        for (int i=0; i< N; i++)
12
          head\lceil i \rceil = -1;
13
        memset(in,0,sizeof(in));
14
        memset(out,0,sizeof(out));
15
        for (int i=0;i< m;i++)
16
17
        {
18
          int x,y,z;
          scanf("%d%d%d",&x,&y,&z);
19
20
          in[y]++;out[x]++;
21
          if (!z)
22
            add_edge(x,y,1);
        }
23
        int flag=1;
24
25
        for (int i=1; i <= n; i++)
26
        {
27
          if (in[i]-out[i]>0)
```

```
28
            add_edge(i,n+1,(in[i]-out[i])/2);
29
          else
30
          if (out[i]—in[i]>0)
31
            add_edge(0,i,(out[i]-in[i])/2);
          //printf("%d %d %d\n",i,out[i],in[i]);
32
33
          if ((in[i]+out[i])&1)
34
          {
35
            flag=0;
36
            break;
          }
37
38
39
        \max flow(0, n+1);
       for (int i=head[0];i!=-1;i=edge[i].next)
40
41
          if (edge[i].cap>0 && edge[i].cap>edge[i].flow)
42
          {
43
            flag=0;
44
            break;
45
        if (flag)
46
47
          puts("possible");
48
        else
49
          puts("impossible");
50
51
     return 0;
52 }
         K 短路
   5.19
 1 |#include<cstdio>
   |#include<cstring>
   |#include<queue>
   using namespace std;
 5
   int K;
 6
   class states
 7
   {
   public:
 8
 9
     int cost, id;
10
   };
   int dist[1000];
11
12
   class cmp
13
   {
14
   public:
15
     bool operator ()(const states &i,const states &j)
16
17
        return i.cost>j.cost;
18
   };
19
20
   class cmp2
21
   {
22
   public:
23
     bool operator ()(const states &i,const states &j)
```

```
24
     {
25
        return i.cost+dist[i.id]>j.cost+dist[j.id];
26
   };
27
28
   struct edges
29
   {
30
     int to, next, cost;
   } edger[100000],edge[100000];
31
   int headr[1000],head[1000],Lr,L;
33
   void dijkstra(int s)
34
   {
35
     states u;
36
     u.id=s;
37
     u.cost=0;
38
     dist[s]=0;
39
     priority_queue<states, vector<states>, cmp> q;
40
     q.push(u);
41
     while (!q.empty())
42
     {
43
        u=q.top();
44
        q.pop();
45
        if (u.cost!=dist[u.id]) continue;
46
        for (int i=headr[u.id]; i!=-1; i=edger[i].next)
47
        {
48
          states v=u:
49
          v.id=edger[i].to;
50
          if (dist[v.id]>dist[u.id]+edger[i].cost)
51
52
            v.cost=dist[v.id]=dist[u.id]+edger[i].cost;
53
            q.push(v);
54
55
       }
     }
56
57
   int num[1000];
58
59
   void init(int n)
60
   {
61
     Lr=L=0;
62
     memset(head, -1,4*n);
63
     memset(headr,-1,4*n);
64
     memset(dist,63,4*n);
65
     memset(num, 0, 4*n);
66
67
   void add_edge(int u,int v,int x)
68
69
     edge[L].to=v;
70
     edge[L].cost=x;
71
     edge[L].next=head[u];
     head[u]=L++;
72
73
     edger[Lr].to=u;
74
     edger[Lr].cost=x;
```

```
75
      edger[Lr].next=headr[v];
 76
      headr[v]=Lr++;
 77
 78
    int a_star(int s,int t)
 79
 80
      if (dist[s]=0x3f3f3f3f)
 81
         return -1;
 82
      priority_queue<states, vector<states>, cmp2> q;
 83
      states tmp;
 84
      tmp.id=s;
 85
      tmp.cost=0;
 86
      q.push(tmp);
 87
      while (!q.empty())
 88
      {
 89
         states u=q.top();
 90
         q.pop();
 91
         num[u.id]++;
 92
         if (num[t]==K)
 93
           return u.cost;
 94
         for (int i=head[u.id]; i!=-1; i=edge[i].next)
 95
         {
 96
           int v=edge[i].to;
97
           tmp.id=v;
 98
           tmp.cost=u.cost+edge[i].cost;
 99
           q.push(tmp);
100
         }
      }
101
102
      return -1;
103
104
    int main()
105
    {
106
      int n,m;
      scanf("%d%d",&n,&m);
107
108
      init(n);
109
      for (int i=0; i<m; i++)
110
      {
111
         int u,v,x;
112
         scanf("%d%d%d",&u,&v,&x);
113
         add_edge(u-1,v-1,x);
      }
114
115
      int s,t;
      scanf("%d%d%d",&s,&t,&K);
116
117
      if (s==t)
118
         K++;
119
      dijkstra(t-1);
120
      printf("%d\n",a_star(s-1,t-1));
121 }
```

5.20 稳定婚姻

假定有 n 个男生和 个女生,理想的拍拖状态就是对于每对情侣 (a,b),找不到另一对情侣 (c,d) 使得 c 更喜欢 b,b 也更喜欢 c,同理,对 a 来说也没有 (e,f) 使得 a 更喜欢 e 而 e 更喜

欢 a_1 当然最后会有一些人落单。这样子一个状态可以称为理想拍拖状态,它也有一个专业的名词叫稳定婚姻。

求解这个问题可以用一个专有的算法,延迟认可算法,其核心就是让每个男生按自己喜欢的顺序逐个向女生表白,例如 leokan 向一个女生求爱,这个过程中,若这个女生没有男朋友,那么这个女生就暂时成为 leokan 的女朋友,或这个女生喜欢她现有男朋友的程度没有喜欢leokan 高,这个女生也暂时成为 leokan 的女朋友,而她原有的男朋友则再将就找下一个次喜欢的女生来当女朋友。

```
1 |#include<strina.h>
   #include<stdio.h>
 3
   #define N 1050
   int boy[N][N];
   int girl[N][N];
   int ans[N];
 7
   int cur[N];
   int n;
 9
   void getMarry(int g)
10
11
      for (int i=ans[a]+1;i<n;i++)
12
      {
13
        int b=girl[g][i]-1;
14
        if (cur[b]<0)
15
        {
16
          ans[g]=i;
17
          cur[b]=q;
18
          return;
        }
19
20
        int og=cur[b];
21
        if (boy[b][og] > boy[b][g])
22
23
          cur[b]=g;
24
          ans[q]=i;
25
          getMarry(og);
26
          return;
27
        }
     }
28
29
30
   int main()
31
   {
32
      int t,a;
      scanf("%d",&t);
33
34
      while(t--)
35
      {
        memset(girl,0,sizeof(girl));
36
37
        memset(boy,0,sizeof(boy));
38
        scanf("%d",&n);
39
        for (int i=0; i< n; i++)
          for (int j=0; j< n; j++)
40
            scanf("%d",&girl[i][j]);
41
42
        for (int i=0; i< n; i++)
43
          for (int j=0; j< n; j++)
44
          {
```

```
45
            scanf("%d",&a);
46
            boy[i][a-1]=j;
         }
47
48
       memset(cur,0xff,sizeof(cur));
49
       memset(ans,0xff,sizeof(ans));
50
       for (int i=0; i< n; i++)
51
          getMarry(i);
52
       for (int i=0;i< n;i++)
53
         printf("%d\n",girl[i][ans[i]]);
54
55
     return 0;
56 |}
         最小树形图
   5.21
   const int inf = 19921005;
 2
   int n,m,u,v,cost,dis[1001][1001],L;
 3
 4
   void init(int n)
 5
   {
 6
     L = 0;
 7
     for (int i = 0; i < n; i++)
 8
       for (int j = 0; j < n; j++)
 9
          dis[i][j] = inf;
10
   }
11
12
   struct Edge
13
14
     int u,v,cost;
15
   };
16
17
   Edge e[1001*1001];
18
19
   int pre[1001],id[1001],visit[1001],in[1001];
20
21
   int zhuliu(int root,int n,int m,Edge e[])
22
   {
23
     int res = 0,u,v;
24
     while (true)
25
     {
26
       for (int i = 0; i < n; i++)
27
          in[i] = inf;
28
       for (int i = 0; i < m; i++)
29
          if (e[i].u != e[i].v && e[i].cost < in[e[i].v])
30
          {
31
            pre[e[i].v] = e[i].u;
32
            in[e[i].v] = e[i].cost;
33
          }
34
       for (int i = 0; i < n; i++)
35
         if (i != root)
36
            if (in[i] == inf)
                                 return -1;
```

```
37
        int tn = 0;
       memset(id,-1,sizeof(id));
38
39
        memset(visit,-1,sizeof(visit));
40
        in[root] = 0;
41
        for (int i = 0; i < n; i++)
42
43
          res += in[i];
44
          V = i;
45
          while (visit[v] != i && id[v] == -1 && v != root)
46
          {
47
            visit[v] = i;
48
            v = pre[v];
49
50
          if(v != root && id[v] == -1)
51
52
            for(int u = pre[v]; u != v; u = pre[u])
53
              id[u] = tn;
54
            id[v] = tn++;
55
          }
56
        }
57
        if(tn == 0) break;
58
        for (int i = 0; i < n; i++)
59
          if (id[i] == -1)
60
            id[i] = tn++;
61
        for (int i = 0; i < m;)
62
63
          int v = e[i].v;
64
          e[i].u = id[e[i].u];
65
          e[i].v = id[e[i].v];
          if (e[i].u != e[i].v)
66
67
            e[i++].cost = in[v];
68
          else
69
            swap(e[i],e[--m]);
70
        }
71
        n = tn;
72
        root = id[root];
73
74
     return res;
   }
75
76
77
   int main()
78
79
     freopen("in.txt","r",stdin);
     while (scanf("%d%d",&n,&m) != EOF)
80
81
        init(n);
82
83
        for (int i = 0; i < m; i++)
84
85
          scanf("%d%d%d",&u,&v,&cost);
86
          if (u == v) continue;
87
          dis[u][v] = min(dis[u][v],cost);
```

```
}
 88
 89
           L = 0;
           for (int i = 0; i < n; i++)
  for (int j = 0; j < n; j++)
    if (dis[i][j] != inf)</pre>
 90
 91
 92
 93
                 {
                    e[L].u = i;
 94
 95
                    e[L].v = j;
                    e[L++].cost = dis[i][j];
 96
 97
 98
           printf("%d\n",zhuliu(0,n,L,e));
         }
 99
100
        return 0;
101 }
```

6 计算几何

6.1 注意事项

如果用整数小心越界(多次乘法?) 如果用浮点数判断的时候一定要用 eps!

6.2 基本函数

6.2.1 Point 定义

```
1
   struct Point
 2
   {
 3
     double x, y;
 4
     Point() {}
 5
     Point(double _x, double _y)
 6
     {
 7
        X = X, y = y;
 8
 9
     Point operator -(const Point &b)const
10
11
        return Point(x-b.x, y-b.y);
12
13
     double operator *(const Point &b)const
14
     {
15
        return x*b.y-y*b.x;
16
17
     double operator &(const Point &b)const
18
19
        return x*b.x+y*b.y;
20
21
     void transXY(double B)
22
23
        double tx = x, ty = y;
24
        x = tx*cos(B)-ty*sin(B);
25
        y = tx*sin(B)+ty*cos(B);
26
27 \};
   6.2.2 Line 定义
   struct Line
 1
 2
   {
 3
     Point s, e;
 4
     double k;
 5
     Line() {}
 6
     Line(Point _s, Point _e)
 7
 8
        s = _s, e = _e;
 9
        k = atan2(e.y-s.y, e.x-s.x);
10
     }
```

```
11
     Point operator &(const Line &b)const
12
13
       Point res = s;
14
       //注意: 有些题目可能会有直线相交或者重合情况
15
       //可以把返回值改成 pair<Point,int> 来返回两直线的状态。
16
       double t = ((s-b.s)*(b.s-b.e))/((s-e)*(b.s-b.e));
17
       res.x += (e.x-s.x)*t;
18
       res.y += (e.y-s.y)*t;
19
       return res;
20
21 | };
   6.2.3 距离:点到直线距离
   result: 点到直线最近点
 1 | Point NPT(Point P, Line L)
 2
   {
 3
     Point result;
 4
     double a, b, t;
 5
 6
     a = L.e.x-L.s.x;
 7
     b = L.e.y-L.s.y;
 8
     t = ((P.x-L.s.x)*a+(P.y-L.s.y)*b)/(a*a+b*b);
 9
     result.x = L.s.x+a*t;
10
     result.y = L.s.y+b*t;
11
12
     return dist(P, result);
13 | }
   6.2.4 距离: 点到线段距离
   res: 点到线段最近点
1 | Point NearestPointToLineSeg(Point P, Line L)
 2
   {
 3
     Point result;
 4
     double a, b, t;
 5
 6
     a = L.e.x-L.s.x;
 7
     b = L.e.y-L.s.y;
     t = ((P.x-L.s.x)*a+(P.y-L.s.y)*b)/(a*a+b*b);
 8
 9
10
     if (t >= 0 \&\& t <= 1)
11
     {
12
       result.x = L.s.x+a*t;
13
       result.y = L.s.y+b*t;
     }
14
     else
15
16
     {
17
       if (dist(P,L.s) < dist(P,L.e))
18
         result = L.s;
19
       else
20
         result = L.e;
```

```
21
     }
22
     return result;
23 |}
   旧版
 1 | double CalcDis(Point a, Point s, Point e) //点到线段距离
 2
   {
 3
     if (sgn((e-s)*(a-s)) < 0 \mid sgn((s-e)*(a-e)) < 0)
       return min(dist(a,s),dist(a,e));
 5
     return abs(((s-a)*(e-a))/dist(s-e));
 6
   }
        面积:多边形
   6.2.5
   点按逆时针排序。
   |double CalcArea(Point p∏, int n)
 2
   {
 3
     double res = 0;
     for (int i = 0; i < n; i++)
 5
       res += (p[i]*p[(i+1) % n])/2;
 6
     return res;
   }
   6.2.6 判断: 线段相交
 1 |bool inter(Line l1,Line l2)
 2
 3
     return
 4
     max(l1.s.x, l1.e.x) >= min(l2.s.x, l2.e.x) &&
 5
     max(12.s.x,12.e.x) >= min(11.s.x,11.e.x) &&
     max(l1.s.y, l1.e.y) >= min(l2.s.y, l2.e.y) &&
 6
 7
     max(l2.s.y, l2.e.y) >= min(l1.s.y, l1.e.y) &&
     sgn((l2.s-l1.s)*(l1.e-l1.s))*sgn((l2.e-l1.s)*(l1.e-l1.s)) <= 0 \&\&
 8
     sgn((l1.s-l2.s)*(l2.e-l2.s))*sgn((l1.e-l2.s)*(l2.e-l2.s)) <= 0;
9
10 | }
   6.2.7 判断: 点在线段上
 1 |bool OnSeg(Line a,Point b)
 2
 3
     return ((a.s-b)*(a.e-b) == 0 \&\&
 4
         (b.x-a.s.x)*(b.x-a.e.x) <= 0 &&
 5
         (b.y-a.s.y)*(b.y-a.e.y) <= 0);
 6
   |}
   6.2.8 判断:点在多边形内
   凸包且按逆时针排序
 1 |bool inPoly(Point a,Point p[],int n)
 2
 3
     for (int i = 0; i < n; i++)
       if ((p[i]-a)*(p[(i+1)%n]-a) < 0)
```

