ACM TEMPLATE

UESTC_Lasagne

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1 注意事项

输入输出格式?调试信息?初始化?算术溢出?数组大小?

左右端点范围? acos/asin/sqrt 函数定义域? 精度问题?

二分答案?暴力?单调性?凸性?块状结构?函数式?对偶问题?

排序的时候注意一下是否需要记录排序前的位置!

使用 map 进行映射的时候,不要用下面这种不安全写法

```
1 | if (mp.find(s) == mp.end())
2    mp[s] = mp.size()-1;//挂成狗
3    
4    if (mp.find(s) == mp.end())
5    {
6       int tmp = mp.size();
7    mp[s] = tmp;//正确
8    }
```

106 数量级慎用后缀数组

TLE 的时候要冷静哟。。

思考的时候结合具体步骤来的话会体会到一些不同的东西

C++ 与 G++ 是很不一样的。。。

map 套字符串是很慢的。。。

栈会被记录内存。。。

浮点数最短路要注意取 < 来判断更新。。。

注意 long long

不要相信.size()

重复利用数组时小心数组范围

先构思代码框架每当实际拍马框架变化时停手重新思考

有时候四边形不等式也是帮得上忙的 dp 优化是可以水的

结构体里面带数组会非常慢, 有时候 BFS 把数组压成数字会快很多。

```
1 void fun(int a[])
2 {
3 printf("%d\n",sizeof(a));
4 }
```

结果是 sizeof(a[0]), 如果传数组指针然后要清空的话不要用 sizeof。

sqrt 某些时候会出现 sqrt(-0.00) 的问题。

将 code::blocks 的默认终端改成 gnome-terminal

1 gnome—terminal —t \$TITLE -x

最小割割集找法在残量网络中从源点出发能到的点集记为 S 原图中 S 到 S' 的边即是最小割集

double 全局变量初始值可能不是 0

2 字符串处理

2.1 *AC 自动机

别忘记 Build

2.1.1 指针

```
1 const int CHAR=26;
   const int TOTLEN=500000;
   const int MAXLEN=1000000;
   struct Vertex
 5
   {
     Vertex *fail,*next[CHAR];
 6
 7
     Vertex(){}
 8
     Vertex(bool flag)//为什么要这样写?
 9
        fail=0;
10
11
       memset(next,0,sizeof(next));
     }
12
13
   };
14
   int size;
   Vertex vertex[TOTLEN+1];
   void init()
16
17
18
     vertex[0]=Vertex(0);
19
     size=1;
20
21
   void add(Vertex *pos,int cha)
22
23
     vertex[size]=Vertex(0);
24
     pos->next[cha]=&vertex[size++];
25
   }
26
   void add(vector<int> s)
27
28
     int l=s.size();
29
     Vertex *pos=&vertex[0];
     for (int i=0; i<l; i++)</pre>
30
31
32
        if (pos->next[s[i]]==NULL)
33
          add(pos,s[i]);
34
        pos=pos->next[s[i]];
35
     }
36
   }
   void bfs()
37
38
39
     queue<Vertex *> que;
40
     Vertex *u=&vertex[0];
     for (int i=0; i<CHAR; i++)</pre>
41
42
        if (u->next[i]!=NULL)
43
        {
```

```
44
          que.push(u->next[i]);
45
          u->next[i]->fail=u;
        }
46
47
        else
48
          u->next[i]=u;
49
      u->fail=NULL;
     while (!que.empty())
50
51
      {
52
        u=que.front();
53
        que.pop();
        for (int i=0; i<CHAR; i++)</pre>
54
          if (u->next[i]!=NULL)
55
56
          {
57
            que.push(u->next[i]);
            u->next[i]->fail=u->fail->next[i];
58
          }
59
60
          else
61
            u->next[i]=u->fail->next[i];
62
      }
   }
63
         非指针
   2.1.2
   struct Trie
 1
 2
   {
 3
      int next[50][10], fail[50];
 4
      bool end[50];
 5
      int L,root;
 6
 7
      int newNode()
 8
      {
 9
        for (int i = 0;i < 10;i++)
10
          next[L][i] = -1;
        end[L] = false;
11
12
        return L++;
      }
13
14
      void Init()
15
16
17
        L = 0;
        root = newNode();
18
      }
19
20
21
      void Insert(char s[])
22
      {
23
        int now = root;
24
        for (int i = 0;s[i] != 0;i++)
25
26
          if (next[now][s[i]-'0'] == -1)
27
            next[now][s[i]-'0'] = newNode();
28
          now = next[now][s[i]-'0'];
29
        }
```

```
end[now] = true;
30
31
     }
32
33
     void Build()
34
35
        queue<int> Q;
        for (int i = 0;i < 10;i++)
36
37
          if (next[root][i] == −1)
38
            next[root][i] = root;
39
          else
40
          {
41
            fail[next[root][i]] = root;
42
            Q.push(next[root][i]);
43
44
        while (!Q.empty())
45
        {
46
          int now = Q.front();
47
          Q.pop();
          end[now] |= end[fail[now]];
48
49
          for (int i = 0;i < 10;i++)
            if (next[now][i] == -1)
50
51
              next[now][i] = next[fail[now]][i];
52
            else
53
            {
              fail[next[now][i]] = next[fail[now]][i];
54
55
              Q.push(next[now][i]);
            }
56
57
        }
58
     }
59 | };
   2.2
        后缀数组
   2.2.1 DC3
   所有下标都是 0 \text{ n-1}, height[0] 无意义。
 1 | / / 所有相关数组都要开三倍
   const int maxn = 300010;
   |# define F(x) ((x)/3+((x)%3==1?0:tb))
   # define G(x) ((x) < tb?(x) *3+1:((x)-tb) *3+2)
   int wa[maxn * 3], wb[maxn * 3], wv[maxn * 3], ws[maxn * 3];
   int c0(int *r, int a, int b)
 7
   {
 8
     return
 9
     r[a] == r[b] \&\& r[a + 1] == r[b + 1] \&\& r[a + 2] == r[b + 2];
10
11
   int c12(int k, int *r, int a, int b)
12
   {
13
     if (k == 2)
        return r[a] < r[b] \mid | r[a] == r[b] && c12(1, r, a + 1, b + 1);
14
     else return r[a] < r[b] \mid | r[a] == r[b] && wv[a + 1] < wv[b + 1];
15
16 | }
```

```
void sort(int *r, int *a, int *b, int n, int m)
18
   {
19
     int i;
20
     for (i = 0; i < n; i++) wv[i] = r[a[i]];
     for (i = 0; i < m; i++) ws[i] = 0;
21
     for (i = 0; i < n; i++) ws[wv[i]]++;</pre>
22
     for (i = 1; i < m; i++) ws[i] += ws[i - 1];
23
24
     for (i = n - 1; i >= 0; i—) b[-ws[wv[i]]] = a[i];
25
     return;
26
   void dc3(int *r, int *sa, int n, int m)
27
28
29
     int i, j, *rn = r + n;
     int *san = sa + n, ta = 0, tb = (n + 1) / 3, tbc = 0, p;
30
31
     r[n] = r[n + 1] = 0;
     for (i = 0; i < n; i++) if (i % 3 != 0) wa[tbc++] = i;</pre>
32
33
     sort(r + 2, wa, wb, tbc, m);
34
     sort(r + 1, wb, wa, tbc, m);
     sort(r, wa, wb, tbc, m);
35
     for (p = 1, rn[F(wb[0])] = 0, i = 1; i < tbc; i++)
36
       rn[F(wb[i])] = c0(r, wb[i - 1], wb[i]) ? p - 1 : p++;
37
38
     if (p < tbc) dc3(rn, san, tbc, p);
39
     else for (i = 0; i < tbc; i++) san[rn[i]] = i;
     for (i = 0; i < tbc; i++) if (san[i] < tb) wb[ta++] = san[i] * 3;</pre>
40
41
     if (n \% 3 == 1) wb[ta++] = n - 1;
42
     sort(r, wb, wa, ta, m);
43
     for (i = 0; i < tbc; i++) wv[wb[i] = G(san[i])] = i;</pre>
     for (i = 0, j = 0, p = 0; i < ta && j < tbc; p++)
44
45
       sa[p] = c12(wb[j] % 3, r, wa[i], wb[j]) ? wa[i++] : wb[j++];
46
     for (; i < ta; p++) sa[p] = wa[i++];
     for (; j < tbc; p++) sa[p] = wb[j++];</pre>
47
48
   //str 和 sa 也要三倍
49
   void da(int str[],int sa[],int rank[],int height[],int n,int m)
50
51
   {
52
     for (int i = n; i < n * 3; i++)
53
       str[i] = 0;
54
     dc3 (str, sa, n + 1, m);
55
     int i, j, k;
56
     for (i = 0; i < n; i++)
57
     {
58
       sa[i] = sa[i + 1];
59
       rank[sa[i]] = i;
60
     for (i = 0, j = 0, k = 0; i < n; height[rank[i ++]] = k)</pre>
61
       if (rank[i] > 0)
62
         for (k ? k - : 0 , j = sa[rank[i] - 1];
63
64
            i + k < n \& i + k < n \& str[i + k] == str[j + k];
65
           k++);
66 |}
```

2.2.2 DA

这份似乎就没啥要注意的了。

```
1 | const int maxn = 200010;
   |int wx[maxn],wy[maxn],*x,*y,wss[maxn],wv[maxn];
 2
 3
   bool cmp(int *r,int n,int a,int b,int l)
 5
 6
     return a+l<n && b+l<n && r[a]==r[b]&&r[a+l]==r[b+l];
 7
 8
   void da(int str[],int sa[],int rank[],int height[],int n,int m)
 9
10
     int *s = str;
11
     int *x=wx,*y=wy,*t,p;
12
     int i,j;
     for(i=0; i<m; i++)wss[i]=0;</pre>
13
14
     for(i=0; i<n; i++)wss[x[i]=s[i]]++;
15
     for(i=1; i<m; i++)wss[i]+=wss[i-1];</pre>
16
     for(i=n-1; i>=0; i--)sa[--wss[x[i]]]=i;
17
     for(j=1,p=1; p<n && j<n; j*=2,m=p)
18
     {
        for(i=n-j,p=0; i<n; i++)y[p++]=i;</pre>
19
        for(i=0; i<n; i++)if(sa[i]-j>=0)y[p++]=sa[i]-j;
20
21
        for(i=0; i<n; i++)wv[i]=x[y[i]];</pre>
        for(i=0; i<m; i++)wss[i]=0;</pre>
22
23
        for(i=0; i<n; i++)wss[wv[i]]++;</pre>
24
        for(i=1; i<m; i++)wss[i]+=wss[i-1];</pre>
25
        for(i=n-1; i>=0; i--)sa[--wss[wv[i]]]=y[i];
26
        for(t=x,x=y,y=t,p=1,i=1,x[sa[0]]=0; i<n; i++)</pre>
27
          x[sa[i]] = cmp(y,n,sa[i-1],sa[i],j)?p-1:p++;
28
     for(int i=0; i<n; i++) rank[sa[i]]=i;</pre>
29
     for(int i=0,j=0,k=0; i<n; height[rank[i++]]=k)</pre>
30
        if(rank[i]>0)
31
32
          for(k?k--:0,j=sa[rank[i]-1];
33
            i+k < n && j+k < n && str[i+k]==str[j+k];
34
            k++);
35 |}
   2.2.3 调用
   注意几个数组的下标是不同的
 1 char s[maxn];
 2
   | int str[maxn],sa[maxn],rank[maxn],height[maxn];
 3
 4
   int main()
 5
   {
 6
     scanf("%s",s);
 7
     int len = strlen(s);
     for (int i = 0;i <= len;i++)</pre>
 8
 9
        str[i] = s[i];
```

```
da(str,sa,rank,height,len,128);
10
11
12
     for (int i = 0;i < len;i++)</pre>
13
     {
        printf("sa=\\d,height=\\d,s=\\s\n",sa[i],height[i],s+sa[i]);
14
15
16
     return 0;
17 | }
   2.2.4 最长公共前缀
   记得不要忘记调用 lcpinit!
 1 | int f[maxn][20];
 2
   int lent[maxn];
   void lcpinit()
 4
   {
 5
     int i,j;
 6
     int n = len,k = 1,l = 0;
     for (i = 0; i < n; i++)</pre>
 7
 8
 9
        f[i][0] = height[i];
        if (i+1 > k*2)
10
11
        {
12
          k *= 2;
13
          l++;
14
15
        lent[i+1] = l;
16
17
     for (j = 1; (1 << j) - 1 < n; j++)
18
        for (i = 0; i+(1<<j)-1<n; i++)
19
          f[i][j] = min(f[i][j-1], f[i+(1<<(j-1))][j-1]);
20
   int lcp(int x,int y)
21
22
23
     if (x > y) swap(x,y);
     if (x == y)
24
        return x-sa[x];//自己和自己当然是自己的长度啦lcp
25
26
     x++;
     int k = lent[y-x+1];
27
28
     return min(f[x][k], f[y-(1<< k)+1][k]);
29 |}
         最长公共前缀大于等于某个值的区间
   2.2.5
   | void getinterv(int pos, int comlen, int& pl, int& pr)
 2
   {
 3
     int l,r,mid,cp;
 4
     l = 0;
 5
     r = pos;
 6
     while (l < r)
```

```
7
     {
 8
        mid = l+r>>1;
        cp = lcp(mid,pos);
 9
        if (cp < comlen)</pre>
10
          l = mid+1;
11
12
        else
13
          r = mid;
14
15
     pl = 1;
16
17
     l = pos;
      r = len-1;
18
19
     while (l < r)
20
21
        mid = l+r+1>>1;
22
        cp = lcp(pos,mid);
23
        if (cp < comlen)</pre>
24
          r = mid-1;
25
        else
26
          l = mid;
27
28
     pr = l;
29 |}
        后缀三兄弟
   2.3
  #include <cstdio>
   #include <cstring>
   #include <algorithm>
   using namespace std;
   const int CHAR = 26;
   const int MAXN = 100000;
 7
   struct SAM_Node
 8
   {
 9
     SAM_Node *fa,*next[CHAR];
10
     int len;
11
     int id,pos;
     SAM_Node() {}
12
13
     SAM_Node(int _len)
14
     {
        fa = 0;
15
        len = _len;
16
17
        memset(next,0,sizeof(next));
18
     }
19
   };
   SAM_Node SAM_node[MAXN * 2], *SAM_root, *SAM_last;
21
   int SAM_size;
22
   SAM_Node *newSAM_Node(int len)
23
   {
24
     SAM_node[SAM_size] = SAM_Node(len);
25
     SAM_node[SAM_size].id=SAM_size;
26
     return &SAM_node[SAM_size++];
```

```
27
   }
28
   SAM_Node *newSAM_Node(SAM_Node *p)
29
30
      SAM_node[SAM_size] = *p;
31
      SAM_node[SAM_size].id=SAM_size;
32
      return &SAM_node[SAM_size++];
33
34
   void SAM_init()
35
   {
36
      SAM_size = 0;
37
      SAM_root = SAM_last = newSAM_Node(0);
38
      SAM_node[0].pos=0;
39
40
   void SAM_add(int x,int len)
41
42
      SAM_Node *p = SAM_last, *np = newSAM_Node(p->len + 1);
43
      np->pos=len;
44
      SAM_last = np;
45
      for (; p && !p->next[x]; p = p->fa)
46
        p->next[x] = np;
47
      if (!p)
48
49
        np->fa = SAM_root;
50
        return ;
51
      }
52
      SAM_Node *q = p->next[x];
53
      if (q->len == p->len + 1)
54
55
        np->fa = q;
56
        return ;
57
58
      SAM_Node *nq = newSAM_Node(q);
59
      nq \rightarrow len = p \rightarrow len + 1;
      q\rightarrow fa = nq;
60
61
      np->fa = nq;
62
      for (; p && p\rightarrownext[x] == q; p = p\rightarrowfa)
63
        p->next[x] = nq;
64
65
   void SAM_build(char *s)
66
67
      SAM_init();
      int l = strlen(s);
68
      for (int i = 0; i < l; i++)
69
70
        SAM_add(s[i] - 'a', i+1);
71
   }
72
73
   SAM_Node * SAM_add(SAM_Node *p, int x, int len)
74
75
      SAM_Node *np = newSAM_Node(p->len + 1);
76
      np->pos = len;
      SAM_last = np;
77
```

```
78
       for (; p && !p->next[x]; p = p->fa)
 79
         p->next[x] = np;
 80
       if (!p)
 81
       {
 82
         np->fa = SAM_root;
 83
         return np;
 84
       }
 85
       SAM_Node *q = p->next[x];
 86
       if (q->len == p->len + 1)
 87
       {
 88
         np \rightarrow fa = q;
 89
         return np;
 90
       }
       SAM_Node *nq = newSAM_Node(q);
 91
 92
       nq \rightarrow len = p \rightarrow len + 1;
 93
       q\rightarrow fa = nq;
 94
       np->fa = nq;
 95
       for (; p && p\rightarrownext[x] == q; p = p\rightarrowfa)
 96
         p->next[x] = nq;
 97
       return np;
 98
 99
    void SAM_build(char *s)//多串建立 注意SAM_init()的调用
100
       int l = strlen(s);
101
       SAM_Node *p = SAM_root;
102
       for (int i = 0; i < l; i++)
103
104
       {
         if (!p->next[s[i] - 'a'] || !(p->next[s[i] - 'a']->len == i +
105
            1))
106
           p=SAM_add(p,s[i] - 'a', i + 1);
107
         else
108
           p = p->next[s[i] - 'a'];
109
       }
    }
110
111
112
    struct ST_Node
113
114
       ST_Node *next[CHAR],*fa;
115
       int len,pos;
116
    }ST_node[MAXN*2],*ST_root;
    int Sufpos[MAXN];
    void ST_add(int u,int v,int chr,int len)
118
119
120
       ST_node[u].next[chr]=&ST_node[v];
121
       ST_node[v].len=len;
122
    void init(int n)
123
124
125
       for (int i=0;i<n;i++)
126
       {
127
         ST_node[i].pos=-1;
```

```
128
         ST_node[i].fa=0;
129
         memset(ST_node[i].next,0,sizeof(ST_node[i].next));
130
      }
131
      ST_node[0].pos=0;
      ST_root=&ST_node[0];
132
133
    void ST_build(char *s)
134
135
136
      int n=strlen(s);
137
      reverse(s,s+n);
138
      SAM_build(s);
      init(SAM_size);
139
      for (int i=1;i<SAM size;i++)</pre>
140
141
         ST_add(SAM_node[i].fa->id,
142
143
           SAM_node[i].id,
           s[SAM_node[i].pos-SAM_node[i].fa->len-1]-'a',
144
145
           SAM_node[i].len—SAM_node[i].fa—>len);
         if (SAM node[i].pos==SAM node[i].len)
146
147
           Sufpos[n—SAM_node[i].pos+1]=i;
148
149
           ST_node[i].pos=n—SAM_node[i].pos+1;
150
         }
      }
151
    }
152
153
154
    int rank[MAXN],sa[MAXN+1];
    int height[MAXN];
155
156
    int L;
157
    void ST_dfs(ST_Node *p)
158
159
      if (p->pos!=-1)
160
         sa[L++]=p->pos;
      for (int i=0;i<CHAR;i++)</pre>
161
         if (p->next[i])
162
163
           ST_dfs(p->next[i]);
164
165
    char s[MAXN+1];
    int main()
166
167
168
      gets(s);
169
      ST_build(s);
170
      L=0;
      ST_dfs(ST_root);
171
      int n=strlen(s);
172
      for (int i=0; i<n; i++)
173
         sa[i]=sa[i+1]-1;
174
      for (int i=0; i<n; i++)
175
176
         rank[sa[i]]=i;
177
      reverse(s,s+n);
      for (int i=0,j=0,k=0; i<n; height[rank[i++]]=k)</pre>
178
```

```
179
        if (rank[i])
180
           for (k?k--:0,j=sa[rank[i]-1]; s[i+k]==s[j+k]; k++);
181 |}
         例题
    2.3.1
  1 #include <iostream>
    #include <algorithm>
    #include <cstdio>
    #include <cstring>
  5 using namespace std;
  6
  7
    const int CHAR = 26;
    const int MAXN = 100000;
  8
  9
 10
    struct SAM_Node
 11
    {
      SAM_Node *fa,*next[CHAR];
 12
 13
      int len;
 14
      int id;
      int mat[9];
 15
      SAM_Node() {}
 16
 17
      SAM_Node(int _len)
 18
      {
 19
        fa = 0;
 20
        len = _len;
 21
        memset(mat,0,sizeof(mat));
 22
        memset(next,0,sizeof(next));
 23
      }
    };
24
25
    SAM_Node SAM_node[MAXN*2],*SAM_root,*SAM_last;
    int SAM_size;
27
    SAM_Node *newSAM_Node(int len)
28
 29
      SAM_node[SAM_size] = SAM_Node(len);
      SAM_node[SAM_size].id = SAM_size;
 30
 31
      return &SAM_node[SAM_size++];
 32
 33
    SAM_Node *newSAM_Node(SAM_Node *p)
 34
    {
 35
      SAM_node[SAM_size] = *p;
      SAM_node[SAM_size].id = SAM_size;
 36
 37
      return &SAM_node[SAM_size++];
 38
 39
    void SAM_init()
40
    {
41
      SAM size = 0;
42
      SAM_root = SAM_last = newSAM_Node(0);
43
44
    void SAM_add(int x,int len)
45
46
      SAM_Node *p = SAM_last,*np = newSAM_Node(p->len+1);
```

```
47
      SAM_last = np;
48
      for (; p&&!p->next[x]; p=p->fa)
49
        p->next[x] = np;
      if (!p)
50
51
52
        np—>fa = SAM_root;
53
        return;
54
      }
55
      SAM_Node *q = p->next[x];
56
      if (q->len == p->len+1)
57
58
        np->fa = q;
59
        return;
60
61
      SAM_Node *nq = newSAM_Node(q);
62
      nq \rightarrow len = p \rightarrow len+1;
63
      q\rightarrow fa = nq;
64
      np->fa = nq;
65
      for (; p\&p->next[x] == q; p = p->fa)
66
        p->next[x] = nq;
67
68
   int getid(char ch)
69
70
      return ch-'a';
71
72
   void SAM_build(char *s)
73
   {
74
      SAM_init();
75
      int l = strlen(s);
76
      for (int i = 0; i < l; i++)
        SAM_add(getid(s[i]),i+1);
77
78
79
   char s[10][MAXN+1];
80 | int ans;
81
   int head[MAXN*2];
82
   struct Edge
83
   {
84
      int to,next;
85
   |} edge[MAXN*2];
   int M;
86
87
   int n;
88
   void add_edge(int u,int v)
89
90
      edge[M].to=v;
91
      edge[M].next=head[u];
92
      head[u]=M++;
93
   }
94
   void dfs(int u)
95
96
      for (int i=head[u]; i!=-1; i=edge[i].next)
97
      {
```

```
98
         int v=edge[i].to;
 99
         dfs(v);
         for (int j=0; j<n-1; j++)
100
101
         SAM_node[u].mat[j]=max(SAM_node[v].mat[j],SAM_node[u].mat[j]);
102
       int tmp=SAM_node[u].len;
103
       for (int i=0; i<n-1; i++)
104
105
         tmp=min(tmp,SAM_node[u].mat[i]);
106
       ans=max(ans,tmp);
107
108
     int main()
109
110
111
       while (scanf("%s",s[n])!=EOF)
112
         n++;
113
       int L=strlen(s[0]);
114
       ans=M=0;
115
       SAM_build(s[0]);
       for (int j=1; j<n; j++)
116
117
         int l=strlen(s[j]),len=0;
118
119
         SAM_Node *p=SAM_root;
120
         for (int i=0; i<l; i++)</pre>
121
         {
           if (p->next[getid(s[i][i])])
122
123
124
              p=p->next[getid(s[j][i])];
125
              p\rightarrow mat[j-1]=max(p\rightarrow mat[j-1],++len);
126
           }
127
           else
128
           {
             while (p && !p->next[getid(s[j][i])])
129
130
                p=p->fa;
              if (!p)
131
132
133
                p=SAM_root;
134
                len=0;
              }
135
              else
136
137
138
                len=p->len+1;
139
                p=p->next[getid(s[j][i])];
140
141
             p\rightarrow mat[j-1]=max(p\rightarrow mat[j-1],len);
142
           }
         }
143
144
145
       memset(head,-1,4*SAM_size);
146
       for (int i=1; i<SAM_size; i++)</pre>
147
         add_edge(SAM_node[i].fa->id,i);
148
       dfs(0);
```

```
printf("%d\n",ans);
149
150
      return 0;
151 |}
    LCS2
  1 | #include < iostream>
    |#include <algorithm>
    #include <cstdio>
    |#include <cstring>
  5
    using namespace std;
  7
    const int CHAR = 26;
    const int MAXN = 100000;
  8
  9
 10
    struct SAM_Node
 11
 12
      SAM_Node *fa,*next[CHAR];
      int len;
 13
 14
      int id;
      int mat[9];
 15
      SAM_Node() {}
 16
      SAM_Node(int _len)
 17
 18
      {
 19
        fa = 0;
 20
        len = _len;
 21
        memset(mat,0,sizeof(mat));
 22
        memset(next,0,sizeof(next));
 23
      }
 24
    };
    SAM_Node SAM_node[MAXN*2],*SAM_root,*SAM_last;
    int SAM_size;
    SAM_Node *newSAM_Node(int len)
 27
 28
 29
      SAM_node[SAM_size] = SAM_Node(len);
 30
      SAM_node[SAM_size].id = SAM_size;
 31
      return &SAM_node[SAM_size++];
 32
 33
    SAM_Node *newSAM_Node(SAM_Node *p)
 34
 35
      SAM_node[SAM_size] = *p;
      SAM_node[SAM_size].id = SAM_size;
 36
 37
      return &SAM_node[SAM_size++];
 38
 39
    void SAM_init()
 40
    {
 41
      SAM_size = 0;
 42
      SAM_root = SAM_last = newSAM_Node(0);
 43
 44
    void SAM_add(int x,int len)
 45
 46
      SAM_Node *p = SAM_last,*np = newSAM_Node(p->len+1);
```

```
47
      SAM_last = np;
48
      for (; p&&!p->next[x]; p=p->fa)
49
        p—>next[x] = np;
      if (!p)
50
51
52
        np—>fa = SAM_root;
53
        return;
      }
54
55
      SAM_Node *q = p->next[x];
56
      if (q->len == p->len+1)
57
58
        np->fa = q;
59
        return;
60
61
      SAM_Node *nq = newSAM_Node(q);
62
      nq \rightarrow len = p \rightarrow len+1;
      q \rightarrow fa = nq;
63
64
      np->fa = nq;
      for (; p\&p->next[x] == q; p = p->fa)
65
66
        p->next[x] = nq;
67
68
   int getid(char ch)
69
70
      return ch-'a';
71
72
   void SAM_build(char *s)
73
   {
74
      SAM_init();
75
      int l = strlen(s);
76
      for (int i = 0; i < l; i++)
        SAM_add(getid(s[i]),i+1);
77
78
79
   char s[MAXN+1];
80 | int ans;
81 | int head[MAXN*2];
82
   struct Edge
83
   {
84
      int to,next;
85
   |} edge[MAXN*2];
   int M;
86
87
   int n;
88
   void add_edge(int u,int v)
89
90
      edge[M].to=v;
91
      edge[M].next=head[u];
92
      head[u]=M++;
93
   }
94
   void dfs(int u)
95
96
      for (int i=head[u]; i!=-1; i=edge[i].next)
97
      {
```

```
98
         int v=edge[i].to;
 99
         dfs(v);
         for (int j=0; j<n; j++)
100
101
         SAM_node[u].mat[j]=max(SAM_node[v].mat[j],SAM_node[u].mat[j]);
      }
102
      int tmp=SAM_node[u].len;
103
      for (int i=0; i<n; i++)
104
105
         tmp=min(tmp,SAM_node[u].mat[i]);
      ans=max(ans,tmp);
106
107
108
    int main()
109
      //freopen("in.txt","r",stdin);
110
      //freopen("out.txt","w",stdout);
111
112
      n=0;
113
      gets(s);
114
      SAM_build(s);
115
      while (gets(s))
116
117
         int l=strlen(s),len=0;
         SAM_Node *p=SAM_root;
118
119
         for (int i=0; i<l; i++)
120
         {
           if (p->next[getid(s[i])])
121
122
           {
123
             p=p->next[getid(s[i])];
             p->mat[n]=max(p->mat[n],++len);
124
           }
125
126
           else
127
           {
128
             while (p && !p->next[getid(s[i])])
129
               p=p->fa;
             if (!p)
130
131
             {
132
               p=SAM_root;
133
               len=0;
134
             }
135
             else
136
             {
137
               len=p->len+1;
               p=p->next[getid(s[i])];
138
139
140
             p->mat[n]=max(p->mat[n],len);
141
           //printf("%d %d %d\n",i,len,p->id);
142
         }
143
144
         n++;
145
      memset(head,-1,4*SAM_size);
146
147
      for (int i=1; i<SAM_size; i++)</pre>
148
         add_edge(SAM_node[i].fa->id,i);
```

```
149 | dfs(0);
150 | printf("%d\n",ans);
151 | return 0;
152 |}
```