```
5
         return false;
 6
     return true;
  }
   射线法, 多边形可以是凸的或凹的
   poly 的顶点数目要大于等于 3
   返回值为:
   0 - 点在 poly 内
   1 - 点在 polv 边界上
   2 - 点在 poly 外
 1 | int inPoly(Point p,Point poly[], int n)
 2
   {
 3
     int i, count;
 4
     Line ray, side;
 5
 6
     count = 0;
 7
     ray.s = p;
 8
     ray.e.y = p.y;
 9
     ray.e.x = -1;//-INF, 注意取值防止越界!
10
11
     for (i = 0; i < n; i++)
12
     {
13
       side.s = poly[i];
14
       side.e = poly[(i+1)\%n];
15
16
       if(OnSeg(p, side))
17
         return 1;
18
19
       // 如果平行轴则不作考虑sidex
20
       if (side.s.y == side.e.y)
21
         continue;
22
23
       if (OnSeq(side.s, ray))
24
       {
25
         if (side.s.y > side.e.y) count++;
26
27
       else if (OnSeg(side.e, ray))
28
29
         if (side.e.y > side.s.y) count++;
30
31
       else if (inter(ray, side))
32
33
         count++;
34
       }
35
36
     return ((count \% 2 == 1) ? 0 : 2);
  }
37
```

6.2.9 判断: 两凸包相交

需要考虑这几个:一个凸包的点在另外一个图包内(包括边界);一个凸包的某条边与另一个 凸包某条边相交;如果凸包可能退化成点线还需要判断点在线段上和点和点重合。

6.2.10 排序: 叉积极角排序

```
|bool cmp(const Point& a,const Point& b)
 2
   {
 3
     if (a.y*b.y <= 0)
 4
 5
       if (a.y > 0 \mid | b.y > 0) return a.y < b.y;
 6
       if (a.y == 0 \& b.y == 0) return a.x < b.x;
 7
 8
     return a*b > 0;
   }
        三维几何
   6.3
   6.3.1 Point 定义
  |struct Point3D
 1
 2
   {
 3
     double x,y,z;
 4
     Point3D() {}
 5
     Point3D(double _x,double _y,double _z)
 6
     {
 7
       X = _X;
 8
       y = _y;
 9
       z = _z;
10
11
     Point3D operator -(const Point3D& b)const
12
     {
13
       return Point3D(x-b.x,y-b.y,z-b.z);
14
     Point3D operator *(const Point3D& b)const
15
16
       return Point3D(y*b.z-z*b.y,z*b.x-x*b.z,x*b.y-y*b.x);
17
18
19
     double operator &(const Point3D& b)const
20
21
       return x*b.x+y*b.y+z*b.z;
22
   };
23
24
   //模
25
   double Norm(Point3D p)
26
27
     return sqrt(p&p);
28
   //绕单位向量 V 旋转 \theta 角度
   Point3D Trans(Point3D pa,Point3D V,double theta)
30
31
32
     double s = sin(theta);
33
     double c = cos(theta);
34
     double x,y,z;
35
     x = V.x;
36
     y = V.y;
```

```
37
       z = V.z;
38
       Point3D pp =
       Point3D(
39
         (x*x*(1-c)+c)*pa.x+(x*y*(1-c)-z*s)*pa.y+(x*z*(1-c)+y*s)*pa.z,
40
         (y*x*(1-c)+z*s)*pa.x+(y*y*(1-c)+c)*pa.y+(y*z*(1-c)-x*s)*pa.z,
41
42
         (x*z*(1-c)-y*s)*pa.x+(y*z*(1-c)+x*s)*pa.y+(z*z*(1-c)+c)*pa.z);
43
       return pp;
44 }
    6.3.2 经度纬度转换
    直角坐标系与极坐标系转换:
       \begin{cases} x = r \times \sin\theta \times \cos\varphi \\ y = r \times \sin\theta \times \sin\varphi \\ z = r \times \cos\theta \end{cases} \begin{cases} r = \sqrt{x \times 2 + y \times 2 + z \times 2} \\ \varphi = \arctan(\frac{y}{x}) \\ \theta = \arccos(\frac{z}{r}) \end{cases} \qquad r \in [0, +\infty), \varphi \in [0, 2\pi], \theta \in [0, \pi]
    经度维度转换(lat1 \in (-\frac{\pi}{2}, \frac{\pi}{2}), lng1 \in (-\pi, \pi))
 1 | Point3D getPoint3D(double lat, double lng, double r)
 2
    {
 3
       lat += pi/2;
 4
      lng += pi;
 5
       return
         Point3D(r*sin(lat)*cos(lng),r*sin(lat)*sin(lng),r*cos(lat));
 7 }
    6.3.3 判断: 直线相交
 1 | bool LineIntersect(Line3D L1, Line3D L2)
 2
 3
       Point3D s = L1.s-L1.e;
       Point3D e = L2.s-L2.e;
       Point3D p = s*e;
 5
       if (ZERO(p)) return false; //是否平行
 7
       p = (L2.s-L1.e)*(L1.s-L1.e);
 8
       return ZERO(p&L2.e); //是否共面
 9 |}
    6.3.4 判断:线段相交
    需要先判断是否在一个平面上:
 1 | bool inter(Point a, Point b, Point c, Point d)
 2
    {
 3
       Point ret = (a-b)*(c-d);
 4
       Point t1 = (b-a)*(c-a);
       Point t2 = (b-a)*(d-a);
 5
 6
       Point t3 = (d-c)*(a-c);
 7
       Point t4 = (d-c)*(b-c);
 8
       return sqn(t1&ret)*sqn(t2&ret) < 0 &&
 9
                sgn(t3&ret)*sgn(t4&ret) < 0;
10 }
```

```
6.3.5 判断:三维向量是否为 0
  |inline bool ZERO(Point3D p)
2
3
     return (ZERO(p.x) && ZERO(p.y) && ZERO(p.z));
4 |}
   6.3.6 判断: 点在直线上
1 |bool OnLine(Point3D p, Line3D L)
2
   {
3
     return ZERO((p-L.s)*(L.e-L.s));
   }
   6.3.7 判断: 点在线段上
1 | bool OnSeg(Point3D p, Line3D L)
2
3
     return (ZERO((L.s-p)*(L.e-p)) &&
       EQ(Norm(p-L.s)+Norm(p-L.e),Norm(L.e-L.s)));
5
   }
   6.3.8 距离: 点到直线
1 | double Distance(Point3D p, Line3D L)
2
3
     return (Norm((p-L.s)*(L.e-L.s))/Norm(L.e-L.s));
   }
   6.3.9 夹角
   返回值是 [0,\pi] 之间的弧度
1 | double Inclination(Line3D L1, Line3D L2)
2
   {
3
     Point3D u = L1.e - L1.s;
     Point3D v = L2.e - L2.s;
5
     return acos( (u \& v) / (Norm(u)*Norm(v)));
6 |}
        员
   6.4
   6.4.1 面积:两圆相交
   圆不可包含
1 | double dis(int x,int y)
2
3
     return sqrt((double)(x*x+y*y));
   double area(int x1,int y1,int x2,int y2,double r1,double r2)
6
7
     double s=dis(x2-x1,y2-y1);
8
     if(r1+r2<s) return 0;
9
     else if(r2-r1>s) return PI*r1*r1;
10
     else if(r1-r2>s) return PI*r2*r2;
```

```
11
     double q1=acos((r1*r1+s*s-r2*r2)/(2*r1*s));
12
     double q2=acos((r2*r2+s*s-r1*r1)/(2*r2*s));
13
     return (r1*r1*q1+r2*r2*q2-r1*s*sin(q1));
14 | }
   6.4.2 三角形外接圆
   void CircumscribedCircle()
 2
   {
 3
     for (int i = 0; i < 3; i++)
     scanf("%lf%lf",&p[i].x,&p[i].y);
tp = Point((p[0].x+p[1].x)/2,(p[0].y+p[1].y)/2);
 4
 5
     l[0] = Line(tp, Point(tp.x-(p[1].y-p[0].y), tp.y+(p[1].x-p[0].x)));
 6
     tp = Point((p[0].x+p[2].x)/2,(p[0].y+p[2].y)/2);
 7
     l[1] = Line(tp, Point(tp.x-(p[2].y-p[0].y), tp.y+(p[2].x-p[0].x)));
 8
 9
     tp = LineToLine(l[0],l[1]);
     r = Point(tp,p[0]).Length();
10
     printf("(%.6f,%.6f,%.6f)\n",tp.x,tp.y,r);
11
12 |}
   6.4.3 三角形内切圆
 1 |void InscribedCircle()
 2
   {
 3
     for (int i = 0; i < 3; i++)
       scanf("%lf%lf",&p[i].x,&p[i].y);
 4
     if (xmult(Point(p[0],p[1]),Point(p[0],p[2])) < 0)
 5
 6
       swap(p[1], p[2]);
 7
     for (int i = 0; i < 3; i++)
 8
       len[i] = Point(p[i],p[(i+1)%3]).Length();
     tr = (len[0]+len[1]+len[2])/2;
 9
     r = sqrt((tr-len[0])*(tr-len[1])*(tr-len[2])/tr);
10
11
     for (int i = 0; i < 2; i++)
12
13
       v = Point(p[i], p[i+1]);
14
       tv = Point(-v.y,v.x);
15
       tr = tv.Length();
16
       tv = Point(tv.x*r/tr,tv.y*r/tr);
17
       tp = Point(p[i].x+tv.x,p[i].y+tv.y);
18
       l[i].s = tp;
19
       tp = Point(p[i+1].x+tv.x,p[i+1].y+tv.y);
20
       l[i].e = tp;
21
22
     tp = LineToLine(l[0],l[1]);
23
     printf("(\%.6f,\%.6f,\%.6f)\n",tp.x,tp.y,r);
24 }
   6.4.4 点对圆的两个切点
 1 | void calc_qie(Point poi, Point o, double r, Point & result1, Point &
      result2)
 2 | {
```

```
3
     double line = sqrt((poi.x-o.x)*(poi.x-o.x)+(poi.y-o.y)*(poi.y-o.y)
        ));
 4
     double angle = acos(r/line);
     Point unitvector, lin;
 5
 6
     lin.x = poi.x-o.x;
 7
     lin.y = poi.y-o.y;
     unitvector.x = lin.x/sqrt(lin.x*lin.x+lin.y*lin.y)*r;
 8
 9
     unitvector.y = lin.y/sqrt(lin.x*lin.x+lin.y*lin.y)*r;
     result1 = unitvector.Rotate(-angle);
10
11
     result2 = unitvector.Rotate(angle);
12
     result1.x += o.x;
     result1.y += o.y;
13
14
     result2.x += o.x;
15
     result2.y += o.y;
16 }
        两圆公切点
   6.4.5
 1 |void Gao()
 2
   {
 3
     tn = 0;
     Point a,b,vab;
 4
 5
     double tab, tt, dis, theta;
     for (int i = 0; i < tc; i++)
 6
 7
       for (int j = 0; j < tc; j++)
 8
          if (i != j)
 9
10
           a = c[i];
11
            b = c[j];
12
           vab = Point(a,b);
13
            tab = atan2(vab.y, vab.x);
14
            dis = sqrt(vab.x*vab.x+vab.y*vab.y);
15
            if (b.r > a.r)
16
              tt = asin((b.r-a.r)/dis);
17
            else
18
              tt = -asin((a.r-b.r)/dis);
19
           theta = tab+pi/2+tt;
20
            tp[tn++] = Point(a.x+a.r*cos(theta),a.y+a.r*sin(theta));
21
            tp[tn++] = Point(b.x+b.r*cos(theta),b.y+b.r*sin(theta));
22
         }
23 |}
   6.4.6
         两圆交点
  |lab = Point(p[j].x-p[i].x,p[j].y-p[i].y);
   AB = lab.Length();
   AC = cr[i];
   BC = cr[j];
 5
   if (cmp(AB+AC,BC) <= 0) continue;//包含
   if (cmp(AB+BC,AC) <= 0) continue;
   if (cmp(AB,AC+BC) > 0) continue;//相离
 9
```

```
10 | theta = atan2(lab.y,lab.x);

11 | fai = acos((AC*AC+AB*AB-BC*BC)/(2.0*AC*AB));

12 | a0 = theta-fai;

13 | if (cmp(a0,-pi) < 0) | a0 += 2*pi;

14 | a1 = theta+fai;

15 | if (cmp(a1,pi) > 0) | a1 -= 2*pi;

16 | //答案

17 | xp[totp++] = Point(p[i].x+cr[i]*cos(a0),p[i].y+cr[i]*sin(a0));

18 | xp[totp++] = Point(p[i].x+cr[i]*cos(a1),p[i].y+cr[i]*sin(a1));
```

6.5 三角形相关

- 费马点: 在 $\triangle ABC$ 内求一点 P, 使 PA + PB + PC 之值为最小的点。当三角形有一个内角大于或等于 120 的时候,费马点就是该内角的顶点若没有,则费马点就是使得该点至三角形三顶点的连线两两夹角为 120 度的点.
- 等角共轭点: 对于三角形内任意一点 P, 过 A 做直线 L_1 与 AP 关于角 A 的角平分线对称, 同样过 B,C 分别做 L_2 , L_3 . 这三条直线交于 P_1 , 则 P_1 是 P 的等角共轭点. 重心的等角共轭点到三边距离的平方和最小的点.
- 6.6 矩阵
- 6.6.1 基本矩阵

按向量 (x,y,z) 平移:

$$\begin{pmatrix} 1 & 0 & 0 & x \\ 0 & 1 & 0 & y \\ 0 & 0 & 1 & z \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

按比例 (x,y,z) 缩放:

$$\begin{pmatrix} x & 0 & 0 & 0 \\ 0 & y & 0 & 0 \\ 0 & 0 & z & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

绕单位向量 (x,y,z) 旋转 angle 角度:

$$\begin{pmatrix} x^2 \times (1-c) + c & x \times y \times (1-c) - z \times s & x \times z \times (1-c) + y \times s & 0 \\ y \times x \times (1-c) + z \times s & y^2 \times (1-c) + c & y \times z \times (1-c) - x \times s & 0 \\ x \times z \times (1-c) - y \times s & y \times z \times (1-c) + x \times s & z^2 \times (1-c) + c & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{cases} s = sin(angle) \\ c = cos(angle) \end{cases}$$

以上矩阵变换都把点当作列向量,旋转角度的正负由右手定则决定

6.6.2 刘汝佳的几何教室

```
const double pi = acos(-1.0);
 2
 3
   int n,m,q;
 4
   struct Point
 5
   {
 6
     double a,b,c,d;
   };
 7
 8
   Point p[50000],f[50000];
9
   |double a,b,c,theta,mt[4][4],tmp[4][4],tmt[4][4],rmt[4][8];
11
   char com[20];
12
13
   void TRANSLATE()
14
15
     memset(tmt,0,sizeof(tmt));
16
     tmt[0][0] = tmt[1][1] = tmt[2][2] = tmt[3][3] = 1;
17
     tmt[3][0] = a;
18
     tmt[3][1] = b;
19
     tmt[3][2] = c;
20
     memset(tmp,0,sizeof(tmp));
     for (int i = 0; i < 4; i++)
21
22
       for (int j = 0; j < 4; j++)
         for (int k = 0; k < 4; k++)
23
24
            tmp[i][j] += mt[i][k]*tmt[k][j];
25
     for (int i = 0; i < 4; i++)
26
       for (int j = 0; j < 4; j++)
27
         mt[i][j] = tmp[i][j];
   }
28
29
30
   void ROTATE()
31
32
     theta = -theta*pi/180;
33
     memset(tmt,0,sizeof(tmt));
34
     tmt[3][3] = 1;
35
     tmt[0][0] = cos(theta) + (1-cos(theta))*a*a;
     tmt[1][0] = (1-cos(theta))*a*b+c*sin(theta);
36
37
     tmt[2][0] = (1-cos(theta))*a*c-b*sin(theta);
38
     tmt[0][1] = (1-cos(theta))*a*b-c*sin(theta);
39
     tmt[1][1] = cos(theta) + (1-cos(theta))*b*b;
40
     tmt[2][1] = (1-cos(theta))*b*c+a*sin(theta);
41
     tmt[0][2] = (1-cos(theta))*a*c+b*sin(theta);
     tmt[1][2] = (1-cos(theta))*b*c-a*sin(theta);
42
43
     tmt[2][2] = cos(theta)+(1-cos(theta))*c*c;
44
     memset(tmp,0,sizeof(tmp));
45
     for (int i = 0; i < 4; i++)
46
       for (int j = 0; j < 4; j++)
47
         for (int k = 0; k < 4; k++)
48
            tmp[i][j] += mt[i][k]*tmt[k][j];
     for (int i = 0; i < 4; i++)
49
50
       for (int j = 0; j < 4; j++)
51
         mt[i][j] = tmp[i][j];
```

```
52 |}
 53
 54
    void SCALE()
 55
    {
 56
      memset(tmt,0,sizeof(tmt));
 57
      tmt[0][0] = a;
 58
      tmt[1][1] = b;
 59
      tmt[2][2] = c;
      tmt[3][3] = 1;
 60
 61
      memset(tmp,0,sizeof(tmp));
 62
      for (int i = 0; i < 4; i++)
        for (int j = 0; j < 4; j++)
 63
64
           for (int k = 0; k < 4; k++)
 65
             tmp[i][j] += mt[i][k]*tmt[k][j];
 66
      for (int i = 0; i < 4; i++)
         for (int j = 0; j < 4; j++)
 67
 68
           mt[i][j] = tmp[i][j];
    }
 69
 70
 71
    void solvep(Point p)
 72
    {
 73
      memset(tmt,0,sizeof(tmt));
 74
      tmt[0][0] = p.a;
 75
      tmt[0][1] = p.b;
 76
      tmt[0][2] = p.c;
 77
      tmt[0][3] = 1;
 78
      memset(tmp,0,sizeof(tmp));
      for (int i = 0; i < 1; i++)
 79
         for (int j = 0; j < 4; j++)
 80
           for (int k = 0; k < 4; k++)
 81
             tmp[i][j] += tmt[i][k]*mt[k][j];
 82
      printf("%.2f_{\bot}%.2f_{\bot}%.2f_{n}",tmp[0][0],tmp[0][1],tmp[0][2]);
 83
    }
 84
 85
 86
    void solvef(Point f)
 87
    {
 88
      memset(tmt,0,sizeof(tmt));
 89
      tmt[0][0] = f.a;
 90
      tmt[1][0] = f.b;
 91
      tmt[2][0] = f.c;
      tmt[3][0] = 0;
 92
      memset(tmp,0,sizeof(tmp));
 93
 94
      for (int i = 0; i < 4; i++)
 95
         for (int j = 0; j < 1; j++)
 96
           for (int k = 0; k < 4; k++)
 97
             tmp[i][j] += mt[i][k]*tmt[k][j];
 98
      tmp[3][0] += f.d;
 99
      double kk = tmp[0][0]*tmp[0][0]+tmp[1][0]*tmp[1][0]+tmp[2][0]*tmp
         [2][0];
100
      kk = sart(1/kk);
101
      for (int i = 0; i < 4; i++)
```

```
102
        103
      printf("\n");
    }
104
105
106
    void solvermt()
107
    {
108
      memset(rmt,0,sizeof(rmt));
      for (int i = 0; i < 4; i++)
109
        for (int j = 0; j < 4; j++)
110
111
           rmt[i][j] = mt[i][j];
      rmt[0][4] = rmt[1][5] = rmt[2][6] = rmt[3][7] = 1;
112
113
      for (int i = 0; i < 4; i++)
114
      {
115
        for (int j = i; j < 4; j++)
          if (fabs(rmt[j][i]) > 1e-8)
116
117
118
             for (int k = i; k < 8; k++)
119
               swap(rmt[i][k],rmt[j][k]);
120
            break;
121
        double tt = rmt[i][i];
122
123
        for (int j = i; j < 8; j++)
          rmt[i][j] /= tt;
124
125
        for (int j = 0; j < 4; j++)
126
          if (i != i)
127
          {
128
            tt = rmt[j][i];
129
             for (int k = i; k < 8; k++)
130
               rmt[j][k] -= rmt[i][k]*tt;
          }
131
132
133
      for (int i = 0; i < 4; i++)
134
        for (int j = 0; j < 4; j++)
135
          mt[i][j] = rmt[i][4+j];
    }
136
137
138
    int main()
139
    {
140
      scanf("%d%d%d",&n,&m,&q);
141
      for (int i = 0; i < n; i++)
        scanf("%lf%lf%lf",&p[i].a,&p[i].b,&p[i].c);
142
      for (int i = 0; i < m; i++)
143
144
        scanf("%lf%lf%lf%lf",&f[i].a,&f[i].b,&f[i].c,&f[i].d);
145
      memset(mt,0,sizeof(mt));
      mt[0][0] = mt[1][1] = mt[2][2] = mt[3][3] = 1;
146
147
      for (int i = 0; i < q; i++)
148
      {
149
        scanf("%s",com);
        if (strcmp(com, "TRANSLATE") == 0)
150
151
        {
152
          scanf("%lf%lf%lf",&a,&b,&c);
```

```
153
          TRANSLATE();
154
        }
155
        else if (strcmp(com, "ROTATE") == 0)
156
        {
157
           scanf("%lf%lf%lf%lf",&a,&b,&c,&theta);
158
          ROTATE();
159
        }
        else if (strcmp(com, "SCALE") == 0)
160
161
           scanf("%lf%lf%lf",&a,&b,&c);
162
163
           SCALE();
164
        }
165
      }
      //处理点
166
167
      for (int i = 0; i < n; i++)
168
        solvep(p[i]);
169
      //处理面
170
      solvermt();
171
      for (int i = 0; i < m; i++)
172
        solvef(f[i]);
173
      return 0;
174 }
    6.7 重心
   |Point CenterOfPolygon(Point poly[],int n)
  1
  2
    {
  3
      Point p, p0, p1, p2, p3;
  4
      double m, m0;
      p1 = poly[0];
  5
  6
      p2 = poly[1];
  7
      p.x = p.y = m = 0;
      for (int i = 2; i < n; i++)
  8
  9
      {
 10
        p3 = poly[i];
 11
        p0.x = (p1.x + p2.x + p3.x) / 3.0;
 12
        p0.y = (p1.y + p2.y + p3.y) / 3.0;
 13
        m0 = p1.x*p2.y+p2.x*p3.y+p3.x*p1.y-p1.y*p2.x-p2.y*p3.x-p3.y*p1.
           х;
 14
        if (cmp(m + m0, 0.0) == 0)
 15
        m0 += eps;
 16
        p.x = (m * p.x + m0 * p0.x) / (m + m0);
 17
        p.y = (m * p.y + m0 * p0.y) / (m + m0);
 18
        m = m + m0;
 19
        p2 = p3;
 20
      }
 21
      return p;
 22 |}
```

查找某个点距离最近的点,基本思想是每次分治把点分成两部分,建议按照坐标规模决定是 垂直划分还是水平划分,查找时先往分到的那一部分查找,然后根据当前最优答案决定是否

KD 树

6.8

```
去另一个区间查找。
  |bool Div[MaxN];
   void BuildKD(int deep,int l, int r, Point p[])\\记得备份一下 P
 3
   {
 4
     if (l > r) return;
 5
     int mid = l + r \gg 1;
     int minX, minY, maxX, maxY;
 6
 7
     minX = min_element(p + l, p + r + 1, cmpX) -> x;
     minY = min_element(p + l, p + r + 1, cmpY) -> y;
 8
9
     maxX = max\_element(p + l, p + r + 1, cmpX) -> x;
     maxY = max_element(p + l, p + r + 1, cmpY) -> y;
10
11
     Div[mid] = (maxX - minX >= maxY - minY);
12
     nth_element(p + l, p + mid, p + r + 1, Div[mid] ? cmpX : cmpY);
13
     BuildKD(l, mid -1, p);
14
     BuildKD(mid + 1, r, p);
15
   }
16
17
   long long res;
18
   void Find(int l, int r, Point a, Point p[])\\查找
19
   {
20
     if (l > r) return;
21
     int mid = l + r \gg 1;
22
     long long dist = dist2(a, p[mid]);
23
     if (dist > 0)//如果有重点不能这样判断
24
       res = min(res, dist);
25
     long long d = Div[mid] ? (a.x - p[mid].x) : (a.y - p[mid].y);
     int 11, 12, r1, r2;
26
     11 = 1, 12 = mid + 1;
27
     r1 = mid - 1, r2 = r;
28
29
     if (d > 0)
30
       swap(11, 12), swap(r1, r2);
     Find(l1, r1, a, p);
31
32
     if (d * d < res)
33
       Find(12, r2, a, p);
34 }
   6.8.1 例题
   查询一个点为中心的给定正方形内所有点并删除(2012 金华网赛 A)
 1 | #include <iostream>
 2 |#include <cstdio>
   #include <cstring>
   |#include <algorithm>
 5
   #include <cmath>
 6 | #include <queue>
7
   using namespace std;
 8
9
   const int MaxN = 100000;
10 | struct Point
```

```
11 | {
12
     int x,y,r;
13
     int id;
14
     bool del;
   };
15
16
17
   int cmpTyp;
18
   bool cmp(const Point& a,const Point& b)
19
20
     if (cmpTyp == 0)
21
       return a.x < b.x;
22
     else
23
       return a.y < b.y;
   }
24
25
26
   int cnt[MaxN];
27
   bool Div[MaxN];
28
   |int minX[MaxN],minY[MaxN],maxX[MaxN],maxY[MaxN];
29
   void BuildKD(int l,int r,Point p□)
30
   {
31
     if (l > r) return;
32
     int mid = l+r>>1;
33
     cmpTyp = 0;
     minX[mid] = min_element(p+l,p+r+1,cmp)->x;
34
     maxX[mid] = max_element(p+l,p+r+1,cmp)->x;
35
36
     cmpTyp = 1;
37
     minY[mid] = min_element(p+l,p+r+1,cmp)->y;
     maxY[mid] = max_element(p+l,p+r+1,cmp)->y;
38
39
40
     cnt[mid] = r-l+1;
41
     cmpTyp = Div[mid] = (maxX[mid]-minX[mid] < maxY[mid]-minY[mid]);</pre>
42
     nth_element(p+l,p+mid,p+r+1,cmp);
43
     BuildKD(l,mid-1,p);
44
     BuildKD(mid+1,r,p);
   }
45
46
47
   queue<int> Q;
48
   int Find(int l,int r,Point a,Point p[])
49
   {
50
     if (l > r) return 0;
51
     int mid = 1+r>>1:
52
     if (cnt[mid] == 0) return 0;
53
54
     if (\max X[\min] < a.x-a.r | |
55
         minX[mid] > a.x+a.r | I
56
         maxY[mid] < a.y-a.r | I
57
         minY[mid] > a.y+a.r)
58
       return 0;
59
60
     int totdel = 0;
61
```

```
if (p[mid].del == false)
 62
 63
         if (abs(p[mid].x-a.x) \le a.r \& abs(p[mid].y-a.y) \le a.r)
 64
 65
           p[mid].del = true;
 66
           Q.push(p[mid].id);
 67
           totdel++;
         }
 68
 69
 70
       totdel += Find(l,mid-1,a,p);
 71
       totdel += Find(mid+1,r,a,p);
 72
 73
       cnt[mid] -= totdel;
 74
 75
       return totdel;
    }
 76
 77
 78
    Point p[MaxN], tp[MaxN];
 79
    int n;
 80
 81
    int main()
 82
    {
 83
       int cas = 1:
 84
      while (true)
 85
       {
 86
         scanf("%d",&n);
 87
         if (n == 0) break;
 88
 89
         for (int i = 0; i < n; i++)
 90
         {
91
           p[i].id = i;
 92
           int tx, ty;
 93
           scanf("%d%d%d",&tx,&ty,&p[i].r);
 94
           p[i].x = tx-ty;
 95
           p[i].y = tx+ty;
           p[i].del = false;
 96
 97
           tp[i] = p[i];
 98
 99
         BuildKD(0, n-1, tp);
100
101
         printf("Case<sub>□</sub>#%d:\n",cas++);
102
         int q;
         scanf("%d",&q);
103
104
         for (int i = 0; i < q; i++)
105
         {
106
           int id;
           scanf("%d",&id);
107
108
           int res = 0:
109
           id--:
110
           Q.push(id);
111
           while (!Q.empty())
112
           {
```

```
113
            int now = Q.front();
114
            Q.pop();
115
             if (p[now].del == true) continue;
116
             p[now].del = true;
117
            res += Find(0,n-1,p[now],tp);
          }
118
119
          printf("%d\n",res);
        }
120
121
122
      return 0;
123 |}
        半平面交
    6.9
    直线左边代表有效区域。
  1 | bool HPIcmp(Line a, Line b)
  2
    {
  3
      if (fabs(a.k - b.k) > eps) return a.k < b.k;
      return ((a.s - b.s) * (b.e-b.s)) < 0;
  5
    }
  6
    Line Q[100];
    void HPI(Line line[], int n, Point res[], int &resn)
  8
 9
 10
      int tot = n;
 11
      sort(line, line + n, HPIcmp);
12
      tot = 1;
13
      for (int i = 1; i < n; i++)
        if (fabs(line[i].k - line[i - 1].k) > eps)
 14
15
          line[tot++] = line[i];
      int head = 0, tail = 1;
 16
17
      Q[0] = line[0];
      0[1] = line[1];
 18
19
      resn = 0;
 20
      for (int i = 2; i < tot; i++)
 21
22
        if (fabs((Q[tail].e-Q[tail].s)*(Q[tail - 1].e-Q[tail - 1].s)) <
            eps ||
23
             fabs((Q[head].e-Q[head].s)*(Q[head + 1].e-Q[head + 1].s)) <
                eps)
 24
           return;
 25
        while (head < tail && (((Q[tail] & Q[tail - 1]) - line[i].s) * (
           line[i].e-line[i].s)) > eps)
26
          tail--;
        while (head < tail && (((Q[head]&Q[head + 1]) - line[i].s) * (
27
           line[i].e-line[i].s)) > eps)
28
          head++;
 29
        Q\Gamma + tail = line[i];
 30
31
      while (head < tail && (((Q[tail] \& Q[tail - 1]) - Q[head].s) * (Q[
         head].e-Q[head].s)) > eps)
```