2.4 KMP

求 A[0..i] 的一个后缀最多能匹配 B 的前缀多长。先对 B 进行自匹配然后与 A 匹配。KMP[i] 就是对应答案,p[i]+1 是 B[0..i] 的一个后缀最多能匹配 B 的前缀多长。

```
1 //自匹配过程
2
  int j;
   p[0] = j = -1;
   for ( int i = 1; i < lb; i++)
5
     while (j >= 0 && b[j + 1] != b[i]) j = p[j];
6
7
     if (b[j + 1] == b[i]) j ++;
8
     p[i] = j;
9
   }
   //下面是匹配过程
10
11
  |j| = -1;
   for ( int i = 0; i < la; i++)
12
13
14
     while (j >= 0 && b[j + 1] != a[i]) j = p[j];
     if (b[j + 1] == a[i]) j ++;
15
     KMP[i] = j + 1;
16
17 | }
```

2.5 e-KMP

求 A[i..len-1] 和 B 的最长公共前缀有多长。先对 B 进行自匹配然后与 A 匹配。eKMP[i] 就是对应答案。p[i] 是 B[i..len-1] 和 B 的最长公共前缀有多长。

```
1 //自匹配过程
   int j = 0;
   while (j < lb && b[j] == b[j + 1])
3
     j++;
   p[0] = lb, p[1] = j;
   |int k = 1;
   for (int i = 2; i < lb; i++)
7
8
   {
     int Len = k + p[k] - 1, L = p[i - k];
9
     if (L < Len - i + 1)
10
       p[i] = L;
11
12
     else
13
     {
14
       j = max(0, Len - i + 1);
15
       while (i + j < lb && b[i + j] == b[j])
16
         j++;
17
       p[i] = j, k = i;
     }
18
19
20 | / /下面是匹配过程
```

```
21 | j = 0;
22
   while (j < la && j < lb && a[j] == b[j])
23
      j++;
24
   eKMP[0] = j;
25
   k = 0;
26
   for (int i = 1; i < la; i++)</pre>
27
28
      int Len = k + eKMP[k] - 1, L = p[i - k];
29
      if (L < Len - i + 1)
30
        eKMP[i] = L;
31
      else
32
      {
33
        j = max(0, Len - i + 1);
        while (i + j < la && j < lb && a[i + j] == b[j])
34
35
          j++;
36
        eKMP[i] = j, k = i;
37
      }
38 | }
```

2.6 Manacher

```
const int maxn = 110000;
 2
 3
   char Ma[maxn*2];
   int Mp[maxn*2];
 5
   void Manacher(char s[],int len)
 6
 7
     int l = 0;
     Ma[l++] = '.';
 8
     Ma[l++] = ',';
9
10
     for (int i = 0;i < len;i++)</pre>
11
12
        Ma[l++] = s[i];
13
        Ma[l++] = ',';
14
     }
     Ma[l] = 0;
15
     int pnow = 0,pid = 0;
16
17
     for (int i = 1;i < l;i++)</pre>
18
        if (pnow > i)
19
20
          Mp[i] = min(Mp[2*pid-i],pnow-i);
21
        else
22
          Mp[i] = 1;
23
        for (;Ma[i-Mp[i]] == Ma[i+Mp[i]];Mp[i]++);
24
        if (i+Mp[i] > pnow)
25
26
          pnow = i+Mp[i];
27
          pid = i;
28
        }
29
     }
30 | }
```

```
31 | /*
32
   abaaba
33
           a ,
                 b
                   , a
                              а,
              1
                 4
                       2
                           7
                              2
                                1
                                        1
34
    0
       1
           2
                   1
35 | * /
        不同回文串
   2.7
   往 hash 表中插入新东西的时候就说明找到了一个新回文字串
   一共 O(n) 个
 1 | typedef unsigned int uint;
 2
 3
   const int maxn = 110000;
 4
 5
   char Ma[maxn*2];
   int Mp[maxn*2];
 7
   void Manacher(char s[],int len)
 8
   {
 9
     int l = 0;
     Ma[l++] = '.';
10
     Ma[l++] = ',';
11
12
     for (int i = 0; i < len; i++)</pre>
13
     {
14
       Ma[l++] = s[i];
15
       Ma[l++] = ',';
16
     }
17
     Ma[l] = 0;
     int pnow = 0, pid = 0;
18
     for (int i = 1; i < l; i++)</pre>
19
20
21
       if (pnow > i)
22
         Mp[i] = min(Mp[2*pid-i],pnow-i);
23
       else
24
          Mp[i] = 1;
25
       for (; Ma[i-Mp[i]] == Ma[i+Mp[i]]; Mp[i]++);
26
       if (i+Mp[i] > pnow)
27
       {
28
          pnow = i+Mp[i];
29
          pid = i;
30
       }
31
     }
   }
32
33
34
   char s[maxn*2];
35
   int len;
   int p[maxn*2];
   const int muts = 129;
37
38
   uint sum[maxn];
39
   uint mutpower[maxn];
40
41 | struct hash_map
42 | {
```

```
43
     const static int mod = 300007;
44
     int head[mod];
45
     struct hash_tables
46
     {
47
        uint key1;
48
        int key2;
49
        int next;
     } ele[maxn*10];
50
51
     int N;
     void init()
52
53
     {
        memset(head,-1,sizeof(head));
54
55
        N = 0;
56
     int totlen[mod];
57
     void clear()
58
59
60
        for (int i = 0; i < N; i++)
          head[ele[i].key1\%mod] = -1;
61
62
        N = 0;
63
64
     int find(uint x,int len)
65
        int hashcode = x%mod;
66
67
        for (int i = head[hashcode]; i != -1; i = ele[i].next)
          if (ele[i].key1 == x && ele[i].key2 == len)
68
69
            return i;
70
        return -1;
71
     }
72
     void insert(uint x,int len)
73
74
        int tmp = x%mod;
75
        ele[N].key1 = x;
76
        ele[N].key2 = len;
77
        ele[N].next = head[tmp];
78
        head[tmp] = N++;
79
     }
80
   };
81
82
   hash_map hash;
83
   uint gethashcode(int l,int r)
84
85
86
     uint ret;
87
     ret = sum[r];
88
     if (l)
89
        ret -= sum[l-1]*mutpower[r-l+1];
90
     return ret;
   }
91
92
93 | int calc(char s[])
```

```
94
    {
 95
       len = strlen(s);
       Manacher(s,len);
 96
 97
98
       sum[0] = s[0];
 99
       for (int i = 1; i < len; i++)</pre>
         sum[i] = sum[i-1]*muts+s[i];
100
101
102
       int res = 0;
103
       uint tmp;
104
       int nt = 0;
105
       hash.clear();
       //odd
106
       for (int i = 0; i < len; i++)</pre>
107
         if (Mp[i*2+2]\%2 == 0)
108
109
         {
           int pl = Mp[i*2+2]/2;
110
           if (i+pl < nt || pl == 0) continue;</pre>
111
           for (int j = i-pl+1; j <= i; j++)
112
113
             tmp = gethashcode(j,i);
114
115
             if (hash.find(tmp,i-j+1) != -1) break;
116
             hash.insert(tmp,i-j+1);
           }
117
118
           nt = i+pl;
         }
119
120
       res += hash.N;
121
122
       nt = 0;
123
       hash.clear();
124
       //even
125
       for (int i = 0; i < len; i++)</pre>
         if (Mp[i*2+3] > 1)
126
127
           int pl = Mp[i*2+3]/2;
128
129
           if (i+pl < nt || pl == 0) continue;</pre>
130
           for (int j = i-pl+1; j <= i; j++)
131
           {
132
             tmp = gethashcode(j,i);
133
             if (hash.find(tmp,i-j+1) != -1) break;
             hash.insert(tmp,i-j+1);
134
135
136
           nt = i+pl;
         }
137
138
       res += hash.N;
139
       return res;
    }
140
141
    int main()
142
143
144
       mutpower[0] = 1;
```

```
145
       for (int i = 1; i < maxn; i++)</pre>
146
         mutpower[i] = mutpower[i-1]*muts;
       hash.init();
147
148
       int totcas;
149
       scanf("%d",&totcas);
150
       for (int cas = 1; cas <= totcas; cas++)</pre>
151
152
       {
153
         scanf("%s",s);
154
         printf("Case<sub>□</sub>#%d:<sub>□</sub>%d\n",cas,calc(s));
155
156
       }
157
       return 0;
158 }
         * 字符串最小表示法
    2.8
    int Gao(char a[],int len)
  1
  2
  3
       int i = 0, j = 1, k = 0;
       while (i < len && j < len && k < len)
  4
  5
       {
  6
         int cmp = a[(j+k)\%len]-a[(i+k)\%len];
         if (cmp == 0)
  7
  8
           k++;
  9
         else
 10
         {
           if (cmp > 0)
 11
 12
             j += k+1;
 13
           else
 14
             i += k+1;
 15
           if (i == j) j++;
           k = 0;
 16
         }
 17
 18
 19
       return min(i,j);
 20 |}
          带 * 通配符的匹配
    2.9
  1 | #include < iostream>
    #include <algorithm>
  2
    #include <cstdio>
    #include <cstring>
  5
    using namespace std;
  6
  7
    char a[110],b[110],sp[110][110],tot,place[110];
  8
    |int n,la,lb,ll;
  9
 10 | bool check(int id,int pos)
 11 | {
```

```
12
      for (int i = 0;sp[id][i] != 0;i++)
13
        if (b[pos+i] != sp[id][i])
14
          return false;
15
      return true;
   }
16
17
18
   bool check()
19
20
      lb = strlen(b);
21
      int pre = 0;
      for (int i = 0;i < tot;i++)</pre>
22
23
24
        bool find = false;
25
        for (int j = pre; j < lb; j++)
26
          if (check(i,j) == true)
27
          {
28
            place[i] = j;
            pre = place[i]+1;
29
            find = true;
30
31
            break;
32
33
        if (find == false)
                             return false;
34
      if (a[0] != '*')
35
36
        if (place[0] != 0)
37
          return false;
      if (a[la-1] != '*')
38
39
        if (check(tot-1,lb-ll) == false)
40
          return false;
41
      return true;
   }
42
43
   int main()
44
45
46
     while (scanf("%s",a) != EOF)
47
      {
48
        tot = 0;
        for (int i = 0;a[i] != 0;i++)
49
          if (a[i] != '*')
50
51
          {
52
            int j;
53
            for (j = i;a[j] != 0 && a[j] != '*';j++)
54
              sp[tot][j-i] = a[j];
55
            sp[tot++][j-i] = 0;
56
            i = j;
          }
57
58
        la = strlen(a);
59
        ll = strlen(sp[tot-1]);
60
        scanf("%d",&n);
61
        for (int i = 0; i < n; i++)
62
        {
```

```
scanf("%s",b);
63
          if (check() == true)
64
65
            puts(b);
       }
66
     }
67
     return 0;
68
   }
69
   /*
70
   Sample Input 1
71
72
   *.*
73
   4
74 main.c
75 a.out
   readme
76
77 yacc
78
79 | Sample Input 2
80
   *a*a*a
81 4
82
   aaa
83
   aaaaa
84
   aaaaax
   abababa
85
86
87
   Sample Output 1
88 main.c
89
   a.out
90
91 | Sample Output 2
92 aaa
93 aaaaa
94
   abababa
95 */
```

3 数学

3.1 扩展 GCD

```
 \bar{\mathbf{x}}   ax+by=gcd(a,b)  的一组解
   long long ex_gcd(long long a,long long b,long long &x,long long &y)
 2
   {
      if (b)
 3
 4
      {
 5
        long long ret = ex_gcd(b,a\%b,x,y), tmp = x;
 6
 7
        y = tmp-(a/b)*y;
 8
        return ret;
 9
      }
      else
10
11
      {
12
        x = 1;
        y = 0;
13
14
        return a;
15
16 | }
```

3.2 模线性方程组

```
1 / / 有更新
   int m[10],a[10];//模数m 余数a
   bool solve(int &m0,int &a0,int m,int a)//模线性方程组
 4
   {
 5
     int y,x;
     int g=ex_gcd(m0,m,x,y);
 6
 7
     if (abs(a-a0)%g) return 0;
 8
     x*=(a-a0)/g;
 9
     x\%=m/g;
10
     a0=(x*m0+a0);
11
     m0*=m/g;
12
     a0\% = m0;
13
     if (a0<0) a0+=m0;
14
     return 1;
15
   }
16
   int MLES()
17
18
     bool flag=1;
19
     int m0=1,a0=0;
     for (int i=0; i<n; i++)
20
        if (!solve(m0,a0,m[i],a[i]))
21
22
        {
23
          flag=0;
24
          break;
25
     if (flag)
26
```

```
27
        return a0;
28
     else
29
        return -1;
30 |}
        矩阵
   3.3
   乘法的时候将 B 数组转置一下然后 C[i][j] = \sum A[i][k] \times B[j][k] 会有奇效。
   struct Matrix
 1
 2
   {
 3
     int a[52][52];
 4
     void clear()
 5
 6
        memset(a,0,sizeof(a));
 7
     int det(int n)//求行列式的值模上一个数,需要预处理逆元
 8
 9
10
        for (int i = 0; i < n; i++)
11
          for (int j = 0; j < n; j++)
12
            a[i][j] = (a[i][j]\%mod+mod)\%mod;
13
        int res = 1;
        for (int i = 0; i < n; i++)
14
15
        {
          for (int j = i; j < n; j++)
16
17
            if (a[j][i] != 0)
18
            {
              for (int k = i; k < n; k++)
19
                swap(a[i][k],a[j][k]);
20
21
              if (i != j)
22
                res = (res+mod)%mod;
23
              break;
24
25
          if (a[i][i] == 0)
26
27
            res = -1; // 不存在
28
            break;
29
          for (int j = i+1; j < n; j++)
30
31
            int mut = (a[j][i]*inv[a[i][i]])%mod;
32
            for (int k = i;k < n;k++)
33
34
              a[j][k] = (a[j][k]-(a[i][k]*mut)%mod*mod)%mod;
          }
35
          res = (res*a[i][i])%mod;
36
37
        }
38
        return res;
39
40
     Matrix operator * (const Matrix &b)const
41
     {
42
        Matrix res;
        for (int i = 0; i < 52; i++)
43
44
          for (int j = 0; j < 52; j++)
```

```
ACM Template
          {
45
46
            res.a[i][j] = 0;
            for (int k = 0; k < 52; k++)
47
48
              res.a[i][j] += a[i][k] * b.a[k][j];
49
          }
50
       return res;
51
52
     Matrix operator ^ (int y)const
53
       Matrix res, x;
54
55
       for (int i = 0; i < 52; i++)
56
          for (int j = 0; j < 52; j++)
57
            res.a[i][j] = 0, x.a[i][j] = a[i][j];
58
59
          res.a[i][i] = 1;
60
       }
61
       for (; y; y >>= 1, x = x * x)
          if (y & 1)
62
63
            res = res * x;
64
       return res;
65
     }
66 | };
        康拓展开
   3.4
  const int PermSize = 12;
   int factory[PermSize] =
   {1, 1, 2, 6, 24, 120, 720, 5040, 40320, 3628800, 3628800, 39916800};
```

```
4
   int Cantor(int a[])
 5
   {
 6
     int i, j, counted;
 7
     int result = 0;
     for (i = 0; i < PermSize; ++i)</pre>
 8
 9
     {
        counted = 0;
10
        for (j = i + 1; j < PermSize; ++j)
11
          if (a[i] > a[j])
12
13
            ++counted;
14
        result = result + counted * factory[PermSize - i - 1];
15
16
     return result;
17
   }
18
19
   bool h[13];
20
21
   void UnCantor(int x, int res[])
22
23
     int i,j,l,t;
24
     for (i = 1;i <= 12;i++)
25
        h[i] = false;
26
     for (i = 1; i <= 12; i++)
```

```
{
27
28
        t = x / factory[12 - i];
        x = t * factory[12 - i];
29
        for (j = 1, l = 0; l \le t; j++)
30
          if (!h[j])l++;
31
32
        h[j] = true;
33
34
        res[i-1] = j;
35
     }
36
   }
        FFT
   3.5
   const double PI= acos(-1.0);
 2
   struct vir
 3
   {
 4
     double re,im; //实部和虚部
     vir(double a=0,double b=0)
 5
 6
 7
        re=a;
 8
        im=b;
 9
10
     vir operator +(const vir &b)
11
     {return vir(re+b.re,im+b.im);}
12
     vir operator -(const vir &b)
13
      {return vir(re-b.re, im-b.im);}
14
     vir operator *(const vir &b)
15
      {return vir(re*b.re—im*b.im , re*b.im+im*b.re);}
16
   };
17
   vir x1[200005],x2[200005];
   void change(vir *x,int len,int loglen)
19
   {
20
     int i,j,k,t;
21
     for(i=0;i<len;i++)</pre>
22
     {
23
        t=i;
24
        for(j=k=0; j<loglen; j++,t>>=1)
          k = (k << 1) | (t&1);
25
        if(k<i)</pre>
26
27
        {
28
        // printf("%d %d\n",k,i);
29
          vir wt=x[k];
30
          x[k]=x[i];
31
          x[i]=wt;
32
        }
     }
33
34
   void fft(vir *x,int len,int loglen)
35
36
   {
     int i,j,t,s,e;
37
38
     change(x,len,loglen);
39
     t=1;
```

```
40
      for(i=0;i<loglen;i++,t<<=1)</pre>
41
      {
42
        s=0;
        e=s+t;
43
44
        while(s<len)</pre>
45
           vir a,b,wo(cos(PI/t),sin(PI/t)),wn(1,0);
46
47
           for(j=s;j<s+t;j++)
48
           {
49
             a=x[j];
50
             b=x[j+t]*wn;
51
             x[j]=a+b;
52
             x[j+t]=a-b;
53
             wn=wn*wo;
           }
54
55
           s=e+t;
56
           e=s+t;
57
        }
      }
58
59
    }
60
    void dit_fft(vir *x,int len,int loglen)
61
62
      int i,j,s,e,t=1<<loglen;</pre>
      for(i=0;i<loglen;i++)</pre>
63
64
      {
65
        t>>=1;
66
        s=0;
67
        e=s+t;
68
        while(s<len)</pre>
69
        {
           vir a,b,wn(1,0),wo(cos(PI/t),-sin(PI/t));
70
71
           for(j=s;j<s+t;j++)
72
73
             a=x[j]+x[j+t];
74
             b=(x[j]-x[j+t])*wn;
75
             x[j]=a;
76
             x[j+t]=b;
77
             wn=wn*wo;
78
           }
79
           s=e+t;
80
           e=s+t;
81
        }
82
      }
83
      change(x,len,loglen);
84
      for(i=0;i<len;i++)</pre>
        x[i].re/=len;
85
86
87
   int main()
88
    {
89
      char a[100005],b[100005];
90
      int i,len1,len2,len,loglen;
```

```
91
       int t,over;
 92
       while(scanf("%s%s",a,b)!=EOF)
 93
         len1=strlen(a)<<1;</pre>
 94
 95
         len2=strlen(b)<<1;</pre>
         len=1;loglen=0;
 96
         while(len<len1)</pre>
 97
 98
         {
 99
           len<<=1;
                       loglen++;
         }
100
         while(len<len2)</pre>
101
102
           len<<=1;
                      loglen++;
103
104
105
         for(i=0;a[i];i++)
106
         {
           x1[i].re=a[i]-'0';
107
           x1[i].im=0;
108
         }
109
         for(;i<len;i++)</pre>
110
           x1[i].re=x1[i].im=0;
111
112
         for(i=0;b[i];i++)
113
         {
           x2[i].re=b[i]-'0';
114
115
           x2[i].im=0;
         }
116
         for(;i<len;i++)</pre>
117
           x2[i].re=x2[i].im=0;
118
119
         fft(x1,len,loglen);
120
         fft(x2,len,loglen);
         for(i=0;i<len;i++)</pre>
121
           x1[i] = x1[i]*x2[i];
122
         dit_fft(x1,len,loglen);
123
         for(i=(len1+len2)/2-2,over=len=0;i>=0;i—)
124
125
         {
126
           t=(int)(x1[i].re+over+0.5);
127
           a[len++]= t%10;
128
           over = t/10;
129
         }
         while(over)
130
131
         {
           a[len++]=over%10;
132
           over/=10;
133
         }
134
135
         for(len—;len>=0&&!a[len];len—);
           if(len<0)
136
           putchar('0');
137
           else
138
139
              for(;len>=0;len—)
140
                putchar(a[len]+'0');
141
         putchar('\n');
```

```
142
      }
143
      return 0;
144 |}
         爬山法计算器
    3.6
    注意灵活运用。
    双目运算符在 calc() 中,左结合单目运算符在 P() 中,右结合单目运算符在 calc\_exp 中。(但
    是还没遇到过。。)
  1 | #include < iostream>
    #include <cstdio>
  3 #include <cstring>
  4 | #include <algorithm>
  5 #include <string>
    using namespace std;
  6
  7
  8 | char s[100000];
 9
    int n,cur;
 10
    const string OP = "+-*";
 11
 12
    char next_char()
 13
    {
 14
      if (cur >= n) return EOF;
 15
      return s[cur];
    }
 16
 17
    int get_priority(char ch)
 18
 19
    {
      if (ch == '*') return 2;
 20
 21
      return 1;
 22
    }
23
 24
    int P();
25
    int calc(int a,char op,int b)
26
27
    {
 28
      if (op == '+')
 29
        return a+b;
      if (op == '-')
 30
 31
        return a—b;
      if (op == '*')
 32
 33
        return a*b;
    }
 34
 35
 36
    int calc_exp(int p)
 37
 38
      int a = P();
      while ((OP.find(next_char()) != OP.npos) &&
 39
        (get_priority(next_char()) >= p))
40
41
      {
42
        char op = next_char();
```

```
43
        cur++;
44
        a = calc(a,op,calc_exp(get_priority(op)+1));
45
46
      return a;
47
   }
48
49
   int totvar,m,var[26],varid[26];
50
   int P()
51
52
   {
53
      if (next_char() == '-')
54
55
        cur++;
56
        return -P();
57
      }
58
      else if (next_char() == '+')
59
60
        cur++;
61
        return P();
62
63
      else if (next_char() == '(')
64
      {
65
        cur++;
66
        int res = calc_exp(0);
67
        cur++;
68
        return res;
      }
69
70
      else
71
      {
72
        cur++;
        return var[varid[s[cur-1]-'a']];
73
74
      }
   }
75
76
77
   int id[26],minid;
78
   int main()
79
80
81
     while (true)
82
        scanf("%d%d",&totvar,&var[0]);
83
        if (totvar == 0 && var[0] == 0)
84
                                            break;
85
        for (int i = 1; i < totvar; i++)
86
          scanf("%d",&var[i]);
87
        scanf("%d",&m);
        scanf("%s",s);
88
        for (int i = 0;i < 26;i++)
89
90
          id[i] = -1;
        minid = 0;
91
92
        n = strlen(s);
        for (int i = 0; i < n; i++)
93
```

```
94
           if (s[i] >= 'a' && s[i] <= 'z')
 95
           {
             if (id[s[i]−'a'] == −1)
 96
 97
             {
                id[s[i]-'a'] = minid;
 98
 99
               minid++;
             }
100
101
             s[i] = 'a' + id[s[i] - 'a'];
           }
102
103
         for (int i = 0;i < totvar;i++)</pre>
104
           varid[i] = i;
105
         int res = 0;
         do
106
         {
107
           cur = 0;
108
109
           int tmp = calc_exp(0);
110
           if (tmp == m)
111
           {
112
             res++;
113
             break;
           }
114
115
116
         while (next_permutation(varid,varid+totvar));
117
         //puts(s);
118
         if (res > 0)
           puts("YES");
119
120
         else
           puts("NO");
121
122
123
       return 0;
124 }
          线性筛
    3.7
    int N;
    bool isPrime[10001];
    int prime[10000];
  4
    void getPrime(int n)
  5
    {
  6
       memset(isPrime,1,++n);
  7
       N=0;
  8
       isPrime[0]=isPrime[1]=0;
  9
       for (int i=2;i<n;i++)
 10
 11
         if (isPrime[i])
 12
           prime[N++]=i;
 13
         for (int j=0;j<N && prime[j]*i<n;j++)</pre>
 14
 15
           isPrime[i*prime[j]]=0;
 16
           if (i%prime[j]==0)
 17
             break;
```

```
18
        }
19
      }
20
   }
         线性规划
   3.8
   #define MAXM 20 //max num of basic varibles
   #define INF 1E200
   double A[MAXM+5][MAXN+MAXM+5];
 5
   double b[MAXM+5],c[MAXN+MAXM+5];
   int N[MAXN+5],B[MAXM+5];
 7
   double X[MAXN+MAXM+5],V;
   int n,m,R,C,nCnt,bCnt;
 9
   int v1[MAXN],v2[MAXN];
10
11
   int fcmp(double a,double b)
12
   {
13
      if(fabs(a-b)<1E-7) return 0;</pre>
14
      if(a>b) return 1;
15
      return -1;
   }
16
17
18
   void Pivot(int l,int e)
19
20
      double t=A[l][e],p=c[e];
21
      b[l]=b[l]/t;
      for(int i=1;i<=C;i++)</pre>
22
23
        A[l][i]/=t;
24
      V=V-c[e]*b[l];
25
      for(int i=1;i<=R;i++)</pre>
26
      {
27
        if(i==l||fcmp(A[i][e],0.0)==0)
28
          continue;
29
        t=A[i][e];
30
        b[i]=b[i]-t*b[l];
31
        for(int j=1;j<=C;j++)
          A[i][j]=A[i][j]-t*A[l][j];
32
33
34
      for(int i=1;i<=C;i++)</pre>
35
        c[i]=c[i]-p*A[l][i];
      for(int i=1;i<=nCnt;i++)</pre>
36
37
      {
38
        if(N[i]==e)
39
        {
          N[i]=B[l];
40
41
          break;
42
        }
43
      B[l]=e;
44
45
46
```

```
47
   bool Process(double P[])
48
   {
49
      while(true)
50
      {
        int e=-1;
51
52
        double mV=—INF;
        for(int i=1;i<=nCnt;i++)</pre>
53
54
          if(fcmp(P[N[i]],mV)==1)
55
            mV=P[N[i]],e=N[i];
56
        if(fcmp(mV,0.0)<=0) break;
57
        int l=-1;
58
59
        mV=INF;
60
        for(int i=1;i<=bCnt;i++)
61
62
          if(fcmp(A[i][e],0.0)==1)
63
          {
64
            double t=b[i]/A[i][e];
             if(fcmp(mV,t)==1||(fcmp(mV,t)==0&&(l==-1||B[l]>B[i])))
65
               mV=t,l=i;
66
          }
67
68
        }
69
        if(l==-1) return false;
        Pivot(l,e);
70
71
72
      return true;
73
   }
74
75
   bool initSimplex()
76
   {
77
      nCnt=bCnt=0;
78
      for(int i=1;i<=n;i++)</pre>
79
        N[++nCnt]=i;
80
      for(int i=1;i<=m;i++)</pre>
81
        B[++bCnt]=i+n,A[i][n+i]=1.0;
82
      R=bCnt,C=bCnt+nCnt;
83
      double minV=INF;
84
      int p=-1;
85
      for(int i=1;i<=m;i++)</pre>
        if(fcmp(minV,b[i])==1)
86
87
          minV=b[i],p=i;
      if(fcmp(minV,0.0)>=0)
88
89
        return true;
90
      N[++nCnt]=n+m+1;R++,C++;
91
      for(int i=0;i<=C;i++)</pre>
        A[R][i]=0.0;
92
      for(int i=1;i<=R;i++)</pre>
93
94
        A[i][n+m+1]=-1.0;
      Pivot(p,n+m+1);
95
96
      if(!Process(A[R])) return false;
      if(fcmp(b[R],0.0)!=0)
97
```

```
98
         return false;
 99
       p=-1;
       for(int i=1;i<=bCnt&&p==-1;i++)</pre>
100
         if(B[i]==n+m+1) p=i;
101
       if(p!=-1)
102
103
       {
         for(int i=1;i<=nCnt;i++)</pre>
104
105
106
           if(fcmp(A[p][N[i]],0.0)!=0)
107
           {
108
             Pivot(p,N[i]);
109
             break;
           }
110
         }
111
112
       }
113
       bool f=false;
       for(int i=1;i<=nCnt;i++)</pre>
114
115
       {
         if(N[i]==n+m+1) f=true;
116
         if(f&&i+1<=nCnt)
117
           N[i]=N[i+1];
118
119
       }
120
       nCnt--;
       R--, C--;
121
122
       return true;
    }
123
124
    //-1: no solution 1: no bound 0: has a solution -V
125
    int Simplex()
126
127
    {
       if(!initSimplex())
128
129
         return -1;
130
       if(!Process(c))
131
         return 1;
       for(int i=1;i<=nCnt;i++)</pre>
132
133
         X[N[i]]=0.0;
134
       for(int i=1;i<=bCnt;i++)
135
         X[B[i]]=b[i];
136
       return 0;
    }
137
138
    int main()
139
140
       //n = 1; m=1;
141
142
       //V = 0.0;
       //c[1] = 1.0;
143
       //A[1][1] = 1.0;
144
145
       //b[1] = 5.0;
       //Simplex();
146
147
       //printf("V = %.3f\n",V);
148
```

```
149
      while(scanf("%d",&v1[1]) == 1)
150
         {
           for(int i = 2; i<=6;i++)
151
152
             scanf("%d",&v1[i]);
           n = 4; m = 6;
153
           for(int i = 0 ; i<=m+1;i++)</pre>
154
             for(int j=0;j<=n+m+2;j++)</pre>
155
156
               A[i][j] = c[j] = 0;
157
           memset(b,0,sizeof(b));
158
           V = 0.0;
           /*
159
           n 为未知数个数
160
           m 为约束个数
161
           目标: siama(c[i]*xi)
162
           约束: sigma(A[i][j]*xj) <=b[i]; j = 1 ... n
163
164
           解存在 X 里面
165
           */
           b[1] = v1[1]; A[1][1] = 1; A[1][4] = 1;
166
           b[2] = v1[2]; A[2][1] = 1; A[2][3] = 1;
167
           b[3] = v1[3]; A[3][3] = 1; A[3][4] = 1;
168
           b[4] = v1[4]; A[4][2] = 1; A[4][3] = 1;
169
170
           b[5] = v1[5]; A[5][2] = 1; A[5][4] = 1;
171
           b[6] = v1[6]; A[6][1] = 1; A[6][2] = 1;
172
           c[1] = 1; c[2] = 1; c[3] = 1; c[4] = 1;
           Simplex():
173
           //printf("V = %.3f\n",V);
174
175
           printf("%.3f_{\perp}%.3f_{\perp}%.3f_{\perp}%.3f_{\parallel},X[1],X[2],X[3],X[4]);
176
177
         }
178
      return 0;
179
    }
    3.9
         分解质因数
    3.9.1 米勒拉宾 + 分解因数
  1 | #include < ctime >
    #include<iostream>
    #define bint long long
    using namespace std;
  5
    |const int TIME = 8;//测试次数,够了8~10
    int factor[100], fac_top = -1;
  7
  8
    //计算两个数的gcd
    bint gcd(bint small,bint big)
 10
    {
 11
      while(small)
 12
      {
         swap(small,big);
 13
 14
         small%=big;
 15
 16
      return abs(big);
```

```
17
   }
18
19
   //ret = (a*b)%n (n<2^62)
20
   bint muti_mod(bint a,bint b,bint n)
21
22
     bint exp = a%n, res = 0;
23
     while(b)
24
     {
25
        if(b&1)
26
        {
27
          res += exp;
28
          if(res>n) res -= n;
29
        }
30
        exp <<= 1;
31
        if (exp>n) exp —= n;
32
        b>>=1;
33
     }
34
     return res;
   }
35
36
37
   // ret = (a^b)%n
38
   bint mod_exp(bint a,bint p,bint m)
39
     bint exp=a%m, res=1; //
40
41
     while(p>1)
42
43
        if(p&1)
44
          res=muti_mod(res,exp,m);
45
        exp = muti_mod(exp,exp,m);
46
        p>>=1;
47
48
     return muti_mod(res,exp,m);
   }
49
50
51
   //miller-法测试素数rabin, time 测试次数
52
   bool miller_rabin(bint n, int times)
53
54
     if(n==2)return 1;
55
     if(n<2||!(n&1))return 0;
56
     bint a, u=n-1, x, y;
57
     int t=0;
     while(u%2==0)
58
59
60
        t++;
61
        u/=2;
     }
62
63
     srand(time(0));
64
     for(int i=0; i<times; i++)</pre>
65
66
        a = rand() \% (n-1) + 1;
67
        x = mod_exp(a, u, n);
```

```
68
        for(int j=0; j<t; j++)
 69
           y = muti_mod(x, x, n);
 70
           if ( y == 1 && x != 1 && x != n-1 )
 71
             return false; //must not
 72
 73
           x = y;
 74
 75
        if( y!=1) return false;
 76
 77
      return true;
 78
    }
 79
 80
    bint pollard_rho(bint n, int c) //找出一个因子
 81
 82
      bint x,y,d,i = 1,k = 2;
 83
      srand(time(0));
 84
      x = rand()%(n-1)+1;
 85
      y = x;
 86
      while(true)
 87
      {
        i++;
 88
 89
        x = (muti\_mod(x,x,n) + c) % n;
 90
        d = gcd(y-x, n);
        if (1 < d && d < n) return d;
 91
 92
        if( y == x) return n;
        if(i == k)
 93
 94
         {
 95
           y = x;
 96
           k <<= 1;
 97
        }
 98
      }
    }
 99
100
    void findFactor(bint n, int k)//二分找出所有质因子,存入factor
101
102
    {
103
      if(n==1)return;
104
      if(miller_rabin(n, TIME))
105
        factor[++fac_top] = n;
106
107
        return;
      }
108
      bint p = n;
109
110
      while(p >= n)
         p = pollard_rho(p,k--);//值变化, 防止死循环k
111
112
      findFactor(p,k);
      findFactor(n/p,k);
113
114
    }
115
    int main()
116
117
118
      bint cs,n,min;
```

```
119
       cin>>cs;
120
       while (cs—)
121
122
         cin>>n;
123
         fac_{top} = min = -1;
         if(miller_rabin(n,TIME)) cout<<"Prime"<<endl;</pre>
124
         else
125
126
         {
127
           findFactor(n,107);
           for(int i=0; i<=fac_top; i++)</pre>
128
129
              if(min<0||factor[i]<min)</pre>
130
                min = factor[i];
131
132
133
           cout<<min<<endl;</pre>
134
         }
135
136
       return 0;
    }
137
    3.9.2 暴力版本
    ∣int N;
    int num[30], fac[30];
    void getFactor(int x)
  4
    {
  5
       N=0;
  6
       memset(num,0,sizeof(num));
  7
       for (int i=0; prime[i]*prime[i]<=x && i<L; i++)</pre>
  8
  9
         if (x%prime[i]==0)
 10
         {
 11
           while (x%prime[i]==0)
 12
           {
             x/=prime[i];
 13
 14
             num[N]++;
           }
 15
 16
           fac[N++]=prime[i];
 17
         }
       }
 18
 19
       if (x>1)
 20
 21
         num[N]=1;
 22
         fac[N++]=x;
 23
       }
 24 | }
           baby step giant step
    3.10
    3.10.1 BSGS
  1 #define MOD 76543
    int hs[MOD], head[MOD], next[MOD], id[MOD], top;
```

```
void insert(int x, int y)
 4
   {
 5
     int k = x\%MOD;
 6
     hs[top] = x, id[top] = y, next[top] = head[k], head[k] = top++;
 7
   }
   int find(int x)
 8
 9
   {
10
     int k = x\%MOD;
     for (int i = head[k]; i; i = next[i]) if (hs[i] == x)
11
12
       return id[i];
13
     return -1;
   }
14
15
   int BSGS(int a, int b, int n)
16
     memset(head, 0, sizeof(head));
17
18
     top = 1;
19
     if (b==1) return 0;
20
     int m = sqrt(n+.0), j;
     long long x = 1, p = 1;
21
     for (int i = 0; i < m; ++i, p = p*a%n) insert(p*b%n, i);</pre>
22
23
     for (long long i = m; ; i += m)
24
     {
25
       if ((j = find(x=x*p%n)) != -1) return i-j;
26
       if (i > n) break;
27
28
     return -1;
29 |}
   3.10.2 何老师的版
 1 //离散对数
 2 | #include <cstdio>
   #include <cstring>
 4 | #include <cmath>
   #include <algorithm>
   using namespace std;
   typedef long long LL;
   struct Hash
 8
 9
   {
10
       static const int MOD = 100007;
       static const int MaxN = 100005;
11
       struct Node
12
13
14
            LL k, v;//A^k = v
            Node *nxt;
15
16
       } buf[MaxN], *g[MaxN], *pt;
17
       void init()
       {
18
19
            memset(g, 0, sizeof(g));
20
            pt = buf;
21
22
       LL find(LL v)
```

```
23
        {
24
            for (Node *now = g[v\%MOD]; now; now = now->nxt)
25
                 if (now->v == v)
26
                     return now->k;
27
            return -1;
28
        }
29
        void Ins(LL k, LL v)
30
        {
31
            if ( find (v) !=-1)return;
32
            pt->k = k;
33
            pt->v = v;
34
            pt->nxt = g[v \% MOD];
35
            g[v \% MOD] = pt++;
36
37
   }hash;
38
   LL gcd(LL x, LL y)
39
40
        return y==0?x:gcd(y,x%y);
41
   LL e_gcd(LL a, LL b, LL &x, LL &y)
42
43
   {
44
        if (b==0)
45
        {
46
            x = 1;
47
            y = 0;
48
            return a;
49
        }
50
        LL ret = e_gcd(b, a\%b, y, x);
51
        y = y - a/b*x;
52
        return ret ;
53
54
   LL Baby(LL A, LL B, LL C)//A^x = B (mod C)
55
   {
56
        B %= C;
57
        A \% = C;
58
        LL x = 1\%C, y;
59
        for (int i = 0; i <= 64; i++)
60
        {
61
            if (x==B)return i;
62
            x = x*A % C;
63
        }
64
65
        LL D = 1\%C, g;
66
        int cnt = 0;
        while ((g = gcd(A,C)) != 1)
67
68
        {
69
            if (B%g) return -1;
70
            cnt++;
71
            C /= g;
            B /= g;
72
73
            D = A/g * D % C;
```

```
74
         }
 75
         hash. init ();
         int m = (int)sqrt(C);
 76
         LL Am = 1\%C;
 77
 78
         hash.Ins(0,Am);
 79
         for (int i = 1; i <= m; i++)
 80
         {
 81
              Am = Am*A \% C;
 82
              hash. Ins ( i ,Am);
 83
         for (int i = 0; i <= m; i++)</pre>
 84
 85
         //D*x = B \pmod{C}, D*x + C*y = B
 86
              g = e_gcd(D,C,x,y);
 87
 88
              x = (x*B/g%C+C)%C;
 89
              LL k = hash.find(x);
              if (k != -1) return i*m+k+cnt;
 90
 91
              D = D*Am \% C;
 92
         }
 93
         return -1;
 94
 95
    int main()
 96
     {
 97
         int A,B,C;
 98
         while(scanf("%d%d%d",&A,&C,&B) == 3 && (A+B+C))
 99
              if (B>=C)
100
101
              {
102
                   puts("Orz,I<sub>□</sub>' cant<sub>□</sub>find<sub>□</sub>D!");
103
                   continue;
104
              LL ret = Baby(A,B,C);
105
              if ( ret == -1)puts("0rz,I_{\square}' cant_{\square}find_{\square}D!");
106
              else printf ("%I64d\n",ret);
107
108
109
         return 0;
110 |}
            原根
     3.11
     int getPriRoot(int p)
  1
  2
  3
       if (p==2) return 1;
  4
       int phi = p - 1;
  5
       getFactor(phi);
       for (int g = 2; g < p; ++g)
  6
  7
  8
         bool flag=1;
         for (int i = 0; flag && i < N; ++i)</pre>
  9
 10
            if (power(g, phi/fac[i], p) == 1)
 11
              flag=0;
         if (flag)
 12
```

```
13
         return g;
14
     }
15
   }
         逆元
   3.12
  void getInv2(int x)
 1
 2
 3
     inv[1]=1;
 4
     for (int i=2; i<=x; i++)
       inv[i] = (mod-(mod/i) * inv[mod%i]%mod)%mod;
 5
 6
   int getInv(int x)//为素数mod
 7
 8
 9
     return power(x, mod-2);
   }
10
        卢卡斯
   3.13
   卢卡斯,num[i] 阶乘也
   int comLucus(int n,int m,int p)
 2
   {
 3
     int ans=1;
 4
     for (; n && m && ans; n/=p,m/=p)
 5
 6
       if (n%p>=m%p)
 7
         ans = ans*num[n%p]%p*getInv(num[m%p]%p)%p
 8
            *getInv(num[n%p-m%p])%p;
 9
       else
10
         ans=0;
11
     }
12
     return ans;
13 | }
   3.14
         欧拉函数
   3.14.1 分解质因数
   | int getEuler(int x)
 2
   {
 3
     getFactor(x);
 4
     int ret=x;
 5
     for (int i=0; i<N; i++)
       ret = ret/fac[i]*(fac[i]-1);
 6
 7
     return ret;
 8 | }
   3.14.2 一次预处理
 1 void getEuler2()
 2
 3
     memset(euler,0,sizeof(euler));
 4
     euler[1] = 1;
```

```
5
      for (int i = 2; i <= 3000000; i++)
 6
 7
        if (!euler[i])
 8
        {
          for (int j = i; j \le 3000000; j += i)
 9
10
          {
            if (!euler[j])
11
12
               euler[j] = j;
13
            euler[j] = euler[j]/i*(i-1);
14
          }
        }
15
      }
16
17
   }
          费马降阶法
   3.15
   分解素数 p 为 x^2+y^2 的费马降阶法,失败返回 -1,主程序调用 \operatorname{calcu}(\mathbf{p},\mathbf{x},\mathbf{y})
 1 |#include <stdio.h>
   #include <string.h>
   #include <stdlib.h>
   int p,expp,A,B,aa,ans,tt;
   long long M;
   long long exp(int a,int b,long long mod)
 7
 8
       long long ans=1,num=a;
      while (b!=0)
 9
10
       {
11
           if (b&1)
12
           {
13
                ans=((ans%mod)*(num%mod))%mod;
14
           }
15
           num=((num%mod)*(num%mod))%mod;
16
           b>>=1;
17
18
       return ans;
19
   int calcu(int p,int &x,int &y)
20
21
   {
          if (p\%4!=1) return -1;
22
23
          else
24
          {
25
            expp=(p-1)/4;
26
            A,B;
27
            while (1)
28
29
               aa=rand()%p;
30
               if (aa==0) continue;
31
               A=exp(aa,expp,p);
32
               ans=(((long long)A%p)*((long long)A%p))%p;
33
               if (ans==p-1) break;
34
            }
35
            B=1;
```

```
36
            M=((long long)A*(long long)A+(long long)B*(long long)B)/p;
37
             if (M!=1) B=p;
            while (M!=1)
38
39
             {
40
               if (B>A)
41
               {tt=A; A=B; B=tt;}
42
               tt=A;
43
               A=B;
44
               B=tt%B;
45
               M=((long long)A*(long long)A
46
                 +(long long)B*(long long)B)/p;
47
             }
             if (B<=A)
48
49
             {
50
                  x=B;
51
                  y=A;
52
             }
53
             else
54
55
             x=A;
             y=B;
56
57
          }
58
59
60
   int main()
61
     while (scanf("%d",&p)!=EOF)
62
63
      {
64
          int x,y;
65
          if (calcu(p,x,y)!=-1)
66
67
      return 0;
   }
68
```