```
32
       tail—;
     while (head < tail && (((Q[head]&Q[head + 1]) - Q[tail].s) * (Q[
33
        tail\ .e-Q[tail\ .s)) > eps)
34
       head++;
     if (tail <= head + 1) return;</pre>
35
     for (int i = head; i < tail; i++)
36
37
       res[resn++] = Q[i] & Q[i + 1];
38
     if (head < tail + 1)
39
       res[resn++] = Q[head] & Q[tail];
40 }
   6.10 凸包
   得到的凸包按照逆时针方向排序。
  1//判断是否是共点或者共线用
   bool conPoint(Point p[],int n)
 3
   {
 4
     for (int i = 1; i < n; i++)
 5
       if (p[i].x != p[0].x || p[i].y != p[0].y)
 6
          return false;
 7
     return true;
 8
   bool conLine(Point p[],int n)
10
11
     for (int i = 2; i < n; i++)
12
       if ((p[i]-p[0])*(p[1]-p[0]) != 0)
13
         return false;
14
     return true;
   }
15
16
17
   bool GScmp(Point a, Point b)
18
19
     if (fabs(a.x - b.x) < eps)
20
       return a.y < b.y - eps;
21
     return a.x < b.x - eps;
   }
22
23
24
   void GS(Point p[],int n,Point res[],int &resn)
25
   {
26
     resn = 0;
27
     int top = 0;
28
     sort(p,p+n,GScmp);
29
30
     if (conPoint(p,n))
31
     {
32
       res[resn++] = p[0];
33
       return;
34
35
     if (conLine(p,n))
36
       res[resn++] = p[0];
37
```

```
38
       res[resn++] = p[n-1];
39
       return;
     }
40
41
42
     for (int i = 0; i < n;)
43
       if (resn < 2 | I)
         (res[resn-1]-res[resn-2])*(p[i]-res[resn-1]) > 0)
44
45
         res[resn++] = p[i++];
46
       else
47
         --resn;
48
     top = resn-1;
49
     for (int i = n-2; i >= 0;)
50
       if (resn < top+2 ||
         res[resn-1]-res[resn-2])*(p[i]-res[resn-1]) > 0)
51
52
         res[resn++] = p[i--];
53
       else
54
         --resn;
55
     resn--;
56 |}
         直线与凸包求交点
   6.11
   复杂度 O(\log n)。
   需要先预处理几个东西。
  |//二分「la,lb] 这段区间那条边与 line 相交
   int Gao(int la,int lb,Line line)
 3
   {
 4
     if (la > lb)
 5
       lb += n;
 6
     int l = la, r = lb, mid;
 7
     while (l < r)
 8
     {
9
       mid = 1+r+1>>1;
       if (cmp((line.e-line.s)*(p[la]-line.s),0)*cmp((line.e-line.s)*(
10
          p[mid]-line.s),0) >= 0)
11
         l = mid;
12
       else
13
         r = mid-1;
14
15
     return 1%n;
16
17
   //求 l 与凸包的交点
18
19
   //先调用 Gettheta 预处理出凸包每条边的斜率,然后处理成升序排列
20
   double theta[maxn];
21
22
   void Gettheta()
23
24
     for (int i = 0; i < n; i++)
25
     {
```

```
26
       Point v = p[(i+1)\%n]-p[i];
       theta[i] = atan2(v.y,v.x);
27
28
29
     for (int i = 1; i < n; i++)
30
       if (theta[i-1] > theta[i]+eps)
         theta[i] += 2*pi;
31
   }
32
33
34
   double Calc(Line 1)
35
   {
36
     double tnow;
37
     Point v = l.e-l.s;
38
     tnow = atan2(v.y,v.x);
     if (cmp(tnow, theta[0]) < 0) tnow += 2*pi;
39
     int pl = lower_bound(theta,theta+n,tnow)—theta;
40
     tnow = atan2(-v.y,-v.x);
41
42
     if (cmp(tnow,theta[0]) < 0) tnow += 2*pi;
43
     int pr = lower_bound(theta, theta+n, tnow)—theta;
44
     //pl 和 pr 是在 l 方向上距离最远的点对
45
     pl = pl%n;
46
     pr = pr%n;
47
48
     if (cmp(v*(p[pl]-l.s),0)*cmp(v*(p[pr]-l.s),0) >= 0)
       return 0.0;
49
50
51
     int xa = Gao(pl,pr,l);
52
     int xb = Gao(pr,pl,l);
53
54
     if (xa > xb) swap(xa,xb);
55
     //与 [xa,xa+1] 和 [xb,xb+1] 这两条线段相交
56
57
     if (cmp(v*(p[xa+1]-p[xa]),0) == 0) return 0.0;
58
     if (cmp(v*(p[xb+1]-p[xb]),0) == 0) return 0.0;
59
60
     Point pa,pb;
     pa = Line(p[xa], p[xa+1])&l;
61
62
     pb = Line(p[xb], p[xb+1])&l;
     //题目: 求直线切凸包得到的两部分的面积
63
64
     double area0 = sum[xb]-sum[xa+1]+(pa*p[xa+1])/2.0+(p[xb]*pb)
        /2.0+(pb*pa)/2.0;
65
     double area1 = sum[xa+n]-sum[xb+1]+(pb*p[xb+1])/2.0+(p[xa]*pa)
        /2.0+(pa*pb)/2.0;
66
67
     return min(area0, area1);
68 |}
         点对凸包的两切点
   6.12
   过了 sgu500 的前七组数据,用前需谨慎,虽然我不认为这个有问题。
 1 | double theta[MaxN];
  |void Gettheta(Point p[],int n)
```

```
3
   {
      for (int i = 0; i < n; i++)
 4
 5
 6
        Point v = p[(i+1)\%n]-p[i];
 7
        theta[i] = atan2(v.y,v.x);
 8
 9
      for (int i = 1; i < n; i++)
        if (theta[i-1] > theta[i]+eps)
10
11
          theta[i] += 2*pi;
12
13
   int cmp(double a,double b)
14
15
     if (fabs(a-b) < eps) return 0;
16
      if (a < b) return -1;
17
      return 1;
18
19
   int Gao(int la,int lb,Line line,Point p[],int n)
20
   {
21
      if (la > lb)
22
        lb += n;
23
      int l = la, r = lb, mid;
     while (l < r)
24
25
      {
26
        mid = 1+r+1>>1;
27
        if (cmp((line.e-line.s)*(p[la%n]-line.s),0)*cmp((line.e-line.s)
           *(p\lceil mid\%n\rceil - line.s),0) >= 0)
28
          l = mid;
29
        else
30
          r = mid-1;
      }
31
32
      return 1%n;
33
34
   int Gao(int la,int lb,int dir,Point s,Point p[],int n)
35
   {
36
      if (la > lb)
37
        lb += n;
38
      if (la == lb) return la;
39
40
      int l = la+1, r = lb, mid;
41
42
     while (l < r)
43
      {
44
        mid = 1+r+1>>1;
45
46
        int ret = cmp((p[mid%n]-s)*(p[(mid-1)%n]-s),0);
47
        if (dir*ret < 0)
48
          l = mid;
49
        else if (dir*ret > 0)
50
          r = mid-1;
51
        else
52
        {
```

```
53
          if (dir == 1)
54
            l = mid;
55
          else
            r = mid-1;
56
       }
57
58
     }
59
60
     int ret = cmp((p[1\%n]-s)*(p[(1-1)\%n]-s),0);
61
     if (dir*ret < 0)
62
        return 1%n;
63
     else if (dir*ret > 0)
64
        return (l-1)%n;
65
     else
66
     {
67
        if (dir == 1)
68
          return 1%n;
69
        else
70
          return (l-1)%n;
71
     }
   }
72
73
   //Gettheta(p,n) first!
   //返回 S 对于 p[] 的两个切点 p[pl],p[pr]
   void Calc(Point s,Point p[],int n,int& pl,int& pr)
76
   {
77
     Line l = Line(s,p[0]);
78
     Point v = l.e-l.s;
79
     double tnow = atan2(v.y,v.x);
80
     if (tnow < theta[0]-eps) tnow += 2*pi;
81
     int tpl = lower_bound(theta,theta+n,tnow)—theta;
82
     tnow = atan2(-v.y,-v.x);
83
     if (tnow < theta[0]-eps) tnow += 2*pi;
84
     int tpr = lower_bound(theta,theta+n,tnow)—theta;
85
86
     pl = tpl = tpl%n;
87
     pr = tpr = tpr%n;
88
89
     int px = Gao(pr,pl,l,p,n);
90
     //printf("pr = %d \rightarrow px = %d\n",tpr,px);
91
     //printf("px = %d \rightarrow pl = %d\n",px,tpl);
92
     //pr \rightarrow px
93
     //px \rightarrow pl
94
95
     pl = Gao(tpr,px,1,s,p,n);
96
     pr = Gao(px,tpl,-1,s,p,n);
97
98 }
         三维凸包
   6.13
   暴力写法
```

UESTC_Lasagne

1 |#define eps 1e-7

```
2
   #define MAXV 505
 3
 4
   struct pt
 5
   {
 6
      double x, y, z;
 7
      pt() {}
 8
      pt(double _x, double _y, double _z): x(_x), y(_y), z(_z) {}
 9
     pt operator - (const pt p1)
10
11
        return pt(x - p1.x, y - p1.y, z - p1.z);
12
13
     pt operator * (pt p)
14
15
        return pt(y*p.z-z*p.y, z*p.x-x*p.z, x*p.y-y*p.x);
16
17
      double operator ^ (pt p)
18
19
        return x*p.x+y*p.y+z*p.z;
20
      }
   };
21
22
   struct _3DCH
23
   {
24
      struct fac
25
26
        int a, b, c;
27
        bool ok;
28
     };
29
      int n;
30
      pt P[MAXV];
31
      int cnt;
32
      fac F[MAXV*8];
33
      int to[MAXV][MAXV];
34
      double vlen(pt a)
35
      {
36
        return sqrt(a.x*a.x+a.y*a.y+a.z*a.z);
37
38
      double area(pt a, pt b, pt c)
39
40
        return vlen((b-a)*(c-a));
41
42
      double volume(pt a, pt b, pt c, pt d)
43
44
        return (b-a)*(c-a)^(d-a);
45
      double ptof(pt &p, fac &f)
46
47
48
        pt m = P[f.b] - P[f.a], n = P[f.c] - P[f.a], t = p - P[f.a];
49
        return (m * n) ^ t;
50
51
     void deal(int p, int a, int b)
52
      {
```

```
53
        int f = to[a][b];
 54
        fac add;
 55
        if (F[f].ok)
 56
        {
 57
           if (ptof(P[p], F[f]) > eps)
 58
             dfs(p, f);
 59
           else
 60
           {
 61
             add.a = b, add.b = a, add.c = p, add.ok = 1;
 62
             to[p][b] = to[a][p] = to[b][a] = cnt;
 63
             F[cnt++] = add;
 64
           }
 65
        }
 66
 67
      void dfs(int p, int cur)
 68
 69
        F[cur].ok = 0;
 70
        deal(p, F[cur].b, F[cur].a);
 71
        deal(p, F[cur].c, F[cur].b);
 72
        deal(p, F[cur].a, F[cur].c);
 73
 74
      bool same(int s, int t)
 75
        pt a = P[F[s].a], &b = P[F[s].b], &c = P[F[s].c];
 76
 77
        return fabs(volume(a, b, c, P[F[t].a])) < eps && fabs(volume(a,
 78
             P[F[t].b]) < eps && fabs(volume(a, b, c, P[F[t].c])) < eps
 79
      }
 80
      void construct()
 81
 82
        cnt = 0;
 83
        if (n < 4)
 84
           return;
 85
        bool sb = 1;
 86
        for (int i = 1; i < n; i++)
 87
 88
           if (vlen(P[0] - P[i]) > eps)
 89
 90
             swap(P[1], P[i]);
 91
             sb = 0;
 92
             break;
           }
 93
 94
        }
        if (sb)return;
 95
 96
        sb = 1;
 97
        for (int i = 2; i < n; i++)
 98
           if (vlen((P[0] - P[1]) * (P[1] - P[i])) > eps)
 99
100
           {
101
             swap(P[2], P[i]);
```

```
102
             sb = 0;
103
             break;
           }
104
105
         }
106
         if (sb)return;
107
         sb = 1;
108
         for (int i = 3; i < n; i++)
109
           if (fabs((P[0] - P[1]) * (P[1] - P[2]) ^ (P[0] - P[i])) > eps
110
              )
           {
111
112
             swap(P[3], P[i]);
113
             sb = 0;
114
             break;
           }
115
         }
116
         if (sb)return;
117
118
         fac add;
119
         for (int i = 0; i < 4; i++)
120
           add.a = (i+1)\%4, add.b = (i+2)\%4, add.c = (i+3)\%4, add.ok = (i+3)\%4
121
           if (ptof(P[i], add) > 0)
122
123
             swap(add.b, add.c);
124
           to[add.a][add.b] = to[add.b][add.c] = to[add.c][add.a] = cnt;
125
           F[cnt++] = add;
126
127
         for (int i = 4; i < n; i++)
128
129
           for (int j = 0; j < cnt; j++)
130
131
             if (F[j].ok \&\& ptof(P[i], F[j]) > eps)
132
133
               dfs(i, j);
134
               break;
135
             }
           }
136
137
138
         int tmp = cnt;
139
         cnt = 0;
140
         for (int i = 0; i < tmp; i++)
141
           if (F[i].ok)
142
143
144
             F[cnt++] = F[i];
145
146
         }
147
148
    //表面积
149
       double area()
150
       {
```

```
151
        double ret = 0.0;
152
        for (int i = 0; i < cnt; i++)
153
154
           ret += area(P[F[i].a], P[F[i].b], P[F[i].c]);
155
156
        return ret / 2.0;
157
    //体积
158
159
      double volume()
160
      {
161
        pt 0(0, 0, 0);
162
        double ret = 0.0;
163
        for (int i = 0; i < cnt; i++)
164
165
           ret += volume(0, P[F[i].a], P[F[i].b], P[F[i].c]);
166
167
        return fabs(ret / 6.0);
168
169
    //表面三角形数
170
      int facetCnt_tri()
171
      {
172
        return cnt;
173
174
    //表面多边形数
175
      int facetCnt()
176
177
        int ans = 0;
178
        for (int i = 0; i < cnt; i++)
179
180
           bool nb = 1;
           for (int j = 0; j < i; j++)
181
182
183
             if (same(i, j))
184
             {
185
               nb = 0;
186
               break;
187
             }
           }
188
189
          ans += nb;
        }
190
191
        return ans;
192
193
194
      pt Fc[MAXV*8];
195
      double V[MAXV*8];
196
      pt Center()//重心
197
      {
198
        pt 0(0,0,0);
199
        for (int i = 0; i < cnt; i++)
200
         {
           Fc[i].x = (0.x+P[F[i].a].x+P[F[i].b].x+P[F[i].c].x)/4.0;
201
```