3.16 自适应 simp

过了哈尔滨积分题,精度要求不高的时候可以考虑使用。 暂时我只能用这个做做类似于凸函数或者凹函数的函数。

```
double Simp(double l,double r)
 1
 2
   {
 3
     double h = (r-1)/2.0;
 4
     return h*(calc(l)+4*calc((l+r)/2.0)+calc(r))/3.0;
   }
 5
 6
 7
   double rSimp(double l,double r)
 8
 9
     double mid = (l+r)/2.0;
     if (abs((Simp(l,r)-Simp(l,mid)-Simp(mid,r)))/15 < eps)</pre>
10
11
       return Simp(l,r);
12
     else
13
       return rSimp(l,mid)+rSimp(mid,r);
```

14 |}

3.17 组合数求模

```
模是质数
```

```
1 | #include < cstdio >
   #include<cstring>
   #include<iostream>
   using namespace std;
 5
   int mod;
   long long num[100000];
 7
   int ni[100],mi[100];
 8
   int len;
   void init(int p)
10
   {
11
     mod=p;
12
     num[0]=1;
13
     for (int i=1; i<p; i++)
14
        num[i]=i*num[i-1]%p;
15
16
   void get(int n,int ni[],int p)
17
18
     for (int i = 0; i < 100; i++)
19
        ni[i] = 0;
20
     int tlen = 0;
     while (n != 0)
21
22
23
        ni[tlen++] = n%p;
24
        n /= p;
25
26
     len = tlen;
27
28
   long long power(long long x,long long y)
29
30
     long long ret=1;
31
     for (long long a=x%mod; y; y>>=1,a=a*a%mod)
32
        if (y&1)
33
          ret=ret*a%mod;
34
     return ret;
35
36
   long long getInv(long long x)//mod 为素数
37
38
     return power(x,mod-2);
39
40
   long long calc(int n,int m,int p)//C(n,m)%p
41
42
     init(p);
43
     long long ans=1;
44
     for (; n && m && ans; n/=p,m/=p)
45
     {
46
        if (n%p>=m%p)
```

```
47
          ans = ans*num[n%p]%p*getInv(num[m%p]%p)%p
48
            *getInv(num[n%p-m%p])%p;
49
        else
50
          ans=0;
51
     }
52
     return ans;
53
54
   int main()
55
   {
56
     int t;
     scanf("%d",&t);
57
     while (t—)
58
59
     {
60
        int n,m,p;
61
        scanf("%d%d%d",&n,&m,&p);
62
        printf("%I64d\n",calc(n+m,m,p));
63
64
     return 0;
65 }
          高斯消元
   3.18
   const double eps = 1e-8;
 1
 2
 3
   void Guess(int n)
 4
   {
 5
     for (int i = 0; i < n; i++)
 6
     {
 7
        for (int j = i; j < n; j++)
 8
          if (fabs(a[j][i]) > eps)
 9
          {
            for (int k = i; k <= n; k++)
10
11
              swap(a[i][k],a[j][k]);
12
            break;
          }
13
14
15
        if (fabs(a[i][i]) < eps) continue;</pre>
16
17
        for (int j = 0; j < n; j++)
          if (i != j && fabs(a[j][i]) > eps)
18
19
          {
20
            double det = a[j][i]/a[i][i];
21
            for (int k = i; k <= n; k++)
22
              a[j][k] = a[i][k]*det;
          }
23
24
     }
25
26
     for (int i = 0; i < n; i++)
27
28
        if (fabs(a[i][i]) < eps)
29
        {
```

```
30
          if (fabs(a[i][n]) > eps)
31
          {
32
            //无解
33
            puts("Fuck");
34
          }
35
          //否则 x_i 可以是任意解
        }
36
37
        else
38
        {
39
          a[i][n] /= a[i][i];
40
          if (fabs(a[i][n]) < eps)
            a[i][n] = 0;
41
42
        }
43
44
45 |}
          整数拆分
   3.19
 1 |#include <cstdio>
   #include <cmath>
   #include <cstring>
   #include <map>
   |#include <algorithm>
   using namespace std;
   bool check(int x)
 7
 8
      for (int i=2; i*i<=x; i++)</pre>
 9
        if (x\%i == 0)
10
11
          return 0;
12
      return 1;
13
   }
14
   int p[100000];
   inline int calc(int x)
15
16
   {
17
      return x*(x*3-1)/2;
18
19
   int main()
20
   {
21
      p[0]=1;
22
      for (int i=1;i<100000;i++)</pre>
23
24
        for (int j=1,k=1;calc(j)<=i;j++,k*=-1)
25
        {
26
          p[i]+=k*p[i-calc(j)];
27
          if (p[i]<0)
28
            p[i]+=1000000;
29
          if (p[i]>=1000000)
30
            p[i]-=1000000;
          if (calc(-j)<=i)
31
32
            p[i]+=k*p[i-calc(-j)];
          if (p[i]<0)
```

33

```
34
            p[i]+=1000000;
35
          if (p[i]>=1000000)
36
            p[i]-=1000000;
37
       }
       if (!p[i])
38
          printf("%d\n",i);
39
40
41
     return 0;
42 |}
   3.20
         佩尔方程
   写的不好稍微收一下
   import java.math.BigInteger;
   import java.util.*;
   public class Main
 4
 5
     public static class Fraction
 6
       public BigInteger num,den;
 7
 8
       public Fraction()
 9
10
          num=BigInteger.ZERO;
11
          den=BigInteger.ONE;
12
13
       public Fraction(int _num,int _den)
14
          num=BigInteger.valueOf(_num);
15
          den=BigInteger.valueOf(_den);
16
17
       public Fraction(BigInteger _num, BigInteger _den)
18
19
       {
20
          num=_num;
21
          den=_den;
       }
22
23
       public Fraction gen()
24
        {
25
          BigInteger g=num.gcd(den);
          return new Fraction(num.divide(g),den.divide(g));
26
27
       }
       public Fraction add(Fraction x)
28
29
          return new Fraction(x.num.multiply(den).add(num.multiply(x.
30
            den)),x.den.multiply(den)).gen();
31
       }
32
       public Fraction reciprocal()
33
34
          return new Fraction(den,num);
35
       public void out()
36
37
        {
38
          System.out.println(num+"/"+den);
```

```
39
        }
40
      }
41
      public static BigInteger sqrt(BigInteger a)
42
43
        BigInteger b=a;
            while (a.compareTo(b.multiply(b))<0)</pre>
44
45
              b=b.multiply(b).add(a).divide(b.multiply(BigInteger.
                  valueOf(2)));
46
            return b;
47
      public static boolean check(Fraction x,int n)
48
49
        return x.num.multiply(x.num).add(x.den.multiply(x.den.multiply(
50
           BigInteger.valueOf(n))).negate()).compareTo(BigInteger.ONE)
           ==0;
51
      }
      static int p[]=new int[1000];
52
      static int l;
53
      public static void main(String[] args)
54
55
        BigInteger ans=BigInteger.ZERO;
56
57
        int idx=0;
        for (int n=2,r=2;n<=1000;n++)</pre>
58
59
        {
60
          if (n==r*r)
61
          {
62
            r++;
63
            continue;
64
          }
65
          int tmp=calc(n,0,1),a=tmp,b=n-tmp*tmp;
66
          p[0]=tmp;
          l=1;
67
          while (true)
68
69
          {
            tmp=calc(n,a,b);
70
71
            p[l++]=tmp;
72
            a=a-tmp*b;
            Fraction x=getFrac();
73
74
            if (check(x,n))
75
76
               if (ans.compareTo(x.num)<0)</pre>
77
               {
78
                 ans=x.num;
79
                 idx=n;
80
               }
81
              break;
            }
82
83
            a=-a;
84
            b=(n-a*a)/b;
85
          }
        }
86
```

```
87
        System.out.println(idx);
 88
      private static Fraction getFrac() {
 89
        Fraction ret=new Fraction(p[l-1],1);
 90
        for (int i=l-2;i>=0;i--)
 91
           ret=new Fraction(p[i],1).add(ret.reciprocal());
 92
 93
        return ret;
 94
 95
      private static int calc(int n, int a, int b) {
        for (long i=2;;i++)
 96
           if ((i*b-a)*(i*b-a)>n)
 97
             return (int)i-1;
 98
 99
      }
    }
100
```