```
Fc[i].y = (0.y+P[F[i].a].y+P[F[i].b].y+P[F[i].c].y)/4.0;
202
           Fc[i].z = (0.z+P[F[i].a].z+P[F[i].b].z+P[F[i].c].z)/4.0;
203
204
           V[i] = volume(0, P[F[i].a], P[F[i].b], P[F[i].c]);
205
206
         pt res = Fc[0], tmp;
207
         double m = V[0];
         for (int i = 1; i < cnt; i++)
208
209
210
           if (fabs(m+V[i]) < eps)
211
             V[i] += eps;
           tmp.x = (m*res.x+V[i]*Fc[i].x)/(m+V[i]);
212
213
           tmp.y = (m*res.y+V[i]*Fc[i].y)/(m+V[i]);
214
           tmp.z = (m*res.z+V[i]*Fc[i].z)/(m+V[i]);
215
           m += V[i];
216
           res = tmp;
217
         }
218
         return res;
219
220
    };
221
222
    _3DCH hull;
223
224
    int main()
225
    {
226
      while (scanf("%d",&hull.n) != EOF)
227
228
         for (int i = 0; i < hull.n; i++)
229
           scanf("%lf%lf%lf", &hull.P[i].x, &hull.P[i].y, &hull.P[i].z);
230
         hull.construct();
231
232
      return 0;
233 |}
    6.14
           旋转卡壳
    "对踵"
    6.14.1 单个凸包
    |void solve(Point p[],int n)
  2
    {
  3
      Point v;
  4
      int cur = 1;
  5
      for (int i = 0; i < n; i++)
  6
  7
         v = p[i]-p[(i+1)%n];
  8
         while (v*(p\lceil(cur+1)\%n\rceil-p\lceil cur\rceil) < 0)
  9
           cur = (cur + 1)%n;
 10
         //p[cur] -> p[i]
 11
         //p[cur] -> p[i+1]
```

```
12
       //p[cur] -> (p[i],p[i+1])
     }
13
14 |}
   6.14.2 两个凸包
   注意初始点的选取,代码只是个示例。
   有时候答案需要取 solve(p0,n,p1,m) 和 solve(p1,m,p0,n) 的最优值。
   何老鱼说我的是错的。。
   void solve(Point p0[],int n,Point p1[],int m)
 2
   {
 3
     Point v;
 4
     int cur = 0;
 5
     for (int i = 0; i < n; i++)
 6
 7
        v = p0[i]-p0[(i+1)%n];
 8
        while (v*(p1[(cur+1)%m]-p1[cur]) < 0)
 9
          cur = (cur+1)\%m;
10
        //p1[cur] -> p0[i]
11
        //p1[cur] -> p0[i+1]
12
        //p1[cur] -> (p0[i],p0[i+1])
13
     }
14 |}
   6.14.3 外接矩形
 1 |void solve()
 2
   {
 3
     resa = resb = 1e100;
 4
     double dis1, dis2;
 5
     Point xp[4];
 6
     Line 1[4];
 7
     int a,b,c,d;
 8
     int sa, sb, sc, sd;
 9
     a = b = c = d = 0;
     sa = sb = sc = sd = 0;
10
11
     Point va, vb, vc, vd;
12
     for (a = 0; a < n; a++)
13
     {
14
        va = Point(p[a],p[(a+1)%n]);
15
        vc = Point(-va.x,-va.y);
16
        vb = Point(-va.y, va.x);
17
        vd = Point(-vb.x,-vb.y);
18
        if (sb < sa)
19
        {
20
          b = a;
21
          sb = sa;
22
       while (xmult(vb, Point(p[b], p[(b+1)%n])) < 0)
23
24
        {
25
          b = (b+1)%n;
```

```
26
          sb++;
27
        }
28
        if (sc < sb)
29
        {
30
          c = b;
31
          sc = sb;
32
33
       while (xmult(vc, Point(p[c], p[(c+1)%n])) < 0)
34
35
          c = (c+1)%n;
36
          SC++;
37
        }
38
        if (sd < sc)
39
40
          d = c;
41
          sd = sc;
42
        while (xmult(vd, Point(p[d], p[(d+1)%n])) < 0)
43
44
45
          d = (d+1)%n;
46
          sd++;
        }
47
48
       //卡在 p[a],p[b],p[c],p[d] 上
49
50
        sa++;
51
     }
52
   }
         三角形内点个数
   6.15
   6.15.1 无三点共线
 1 | Point p[1000], tp[2000], base;
 2
 3
   bool cmp(const Point &a, const Point &b)
 4
   {
 5
     return a.theta < b.theta;
   }
 6
 7
   int cnt[1000][1000];
 9
   int cntleft[1000][1000];
10
   int n, m;
11
12
   int calc(int a, int b, int c)
13
   {
14
     Point p1 = p[b] - p[a], p2 = p[c] - p[a];
15
     if (atan2(p1.y, p1.x) > atan2(p2.y, p2.x))
16
        swap(b, c);
     if ((p[b] - p[a]) * (p[c] - p[a]) > 0)
17
18
        return cnt[a][c] - cnt[a][b] - 1;
19
     else
        return n - 3 - (cnt[a][c] - cnt[a][b] - 1);
20
```

```
21 |}
22
23
   |int main(int argc, char const *argv∏)
24
   {
25
      int totcas;
26
      scanf("%d", &totcas);
27
      for (int cas = 1; cas <= totcas; ++cas)</pre>
28
29
        scanf("%d", &n);
30
        for (int i = 0; i < n; ++i)
31
32
          scanf("%lld%lld", &p[i].x, &p[i].y);
33
          p[i].id = i;
34
35
        for (int i = 0; i < n; ++i)
36
        {
37
          m = 0;
          base = p[i];
38
39
          for (int j = 0; j < n; ++j)
40
            if (i != j)
41
            {
42
              tp[m] = p[j];
43
              Point v = tp[m]-base;
44
              tp[m++].theta = atan2(v.y,v.x);
45
            }
46
47
          sort(tp, tp + m, cmp);
          for (int j = 0; j < m; ++j)
48
49
            tp[m + j] = tp[j];
50
          //calc cnt
51
52
          for (int j = 0; j < m; ++j)
53
            cnt[i][tp[j].id] = j;
54
55
          //calc cntleft
56
          for (int j = 0, k = 0, tot = 0; j < m; ++j)
57
58
            while (k == j \mid | (k < j + m \& (tp[j] - base) * (tp[k] -
               base) > 0)
59
              k++, tot++;
60
            cntleft[i][tp[j].id] = --tot;
61
        }
62
63
64
        printf("Case<sub>\\\\</sub>%d:\n", cas);
65
        int q;
66
        scanf("%d", &q);
67
        for (int i = 0; i < q; ++i)
68
        {
69
          int x, y, z;
          scanf("%d%d%d", &x, &y, &z);
70
```

```
71
          if ((p[z] - p[x]) * (p[y] - p[x]) > 0)
72
            swap(y, z);
73
          int res = cntleft[x][z] + cntleft[z][y] + cntleft[y][x];
74
          res += calc(x, y, z) + calc(y, z, x) + calc(z, x, y);
75
          res -= 2 * (n - 3);
76
         printf("%d\n", res);
77
       }
78
     }
79
     return 0;
80 | }
   6.15.2 有三点共线且点有类别之分
  |int n,n0,n1,m;
   Point p[3000], tp[3000], base;
 3
   bool cmp(const Point &a, const Point &b)
 5
   {
 6
     if ((a-base)*(b-base) == 0)
 7
       return (a-base).getMol() < (b-base).getMol();</pre>
 8
 9
10
     return a.theta < b.theta;
11
12
13
   int cnt[100][100];
   int cntleft[100][100];
15
16
   int calc(int a,int b,int c)
17
18
     Point p1 = p[b]-p[a], p2 = p[c]-p[a];
19
     if (atan2(1.0*p1.y,1.0*p1.x) > atan2(1.0*p2.y,1.0*p2.x))
20
       swap(b,c);
21
     int res = cnt[a][c]-cnt[a][b];
22
     if ((p[b]-p[a])*(p[c]-p[a]) > 0)
23
       return res;
24
     else
25
       return n1-res;
   }
26
27
28
   int main()
29
   {
30
     int cas = 0;
31
     while (scanf("%d%d",&n0,&n1) != EOF)
32
     {
33
       n = n1+n0;
34
       for (int i = 0; i < n; i++)
35
36
          scanf("%I64d%I64d",&p[i].x,&p[i].y);
37
         p[i].id = i;
38
       }
39
       for (int i = 0; i < n0; ++i)
```

```
40
        {
41
          m = 0;
42
          base = p[i];
          for (int j = 0; j < n; ++j)
43
44
            if (i != j)
45
            {
46
              tp[m] = p[j];
47
              Point v = tp[m]-base;
48
              tp[m++].theta = atan2(1.0*v.y,1.0*v.x);
49
50
51
          sort(tp, tp + m, cmp);
52
          for (int j = 0; j < m; ++j)
53
            tp[m + j] = tp[j];
54
55
          for (int j = 0, tot = 0; j < m; ++j)
56
57
            if (tp[j].id < n0)
58
              cnt[i][tp[j].id] = tot;
59
            else
60
              tot++;
          }
61
62
63
          for (int j = 0, k = 0, tot = 0; j < m; ++j)
64
65
            while (k == j \mid l \mid (k < j + m \&\& (tp[j] - base) * (tp[k] -
               base) > 0)
66
67
              if (tp[k].id >= n0)
68
                tot++;
69
              k++;
70
            }
71
            if (tp[j].id >= n0)
72
              tot—;
73
            else
74
              cntleft[i][tp[j].id] = tot;
75
         }
       }
76
77
78
        int ans = 0;
79
        for (int i = 0; i < n0; i++)
          for (int j = i+1; j < n0; j++)
80
81
            for (int k = j+1; k < n0; k++)
82
            {
83
              int x = i, y = j, z = k;
84
85
              if ((p[z] - p[x]) * (p[y] - p[x]) > 0)
86
                swap(y, z);
87
              int res = cntleft[x][z] + cntleft[z][y] + cntleft[y][x];
88
89
              res += calc(x, y, z) + calc(y, z, x) + calc(z, x, y);
```

```
90
91
               res -= 2 * n1;
92
93
               //printf("%d %d %d %d\n",x,y,z,res);
94
95
               if (res\%2 == 1)
96
                 ans++;
97
98
        printf("Case_\%d:_\%d\n",++cas,ans);
99
100
      return 0;
101 |}
    6.16
          最近点对
    6.16.1 类快排算法
    |double calc_dis(Point &a ,Point &b) {
      return sqrt((a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y));
    }
  3
    //别忘了排序
  5
    bool operator<(const Point &a ,const Point &b) {</pre>
 6
      if(a.y != b.y) return a.x < b.x;
  7
      return a.x < b.x;
    }
 8
 9
    double Gao(int l ,int r ,Point pnts[]) {
 10
      double ret = inf;
      if(l == r) return ret;
 11
 12
      if(l+1 ==r) {
13
        ret = min(calc_dis(pnts[l],pnts[l+1]) ,ret);
14
        return ret;
 15
16
      if(l+2 ==r) {
 17
        ret = min(calc_dis(pnts[l],pnts[l+1]) ,ret);
        ret = min(calc_dis(pnts[l],pnts[l+2]) ,ret);
18
 19
        ret = min(calc_dis(pnts[l+1],pnts[l+2]) ,ret);
 20
        return ret;
 21
      }
 22
 23
      int mid = 1+r>>1;
      ret = min (ret ,Gao(l ,mid,pnts));
24
 25
      ret = min (ret , Gao(mid+1, r,pnts));
 26
 27
      for(int c = l ; c<=r; c++)
28
        for(int d = c+1; d <= c+7 \&\& d <= r; d++) {
 29
           ret = min(ret , calc_dis(pnts[c],pnts[d]));
 30
 31
      return ret;
 32 | }
    6.16.2 随机增量法
```

1 |#include <iostream>

```
2 |#include <cstdio>
   #include <cstring>
   |#include <map>
 5
   #include <vector>
 6 | #include < cmath>
   #include <algorithm>
   |#define Point pair<double,double>
 9
   using namespace std;
10
11
   const int step[9][2] =
      \{\{-1,-1\},\{-1,0\},\{-1,1\},\{0,-1\},\{0,0\},\{0,1\},\{1,-1\},\{1,0\},\{1,1\}\};
12
   int n,x,y,nx,ny;
13 |map<pair<int,int>,vector<Point > > g;
14 | vector<Point > tmp;
15 | Point p[20000];
16
   double tx,ty,ans,nowans;
17
   vector<Point >::iterator it,op,ed;
18
   pair<int,int> gird;
19 |bool flag;
20
21
   double Dis(Point p0,Point p1)
22
   {
23
     return sqrt((p0.first-p1.first)*(p0.first-p1.first)+
24
            (p0.second-p1.second)*(p0.second-p1.second));
25
26
27
   double CalcDis(Point p0, Point p1, Point p2)
28
29
     return Dis(p0,p1)+Dis(p0,p2)+Dis(p1,p2);
   }
30
31
32
   void build(int n,double w)
33
   {
34
     g.clear();
35
     for (int i = 0; i < n; i++)
       g[make_pair((int)floor(p[i].first/w),(int)floor(p[i].second/w))
36
           ].push_back(p[i]);
   }
37
38
39
   int main()
40
   {
41
     int t;
42
     scanf("%d",&t);
43
     for (int ft = 1;ft <= t;ft++)
44
45
       scanf("%d",&n);
46
       for (int i = 0; i < n; i++)
47
          scanf("%lf%lf",&tx,&ty);
48
49
          p[i] = make_pair(tx,ty);
50
       }
```

```
51
       random_shuffle(p,p+n);
52
       ans = CalcDis(p[0], p[1], p[2]);
53
       build(3,ans/2.0);
54
       for (int i = 3; i < n; i++)
55
        {
56
         x = (int)floor(2.0*p[i].first/ans);
57
          y = (int)floor(2.0*p[i].second/ans);
58
          tmp.clear();
59
          for (int k = 0; k < 9; k++)
60
          {
61
            nx = x+step[k][0];
62
            ny = y+step[k][1];
63
            gird = make_pair(nx,ny);
64
            if (q.find(qird) != q.end())
65
66
              op = g[gird].begin();
              ed = q[qird].end();
67
68
              for (it = op;it != ed;it++)
69
                tmp.push_back(*it);
            }
70
71
72
          flag = false;
          for (int j = 0; j < tmp.size(); j++)
73
            for (int k = j+1; k < tmp.size(); k++)
74
75
76
              nowans = CalcDis(p[i],tmp[j],tmp[k]);
77
              if (nowans < ans)
78
79
                ans = nowans;
80
                flag = true;
81
              }
82
83
          if (flag == true)
84
            build(i+1,ans/2.0);
85
          else
            g[make_pair((int)floor(2.0*p[i].first/ans),(int)floor(2.0*p
86
               [i].second/ans))].push_back(p[i]);
87
       }
88
       printf("%.3f\n",ans);
89
     }
90
   1
          多圆面积并
   6.17
          去重
   6.17.1
   有时候可能需要去掉不需要的圆
 1 | for (int i = 0; i < n; i++)
 2
 3
     scanf("%lf%lf%lf",&c[i].c.x,&c[i].c.y,&c[i].r);
 4
     del[i] = false;
 5
   }
```