3.21 其它公式

3.21.1 Polya

设 G 是 p 个对象的一个置换群,用 k 种颜色去染这 p 个对象,若一种染色方案在群 G 的作用下变为另一种方案,则这两个方案当作是同一种方案,这样的不同染色方案数为:

$$L = \frac{1}{|G|} \times \Sigma(k^{C(f)}), f \in G$$

 $C(f)$ 为循环节, $|G|$ 表示群的置换方法数

对于有 n 个位置的手镯, 有 n 种旋转置换和 n 种翻转置换

对于旋转置换:

$$C(f_i) = \gcd(n,i)$$
 , i 表示一次转过 i 颗宝石, $i = 0$ 时 $c = n$;

对于翻转置换:

如果 n 为偶数: 则有 $\frac{n}{2}$ 个置换 $C(f) = \frac{n}{2}$,有 $\frac{n}{2}$ 个置换 $C(f) = \frac{n}{2} + 1$

如果 n 为奇数: $C(f) = \frac{n}{2} + 1$

3.21.2 拉格朗日插值法

已知 $y = a_0 + a_1 x + a_2 x^2 + \cdots + a_{n-1} x^{n-1}$ 曲线上的 n 个点 $(x_1, y_1), (x_2, y_2), (x_3, y_3) \cdots (x_n, y_n)$ 用拉格朗日插值法可以不求系数可知任意 x 对应的 y 值。

$$y = y_1 \frac{(x - x_2)(x - x_3) \cdots (x - x_n)}{(x_1 - x_2)(x_1 - x_3) \cdots (x_1 - x_n)}$$

$$+ y_2 \frac{(x - x_1)(x - x_3) \cdots (x - x_n)}{(x_2 - x_1)(x_2 - x_3) \cdots (x_2 - x_n)}$$

$$+ \cdots$$

$$+ y_n \frac{(x - x_1)(x - x_2) \cdots (x - x_{n-1})}{(x_n - x_1)(x_n - x_2) \cdots (x_n - x_{n-1})}$$

特别的,如果 $x_1 \sim x_n$ 为连续自然数,那么对于下一个自然数对应的 y 值为:

$$y_{n+1} = (-1)^{n-1}C_n^0y_1 + (-1)^{n-2}C_n^1y_2 + \dots + (-1)^0C_n^{n-1}y_n$$

这个组合系数可以通过高斯消元暴出来,前提是要猜到它满足递推关系。

3.21.3 正多面体顶点着色

正四面体:
$$N=\frac{(n^4+11\times n^2)}{12}$$
 正六面体: $N=\frac{(n^8+17\times n^4+6\times n^2)}{24}$ 正八面体: $N=\frac{(n^6+3\times n^4+12\times n^3+8\times n^2)}{24}$ 正十二面体: $N=\frac{(n^{20}+15\times n^{10}+20\times n^8+24\times n^4)}{60}$ 正二十面体: $N=\frac{(n^{12}+15\times n^6+44\times n^4)}{60}$

3.21.4 求和公式

$$\begin{array}{l} \sum k = \frac{n \times (n+1)}{2} \\ \sum 2k - 1 = n^2 \\ \sum k^2 = \frac{n \times (n+1) \times (2n+1)}{6} \\ \sum (2k-1)^2 = \frac{n \times (4n^2-1)}{3} \\ \sum k^3 = (\frac{n \times (n+1)}{2})^2 \\ \sum (2k-1)^3 = n^2 \times (2n^2-1) \\ \sum k^4 = \frac{n \times (n+1) \times (2n+1) \times (3n^2+3n-1)}{30} \\ \sum k^5 = \frac{n^2 \times (n+1)^2 \times (2n^2+2n-1)}{12} \\ \sum k \times (k+1) = \frac{n \times (n+1) \times (n+2)}{3} \\ \sum k \times (k+1) \times (k+2) = \frac{n \times (n+1) \times (n+2) \times (n+3)}{4} \\ \sum k \times (k+1) \times (k+2) \times (k+3) = \frac{n \times (n+1) \times (n+2) \times (n+3)}{5} \end{array}$$

3.21.5 几何公式

球扇形:

全面积: $T = \pi r (2h + r_0)$, h 为球冠高, r_0 为球冠底面半径体积: $V = \frac{2\pi r^2 h}{3}$

3.21.6 小公式

Pick 公式: $A = E \times 0.5 + I - 1$ (A 是多边形面积, E 是边界上的整点, I 是多边形内部的整点)海伦公式: $S = \sqrt{p(p-a)(p-b)(p-c)}$,其中 $p = \frac{(a+b+c)}{2}$,abc 为三角形的三条边长 求 $\binom{n}{k}$ 中素因子 P 的个数:

- 1. 把 n 转化为 P 进制,并记它每个位上的和为 S1
- 2. 把 n-k, k 做同样的处理, 得到 S2, S3

则 $\binom{n}{k}$ 中素因子 P 的个数: $\frac{S2+S3-S1}{P-1}$

部分错排公式:

n+m 个数中 m 个数必须错排求排列数

```
1 | dp[i] = n*dp[i-1]+(i-1)*(dp[i-1]+dp[i-2]);
2 | dp[0] = n!;
3 | dp[1] = n*n!;
dp[m] 为所求解
```

3.21.7 马步问题

任意步长 (p,q) 无限棋盘可达性判定

```
bool check(int dx,int dy,int p,int q)

if (p < 0) p = -p;

if (q < 0) q = -q;

LL g = gcd(p,q);

if (dx % g || dy % g) return false;

dx /= g,dy /= g,p = (p / g) & 1,q = (q / g) & 1;

return !(p == q && ((dx ^ dy) & 1));

}</pre>
```

拓展:

若可选马步可以有 N 种 (p_i,q_i) , 令 $g = gcd(p_1,q_1,p_2,q_2\cdots p_N,q_N)$, 则不在 g 的整数倍点上的节点肯定不可达。坐标除 2g, 同时将可选马步除 g 之后放缩到 2×2 之内, 即 $(\frac{p_i}{g}\mod 2,\frac{q_i}{g}\mod 2)$ 。 若放缩后马步中有 (1,0) 或 (0,1),则全放缩后全棋盘可达,否则只可达偶点。

(2.1) 马步无限棋盘最小距离

```
1 | int dis(int dx,int dy)
 2
   {
     if (dx < 0) dx = -dx;
 3
 4
     if (dy < 0) dy = -dy;
 5
     if (dx < dy) swap(dx,dy);</pre>
 6
     if (dx & 1)
 7
 8
        if (dy \& 1) return dis(dx+1,dy-1);
 9
        if (dx == 1 && dy == 0) return 3;
10
        return dis(dx+3,dy)-1;
11
     }
     if (dy & 1)
12
13
        if (dx == 4 && dy == 3) return 3;
14
15
        return dis(dx-2,dy-1)+1;
16
17
     if (dx == 0 && dy == 0) return 0;
     if (dx == 2 && dy == 2) return 4;
18
     int c = (((dx-1) / 4)+1)*2;
19
20
     if (dx \& 2) dy = 2;
21
     if (dy <= c) return c;</pre>
```

```
22 | dy -= c;
23 | return c+(dy-2) / 6*2+2;
24 |}
```

4 数据结构

4.1 *Splay

持续学习中。

注意节点的 size 值不一定是真实的值! 如果有需要需要特别维护!

- 1. 旋转和 Splay 操作
- 2. rank 操作
- 3. insert 操作(。。很多题目都有)
- 4. del 操作(郁闷的出纳员)
- 5. 由数组建立 Splay
- 6. 前驱后继(营业额统计)
- 7. Pushdown Pushup 的位置
- 8. *。。。暂时想不起了

const int MaxN = 50003;

4.1.1 节点定义

2

```
struct Node
 3
 4
   {
 5
     int size,key;
 6
 7
     Node *c[2];
 8
     Node *p;
 9 |} mem[MaxN], *cur, *nil;
   无内存池的几个初始化函数。
 1 | Node *newNode(int v, Node *p)
2
 3
     cur - c[0] = cur - c[1] = nil, cur - p = p;
 4
     cur->size = 1;
 5
     cur->key = v;
 6
     return cur++;
   }
 7
 8
9
   void Init()
10
   {
11
     cur = mem;
12
     nil = newNode(0, cur);
13
     nil->size = 0;
14 |}
```

带内存池的几个函数。

```
int emp[MaxN], totemp;
 2
 3
   Node *newNode(int v, Node *p)
 4
   {
 5
      cur = mem + emp[—totemp];
      cur - c[0] = cur - c[1] = nil, cur - p = p;
 6
 7
      cur->size = 1;
 8
      cur->key = v;
 9
      return cur;
   }
10
11
   void Init()
12
13
      for (int i = 0; i < MaxN; ++i)</pre>
14
15
        emp[i] = i;
16
      totemp = MaxN;
17
      cur = mem + emp[—totemp];
18
      nil = newNode(0, cur);
      nil->size = 0;
19
   }
20
21
22
   |void Recycle(Node *p)
23
24
      if (p == nil)
                        return;
25
      Recycle(p\rightarrow c[0]), Recycle(p\rightarrow c[1]);
      emp[totemp++] = p - mem;
26
27 |}
    4.1.2 维护序列
    一切下标从①开始。
 1 | struct SplayTree
 2
    {
 3
      Node *root;
      void Init()
 4
 5
      {
 6
        root = nil;
 7
 8
      void Pushup(Node *x)
 9
        if (x == nil)
10
                           return;
        Pushdown(x); Pushdown(x\rightarrowc[0]); Pushdown(x\rightarrowc[1]);
11
12
        x \rightarrow size = x \rightarrow c[0] \rightarrow size + x \rightarrow c[1] \rightarrow size + 1;
      }
13
14
      void Pushdown(Node *x)
15
        if (x == nil)
16
                            return;
17
        //do something
18
19
      void Rotate(Node *x, int f)
20
      {
```

```
21
        if (x == nil)
                          return;
22
        Node *y = x - p;
        y - c[f ^ 1] = x - c[f], x - p = y - p;
23
        if (x->c[f] != nil)
24
25
          x->c[f]->p = y;
26
        if (y->p != nil)
27
          y-p-c[y-p-c[1] == y] = x;
28
        x->c[f] = y, y->p = x;
29
        Pushup(y);
30
31
      void Splay(Node *x, Node *f)
32
33
        static Node *stack[maxn];
34
        int top = 0;
        stack[top++] = x;
35
36
        for (Node *y = x; y != f;y = y->p)
37
          stack[top++] = y->p;
38
        while (top)
39
          Pushdown(stack[—top]);
40
41
        while (x->p != f)
42
        {
43
          Node *y = x - p;
44
          if (y->p == f)
45
            Rotate(x, x == y->c[0]);
46
          else
47
          {
            int fd = y-p-c[0] == y;
48
49
            if (y->c[fd] == x)
50
              Rotate(x, fd ^{\wedge} 1), Rotate(x, fd);
51
            else
52
              Rotate(y, fd), Rotate(x, fd);
          }
53
54
        }
55
        Pushup(x);
56
        if (f == nil)
57
          root = x;
58
59
      void Select(int k, Node *f)
60
61
        Node *x = root;
62
        Pushdown(x);
        int tmp;
63
        while ((tmp = x->c[0]->size) != k)
64
65
          if (k < tmp) x = x -> c[0];
66
67
          else
68
            x = x \rightarrow c[1], k = tmp + 1;
69
          Pushdown(x);
70
        }
71
        Splay(x, f);
```

```
72
       }
 73
       void Select(int l, int r)
 74
 75
         Select(l, nil), Select(r + 2, root);
 76
 77
       Node *Make_tree(int a[], int l, int r, Node *p)
 78
       {
         if (l > r) return nil;
 79
 80
         int mid = l + r >> 1;
         Node *x = newNode(a[mid], p);
 81
 82
         x\rightarrow c[0] = Make\_tree(a, l, mid - 1, x);
         x\rightarrow c[1] = Make\_tree(a, mid + 1, r, x);
 83
 84
         Pushup(x);
 85
         return x;
 86
       }
 87
       void Insert(int pos, int a[], int n)
 88
 89
         Select(pos, nil), Select(pos + 1, root);
         root \rightarrow c[1] \rightarrow c[0] = Make\_tree(a, 0, n - 1, root \rightarrow c[1]);
 90
 91
         Splay(root->c[1]->c[0], nil);
 92
 93
       void Insert(int v)
 94
       {
         Node *x = root, *y = nil;
 95
 96
         //注意! 需要 pushdown, 之前只在初始化调用过这个函数所有没问题
         while (x != nil)
 97
 98
          {
            y = x;
 99
100
            y->size++;
101
            x = x - c[v > = x - key];
102
         y \rightarrow c[v >= y \rightarrow key] = x = newNode(v, y);
103
         Splay(x, nil);
104
105
       void Remove(int l, int r)
106
107
       {
108
         Select(l, r);
109
          //Recycle(root->c[1]->c[0]);
         root \rightarrow c[1] \rightarrow c[0] = nil;
110
111
         Splay(root->c[1], nil);
       }
112
113 | };
     例题:旋转区间赋值求和求最大子序列。
     注意打上懒标记后立即 Pushup。Pushup(root-c[1]-c[0]),Pushup(root-c[1]),Pushup(root);
  1
       void Pushup(Node *x)
  2
  3
         if (x == nil) return;
         Pushdown(x); Pushdown(x->c[0]); Pushdown(x->c[1]);
  4
  5
         x\rightarrow size = x\rightarrow c[0]\rightarrow size+x\rightarrow c[1]\rightarrow size+1;
  6
```

```
7
           x \rightarrow sum = x \rightarrow c[0] \rightarrow sum + x \rightarrow c[1] \rightarrow sum + x \rightarrow key;
 8
           x\rightarrow lsum = max(x\rightarrow c[0]\rightarrow lsum,
 9
               x\rightarrow c[0]->sum+x\rightarrow key+max(0,x\rightarrow c[1]->lsum));
           x\rightarrow rsum = max(x\rightarrow c[1]\rightarrow rsum,
10
               x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[0] \rightarrow rsum));
11
           x\rightarrow \max = \max(\max(x\rightarrow c[0] \rightarrow \max , x\rightarrow c[1] \rightarrow \max , x),
12
              x \rightarrow key + max(0, x \rightarrow c[0] \rightarrow rsum) + max(0, x \rightarrow c[1] \rightarrow lsum));
13
14
        }
15
        void Pushdown(Node *x)
16
17
           if (x == nil) return;
           if (x->rev)
18
19
           {
20
              x\rightarrow rev = 0;
21
              x->c[0]->rev ^= 1;
              x->c[1]->rev ^= 1;
22
23
               swap(x->c[0],x->c[1]);
24
25
              swap(x->lsum,x->rsum);
           }
26
           if (x->same)
27
28
           {
              x->same = false;
29
30
              x \rightarrow key = x \rightarrow lazy;
              x\rightarrow sum = x\rightarrow key *x\rightarrow size;
31
               x \rightarrow lsum = x \rightarrow rsum = x \rightarrow maxsum = max(x \rightarrow key, x \rightarrow sum);
32
              x\rightarrow c[0]-same = true, x\rightarrow c[0]-slazy = x\rightarrow key;
33
              x\rightarrow c[1]-same = true, x\rightarrow c[1]-slazy = x\rightarrow key;
34
35
           }
36
        }
37
38
     int main()
39
     {
40
        int totcas;
        scanf("%d",&totcas);
41
42
        for (int cas = 1;cas <= totcas;cas++)</pre>
43
44
           Init();
45
           sp.Init();
46
           nil->lsum = nil->rsum = nil->maxsum = -Inf;
47
           sp.Insert(0);
48
           sp.Insert(0);
49
50
           int n,m;
           scanf("%d%d",&n,&m);
51
52
           for (int i = 0; i < n; i++)
               scanf("%d",&a[i]);
53
54
           sp.Insert(0,a,n);
55
56
           for (int i = 0; i < m; i++)
57
           {
```

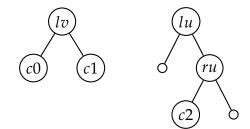
```
int pos,tot,c;
 58
 59
           scanf("%s",buf);
           if (strcmp(buf, "MAKE—SAME") == 0)
 60
 61
           {
              scanf("%d%d%d",&pos,&tot,&c);
 62
 63
              sp.Select(pos-1,pos+tot-2);
 64
              sp.root \rightarrow c[1] \rightarrow c[0] \rightarrow same = true;
 65
              sp.root->c[1]->c[0]->lazy = c;
 66
              sp.Pushup(sp.root->c[1]), sp.Pushup(sp.root);
           }
 67
           else if (strcmp(buf,"INSERT") == 0)
 68
 69
              scanf("%d%d",&pos,&tot);
 70
 71
              for (int i = 0; i < tot; i++)
 72
                scanf("%d",&a[i]);
 73
             sp.Insert(pos,a,tot);
           }
 74
 75
           else if (strcmp(buf,"DELETE") == 0)
 76
              scanf("%d%d",&pos,&tot);
 77
 78
              sp.Remove(pos-1,pos+tot-2);
 79
           }
 80
           else if (strcmp(buf, "REVERSE") == 0)
 81
           {
              scanf("%d%d",&pos,&tot);
 82
 83
              sp.Select(pos-1,pos+tot-2);
 84
              sp.root->c[1]->c[0]->rev ^= 1;
 85
              sp.Pushup(sp.root->c[1]), sp.Pushup(sp.root);
 86
           }
 87
           else if (strcmp(buf, "GET-SUM") == 0)
 88
              scanf("%d%d",&pos,&tot);
 89
 90
              sp.Select(pos-1,pos+tot-2);
 91
              printf("%d\n",sp.root\rightarrowc[1]\rightarrowc[0]\rightarrowsum);
           }
 92
 93
           else if (strcmp(buf,"MAX—SUM") == 0)
 94
 95
              sp.Select(0,sp.root->size-3);
 96
              printf("%d\n", sp.root->c[1]->c[0]->maxsum);
 97
           }
         }
 98
 99
100
       return 0;
    }
101
```

4.1.3 维护括号序列

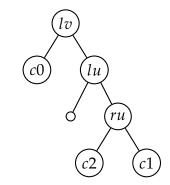
不需要哨兵。

合并操作:

先转成下面的样子:

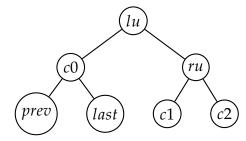


再链接成这样:

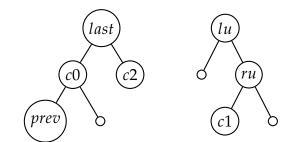


分离操作:

先把 lu 和 ru 转上去:



把 c0 和 c2 从原来的位置断开 然后接上:



```
#include <iostream>
#include <cstdio>
#include <cstring>
using namespace std;

const int maxn = 5000000;
const int mod = 99990001;
struct Node

int size,key;
```

```
11
12
      int a,b;
      int minid,id;
13
14
15
      Node *c[2];
16
      Node *p;
    }mem[maxn],*cur,*nil;
17
   Node *l[maxn],*r[maxn];//左括号右括号定义在前面
18
19
20
   int emp[maxn],totemp;
21
   Node *newNode(int v,Node *p)
22
23
      cur->c[0] = cur->c[1] = nil,cur->p = p;
24
      cur->size = 1;
25
      cur->key = v;
26
27
      cur->a = 1;
      cur->b = 0;
28
29
      cur->minid = cur->id = maxn;
30
31
      return cur++;
32
   }
33
   void Init()
34
35
      cur = mem;
36
      nil = newNode(0,cur);
37
      nil->size = 0;
   }
38
39
40
   struct SplayTree
41
42
      Node *root;
43
      void Init()
44
45
        root = nil;
46
      }
47
      void Pushup(Node *x)
48
49
        if (x == nil) return;
50
        Pushdown(x);
51
        Pushdown(x->c[0]);
        Pushdown(x->c[1]);
52
        x\rightarrow size = x\rightarrow c[0]\rightarrow size+x\rightarrow c[1]\rightarrow size+1;
53
54
55
        x->minid = x->id;
        for (int i = 0; i < 2; i++)
56
          if (x->c[i] != nil)
57
58
            x->minid = min(x->minid,x->c[i]->minid);
59
      }
60
      void Pushdown(Node *x)
61
      {
```

```
62
          if (x == nil) return;
 63
 64
          x\rightarrow key = ((long long)x\rightarrow key*x\rightarrow a\%mod+x\rightarrow b)\%mod;
 65
          for (int i = 0; i < 2; i++)
             if (x->c[i] != nil)
 66
 67
             {
 68
               x\rightarrow c[i]\rightarrow a = (long long)x\rightarrow c[i]\rightarrow a*x\rightarrow a\%mod;
 69
               x\rightarrow c[i]\rightarrow b = ((long long)x\rightarrow c[i]\rightarrow b*x\rightarrow a\%mod+x\rightarrow b)\%mod;
 70
             }
 71
          x->a = 1;
 72
          x->b = 0;
        }
 73
 74
        void Rotate(Node *x,int f)
 75
 76
          if (x == nil) return;
 77
          Node *y = x - p;
          y->c[f^1] = x->c[f], x->p = y->p;
 78
 79
          if (x->c[f] != nil)
             x->c[f]->p = y;
 80
 81
          if (y->p != nil)
 82
             y-p-c[y-p-c[1] == y] = x;
 83
          x - c[f] = y, y - p = x;
 84
          Pushup(y);
 85
 86
        void Splay(Node *x,Node *f)
 87
 88
          static Node *stack[maxn];
 89
          int top = 0;
 90
          stack[top++] = x;
          for (Node *y = x; y != f; y = y -> p)
 91
 92
             stack[top++] = y->p;
          while (top)
 93
             Pushdown(stack[—top]);
 94
 95
 96
          while (x->p != f)
 97
          {
 98
            Node *y = x -> p;
 99
             if (y->p == f)
100
               Rotate(x,x == y\rightarrow c[0]);
101
             else
102
             {
               int fd = y->p->c[0] == y;
103
               if (y->c[fd] == x)
104
105
                  Rotate(x, fd^1), Rotate(x, fd);
106
               else
                  Rotate(y,fd), Rotate(x,fd);
107
             }
108
          }
109
110
          Pushup(x);
111
          if (f == nil)
112
             root = x;
```

```
113
       }
114
       Node *Last(Node *now)
115
116
         Splay(now,nil);
         while (now->c[1] != nil)
117
           now = now -> c[1];
118
119
         return now;
       }
120
121
       //把 u 接到 v 下面去,边权为 w
       //需要保证 u 是某棵树的根
122
      void Link(int u,int v,int w)
123
124
125
         Splay(l[v],nil);
126
127
         Splay(l[u],nil);
128
         l[u] \rightarrow key = w;
129
         Pushup(l[u]);
130
         Splay(r[u],l[u]);
131
132
         Node *c1 = l[v] - c[1];
         l[v]->c[1] = l[u];
133
134
         r[u] - c[1] = c1;
135
         l[u] \rightarrow p = l[v];
         c1->p = r[u];
136
         Pushup(r[u]);
137
         Pushup(l[u]);
138
139
         Pushup(l[v]);
140
         Splay(l[u],nil);
141
       }
142
       //把 u 为根的子树分离开
       int Split(int u)
143
144
       {
145
         Splay(l[u],nil);
146
         int ret = l[u]->key;
147
148
         Splay(r[u],l[u]);
149
         Node *c0 = l[u] - c[0], *c2 = r[u] - c[1];
150
151
         l[u]->key = 0;//去掉边权
         l[u] -> c[0] = r[u] -> c[1] = c0 -> p = c2 -> p = nil;
152
         Pushup(r[u]);
153
154
         Pushup(l[u]);
155
         Node *last = Last(c0);
156
157
         Splay(last,nil);
         last->c[1] = c2;
158
         c2\rightarrow p = last;
159
         Pushup(last);
160
161
162
         //对拆分后的两部份进行处理
163
         Node *nu = last;
```

```
Node *nv = l[u];
164
165
        if (nu->size > nv->size || (nu->size == nv->size && nu->minid >
             nv->minid))
166
           swap(nu,nv);
        nu->a = (long long)nu->a*ret%mod;
167
        nu->b = (long long)nu->b*ret%mod;
168
        nv->b = (nv->b+ret)\%mod;
169
170
171
        return ret;//返回原边权
172
      }
173
    };
174
175
    SplayTree sp;
176
    int n;
177
    struct Edge
178
179
      int to,next,w,id;
180
    };
181
    Edge edge[maxn];
    int head[maxn],L;
182
183
    int eid[maxn],toid[maxn];
184
185
    void addedge(int u,int v,int w,int id)
186
    {
187
      edge[L].to = v;
      edge[L].w = w;
188
189
      edge[L].id = id;
190
      edge[L].next = head[u];
191
      head[u] = L++;
192
    }
193
    void DFS(int now,int fa)
194
195
196
      for (int i = head[now]; i != -1; i = edge[i].next)
        if (edge[i].to != fa)
197
198
         {
           sp.Link(edge[i].to,now,edge[i].w);
199
200
           eid[edge[i].id] = edge[i].to;
           toid[edge[i].id] = now;
201
202
203
           DFS(edge[i].to,now);
204
        }
205
    }
206
207
    int main()
208
209
      Init();
210
      sp.Init();
211
212
      scanf("%d",&n);
213
```

```
214
       for (int i = 0; i < n; i++)
215
         l[i] = newNode(0,nil);
216
217
         r[i] = newNode(0,nil);
         l[i] \rightarrow id = r[i] \rightarrow id = i;
218
         l[i]->c[1] = r[i], r[i]->p = l[i];
219
220
         sp.Pushup(l[i]);
221
222
         head[i] = -1;
       }
223
224
       L = 0;
225
       for (int i = 0; i < n-1; i++)
226
227
228
         int u,v,w;
229
         scanf("%d%d%d",&u,&v,&w);
230
         u--,v--;
231
232
         addedge(u,v,w,i);
         addedge(v,u,w,i);
233
234
       }
235
236
       DFS(0,-1);
237
       for (int i = 0; i < n-1; i++)
238
239
         fflush(stdout);
240
241
242
         int id;
243
         scanf("%d",&id);
244
         id—-;
245
246
         int ret = sp.Split(eid[id]);
         printf("%d\n",ret);
247
       }
248
249
250
       return 0;
251 }
```

4.2 动态树

懒标记是否及时 Pushdown 了? 修改之后有没有及时 Pushup?

4.2.1 维护点权

查询链上的最长字段和 GetRoute 是用换根写的

1 | const int MaxN = 110000;

```
2
 3
    struct Node
 4
 5
       int size, key;
 6
       bool rev;
 7
 8
    //
          bool same;
 9
          int lsum, rsum, sum, maxsum, sa;
    //
10
11
       Node *c[2];
12
       Node *p;
13
    } mem[MaxN], *cur, *nil, *pos[MaxN];
14
15
    Node *newNode(int v, Node *p)
16
    {
17
       cur - c[0] = cur - c[1] = nil, cur - p = p;
18
       cur->size = 1;
19
       cur->key = v;
20
       cur->rev = false;
21
22
    //
          cur->same = false;
23
    //
         cur->sa = 0;
24
    //
          cur->lsum = cur->rsum = cur->maxsum = 0;
25
    // cur->sum = v;
26
27
       return cur++;
    }
28
29
30
    void Init()
31
    {
32
       cur = mem;
33
       nil = newNode(0, cur);
34
       nil—>size = 0;
35
    }
36
37
    struct SplayTree
38
39
       void Pushup(Node *x)
40
       {
41
          if (x == nil)
                                return;
42
          Pushdown(x); Pushdown(x->c[0]); Pushdown(x->c[1]);
43
          x\rightarrow size = x\rightarrow c[0]\rightarrow size + x\rightarrow c[1]\rightarrow size + 1;
44
45
    //
            x -> sum = x -> c[0] -> sum + x -> c[1] -> sum + x -> key;
46
    //
            x\rightarrow lsum = max(x\rightarrow c[0]\rightarrow lsum,
47
    //
               x \rightarrow c[0] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow lsum));
48
    //
            x\rightarrow rsum = max(x\rightarrow c[1]\rightarrow rsum,
49
               x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[0] \rightarrow rsum));
    //
            x\rightarrow \max = \max(\max(x\rightarrow c[0]\rightarrow \max , x\rightarrow c[1]\rightarrow \max , x),
50
    //
51
    //
               x \rightarrow key + max(0, x \rightarrow c[0] \rightarrow rsum) + max(0, x \rightarrow c[1] \rightarrow lsum));
52
```

```
53
        }
 54
        void Pushdown(Node *x)
 55
 56
          if (x == nil)
                              return;
          if (x->rev)
 57
 58
          {
 59
             x\rightarrow rev = 0;
 60
             x->c[0]->rev ^= 1;
 61
             x->c[1]->rev ^= 1;
 62
             swap(x->c[0], x->c[1]);
     //注意修改与位置有关的量
 63
 64
     //
               swap(x->lsum,x->rsum);
 65
          }
 66
 67
     //
            if (x->same)
 68
     //
             {
 69
     //
               x->same = false;
     //
 70
               x\rightarrow key = x\rightarrow sa;
 71
     //
               x\rightarrow sum = x\rightarrow sa * x\rightarrow size;
 72
     //
               x\rightarrowlsum = x\rightarrowrsum = x\rightarrowmaxsum = max(0, x\rightarrowsum);
 73
     //
               if (x->c[0] != nil)
                  x\rightarrow c[0]\rightarrow same = true, x\rightarrow c[0]\rightarrow sa = x\rightarrow sa;
 74
     //
 75
     //
               if (x->c[1] != nil)
 76
     //
                  x\rightarrow c[1]->same = true, x\rightarrow c[1]->sa = x\rightarrow sa;
 77
             }
     //
 78
        }
 79
       bool isRoot(Node *x)
 80
 81
          return (x == nil) || (x->p->c[0] != x && x->p->c[1] != x);
 82
 83
        void Rotate(Node *x, int f)
 84
        {
 85
          if (isRoot(x))
                               return;
 86
          Node *y = x - p;
 87
          y - c[f ^ 1] = x - c[f], x - p = y - p;
 88
          if (x->c[f] != nil)
 89
             x->c[f]->p = y;
 90
          if (y != nil)
 91
          {
 92
             if (y == y->p->c[1])
 93
               y-p-c[1] = x;
 94
             else if (y == y->p->c[0])
 95
               y-p-c[0] = x;
 96
          }
          x->c[f] = y, y->p = x;
 97
 98
          Pushup(y);
 99
        void Splay(Node *x)
100
101
102
          static Node *stack[MaxN];
103
          int top = 0;
```

```
stack[top++] = x;
104
         for (Node *y = x; !isRoot(y); y = y-p)
105
106
           stack[top++] = y->p;
         while (top)
107
           Pushdown(stack[--top]);
108
109
         while (!isRoot(x))
110
111
         {
112
           Node *y = x -> p;
           if (isRoot(y))
113
114
              Rotate(x, x == y->c[0]);
115
           else
116
           {
              int fd = y-p-c[0] == y;
117
118
              if (y->c[fd] == x)
119
                Rotate(x, fd ^ 1), Rotate(x, fd);
120
              else
                Rotate(y, fd), Rotate(x, fd);
121
           }
122
         }
123
124
         Pushup(x);
125
       }
126
       Node *Access(Node *u)
127
128
         Node *v = nil;
         while (u != nil)
129
130
         {
           Splay(u);
131
132
           v \rightarrow p = u;
133
           u\rightarrow c[1] = v;
134
           Pushup(u);
135
           u = (v = u) - p;
           if (u == nil)
136
137
              return ∨;
         }
138
139
       }
140
       Node *LCA(Node *u, Node *v)
141
142
         Access(u);
143
         return Access(v);
144
       }
       Node *Link(Node *u, Node *v)
145
146
147
         Access(u);
         Splay(u);
148
149
         u->rev = true;
150
         u \rightarrow p = v;
151
152
       void ChangeRoot(Node *u)
153
       {
154
         Access(u)->rev ^= 1;
```

```
155
      }
156
      Node *GetRoute(Node *u, Node *v)
157
158
         ChangeRoot(u);
159
         return Access(v);
160
    };
161
162
163
    int n, m;
    SplayTree sp;
164
165
166
    int main(int argc, char const *argv[])
167
      while (scanf("%d", &n) != EOF)
168
169
      {
170
         Init();
         for (int i = 0; i < n; i++)
171
         {
172
173
           int ∨;
           scanf("%d", &v);
174
           pos[i] = newNode(v, nil);
175
176
         }
177
         for (int i = 0; i < n - 1; i++)
178
         {
179
           int u, v;
           scanf("%d%d", &u, &v);
180
181
           u--, v--;
182
           sp.Link(pos[u], pos[v]);
183
         }
184
185
    //
           scanf("%d", &m);
186
           for (int i = 0; i < m; i++)
    //
187
    //
188
    //
             int typ, u, v, c;
189
             scanf("%d%d%d", &typ, &u, &v);
    //
190
    //
             u--, v--;
191
    //
             if (typ == 1)
               printf("%d\n", sp.GetRoute(pos[u], pos[v])->maxsum);
192
    //
193
             else
    //
194
    //
195
               scanf("%d", &c);
    //
196
               Node *p = sp.GetRoute(pos[u], pos[v]);
    //
197
               p->same = true;
    //
198
    //
               p\rightarrow sa = c;
199
    //
200
           }
    //
201
202
      return 0;
203 |}
```

4.2.2 维护边权

刘汝佳的 Happy Painting! 查询链上边的不同颜色数量 不能换根,但是可以 Link 和 Cut

```
1
    const int MaxN = 60000;
 2
 3
    struct Node
 4
    {
 5
       int size,key;
 6
 7
       int msk,lazy;
 8
 9
       Node *c[2];
10
       Node *p;
11
    } mem[MaxN], *cur, *nil, *pos[MaxN];
12
    Node *newNode(int v,Node *p)
13
14
15
       cur - c[0] = cur - c[1] = nil, cur - p = p;
16
       cur->size = 1;
17
       cur \rightarrow key = v;
18
19
       cur->msk = 0;
20
       cur \rightarrow lazy = -1;
21
22
       return cur++;
    }
23
24
25
    void Init()
26
    {
27
       cur = mem;
       nil = newNode(0, cur);
28
29
       nil->size = 0;
30
    }
31
32
    struct SplayTree
33
34
       void Pushup(Node *x)
35
       {
36
         if (x == nil) return;
         Pushdown(x);
37
38
         Pushdown(x \rightarrow c[0]);
39
         Pushdown(x->c[1]);
40
         x\rightarrow size = x\rightarrow c[0]\rightarrow size + x\rightarrow c[1]\rightarrow size + 1;
41
42
         x \rightarrow msk = x \rightarrow c[0] \rightarrow msk \mid x \rightarrow c[1] \rightarrow msk \mid (1 << x \rightarrow key);
43
44
       void Pushdown(Node *x)
45
       {
```

```
46
         if (x == nil) return;
47
48
         if (x-> lazy != -1)
49
         {
           x\rightarrow key = x\rightarrow lazy;
50
           x\rightarrow msk = (1 << x\rightarrow key);
51
           x\rightarrow c[0]\rightarrow lazy = x\rightarrow c[1]\rightarrow lazy = x\rightarrow lazy;
52
53
           x\rightarrow lazy = -1;
54
         }
55
56
      bool isRoot(Node *x)
57
58
         return (x == nil) || (x->p->c[0] != x && x->p->c[1] != x);
59
60
      void Rotate(Node *x, int f)
61
62
         if (isRoot(x)) return;
63
         Node *y = x-p;
         y->c[f ^ 1] = x->c[f], x->p = y->p;
64
         if (x->c[f] != nil)
65
           x\rightarrow c[f]\rightarrow p = y;
66
67
         if (y != nil)
68
         {
69
           if (y == y->p->c[1])
70
              y-p-c[1] = x;
71
           else if (y == y->p->c[0])
72
              y-p-c[0] = x;
73
74
         x->c[f] = y, y->p = x;
75
         Pushup(y);
76
77
      void Splay(Node *x)
78
79
         static Node *stack[MaxN];
80
         int top = 0;
81
         stack[top++] = x;
82
         for (Node *y = x; !isRoot(y); y = y \rightarrow p)
83
           stack[top++] = y->p;
         while (top)
84
85
           Pushdown(stack[—top]);
86
         while (!isRoot(x))
87
88
         {
89
           Node *y = x -> p;
90
           if (isRoot(y))
              Rotate(x, x == y\rightarrowc[0]);
91
           else
92
93
           {
94
              int fd = y->p->c[0] == y;
95
              if (y->c[fd] == x)
                Rotate(x, fd ^{\wedge} 1), Rotate(x, fd);
96
```

```
97
               else
 98
                 Rotate(y, fd), Rotate(x, fd);
 99
            }
100
          }
101
          Pushup(x);
102
       Node *Access(Node *u)
103
104
105
          Node *v = nil;
          while (u != nil)
106
107
          {
108
            Splay(u);
            v \rightarrow p = u;
109
            u\rightarrow c[1] = v;
110
111
            Pushup(u);
112
            u = (v = u) - p;
113
            if (u == nil) return v;
          }
114
115
116
       Node *Root(Node *u)
117
       {
118
          Access(u);
119
          Splay(u);
          for (Pushdown(u); u\rightarrow c[0] != nil; u = u\rightarrow c[0])
120
            Pushdown(u);
121
122
          Splay(u);
123
          return u;
124
125
       Node *LCA(Node *u, Node *v)
126
       {
          if (Root(u) != Root(v))
127
            return nil;
128
129
          Access(u);
130
          return Access(v);
131
       }
132
       void Cut(Node *u)
133
134
          Access(u);
135
          Splay(u);
136
          u \rightarrow c[0] = u \rightarrow c[0] \rightarrow p = nil;
137
          Pushup(u);
138
       }
       void Link(Node *u, Node *v, int val)
139
140
       {
          Access(u);
141
142
          Splay(u);
143
          u \rightarrow p = v;
          u->key = val;
144
145
          Pushup(u);
146
       }
    };
147
```

```
148
149
    int cntbit(int x)
150
      x = (x \& 0x55555555) + ((x >> 1) \& 0x55555555);
151
152
      x = (x \& 0x33333333) + ((x >> 2) \& 0x33333333);
      x = (x \& 0x0F0F0F0F) + ((x >> 4) \& 0x0F0F0F0F);
153
      x = (x \& 0x00FF00FF) + ((x >> 8) \& 0x00FF00FF);
154
155
      x = (x \& 0x0000FFFF) + ((x >> 16) \& 0x0000FFFF);
156
      return x;
    }
157
158
    SplayTree sp;
159
    int n,Q,f[MaxN];
160
161
    int main(int argc, char const *argv[])
162
163
      while (scanf("%d%d",&n,&Q) != EOF)
164
165
      {
166
         Init();
167
         for (int i = 0; i < n; i++)
168
169
           scanf("%d",&f[i]);
170
           pos[i] = newNode(0, nil);
         }
171
         for (int i = 0; i < n; i++)
172
173
         {
174
           int col;
           scanf("%d",&col);
175
176
           if (f[i] > 0)
177
             sp.Link(pos[i],pos[f[i]-1],col-1);
178
         for (int q = 0; q < Q; q++)
179
180
         {
181
           int typ,x,y,c;
           scanf("%d%d%d",&typ,&x,&y);
182
183
           x---,y---;
184
           if (typ == 3)
185
           {
             Node *lca = sp.LCA(pos[x],pos[y]);
186
187
             if (lca == nil || x == y)
188
             {
               printf("0_{\square}0\n");
189
               continue;
190
             }
191
192
             int totedge = lca->c[1]->size;
             int msk = lca->c[1]->msk;
193
194
             if (pos[x] != lca)
195
196
             {
197
               sp.Splay(pos[x]);
198
               totedge += pos[x]->size;
```

```
199
                msk |= pos[x]->msk;
              }
200
201
202
              printf("%d<sub>\\\\</sub>%d\n",totedge,cntbit(msk));
            }
203
            else
204
205
            {
206
              scanf("%d",&c);
207
              c--;
              if (typ == 1)
208
209
              {
                 if (x == y) continue;
210
211
212
                 Node *lca = sp.LCA(pos[x],pos[y]);
                 if (pos[x] == lca) continue;
213
214
                sp.Cut(pos[x]);
215
216
                 sp.Link(pos[x],pos[y],c);
217
              }
218
              else
219
220
              {
221
                Node *lca = sp.LCA(pos[x],pos[y]);
222
223
                 if (lca == nil || x == y)
224
                   continue;
225
                lca \rightarrow c[1] \rightarrow lazy = c;
226
227
                 sp.Pushup(lca->c[1]);
228
                 sp.Pushup(lca);
                 if (pos[x] != lca)
229
230
                 {
231
                   sp.Splay(pos[x]);
232
                   pos[x] \rightarrow lazy = c;
233
                   sp.Pushup(pos[x]);
234
                 }
              }
235
            }
236
         }
237
238
       }
239
       return 0;
240 }
```