```
for (int i = 0; i < n; i++)
 7
     if (del[i] == false)
 8
 9
       if (c[i].r == 0.0) del[i] = true;
       for (int j = 0; j < n; j++)
10
          if (i != j)
11
12
            if (del[j] == false)
13
              if (cmp(Point(c[i].c,c[j].c).Len()+c[i].r,c[j].r) <= 0)
14
                del[i] = true;
15
     }
16
   tn = n;
17
   | n = 0;
18
   for (int i = 0; i < tn; i++)
     if (del[i] == false)
19
20
       c[n++] = c[i];
   6.17.2 圆并
   ans[i] 表示被覆盖 i 次的面积
 1 | const double pi = acos(-1.0);
   const double eps = 1e-8;
 3
   struct Point
 4
   {
 5
     double x,y;
 6
     Point(){}
 7
     Point(double _x,double _y)
 8
       {
 9
          X = _X;
10
          y = _y;
11
       }
12
     double Length()
13
        {
14
          return sqrt(x*x+y*y);
15
       }
16
   |};
17
   struct Circle
18
   {
19
     Point c;
20
     double r;
21
   };
22
   struct Event
23
   {
24
     double tim;
25
     int typ;
26
     Event(){}
27
     Event(double _tim,int _typ)
28
       {
29
          tim = _tim;
30
          typ = _typ;
31
       }
32 \};
```

```
33
34
   int cmp(const double& a,const double& b)
35
36
     if (fabs(a-b) < eps) return 0;
37
     if (a < b) return -1;
38
     return 1;
   }
39
40
41
   bool Eventcmp(const Event& a,const Event& b)
42
43
     return cmp(a.tim,b.tim) < 0;
   }
44
45
46
   double Area(double theta,double r)
47
48
     return 0.5*r*r*(theta-sin(theta));
   }
49
50
51
   double xmult(Point a,Point b)
52
53
     return a.x*b.y-a.y*b.x;
   }
54
55
56
   int n,cur,tote;
57
   Circle c[1000]:
58
   double ans[1001],pre[1001],AB,AC,BC,theta,fai,a0,a1;
59
   Event e[4000];
60
   Point lab;
61
62
   int main()
63
   {
64
     while (scanf("%d",&n) != EOF)
65
     {
66
       for (int i = 0; i < n; i++)
          scanf("%lf%lf",&c[i].c.x,&c[i].c.y,&c[i].r);
67
68
       for (int i = 1; i <= n; i++)
          ans[i] = 0.0;
69
70
       for (int i = 0; i < n; i++)
71
       {
72
          tote = 0;
73
          e[tote++] = Event(-pi,1);
          e[tote++] = Event(pi,-1);
74
75
          for (int j = 0; j < n; j++)
            if (j != i)
76
77
78
              lab = Point(c[j].c.x-c[i].c.x,c[j].c.y-c[i].c.y);
79
              AB = lab.Length();
80
              AC = c[i].r;
              BC = c[j].r;
81
82
              if (cmp(AB+AC,BC) <= 0)
83
              {
```

```
84
                 e[tote++] = Event(-pi,1);
 85
                 e[tote++] = Event(pi,-1);
 86
                 continue;
               }
 87
 88
               if (cmp(AB+BC,AC) <= 0) continue;
               if (cmp(AB,AC+BC) > 0) continue;
 89
 90
               theta = atan2(lab.y, lab.x);
 91
               fai = acos((AC*AC+AB*AB-BC*BC)/(2.0*AC*AB));
               a0 = theta-fai;
 92
 93
               if (cmp(a0,-pi) < 0) a0 += 2*pi;
 94
               a1 = theta+fai;
               if (cmp(a1,pi) > 0) a1 -= 2*pi;
 95
 96
               if (cmp(a0,a1) > 0)
 97
 98
                 e[tote++] = Event(a0,1);
99
                 e[tote++] = Event(pi,-1);
100
                 e[tote++] = Event(-pi,1);
101
                 e[tote++] = Event(a1,-1);
102
               }
103
               else
104
               {
105
                 e[tote++] = Event(a0,1);
106
                 e[tote++] = Event(a1,-1);
107
               }
108
             }
109
           sort(e,e+tote,Eventcmp);
110
           cur = 0;
111
           for (int j = 0; j < tote; j++)
112
113
             if (cur != 0 && cmp(e[j].tim,pre[cur]) != 0)
114
115
               ans[cur] += Area(e[j].tim-pre[cur],c[i].r);
116
               ans[cur] += xmult(Point(c[i].c.x+c[i].r*cos(pre[cur]),c[i
                  1.c.y+c[i].r*sin(pre[cur])),
                          Point(c[i].c.x+c[i].r*cos(e[j].tim),c[i].c.y+c[
117
                             i].r*sin(e[j].tim)))/2.0;
118
             }
119
             cur += e[j].typ;
120
             pre[cur] = e[j].tim;
121
           }
122
         for (int i = 1; i < n; i++)
123
124
           ans[i] = ans[i+1];
125
         for (int i = 1; i <= n; i++)
126
           printf("[%d]_{\square}=_{\square}%.3f\n",i,ans[i]);
127
128
      return 0;
129 |}
```

6.18 一个圆与多边形面积交

```
|bool InCircle(Point a, double r)
 2
   {
 3
     return cmp(a.x*a.x+a.y*a.y,r*r) <= 0;
 4
     //这里判断的时候 EPS 一定不要太小!!
 5
   }
 6
   double CalcArea(Point a,Point b,double r)
 8
9
     Point p[4];
10
     int tot = 0:
11
     p[tot++] = a;
12
13
     Point tv = Point(a,b);
     Line tmp = Line(Point(0,0),Point(tv.y,-tv.x));
14
15
     Point near = LineToLine(Line(a,b),tmp);
16
     if (cmp(near.x*near.x+near.y*near.y,r*r) <= 0)</pre>
17
18
       double A,B,C;
19
       A = near.x*near.x+near.y*near.y;
20
       C = r;
       B = C*C-A:
21
22
       double tvl = tv.x*tv.x+tv.y*tv.y;
23
       double tmp = sqrt(B/tvl); //这样做只用一次开根
24
       p[tot] = Point(near.x+tmp*tv.x,near.y+tmp*tv.y);
25
       if (OnSeq(Line(a,b),p[tot]) == true) tot++;
26
       p[tot] = Point(near.x-tmp*tv.x,near.y-tmp*tv.y);
27
       if (OnSeg(Line(a,b),p[tot]) == true) tot++;
28
     if (tot == 3)
29
30
31
       if (cmp(Point(p[0],p[1]).Length(),Point(p[0],p[2]).Length()) >
          0)
32
         swap(p[1],p[2]);
33
34
     p[tot++] = b;
35
36
     double res = 0.0, theta, a0, a1, sgn;
37
     for (int i = 0; i < tot-1; i++)
38
     {
39
       if (InCircle(p[i],r) == true && InCircle(p[i+1],r) == true)
40
       {
41
         res += 0.5*xmult(p[i],p[i+1]);
42
       }
43
       else
44
         a0 = atan2(p[i+1].y,p[i+1].x);
45
46
         a1 = atan2(p[i].y,p[i].x);
47
         if (a0 < a1) a0 += 2*pi;
         theta = a0-a1;
48
49
         if (cmp(theta,pi) >= 0) theta = 2*pi—theta;
50
         sgn = xmult(p[i],p[i+1])/2.0;
```

```
51
         if (cmp(sqn,0) < 0) theta = -theta;
         res += 0.5*r*r*theta;
52
53
       }
54
55
     return res;
56 |}
   调用
 1 | area2 = 0.0;
   for (int i = 0; i < resn; i++) // 遍历每条边,按照逆时针
     area2 += CalcArea(p[i],p[(i+1)\%resn],r);
   6.19
         精度问题
```

6.19.1 浮点数为啥会有精度问题

浮点数 (以 C/C++ 为准),一般用的较多的是 float、double。

	占字节数	数值范围	十进制精度位数
float	4	$-3.4e - 38 \sim 3.4e38$	6 ~ 7
double	8	$\begin{vmatrix} -3.4e - 38 \sim 3.4e38 \\ -1.7e - 308 \sim 1.7e308 \end{vmatrix}$	$14 \sim 15$

如果内存不是很紧张或者精度要求不是很低,一般选用 double。14 位的精度 (是有效数字位,不是小数点后的位数) 通常够用了。注意,问题来了,数据精度位数达到了 14 位,但有些浮点运算的结果精度并达不到这么高,可能准确的结果只有 $10 \sim 12$ 位左右。那低几位呢?自然就是不可预料的数字了。这给我们带来这样的问题:即使是理论上相同的值,由于是经过不同的运算过程得到的,他们在低几位有可能 (一般来说都是) 是不同的。这种现象看似没太大的影响,却会一种运算产生致命的影响:==。恩,就是判断相等。注意,C/C++ 中浮点数的 == 需要完全一样才能返回 true。

6.19.2 eps

eps 缩写自 epsilon,表示一个小量,但这个小量又要确保远大于浮点运算结果的不确定量。 eps 最常见的取值是 1e-8 左右。引入 eps 后,我们判断两浮点数 a、b 相等的方式如下:

 $1 \mid \text{int sqn(double a)} \{ \text{return a} < -\text{eps} ? -1 : a < \text{eps} ? 0 : 1; \}$

这样,我们才能把相差非常近的浮点数判为相等;同时把确实相差较大(差值大于 eps)的数判为不相等。

养成好习惯,尽量不要再对浮点数做 == 判断。

6.19.3 eps 带来的函数越界

如果 sqrt(a), asin(a), acos(a) 中的 a 是你自己算出来并传进来的,那就得小心了。 如果 a 本来应该是 0 的,由于浮点误差,可能实际是一个绝对值很小的负数(比如 -1e-12),

这样 sqrt(a) 应得 0 的,直接因 a 不在定义域而出错。

类似地,如果 a 本来应该是 ± 1 ,则 asin(a)、acos(a) 也有可能出错。

因此,对于此种函数,必需事先对 a 进行校正。

6.19.4 输出陷阱 I

现在考虑一种情况,题目要求输出保留两位小数。有个 case 的正确答案的精确值是 0.005, 按理应该输出 0.01, 但你的结果可能是 0.00500000001(恭喜),也有可能是 0.004999999999(悲剧),如果按照 printf("%.2lf",a)输出,那你的遭遇将和括号里的字相同。解决办法是,如果 a 为正,则输出 a+eps,否则输出 a-eps

6.19.5 输出陷阱 II

ICPC 题目输出有个不成文的规定 (有时也成文),不要输出:-0.000 那我们首先要弄清,什么时候按 printf("%.3lf",a) 输出会出现这个结果。直接给出结果好了: $a \in (-0.000499999 \cdots, -0.000 \cdots 1)$ 所以,如果你发现 a 落在这个范围内,请直接输出 0.000。更保险的做法是用 sprintf 直接判断输出结果是不是 -0.000 再予处理。

6.19.6 范围越界

请注意,虽然 double 可以表示的数的范围很大,却不是不穷大,上面说过最大是 1e308。所以有些时候你得小心了,比如做连乘的时候,必要的时候要换成对数的和。

6.19.7 关于 set

经观察,set 不是通过 == 来判断相等的,是通过 < 来进行的,具体说来,只要 a < b 和 b < a 都不成立,就认为 a 和 b 相等,可以发现,如果将小于定义成:

1 | bool operator < (const Dat dat)const{return val < dat.val − eps;} 就可以解决问题了。(基本类型不能重载运算符, 所以封装了下)

6.19.8 输入值波动过大

这种情况不常见,不过可以帮助你更熟悉 eps。假如一道题输入说,给一个浮点数 a, 1e-20 < a < 1e20。那你还敢用 1e-8 做 eps 么? 合理的做法是把 eps 按照输入规模缩放到合适大小。

6.19.9 一些建议

容易产生较大浮点误差的函数有 asin、acos。欢迎尽量使用 atan2。 另外,如果数据明确说明是整数,而且范围不大的话,使用 int 或者 long long 代替 double 都是极佳选择,因为就不存在浮点误差了

7 搜索

7.1.1 估价函数

7.1 Dancing Links

```
1
  int h()
 2
   {
 3
     bool vis[100];
 4
     memset(vis,false,sizeof(vis));
 5
     int i,j,k,res=0,mi,col;
 6
     while(1)
 7
     {
 8
        mi=inf;
 9
        for(i=R[head]; i!=head&&i<=2*n; i=R[i])
          if(mi>nk[i]&&!vis[i])
10
11
          {
12
            mi=nk[i];
13
            col=i;
14
15
        if(mi==inf)
16
          break;
17
        res++;
18
        vis[col]=true;
19
        for(j=D[col]; j!=col; j=D[j])
          for(k=R[j]; k!=j; k=R[k])
20
21
          {
22
            if(C[k]>2*n)
23
              continue;
24
            vis[C[k]]=true;
25
          }
26
     }
27
     return res;
28
   }
   7.1.2 DLX
 1 |void remove1(int col)
 2
   {
 3
     int i,j;
     L[R[col]]=L[col];
 4
 5
     R[L[col]]=R[col];
 6
     for(i=D[col];i!=col;i=D[i])
 7
 8
        L[R[i]]=L[i];
 9
        R[L[i]]=R[i];
10
11
12
   void remove2(int col)
13
14
     int i,j;
15
     L[R[col]]=L[col];
```

```
16
      R[L[col]]=R[col];
17
      for(i=D[col];i!=col;i=D[i])
18
19
        for(j=R[i];j!=i;j=R[j])
20
21
          U[D[j]]=U[j];
22
          D[U[j]]=D[j];
23
           _nk[C[j]];
        }
24
25
      }
26
   void resume1(int col)
27
28
   {
      int i,j;
29
30
      for(i=U[col];i!=col;i=U[i])
31
32
        L[R[i]]=i;
33
        R[L[i]]=i;
34
35
      L[R[col]]=col;
36
      R[L[col]]=col;
37
38
   void resume2(int col)
39
   {
40
      int i,j;
41
      for(i=U[col];i!=col;i=U[i])
42
43
        for(j=L[i]; j!=i; j=L[j])
44
45
          ++nk[C[j]];
46
          U[D[j]]=j;
47
          D[U[j]]=j;
        }
48
49
50
      L[R[col]]=col;
51
      R[L[col]]=col;
52
53
   int h()
54
   {
55
      bool vis[100];
      memset(vis,false,sizeof(vis));
56
57
      int i,j,k,res=0,mi,col;
58
      while(1)
59
      {
60
        mi=inf;
61
        for(i=R[head];i!=head\&i<=2*n;i=R[i])
62
          if(mi>nk[i]&&!vis[i])
63
64
            mi=nk[i];
65
            col=i;
          }
66
```