4.3 可持久化线段树

区间第 k 小数,内存压缩版,POJ2014。

```
1 |#include <cstdio>
2 |#include <algorithm>
3 | using namespace std;
4 |
5 | const int MAXN=100000, MAXM=100000;
```

```
6
 7
   struct node
 8
 9
      node *l,*r;
10
      int sum;
   }tree[MAXN*4+MAXM*20];
11
12
13
   int N;
14
   node *newnode()
15
16
      tree[N].l=tree[N].r=NULL;
17
      tree[N].sum=0;
18
      return &tree[N++];
19
20
   node *newnode(node *x)
21
   {
22
      tree[N].l=x->l;
23
      tree[N].r=x->r;
      tree[N].sum=x->sum;
24
25
      return &tree[N++];
26
27
   node *build(int l,int r)
28
29
      node *x=newnode();
30
      if (l<r)
31
      {
32
        int mid=l+r>>1;
        x->l=build(l,mid);
33
34
        x->r=build(mid+1,r);
        x\rightarrow sum=x\rightarrow l\rightarrow sum+x\rightarrow r\rightarrow sum;
35
      }
36
37
      else
38
        x->sum=0;
39
      return x;
40
41
   node *update(node *x,int l,int r,int p,int v)
42
      if (l<r)
43
44
      {
45
        int mid=l+r>>1;
        node *nx=newnode(x);
46
        if (p<=mid)
47
        {
48
          node *ret=update(x->1,1,mid,p,v);
49
          nx->l=ret;
50
        }
51
        else
52
53
        {
54
          node *ret=update(x->r,mid+1,r,p,v);
55
           nx->r=ret;
56
        }
```

```
nx->sum=nx->l->sum+nx->r->sum;
 57
 58
         return nx;
 59
       }
 60
      else
 61
 62
         node *nx=newnode(x);
 63
         nx->sum+=v;
 64
         return nx;
 65
       }
 66
    int query(node *x1,node *x2,int l,int r,int k)
 67
 68
       if (l<r)
 69
 70
       {
         int mid=l+r>>1;
 71
 72
         int lsum=x2->l->sum-x1->l->sum;
         if (lsum>=k)
 73
 74
           return query(x1->l,x2->l,l,mid,k);
 75
         else
           return query(x1->r,x2->r,mid+1,r,k-lsum);
 76
 77
       }
 78
       else
 79
         return l;
 80
    }
 81
    char s[10];
    node *root[MAXM+1];
 82
    int a[MAXN],b[MAXN];
 84
    int init(int n)
 85
    {
 86
       for (int i=0;i<n;i++)
 87
         b[i]=a[i];
       sort(b,b+n);
 88
       int tn=unique(b,b+n)-b;
 89
 90
       for (int i=0;i<n;i++)
 91
       {
 92
         int l=0,r=tn-1;
 93
         while (l<r)
 94
         {
 95
           int mid=l+r>>1;
 96
           if (b[mid]>=a[i])
 97
             r=mid;
 98
           else
 99
             l=mid+1;
100
         }
         a[i]=l;
101
102
       }
103
       return tn;
104
    int main()
105
106
       int cas=1,n;
107
```

```
108
      while (scanf("%d",&n)!=EOF)
109
         printf("Case<sub>□</sub>%d:\n",cas++);
110
         for (int i=0;i<n;i++)</pre>
111
           scanf("%d",&a[i]);
112
         int tn=init(n);
113
114
         N=0;
         root[0]=build(0,tn-1);
115
116
         for (int i=1;i<=n;i++)
           root[i]=update(root[i-1],0,tn-1,a[i-1],1);
117
118
         int m;
         scanf("%d",&m);
119
         for (int i=0;i<m;i++)</pre>
120
121
122
           int s,t;
123
           scanf("%d%d",&s,&t);
           printf("%d\n",b[query(root[s-1],root[t],0,tn-1,t-s+2>>1)]);
124
         }
125
126
       }
127
       return 0;
128 |}
    4.4 treap 正式版
    支持翻转。
  1 #include <cstdio>
    #include <cstdlib>
    |#include <algorithm>
  4
    using namespace std;
  5
    const int MAXN = 100000;
    const int MAXM = 100000;
    const int inf = 0x7ffffffff;
    int a[MAXN];
    struct Treap
 10
 11
    {
       int N;
 12
 13
       Treap()
       {
 14
 15
         N = 0;
         root = NULL;
 16
 17
       }
       void init()
 18
 19
 20
         N = 0;
 21
         root = NULL;
 22
       }
 23
       struct Treap_Node
 24
 25
         Treap_Node *son[2];//left & right
 26
         int value, fix;
```

```
27
         bool lazy;
28
         int size;
29
         Treap_Node() {}
30
         Treap_Node(int _value)
31
         {
32
           son[0] = son[1] = NULL;
           value = _value;
33
34
           fix = rand() * rand();
35
           lazy = 0;
36
           size = 1;
         }
37
38
         int sonSize(bool flag)
39
         {
40
           if (son[flag] == NULL)
41
             return 0;
42
           else
43
              return son[flag]->size;
44
         }
45
      } node[MAXN], *root, *pos[MAXN];
46
      void up(Treap_Node *p)
47
      {
48
         p\rightarrow size = p\rightarrow sonSize(0) + p\rightarrow sonSize(1) + 1;
49
      void down(Treap_Node *p)
50
51
      {
52
         if (!p->lazy)
53
           return ;
         for (int i = 0; i < 2; i++)</pre>
54
55
           if (p->son[i])
56
             p->son[i]->lazy = !p->son[i]->lazy;
57
         swap(p\rightarrow son[0], p\rightarrow son[1]);
58
         p\rightarrow lazy = 0;
      }
59
60
      Treap_Node *merge(Treap_Node *p, Treap_Node *q)
61
      {
62
         if (p == NULL)
63
           return q;
         else if (q == NULL)
64
65
           return p;
66
         if (p->fix <= q->fix)
67
         {
68
           down(p);
69
           p\rightarrow son[1] = merge(p\rightarrow son[1], q);
70
           up(p);
71
           return p;
         }
72
73
         else
74
         {
75
           down(q);
76
           q \rightarrow son[0] = merge(p, q \rightarrow son[0]);
77
           up(q);
```

```
78
           return q;
 79
        }
      }
 80
      pair<Treap_Node *, Treap_Node *> split(Treap_Node *p, int n)
 81
 82
 83
        if (p == NULL)
           return make_pair((Treap_Node *)NULL, (Treap_Node *)NULL);
 84
 85
 86
           return make_pair((Treap_Node *)NULL, p);
        if (n == p->size)
 87
 88
           return make_pair(p, (Treap_Node *)NULL);
 89
        down(p);
 90
        if (p->sonSize(0) >= n)
 91
 92
           pair<Treap_Node *, Treap_Node *> ret = split(p->son[0], n);
 93
           p->son[0] = ret.second;
 94
          up(p);
 95
           return make_pair(ret.first, p);
        }
 96
        else
 97
 98
        {
 99
          pair<Treap_Node *, Treap_Node *>
100
             ret = split(p->son[1], n - p->sonSize(0) - 1);
101
           p->son[1] = ret.first;
102
          up(p);
           return make_pair(p, ret.second);
103
        }
104
105
      int smalls(Treap_Node *p,int value)
106
107
      {
        if (p==NULL)
108
109
           return 0;
        if (p->value<=value)</pre>
110
           return 1+p->sonSize(0)+smalls(p->son[1],value);
111
112
        else
113
           return smalls(p->son[0],value);
114
      }
115
      void insert(int value)
116
117
        Treap_Node *p = &node[N++];
        *p = Treap Node(value);
118
        pair<Treap_Node *, Treap_Node *>
119
           ret = split(root, smalls(root, value));
120
121
        root = merge(merge(ret.first, p), ret.second);
122
      void remove(int value)
123
124
        pair<Treap_Node *, Treap_Node *> ret = split(root, smalls(root,
125
             value) - 1);
126
         root = merge(ret.first, split(ret.second, 1).second);
127
      }
```

```
128
      Treap_Node *build(int s, int t)
129
      {
        int idx = t + s >> 1;
130
        Treap_Node *p = &node[N++];
131
        *p = Treap_Node(a[idx]);
132
        pos[a[idx]] = p;
133
134
        if (idx > s)
135
          p = merge(build(s, idx - 1), p);
136
        if (idx < t)
          p = merge(p, build(idx + 1, t));
137
138
        up(p);
        return p;
139
140
      }
      void build(int n)
141
142
143
        root = build(0, n - 1);
144
145
      void *reverse(int s, int t)
146
        pair<Treap_Node *, Treap_Node *> tmp1, tmp2;
147
        tmp1 = split(root, s - 1);
148
149
        tmp2 = split(tmp1.second, t - s + 1);
150
        tmp2.first->lazy = !tmp2.first->lazy;
151
        root = merge(tmp1.first, merge(tmp2.first, tmp2.second));
152
      }
    };
153
154
    Treap treap;
    int main()
155
156
    {
157
      treap.init();
158
      int n;
      scanf("%d", &n);
159
      for (int i = 0; i < n; i++)
160
        scanf("%d", &a[i]);
161
      treap.build(n);
162
163 |}
         树链剖分
    4.5
    4.5.1 点权
  1 |#include <cstdio>
    #include <cstring>
    #include <cstdlib>
    |#include <algorithm>
    using namespace std;
    const int MAX = 12000;
  7
    const int LOG = 15;
    const int oo = 0x3f3f3f3f;
    struct Edge
 10 |{
```

```
11
        int to, w, id;
12
        Edge* next;
   } memo[MAX<<1],*cur,*g[MAX],*pree[MAX],*solid[MAX],*valid[MAX];</pre>
13
   int dp[MAX][LOG], pos[MAX], lst[MAX], dep[MAX], cnt[MAX], h[MAX], K
       , n;
15
   void init()
16
17
      for (int i = 1; i <= n; i++)
18
19
        g[i] = NULL;
20
        valid[i] = NULL;
21
        solid[i] = NULL;
22
        pree[i] = NULL;
23
24
      for (int i = 0; i < LOG; i++)
25
      {
26
        dp[1][i] = 1;
27
28
      cur = memo;
29
      K = 0;
30
31
   void add(int u, int v, int w, int id)
32
33
     cur->to = v;
34
      cur->w = w;
35
      cur->id = id;
36
      cur->next = g[u];
37
      g[u] = cur++;
38
   }
39
   void dfsLCA(int d, int u, int f)
40
41
     dep[u] = d;
42
      dp[u][0] = f;
43
      cnt[u] = 1;
      for (int i = 1; i < LOG; i++)
44
45
      {
46
        dp[u][i] = dp[dp[u][i - 1]][i - 1];
47
48
      for (Edge* it = g[u]; it; it = it->next)
49
50
        int \vee = it\rightarrowto;
        if (v != f)
51
52
        {
53
          pree[v] = it;
54
          valid[it->id] = it;
          dfsLCA(d + 1, v, u); //RE
55
56
          cnt[u] += cnt[v];
          if (solid[u] == NULL || cnt[solid[u]->to] < cnt[v])</pre>
57
58
          {
59
            solid[u] = it;
60
          }
```

```
61
         }
 62
       }
 63
 64
    void dfsChain(int u, int head)
 65
 66
       h[u] = head;
       if (solid[u])
 67
 68
 69
         lst[pos[u] = K++] = u;
 70
         dfsChain(solid[u]->to, head);
       }
 71
 72
       else
 73
       for (Edge* it = g[u]; it; it = it->next)
 74
 75
         int v = it—>to;
 76
         if (it != solid[u] && v != dp[u][0])
 77
 78
           dfsChain(v, v);
 79
         }
       }
 80
 81
 82
    int getLCA(int u, int v)
 83
 84
       if (dep[u] < dep[v])
 85
         swap(u, v);
       for (int st = 1 << (LOG - 1), i = LOG - 1; i >= 0; i--, st >>= 1)
 86
 87
 88
         if (st <= dep[u] - dep[v])
 89
 90
           u = dp[u][i];
         }
 91
 92
       if (u == v)
 93
 94
         return u;
 95
       for (int i = LOG - 1; i >= 0; i—)
 96
         if (dp[u][i] != dp[v][i])
 97
 98
 99
           u = dp[u][i];
100
           v = dp[v][i];
         }
101
102
103
       return dp[u][0];
104
    }
105
    struct Node
106
107
         int l, r, ma, mi;
108
         bool rev;
    } seg[MAX << 2];</pre>
109
110
    void reverse(int k)
111 | {
```

```
112
      seg[k].mi *= -1;
113
      seg[k].ma *= -1;
114
      seg[k].rev ^= 1;
115
      swap(seg[k].mi, seg[k].ma);
116
117
    void pushdown(int k)
118
119
      if (seg[k].rev)
120
121
         reverse(k << 1);
122
         reverse(k << 1 | 1);
123
         seg[k].rev = false;
      }
124
125
126
    void update(int k)
127
      seg[k].mi = min(seg[k << 1].mi, seg[k << 1 | 1].mi);
128
129
      seg[k].ma = max(seg[k << 1].ma, seg[k << 1 | 1].ma);
130
    void init(int k, int l, int r)
131
132
    {
133
      seg[k].l = l;
134
      seg[k].r = r;
135
      seg[k].rev = false;
      if (l == r)
136
137
138
         seg[k].mi = seg[k].ma = solid[lst[l]]->w; //solid WA
139
         return:
140
      }
141
      int mid = l + r >> 1;
      init(k << 1, l, mid);</pre>
142
143
      init(k << 1 | 1, mid + 1, r);
144
      update(k);
145
    void update(int k, int id, int v)
146
147
148
      if (seg[k].l == seg[k].r)
149
150
         seg[k].mi = seg[k].ma = solid[lst[id]]->w = v;
151
         return;
152
      }
153
      pushdown(k);
      int mid = seg[k].l + seg[k].r >> 1;
154
155
      if (id <= mid)
156
         update(k << 1, id, v);
157
      else
         update(k << 1 \mid 1, id, v);
158
159
      update(k);
160
161
    void reverse(int k, int l, int r)
162 | {
```

```
163
      if (seg[k].l > r || seg[k].r < l)
164
         return;
      if (seg[k].l >= l && seg[k].r <= r)
165
166
      {
167
         reverse(k);
168
         return;
169
170
      pushdown(k);
171
      reverse(k << 1, l, r);
      reverse(k << 1 | 1, l, r);
172
173
      update(k);
174
    int read(int k, int l, int r)
175
176
      if (seg[k].l > r || seg[k].r < l)
177
178
         return -oo;
      if (seg[k].l >= l && seg[k].r <= r)
179
         return seg[k].ma;
180
181
      pushdown(k);
      return max(read(k << 1, l, r), read(k << 1 | 1, l, r));
182
183
184
    void setEdge(int id, int v)
185
      Edge* it = valid[id];
186
187
      if (h[it->to] != it->to)
188
         update(1, pos[dp[it->to][0]], v);
189
190
      }
191
      else
192
      {
193
         it->w = v;
194
      }
195
    void negateLCA(int t, int u)
196
197
198
      while (t != u)
199
      {
200
         int tmp = h[u];
         if (dep[tmp] < dep[t])</pre>
201
           tmp = t;
202
         if (h[u] == u)
203
204
         {
205
           pree[u] -> w *= -1;
206
           u = dp[u][0];
         }
207
         else
208
209
           reverse(1, pos[tmp], pos[dp[u][0]]);
210
211
           u = tmp;
212
         }
213
      }
```

```
214 |}
215
    void negate(int u, int v)
216
217
       int t = getLCA(u, v);
218
       negateLCA(t, u);
       negateLCA(t, v);
219
220
    int maxLCA(int t, int u)
221
222
       int ret = -00;
223
224
      while (t != u)
225
       {
         int tmp = h[u];
226
227
         if (dep[tmp] < dep[t])</pre>
228
           tmp = t;
229
         if (h[u] == u)
230
231
           ret = max(ret, pree[u]->w);
           u = dp[u][0];
232
         }
233
         else
234
235
         {
236
           ret = max(ret, read(1, pos[tmp], pos[dp[u][0]]));
237
           u = tmp;
238
         }
239
       }
240
       return ret;
241
242
    int query(int u, int v)
243
    {
      int t = getLCA(u, v);
244
245
       return max(maxLCA(t, u), maxLCA(t, v));
    }
246
247
    int main()
248
    {
249
       int ⊺;
       int u, v, w;
250
      char op[15];
251
      scanf("%d", &T);
252
      while (T—)
253
254
       {
         scanf("%d", &n);
255
256
         init();
         for (int i = 1; i < n; i++)
257
258
           scanf("%d%d%d", &u, &v, &w);
259
           add(u, v, w, i);
260
261
           add(v, u, w, i);
262
263
         dfsLCA(0, 1, 1);
264
         dfsChain(1, 1);
```

```
265
         init(1, 0, K - 1);
266
         while (scanf("%s", op), op[0] != 'D')
267
           scanf("%d%d", &u, &v);
268
           if (op[0] == 'C')
269
270
           {
271
             setEdge(u, v);
272
           }
273
           else if (op[0] == 'N')
274
           {
275
             negate(u, v);
276
           }
           else
277
278
279
             printf("%d\n", query(u, v));
           }
280
         }
281
282
283
      return 0;
284
    }
    4.5.2 边权
  1 |#include <cstdio>
    #include <iostream>
  3
    #include <cstdlib>
    |#include <algorithm>
  5 #include <cmath>
    |#include <cstring>
    using namespace std;
    int n,m,sum,pos;
    | int head[50005],e;
    |int s[50005],from[50005];
    int fa[50005][20],deep[50005],num[50005];
    int solid[50005],p[50005],fp[50005];
 12
 13
    struct N
 14
    {
      int l,r,mid;
 15
      int add,w;
 16
    }nod[50005*4];
 17
    struct M
 18
 19
    {
      int v,next;
 20
 21
    }edge[100005];
    void addedge(int u,int v)
 22
 23
    {
 24
      edge[e].v=v;
 25
      edge[e].next=head[u];
 26
      head[u]=e++;
 27
 28
      edge[e].v=u;
 29
      edge[e].next=head[v];
```

```
30
      head[v]=e++;
31
32
   void LCA(int st,int f,int d)
33
   {
34
      deep[st]=d;
35
      fa[st][0]=f;
36
      num[st]=1;
37
      int i,∨;
38
      for(i=1;i<20;i++)</pre>
39
        fa[st][i]=fa[fa[st][i-1]][i-1];
40
      for(i=head[st];i!=-1;i=edge[i].next)
41
42
        v=edge[i].v;
43
        if(v!=f)
44
        {
45
          LCA(v,st,d+1);
          num[st]+=num[v];
46
47
          if(solid[st]==-1||num[v]>num[solid[st]])
48
            solid[st]=v;
49
        }
50
      }
51
52
   void getpos(int st,int sp)
53
   {
54
      from[st]=sp;
55
      if(solid[st]!=−1)
56
      {
57
        p[st]=pos++;
58
        fp[p[st]]=st;
59
        getpos(solid[st],sp);
      }
60
61
     else
62
63
        p[st]=pos++;
64
        fp[p[st]]=st;
65
        return;
      }
66
67
      int i,v;
68
      for(i=head[st];i!=-1;i=edge[i].next)
69
70
        v=edge[i].v;
71
        if(v!=solid[st]&&v!=fa[st][0])
72
          getpos(v,v);
      }
73
74
75
   int getLCA(int u,int v)
76
   {
77
      if(deep[u]<deep[v])</pre>
78
        swap(u,v);
79
      int d=1<<19,i;
80
      for(i=19;i>=0;i—)
```

```
81
       {
 82
         if(d<=deep[u]-deep[v])</pre>
 83
           u=fa[u][i];
 84
         d>>=1;
       }
 85
       if(u==v)
 86
 87
         return u;
 88
       for(i=19;i>=0;i---)
 89
         if(fa[u][i]!=fa[v][i])
 90
         {
 91
           u=fa[u][i];
 92
           v=fa[v][i];
 93
 94
       return fa[u][0];
 95
    }
 96
    void init(int p,int l,int r)
 97
 98
       nod[p].l=l;
 99
       nod[p].r=r;
       nod[p].mid=(l+r)>>1;
100
       nod[p].add=0;
101
102
       if(l==r)
103
         nod[p].w=s[fp[l]];
       else
104
105
       {
         init(p<<1,l,nod[p].mid);</pre>
106
107
         init(p<<1|1,nod[p].mid+1,r);
       }
108
109
     }
110
    void lazy(int p)
111
112
       if(nod[p].add!=0)
113
114
         nod[p<<1].add+=nod[p].add;</pre>
         nod[p<<1|1].add+=nod[p].add;</pre>
115
116
         nod[p].add=0;
       }
117
118
119
     void update(int p,int l,int r,int v)
120
121
       if(nod[p].l==l&&nod[p].r==r)
122
       {
         nod[p].add+=v;
123
124
         return;
125
       lazy(p);
126
       if(nod[p].mid<l)</pre>
127
         update(p<<1|1,l,r,v);
128
       else if(nod[p].mid>=r)
129
130
         update(p<<1,l,r,v);
131
       else
```

```
132
       {
133
         update(p<<1,l,nod[p].mid,v);
         update(p<<1|1,nod[p].mid+1,r,v);
134
135
       }
136
    }
    int read(int p,int l,int r)
137
138
     {
       if(nod[p].l==l&&nod[p].r==r)
139
140
         return nod[p].w+nod[p].add;
141
       lazy(p);
       if(nod[p].mid<l)</pre>
142
         return read(p<<1|1,1,r);
143
       else if(nod[p].mid>=r)
144
145
         return read(p<<1,l,r);</pre>
146
    }
    void jump(int st,int ed,int val)
147
148
149
      while(deep[st]>=deep[ed])
150
151
         int tmp=from[st];
         if(deep[tmp] < deep[ed])</pre>
152
153
           tmp=ed;
154
         update(1,p[tmp],p[st],val);
         st=fa[tmp][0];
155
156
       }
157
    }
    void change(int st,int ed,int val)
158
159
160
       int lca=getLCA(st,ed);
161
       jump(st,lca,val);
162
       jump(ed,lca,val);
       jump(lca,lca,-val);
163
164
    }
165
    int main()
166
     {
167
      while(scanf("%d%d%d",&n,&m,&sum)==3)
168
169
         int i;
         s[0]=0;pos=0;deep[0]=-1;
170
         memset(fa,0,sizeof(fa));
171
         for(i=1;i<=n;i++)
172
173
         {
           solid[i]=-1;
174
           scanf("%d",&s[i]);
175
         }
176
         memset(head,-1,sizeof(head));
177
178
         e=0;
         for(i=0;i<m;i++)</pre>
179
180
         {
181
           int a,b;
           scanf("%d%d",&a,&b);
182
```

```
183
           addedge(a,b);
184
         }
         LCA(1,0,0);
185
         getpos(1,1);
186
         init(1,0,pos-1);
187
         for(i=0;i<sum;i++)</pre>
188
         {
189
           char que[5];
190
191
           scanf("%s",que);
           if(que[0]!='Q')
192
193
           {
194
              int a,b,c;
              scanf("%d%d%d",&a,&b,&c);
195
              if(que[0]=='D')
196
                c=-c;
197
198
             change(a,b,c);
           }
199
           else
200
201
           {
202
              int a;
              scanf("%d",&a);
203
204
              printf("%d\n",read(1,p[a],p[a]));
205
           }
         }
206
207
       }
208
       return 0;
209
    |}
          划分树
    4.6
    | int n,m;
  2
    struct elem
  3
    {
  4
       int v,index;
    }a[120000];
    int d[30][120000];
  7
    int s[30][120000];
  8
  9
    bool cmp(elem a,elem b)
 10
    {
 11
       if (a.v == b.v)
 12
         return a.index <= b.index;</pre>
 13
       return a.v < b.v;</pre>
    }
 14
 15
    void build(int depth,int l,int r)
 16
 17
 18
       if (l == r)
 19
         return;
 20
       int mid = (l+r)/2;
       int tl,tr;
 21
 22
       tl = tr = 0;
```

```
23
     for (int i = l;i <= r;i++)
24
25
       if (cmp(a[d[depth][i]],a[mid]))
26
       {
27
         d[depth+1][l+tl] = d[depth][i];
28
         tl++;
29
       }
30
       else
31
       {
         d[depth+1][mid+1+tr] = d[depth][i];
32
33
         tr++;
       }
34
35
       s[depth][i] = tl;
36
37
     build(depth+1,l,mid);
38
     build(depth+1,mid+1,r);
39
   }
40
41
   int find(int depth,int dl,int dr,int fl,int fr,int k)
42
43
     if (fl == fr)
44
       return a[d[depth][fl]].v;
45
     int ls,rs;
     int mid = (dl+dr)/2;
46
47
     ls = (fl == dl)? 0 : s[depth][fl-1];
     rs = s[depth][fr];
48
49
     return (rs-ls < k)?</pre>
50
       51
       : find(depth+1,dl,mid,dl+ls,dl+rs-1,k);
52
   }
53
54
   int main()
55
56
     while (scanf("%d%d",&n,&m) != EOF)
57
     {
58
       for (int i = 1; i <= n; i++)
59
       {
         scanf("%d",&a[i].v);
60
         a[i].index = i;
61
62
       }
63
       sort(a+1,a+n+1,cmp);
       for (int i = 1;i <= n;i++)</pre>
64
         d[0][a[i].index] = i;
65
66
       build(0,1,n);
       int l,r,k;
67
       for (int i = 1; i <= m; i++)
68
69
       {
70
         scanf("%d%d%d",&l,&r,&k);
71
         printf("%d\n",find(0,1,n,l,r,k));
72
       }
     }
73
```

```
74
     return 0;
75 }
   4.7 树状数组
   int read(int k)
 2
   {
 3
     int sum = 0;
     for (; k; k^=k-k)
 4
 5
        sum+=tree[k];
 6
      return sum;
   }
 7
   void update(int k, int v)
 9
      for (; k<=MaxN; k+=k&-k)</pre>
10
        tree[k]+=v;
11
12
   }
13
   int find_Kth(int k)
14
      int idx = 0;
15
     for(int i=20; i>=0; i---)
16
17
       idx |= 1 << i;
18
19
        if(idx <= MaxN && tree[idx] < k)</pre>
20
          k -= tree[idx];
        else idx ^= 1 << i;
21
22
23
      return idx + 1;
24 |}
```