```
if(mi==inf)
 67
 68
           break;
 69
         res++; vis[col]=true;
         for(j=D[col]; j!=col; j=D[j])
 70
 71
           for(k=R[j];k!=j;k=R[k])
 72
           {
 73
             if(C[k]>2*n)
 74
                continue;
 75
             vis[C[k]]=true;
 76
 77
       }
 78
       return res;
 79
 80
    bool DLX(int d,int deep)
 81
    {
 82
       if(d+h()>deep) return false;
 83
       if(R[head]==head||R[head]>2*n)
 84
         return true;
 85
       if(d>=deep)
 86
         return false;
 87
       int col,ma=inf;
 88
       int i,j;
      for(i=R[head];i!=head&&i<=2*n;i=R[i])</pre>
 89
 90
         if(nk[i]<ma)
 91
         {
 92
           col=i;
 93
           ma=nk[i];
 94
         }
 95
       remove1(col);
 96
       for(i=D[col];i!=col;i=D[i])
 97
 98
         int flag=1;
99
         for(j=R[i];;j=R[j])
100
           if(j==R[i]&\&!flag)
101
102
             break;
103
           U[D[j]]=U[j];
104
           D[U[j]]=D[j];
105
           if(C[j]>2*n)
             remove2(C[j]);
106
107
           else
108
             remove1(C[j]);
109
           flag=0;
         }
110
         if(DLX(d+1,deep))
111
112
           return true;
113
         flaa=1:
         for(j=L[i];;j=L[j])
114
115
         {
116
           if(j==L[i]&\&!flag)
117
             break;
```

```
if(C[j]>2*n)
  resume2(C[j]);
118
119
120
              else
              resume1(C[j]);
U[D[j]]=j;
D[U[j]]=j;
flag=0;
121
122
123
124
           }
125
126
        }
127
         resume1(col);
         return false;
128
129 }
```

8 动态规划

8.1 斜率优化

```
1 |#include<cstdio>
   #include<algorithm>
   using namespace std;
   |int a[1000],sum[1001],dp[1000][1000];
   int deque[1000];
   const int inf=0x7ffffffff;
 7
   int N,s,t;
8
   |int calc(int i,int l,int j)//决策值计算
9
10
     return dp[j][l-1]-(sum[i]-sum[j])*(sum[N]-sum[i]);
11
12
   bool check(int i,int l)//尾端判断
13
14
     int k1=deque[t-1], k2=deque[t-2];
     return (long long)(dp[k1][l]-dp[k2][l])*(sum[i]-sum[k1])>(long
15
        long)(dp[i][l]-dp[k1][l])*(sum[k1]-sum[k2]);
16
17
   int main()
18
   {
19
     int n,m;
     while (scanf("%d%d",&n,&m),n)
20
21
22
       for (int i=0; i<n; i++)
23
         scanf("%d",&a[i]);
24
       N=n;
25
       sum[0]=0;
26
       for (int i=0; i<n; i++)
27
         sum[i+1]=sum[i]+a[i];
28
       dp[0][0]=0;
       for (int i=0; i<n; i++)
29
         for (int j=i+1; j<n; j++)
30
31
           dp[0][0]+=a[i]*a[j];
32
       for (int i=1; i<n; i++)
33
         dp[i][0]=inf;
34
       for (int i=1; i<n; i++)
35
       {
36
         dp[i][1]=inf;
37
         for (int j=0; j<i; j++)
38
           dp[i][1]=min(dp[i][1],calc(i,1,j));
39
       for (int l=2; l<=m; l++)
40
41
42
         s=t=0;//双端队列清空
43
         for (int i=l; i<n; i++)
44
         {
45
           while (t-s>1 \&\& check(i-1,l-1)) t---;
46
           deque[t++]=i-1;//决策加入
```

```
47
            while (t-s>1 && calc(i,l,deque[s])>calc(i,l,deque[s+1])) s
               ++;
48
            dp[i][l]=calc(i,l,deque[s]);
          }
49
50
        }
51
        int ans=0x7fffffff;
52
        for (int i=m; i<n; i++)
53
          ans=min(ans,dp[i][m]);
       printf("%d\n",ans);
54
55
56
     return 0;
57 |}
   8.2
        RMQ 二版
   void init()
 2
   {
 3
     int i,j;
 4
     int n=N, k=1, l=0;
 5
     for (i=0; i<n; i++)
 6
 7
        f[i][0]=ele[i].num;
        if (i+1>k*2)
 8
 9
        {
          k*=2;
10
11
          1++;
12
13
        lent[i+1]=l;
14
15
     for (j=1; (1<< j)-1< n; j++)
16
        for (i=0; i+(1<< j)-1< n; i++)
17
          f[i][j]=max(f[i][j-1],f[i+(1<<(j-1))][j-1]);
18
19
   int fint(int x,int y)
20
   {
21
     int k=lent[y-x+1];
22
     return \max(f[x][k], f[y-(1<< k)+1][k]);
23 |}
        二维 LIS
   8.3
 1 |#include<cstdio>
   #include<map>
   using namespace std;
   map<int,int> mp[100001];
 5
   bool check(int idx,int x,int y)
 6
   {
 7
     if (!idx) return 1;
     if (mp[idx].begin()->first>=x) return 0;
 9
     map<int,int> ::iterator it=mp[idx].lower_bound(x);
10
     it---;
     if (it->second<y) return 1;</pre>
11
```

```
12
     else return 0;
13
   int main()
14
15
   {
16
     int n;
17
     scanf("%d",&n);
18
     int l=0,r=0;
     for (int i=0;i< n;i++)
19
20
     {
21
       int x,y;
22
       scanf("%d%d",&x,&y);
23
       int tl=l,tr=r;
24
       while (tl<tr)</pre>
25
26
         int mid=(tl+tr+1)/2;
27
         if (check(mid,x,y))
28
           tl=mid;
29
         else
30
           tr=mid-1;
       }
31
32
       if (tl==r) r++;
33
       int idx=tl+1;
34
       map<int,int> ::iterator itl=mp[idx].lower_bound(x),itr=itl;
35
       while (itr!=mp[idx].end() && itr->second>y) itr++;
36
       if (mp[idx].find(x)!=mp[idx].end())
37
         y=min(y,mp[idx][x]);
38
       if (itl!=itr) mp[idx].erase(itl,itr);
       if (mp[idx].find(x)==mp[idx].end() || mp[idx][x]>y)
39
40
         mp[idx][x]=y;
41
42
     printf("%d\n",r);
43
     return 0;
44 | }
        插头 DP
   8.4
   Tower Defence 独立插头 + 构造解
   构造解的时候保存的是在 hash map 的 ele 数组的下标位置
   没想清楚千万别去写
  |int bit[12];
 1
 2
 3
   inline int getbit(long long sta,int pos)
 4
   {
 5
     return sta/bit[pos]%bit[1];
   }
 6
 8
   inline long long setbit(long long sta,int pos,int val)
 9
10
     return sta/bit[pos+1]*bit[pos+1]+val*bit[pos]+sta%bit[pos];
   }
11
12
```

```
13 | int n,m,mp[30][10];
   char buf[30][10];
15
   hash_map dp[2];
16
   bool flag;
17
   int key,val,upd,l,u,res,msk,cov,now,pr,resnow,resmsk,pru;
18
   int w[15],s[15],top;
19
   int pre[210][10007],preuse[210][10007];
20
21
   void decode(int msk,int& key,int& cov)
22
   {
23
     int tmp;
24
     key = cov = 0;
25
     for (int i = 0; i < m+1; i++)
26
27
        tmp = getbit(msk,i);
28
        if (tmp > 0)
29
30
          key = setbit(key,i,tmp-1);
31
          cov = setbit(cov,i,1);
32
       }
33
     }
   }
34
35
36
   int encode(int key,int cov)
37
38
     int res = 0, tmp;
     for (int i = 0; i < m+1; i++)
39
40
41
        tmp = getbit(cov,i);
42
        if (tmp > 0)
43
44
          tmp = getbit(key,i);
45
          res = setbit(res,i,tmp+1);
46
        }
47
48
     return res;
   }
49
50
51
   void update(int a,int key,int cov,int val)
52
53
     int msk = encode(key,cov);
54
     int pos;
55
     if (dp[a][msk] < val)
56
     {
57
        dp[a][msk] = val;
58
        pos = dp[a].fint(msk);
59
        pre[now][pos] = pr;
60
        preuse[now][pos] = pru;
61
   }
62
63
```

```
64 | int count3(int sta)
 65
    {
 66
       int res = 0;
 67
       for (int i = 0; i < m+1; i++)
 68
         if (getbit(sta,i) == 3)
 69
           res++;
 70
       return res;
    }
 71
 72
 73
    void expand(int sta)
 74
 75
       top = 0;
 76
       for (int i = 0; i < m+1; i++)
 77
         if (qetbit(sta,i) == 1)
 78
           s[top++] = i;
 79
         else if (getbit(sta,i) == 2)
 80
 81
           w[s[top-1]] = i;
 82
           w[i] = s[top-1];
 83
           top--;
 84
         }
 85
    }
 86
 87
    int main()
 88
    {
 89
       //freopen("TD.in","r",stdin);
       //freopen("TDM.out","w",stdout);
 90
      bit[0] = 1;
 91
 92
       for (int i = 1; i < 12; i++) bit\lceil i \rceil = bit \lceil i-1 \rceil *5;
93
       int t;
 94
       scanf("%d",&t);
 95
       dp[0].init();
 96
       dp[1].init();
 97
       for (int ft = 1; ft <= t; ft++)
 98
       {
 99
         scanf("%d%d",&n,&m);
100
         res = 0;
101
         memset(mp,0,sizeof(mp));
102
         memset(pre,0,sizeof(pre));
103
         memset(preuse,0,sizeof(preuse));
104
         for (int i = 0; i < n; i++)
105
           scanf("%s",buf[i]);
106
107
           for (int j = 0; j < m; j++)
108
             if (buf[i][j] == '.')
109
               mp[i][j] = 1;
110
             else if (buf[i][j] != 'B')
111
               mp[i][j] = 2;
112
         }
113
         dp[0].clear();
114
         dp[1].clear();
```

```
115
        flaq = 0;
116
        dp[flag][0] = 0;
117
        int res = 0;
118
        now = 0:
119
        for (int i = 0; i < n; i++)
120
121
          for (int j = 0; j < m; j++)
122
          {
123
            dp[!flag].clear();
124
             for (int k = 0; k < dp[flaq].N; k++)
125
126
              msk = dp[flag].ele[k].key;
127
               pr = k;
               val = dp[flag].ele[k].val;
128
               decode(msk,key,cov);
129
130
               l = getbit(key, j);
131
               u = getbit(key, j+1);
132
               if (mp[i][j] == 0)//是障碍
133
134
                 if (1 == 0 \&\& u == 0)
135
                 {
136
                   pru = 0;
137
                   update(!flag,key,setbit(setbit(cov,j,0),j+1,0),val);
138
139
               }
140
               else
141
               {
142
                 if (mp[i][i] == 1 && l == 0 && u == 0)//不要插头
                 {
143
144
                   pru = 1;
                   update(!flag,key,setbit(setbit(cov,j,0),j+1,0),val);
145
146
                 if (qetbit(cov, j) == 1 \&\& l == 0)
147
                                                      continue;//不可以在
                    这里搞插头
148
                 if (getbit(cov, j+1) == 1 \&\& u == 0) continue;
                 cov = setbit(setbit(cov,j,1),j+1,1);//更新覆盖情况
149
150
                 upd = setbit(setbit(key,j,0),j+1,0);
151
                 pru = 2;
152
                 if (mp[i][j] == 2)
153
154
                   if (1 == 0 \&\& u == 0)
155
156
                     if (count3(key) < 2)//可以新建独立插头
157
                     {
158
                       if (mp[i][j+1] != 0)
159
                         update(!flag,setbit(setbit(key,j,0),j+1,3),cov,
                            val+1);
                       if (mp[i+1][j] != 0)
160
                         update(!flag,setbit(setbit(key,j,3),j+1,0),cov,
161
                            val+1);
                     }
162
```

```
163
                   }
164
                   else if (l == 0 \mid l \mid u == 0)
165
166
                     if (l+u < 3 && count3(key) < 2)//可以用一个独立插头来
                        结束这条路径
167
                     {
168
                       expand(key);
169
                       if (1 > 0)
                         update(!flag,setbit(upd,w[j],3),cov,val+1);
170
171
                       else
172
                         update(!flag,setbit(upd,w[j+1],3),cov,val+1);
173
174
                     else if (l+u == 3 && upd == 0)//路径的一端
175
176
                       if (res < val+1)
177
                       {
178
                         res = val+1;
179
                         resnow = now-1;
180
                         resmsk = k;
181
                       }
182
                     }
                   }
183
184
                 }
185
                 else if (l == 0 \&\& u == 0)
186
187
                   if (mp[i][j+1] != 0 && mp[i+1][j] != 0)//可以新建插头
188
                     update(!flag,setbit(setbit(key,j,1),j+1,2),cov,val
                        +1);
189
                 }
190
                 else if (l == 0 \mid l \mid u == 0)
191
192
                   if (mp[i][j+1] != 0)//可以延续插头
193
                     update(!flag,setbit(upd,j+1,l+u),cov,val+1);
194
                   if (mp[i+1][j] != 0)//可以延续插头
195
                     update(!flag,setbit(upd,j,l+u),cov,val+1);
196
197
                 else if (l == u)
198
199
                   if (1 < 3) //合并两个相同的括号
200
                   {
201
                     expand(key);
202
                     if (l == 1)
203
                       update(!flag,setbit(upd,w[j+1],1),cov,val+1);
204
                     else
205
                       update(!flag,setbit(upd,w[j],2),cov,val+1);
206
207
                   else if (upd == 0)//合并两个独立插头
208
209
                     if (res < val+1)
210
211
                       res = val+1;
```

```
212
                       resnow = now-1;
213
                       resmsk = k;
214
                     }
215
                   }
216
                 }
217
                 else if (l == 3 || u == 3)//合并独立插头与括号
218
                   expand(key);
219
                   if (1 == 3)
220
221
                     update(!flag,setbit(upd,w[j+1],3),cov,val+1);
222
223
                     update(!flag,setbit(upd,w[j],3),cov,val+1);
224
                 }
225
                 else if (l == 2 || u == 1) //合并)(
226
                   update(!flag,upd,cov,val+1);
               }
227
228
229
             flag = !flag;
230
             now++;
231
232
           if (i+1 == n)
                           break;
233
234
           dp[!flag].clear();
235
           for (int k = 0; k < dp[flag].N; k++)
236
237
             msk = dp[flaq].ele[k].key;
238
             pr = k;
239
             val = dp[flaq].ele[k].val;
240
             pru = 0;
241
             decode(msk,key,cov);
242
             update(!flag,key*bit[1],cov*bit[1],val);
243
           }
244
           now++;
245
           flag = !flag;
        }
246
247
248
        printf("Case_\%d:\_\%d\n",ft,res);
249
        for (int i = resnow; i >= 0; i--)
250
        {
251
           if (preuse[i][resmsk] == 1)
252
             buf[i/(m+1)][i\%(m+1)] = 'W';
253
           resmsk = pre[i][resmsk];
254
255
        for (int i = 0; i < n; i++)
256
           printf("%s\n",buf[i]);
257
        printf("\n");
258
259
      return 0;
260 |}
```

9 杂物

9.1 高精度数

支持乘以整数和加法。

```
struct BigInt
 2
   {
 3
     const static int mod = 100000000;
 4
     int a[600],len;
 5
     BigInt (){}
 6
     BigInt (int v)
 7
 8
        len = 0;
 9
        do
10
        {
11
          a[len++] = v mod;
12
          v /= mod;
13
        }while(v);
14
15
     BigInt operator *(const int& b) const
16
     {
17
        BigInt res;
        res.len = len;
18
        for (int i = 0; i \le len; ++i)
19
20
          res.a[i] = 0;
21
        for (int i = 0; i < len; ++i)
22
23
          res.a[i] += a[i]*b;
24
          res.a[i+1] += res.a[i]/mod;
25
          res.a[i] %= mod;
26
        }
27
        if (res.a[len] > 0) res.len++;
28
        return res;
29
30
     BigInt operator +(const BigInt& b) const
31
32
        BigInt res;
33
        res.len = max(len,b.len);
34
        for (int i = 0; i \le res.len; ++i)
35
          res.a[i] = 0;
36
        for (int i = 0; i < res.len; ++i)
37
38
          res.a[i] += ((i < len)?a[i]:0)+((i < b.len)?b.a[i]:0);
39
          res.a[i+1] += res.a[i]/mod;
40
          res.a[i] %= mod;
41
        }
42
        if (res.a[res.len] > 0) res.len++;
43
        return res;
44
45
     void output()
```

```
46
     {
       printf("%d",a[len-1]);
47
48
       for (int i = len-2; i >= 0; —i)
49
          printf("%08d",a[i]);
       printf("\n");
50
51
52 };
        整数外挂
   9.2
   int wg;
   char ch;
 3
   bool ng;
   inline int readint()
 6
   {
 7
     ch = getchar();
     while (ch != '-' && (ch < '0' || ch > '9')) ch = getchar();
 8
     if (ch == '-')
 9
10
     {
11
       ng = true;
12
       ch = getchar();
     }
13
14
     else
15
       ng = false;
16
     wq = ch-'0';
     ch = getchar();
17
18
     while (ch >= '0' && ch <= '9')
19
20
       wg = wg*10+ch-'0';
21
       ch = getchar();
22
23
     if (ng == true) wg = -wg;
24
     return wg;
25 |}
   9.3
        Java
   9.3.1 文件操作
  |import java.io.*;
   import java.util.*;
   import java.math.*;
   import java.text.*;
 6
   public class Main
 7
 8
     public static void main(String args□) throws
        FileNotFoundException, IOException
10
11
       Scanner sc = new Scanner(new FileReader("a.in"));
```

```
12
       PrintWriter pw = new PrintWriter(new FileWriter("a.out"));
13
       int n,m;
14
       n=sc.nextInt();//读入下一个INT
15
       m=sc.nextInt();
16
17
       for(ci=1; ci<=c; ++ci)
18
19
         pw.println("Case_#"+ci+":_easy_for_output");
20
       }
21
22
       pw.close();//关闭流并释放,这个很重要,否则是没有输出的
23
       sc.close();//关闭流并释放
24
     }
25 |}
   9.3.2 优先队列
   |PriorityQueue queue = new PriorityQueue( 1, new Comparator()
 2
 3
     public int compare( Point a, Point b )
 4
 5
     if(a.x < b.x | | a.x == b.x && a.y < b.y)
 6
       return -1;
 7
     else if( a.x == b.x \& a.y == b.y )
 8
       return 0;
9
     else
10
       return 1;
11
12 |});
   9.3.3 Map
 1 |Map map = new HashMap();
   map.put("sa","dd");
   |String str = map.get("sa").toString;
 4
 5
   for(Object obj : map.keySet()){
     Object value = map.get(obj );
   }
 7
   9.3.4 sort
   static class cmp implements Comparator
 2
 3
     public int compare(Object o1,Object o2)
 4
 5
     BigInteger b1=(BigInteger)o1;
 6
     BigInteger b2=(BigInteger)o2;
 7
     return b1.compareTo(b2);
 8
9
   public static void main(String[] args) throws IOException
11
   {
```

```
12
     Scanner cin = new Scanner(System.in);
13
     int n;
     n=cin.nextInt();
14
15
     BigInteger[] seg = new BigInteger[n];
16
     for (int i=0;i< n;i++)
17
     seq[i]=cin.nextBigInteger();
18
     Arrays.sort(seq,new cmp());
19 |}
   9.4 hashmap
   struct hash_map
 2
 3
     const static int mod=10007;
 4
     int head[mod];
 5
     struct hash_tables
 6
     {
 7
        int key;
 8
        int val;
 9
        int next;
10
     } ele[10007];
11
     int N;
12
     int getHash(int x)
13
     {
14
        return x%mod; //小心负数
15
16
     void init()
17
18
        memset(head, 255, sizeof(head));
19
       N=0;
20
     }
21
     void clear()
22
23
        for (int i = 0; i < N; i++)
24
          head[getHash(ele[i].key)] = -1;
25
       N = 0;
26
27
     int fint(int x)
28
29
        for (int i=head[getHash(x)]; i!=-1; i=ele[i].next)
30
          if (ele[i].key==x) return i;
31
        return -1;
32
33
     void insert(int x)
34
35
        int tmp=getHash(x);
36
        ele[N].key=x;
37
        ele[N].val=0;
38
        ele[N].next=head[tmp];
39
        head[tmp]=N++;
40
     int& operator \prod (int x)
41
```

```
42
     {
43
       int tmp=fint(x);
44
       if (tmp==-1)
45
       {
46
         insert(x);
47
         return ele[N-1].val;
48
       }
49
       else
50
         return ele[tmp].val;
51
52 };
        C++&STL 常用函数
   9.5
   9.5.1 lower_bound/upper_bound
   不解释
 1 | iterator lower_bound(const key_type &key )
   \\返回一个迭代器, 指向键值 >= key 的第一个元素。
   iterator upper_bound(const key_type &key )
   \\返回一个迭代器, 指向键值 > key 的第一个元素。
 5
 6
   #include <iostream>
 7
   #include <algorithm>
 8
   #include <vector>
 9
   using namespace std;
10
11
   int main () {
12
     int myints [] = \{10, 20, 30, 30, 20, 10, 10, 20\};
13
     vector<int> v(myints,myints+8);
     // 10 20 30 30 20 10 10 20
14
15
     vector<int>::iterator low,up;
16
17
     sort (v.begin(), v.end());
18
     // 10 10 10 20 20 20 30 30
19
20
     low=lower_bound (v.begin(), v.end(), 20);
21
     // 10 10 10 20 20 20 30 30
22
     //
23
     up= upper_bound (v.begin(), v.end(), 20);
24
     // 10 10 10 20 20 20 30 30
25
     //
26
27
     cout << "lower_bound_at_position_" << int(low— v.begin()) << endl
28
     cout << "upper_bound_at_position_" << int(up − v.begin()) << endl
29
30
     return 0;
31 |}
```

Output:

```
1 |lower_bound at position 3
2 upper_bound at position 6
  9.5.2 rotate
  把数组后一半搬到前面
 |template <class ForwardIterator>
2
    void rotate (ForwardIterator first, ForwardIterator middle,
3
                   ForwardIterator last );
  9.5.3 nth element
 |template <class RandomAccessIterator>
1
2
    void nth_element ( RandomAccessIterator first,
       RandomAccessIterator nth,
3
                        RandomAccessIterator last );
4
  template <class RandomAccessIterator, class Comapre>
6
    void nth_element ( RandomAccessIterator first,
       RandomAccessIterator nth,
7
                        RandomAccessIterator last, Compare comp );
  9.5.4 bitset
  取用
1 |bitset<4> mybits;
2
                           // 0010
  mybits[1]=1;
4 | mybits[2]=mybits[1];
                            // 0110
  翻转
1 |bitset<4> mybits (string("0001"));
 cout << mybits.flip(2) << endl;  // 0101</pre>
  cout << mybits.flip() << endl;</pre>
                                       // 1010
  运算
1 |bitset<4> first (string("1001"));
2
  bitset<4> second (string("0011"));
  cout << (first^=second) << endl;</pre>
                                            // 1010 (XOR,assign)
  cout << (first&=second) << endl;
cout << (first!=second) << endl;</pre>
                                             // 0010 (AND,assign)
                                              // 0011 (OR,assign)
 cout << (first<<=2) << endl;</pre>
                                              // 1100 (SHL,assign)
```

```
|cout << (first>>=1) << endl;
                                                  // 0110 (SHR,assign)
10
11
   cout << (~second) << endl;</pre>
                                                  // 1100 (NOT)
                                                  // 0110 (SHL)
12
   cout << (second<<1) << endl;</pre>
                                                  // 0001 (SHR)
13
   cout << (second>>1) << endl;</pre>
14
15
   cout << (first==second) << endl;</pre>
                                                 // false (0110==0011)
   cout << (first!=second) << endl;</pre>
                                                 // true (0110!=0011)
17
18 | cout << (first&second) << endl;
                                                 // 0010
                                                 // 0111
19 | cout << (first|second) << endl;</pre>
20 | cout << (first^second) << endl;</pre>
                                                 // 0101
   9.5.5 multimap
   遍历
  |multimap<char,int> mymm;
 2 |multimap<char,int>::iterator it;
   char c;
 4
   mymm.insert(pair<char,int>('x',50));
6 mymm.insert(pair<char,int>('y',100));
7 mymm.insert(pair<char,int>('y',150));
   mymm.insert(pair<char,int>('y',200));
   mymm.insert(pair<char,int>('z',250));
10 | mymm.insert(pair<char,int>('z',300));
11
12
   for (c='x'; c<='z'; c++)
13
   {
      cout << "There are << (int) mymm.count(c);</pre>
14
     cout << "⊔elements⊔with⊔key⊔" << c << ":";
15
     for (it=mymm.equal_range(c).first; it!=mymm.equal_range(c).second
16
         ; ++it)
        cout << "" << (*it).second;
17
      cout << endl;</pre>
18
   }
19
20
   /*
21 | Output:
22
23 | There are 1 elements with key x: 50
24 There are 3 elements with key y: 100 150 200
25
   There are 2 elements with key z: 250 300
26 |*/
   二分查找
 1 |multimap<char,int> mymultimap;
   multimap<char,int>::iterator it,itlow,itup;
 3
   mymultimap.insert(pair<char,int>('a',10));
```

```
mymultimap.insert(pair<char,int>('b',121));
   mymultimap.insert(pair<char,int>('c',1001));
   mymultimap.insert(pair<char,int>('c',2002));
mymultimap.insert(pair<char,int>('d',11011));
 8
 9
   mymultimap.insert(pair<char,int>('e',44));
10
   itlow=mymultimap.lower_bound ('b'); // itlow points to b
11
12
   itup=mymultimap.upper_bound ('d'); // itup points to e (not d)
13
14
   // print range [itlow,itup):
15
   for ( it=itlow ; it != itup; it++ )
16
     cout << (*it).first << "_=>_" << (*it).second << endl;
17
   /*
18
19
   Output:
20
21 | b = > 121
22 | c => 1001
23 c => 2002
24 | d => 11011
25 |*/
   删除
 1 |multimap<char,int> mymultimap;
   |multimap<char,int>::iterator it;
 3
 4
   // insert some values:
   |mymultimap.insert(pair<char,int>('a',10));
   mymultimap.insert(pair<char,int>('b',20));
   mymultimap.insert(pair<char,int>('b',30));
mymultimap.insert(pair<char,int>('c',40));
   mymultimap.insert(pair<char,int>('d',50));
10
   mymultimap.insert(pair<char,int>('d',60));
11
   |mymultimap.insert(pair<char,int>('e',70));
12
   mymultimap.insert(pair<char,int>('f',80));
13
14 | it=mymultimap.find('b');
15 |mymultimap.erase (it);
16
   // erasing by iterator (1 element)
17
18 | mymultimap.erase ('d');
19
   // erasing by key (2 elements)
20
21 | it=mymultimap.find ('e');
22 | mymultimap.erase ( it, mymultimap.end() );
23
   // erasing by range
24
25
   // show content:
26
   for ( it=mymultimap.begin() ; it != mymultimap.end(); it++ )
27
     cout << (*it).first << "□=>□" << (*it).second << endl;
28
```

```
29 | /*
30 | Output:
31 |
32 | a => 10
33 | b => 30
34 | c => 40
35 | */
```

9.6 位运算

9.6.1 基本操作

注意括号

功能	示例	位运算
	$ \ (101101 \to 10110) $	x shr 1
在最后加一个 0	$(101101 \rightarrow 1011010)$	x shl 1
在最后加一个 1	$(101101 \rightarrow 1011011)$	x shl 1+1
把最后一位变成 1	(101100 o 101101)	x or 1
把最后一位变成 0	(101101 o 101100)	x or 1-1
最后一位取反	(101101 o 101100)	x xor 1
把右数第 k 位变成 1	$(101001 \to 101101, k = 3)$	x or (1 shl (k-1))
把右数第 k 位变成 0	$ (101101 \rightarrow 101001, k = 3) $	x and not $(1 shl (k-1))$
右数第 k 位取反	$ (101001 \to 101101, k = 3) $	x xor (1 shl (k-1))
取末三位	(1101101 o 101)	x and 7
取末 <i>k</i> 位	$(1101101 \to 1101, k = 5)$	x and $(1 shl k-1)$
取右数第 k 位	$ (1101101 \to 1, k = 4) $	x shr (k-1) and 1
把末 k 位变成 1	$ (101001 \to 101111, k = 4) $	x or (1 shl k-1)
末 k 位取反	$ (101001 \to 100110, k = 4) $	x xor (1 shl k-1)
把右边连续的 1 变成 0	$ (1001011111 \rightarrow 100100000) $	x and $(x+1)$
把右起第一个 0 变成 1	$ \mid (1001011111 \rightarrow 1001111111) $	x or (x+1)
把右边连续的 0 变成 1	$(11011000 \rightarrow 11011111)$	x or (x-1)
取右边连续的 1	$ \mid (1001011111 \to 1111) $	(x xor (x+1)) shr 1
去掉右起第一个 1 的左边	$\ \ (100101000 \rightarrow 1000)$	x and $(x xor (x-1))$
-	•	·

9.6.2 枚举长为 n 含 k 个 1 的 01 串

```
1 \mid int n = 5, k = 3;
   for (int \dot{s} = (1 << k)-1, u = 1 << n; s < u;)
 2
 3
 4
      for (int i = 0; i < n; i++)
 5
        printf("%d",(((s>>(n-1-i))\&1) == 1));
      printf("\n");
 6
 7
     int b = s \& -s;
 8
      s = (s+b) | (((s^{(s+b))}>2)/b);
 9
10 }
```

9.7 其它

9.7.1 对跑脚本

```
1 while true; do
2   ./gen > input
3   ./sol < input > output.sol
4   ./bf < input > output.bf
5
6   diff output.sol output.bf
7   if [ $? -ne 0 ] ; then break; fi
8 done
```