5 图论

5.1 优先队列优化的 dijkstra

```
1 | #include < cstdio >
   #include<cstring>
   #include<iostream>
 4 | #include < algorithm >
 5 #include<queue>
   #include<vector>
 7 using namespace std;
 8 const int MAXN=100;
   const int MAXM=1000;
   int N,L;
11 | int head[MAXN];
   struct edges
13
   {
14
     int to,next,cost;
15
   } edge[MAXM];
16
   int dist[MAXN];
17
   class states
18
   {
   public:
19
20
     int cost,id;
21
   };
22
   class cmp
23
   {
   public:
24
25
     bool operator ()(const states &i,const states &j)
26
27
        return i.cost>j.cost;
     }
28
29
   };
   void init(int n)
30
31
   {
32
     N=n;
33
     L=0;
34
     for (int i=0; i<n; i++)</pre>
35
        head[i]=-1;
36
   void add_edge(int x,int y,int cost)
37
38
   {
39
     edge[L].to=y;
40
     edge[L].cost=cost;
41
     edge[L].next=head[x];
42
     head[x]=L++;
43
   int dijkstra(int s,int t)
44
45
46
     memset(dist,63,sizeof(dist));
47
     states u;
```

```
48
     u.id=s;
49
     u.cost=0;
50
     dist[s]=0;
51
     priority_queue<states, vector<states>, cmp> q;
52
     q.push(u);
53
     while (!q.empty())
54
     {
55
        u=q.top();
56
        q.pop();
57
        if (u.id==t) return dist[t];
        if (u.cost!=dist[u.id]) continue;
58
        for (int i=head[u.id]; i!=-1; i=edge[i].next)
59
60
        {
61
          states v=u;
62
          v.id=edge[i].to;
63
          if (dist[v.id]>dist[u.id]+edge[i].cost)
64
65
            v.cost=dist[v.id]=dist[u.id]+edge[i].cost;
66
            q.push(v);
          }
67
        }
68
69
     }
70
     return -1;
71
72
   int main()
73
74
     int n,m;
75
     scanf("%d%d",&n,&m);
76
     init(n);
77
     for (int i=0; i<m; i++)
78
79
        int x,y,z;
        scanf("%d%d%d",&x,&y,&z);
80
81
        add_edge(x,y,z);
82
        add_edge(y,x,z);
83
     }
84
     int s,t;
85
     scanf("%d%d",&s,&t);
86
     printf("%d\n",dijkstra(s,t));
87
     return 0;
88 | }
         SAP 四版
 1 | const int MAXEDGE=20400;
 2
   const int MAXN=400;
   const int inf=0x3fffffff;
   struct edges
 5
   {
 6
     int cap,to,next,flow;
 7
   } edge[MAXEDGE+100];
 8 | struct nodes
```

```
9
   {
10
      int head, label, pre, cur;
   } node[MAXN+100];
11
12
   int L,N;
   int gap[MAXN+100];
13
   void init(int n)
15
   {
16
      L=0;
17
      N=n;
      for (int i=0; i<N; i++)</pre>
18
19
        node[i].head=-1;
20
21
   void add_edge(int x,int y,int z,int w)
22
23
      edge[L].cap=z;
24
      edge[L].flow=0;
25
      edge[L].to=y;
26
      edge[L].next=node[x].head;
27
      node[x].head=L++;
28
      edge[L].cap=w;
29
      edge[L].flow=0;
30
      edge[L].to=x;
31
      edge[L].next=node[y].head;
32
      node[y].head=L++;
33
34
   int maxflow(int s,int t)
35
36
      memset(gap,0,sizeof(gap));
37
      gap[0]=N;
38
      int u,ans=0;
      for (int i=0; i<N; i++)</pre>
39
40
      {
41
        node[i].cur=node[i].head;
42
        node[i].label=0;
43
      }
44
      u=s;
45
      node[u].pre=-1;
      while (node[s].label<N)</pre>
46
47
      {
        if (u==t)
48
49
        {
50
          int min=inf;
51
          for (int i=node[u].pre; i!=-1; i=node[edge[i^1].to].pre)
            if (min>edge[i].cap-edge[i].flow)
52
              min=edge[i].cap—edge[i].flow;
53
          for (int i=node[u].pre; i!=-1; i=node[edge[i^1].to].pre)
54
55
          {
56
            edge[i].flow+=min;
57
            edge[i^1].flow==min;
58
          }
59
          u=s;
```

```
60
          ans+=min;
61
          continue;
        }
62
63
        bool flag=false;
64
        int ∨;
        for (int i=node[u].cur; i!=-1; i=edge[i].next)
65
        {
66
          v=edge[i].to;
67
68
          if (edge[i].cap-edge[i].flow &&
            node[v].label+1==node[u].label)
69
70
          {
71
            flag=true;
            node[u].cur=node[v].pre=i;
72
73
            break;
          }
74
75
        }
        if (flag)
76
77
        {
78
          u=v;
79
          continue;
        }
80
81
        node[u].cur=node[u].head;
82
        int min=N;
        for (int i=node[u].head; i!=-1; i=edge[i].next)
83
84
          if (edge[i].cap-edge[i].flow && node[edge[i].to].label<min)</pre>
85
            min=node[edge[i].to].label;
        gap[node[u].label]--;
86
87
        if (!gap[node[u].label]) return ans;
88
        node[u].label=min+1;
89
        gap[node[u].label]++;
        if (u!=s) u=edge[node[u].pre^1].to;
90
91
     }
92
     return ans;
93 |}
         费用流
   5.3
   5.3.1 三版
   T 了可以改成栈。
 1 | const int MAXM=60000;
   const int MAXN=400;
   const int inf=0x3fffffff;
   int L,N;
   int K;
 5
 6
   struct edges
 7
   {
 8
     int to,next,cap,flow,cost;
   } edge[MAXM];
 9
   struct nodes
10
11
   {
```

```
12
     int dis,pre,head;
13
     bool visit;
   } node[MAXN];
14
15
   void init(int n)
16
   {
17
     N=n;
18
     L=0;
     for (int i=0; i<N; i++)</pre>
19
20
        node[i].head=-1;
21
   void add_edge(int x,int y,int cap,int cost)
22
23
24
     edge[L].to=y;
25
     edge[L].cap=cap;
26
     edge[L].cost=cost;
27
     edge[L].flow=0;
28
     edge[L].next=node[x].head;
29
     node[x].head=L++;
     edge[L].to=x;
30
31
     edge[L].cap=0;
32
     edge[L].cost=-cost;
33
     edge[L].flow=0;
34
     edge[L].next=node[y].head;
     node[y].head=L++;
35
36
   bool spfa(int s,int t)
37
38
   {
39
     queue <int> q;
     for (int i=0; i<N; i++)</pre>
40
41
        node[i].dis=0x3fffffff;
42
43
        node[i].pre=-1;
44
        node[i].visit=0;
45
     node[s].dis=0;
46
47
     node[s].visit=1;
48
     q.push(s);
49
     while (!q.empty())
50
     {
51
        int u=q.front();
52
        node[u].visit=0;
        for (int i=node[u].head; i!=-1; i=edge[i].next)
53
54
        {
          int v=edge[i].to;
55
          if (edge[i].cap>edge[i].flow &&
56
              node[v].dis>node[u].dis+edge[i].cost)
57
          {
58
59
            node[v].dis=node[u].dis+edge[i].cost;
            node[v].pre=i;
60
61
            if (!node[v].visit)
62
```

```
63
              node[v].visit=1;
64
              q.push(v);
65
            }
66
          }
        }
67
68
        q.pop();
69
70
     if (node[t].pre==-1)
71
        return 0;
72
     else
73
        return 1;
74
75
   int mcmf(int s,int t,int &cost)
76
     int flow=0;
77
     while (spfa(s,t))
78
79
80
        int max=inf;
81
        for (int i=node[t].pre; i!=-1; i=node[edge[i^1].to].pre)
82
          if (max>edge[i].cap-edge[i].flow)
83
84
            max=edge[i].cap—edge[i].flow;
85
        for (int i=node[t].pre; i!=-1; i=node[edge[i^1].to].pre)
86
87
        {
          edge[i].flow+=max;
88
          edge[i^1].flow==max;
89
90
          cost+=edge[i].cost*max;
91
        }
92
        flow+=max;
93
94
     return flow;
95 |}
   5.3.2
         dijkstra 加改点堆
 1 |#include <cstdio>
 2
   |#include <cstring>
   #include <algorithm>
   #include <queue>
 5 #include <stack>
 6 using namespace std;
   int N, L;
   int head[2003];
 9
   struct Edge
10
11
        int to, next, flow, cost;
   } edge[2000 * 1999 / 2 + 2000 * 3 << 1];</pre>
12
   |int h[2003], dis[2003], pre[2003];
14
   struct Heap
15 | {
```

```
int value[2004], id[2004];
16
17
        int pos[2003];
        int size;
18
        void init()
19
20
21
            size = 1;
22
        void swap2(int p, int q)
23
24
25
            swap(value[p], value[q]);
26
            swap(id[p], id[q]);
27
            pos[id[p]] = p;
28
            pos[id[q]] = q;
29
        void push_up(int p)
30
31
        {
            while (p > 1 && value[p / 2] > value[p])
32
33
            {
34
                swap2(p, p / 2);
35
                p /= 2;
36
            }
37
        }
38
        void push_down(int p)
39
        {
40
            while (p * 2 < size)
41
42
                int best = p;
                if (p * 2 < size && value[p] > value[p * 2])
43
44
                     best = p * 2;
45
                if (p * 2 + 1 < size && value[best] > value[p * 2 + 1])
46
                     best = p * 2 + 1;
47
                if (p == best)
48
                     break;
49
                swap2(p, best);
50
                p = best;
51
            }
52
        }
53
        void push(int _value, int _id)
54
        {
55
            value[size] = _value;
            id[size] = _id;
56
            pos[_id] = size;
57
58
            push_up(size++);
59
        }
        int top()
60
61
        {
62
            return id[1];
63
        void pop()
64
65
        {
            value[1] = value[size - 1];
66
```

```
id[1] = id[--size];
 67
 68
             pos[id[1]] = 1;
             push_down(1);
 69
 70
         }
 71
         void update(int _value, int _id)
 72
 73
             int p = pos[_id];
 74
             value[p] = _value;
 75
             push_up(p);
 76
         }
 77
    } heap;
    bool inque[2003];
 78
    void init(int n)
 79
 80
    {
 81
         N = n;
 82
         L = 0;
 83
         memset(head, -1, 4 * n);
 84
 85
    void add_edge(int u, int v, int flow, int cost)
 86
    {
 87
         edge[L].to = v;
 88
         edge[L].flow = flow;
 89
         edge[L].cost = cost;
         edge[L].next = head[u];
 90
 91
         head[u] = L++;
 92
         edge[L].to = u;
         edge[L].flow = 0;
 93
         edge[L].cost = -cost;
 94
 95
         edge[L].next = head[v];
 96
         head[v] = L++;
 97
 98
    void spfa(int s)
 99
100
         memset(dis, 63, 4 * N);
         memset(inque, 0, N);
101
102
         memset(pre, -1, 4 * N);
103
         dis[s] = 0;
104
         stack <int> que;
105
         que.push(s);
106
         while (!que.empty())
107
         {
             int u = que.top();
108
             inque[u] = 0;
109
             que.pop();
110
             for (int i = head[u]; i != -1; i = edge[i].next)
111
                 if (edge[i].flow)
112
113
                 {
                      int v = edge[i].to;
114
115
                      if (dis[v] > dis[u] + edge[i].cost)
116
                      {
                          dis[v] = dis[u] + edge[i].cost;
117
```

```
118
                          pre[v] = i;
119
                          if (!inque[v])
120
                          {
121
                              inque[v] = 1;
122
                              que.push(v);
123
                          }
                      }
124
                 }
125
126
         }
127
    void dijkstra(int s)
128
129
130
         for (int i = 0; i < N; ++i)
             h[i] += dis[i];
131
         memset(dis, 63, 4 * N);
132
133
         memset(pre, -1, 4 * N);
134
         memset(inque, 0, N);
135
         dis[s] = 0;
136
         inque[s] = 1;
         heap.init();
137
         heap.push(0, s);
138
139
         while (heap.size > 1)
140
         {
             int u = heap.top();
141
142
             heap.pop();
             for (int i = head[u]; i != -1; i = edge[i].next)
143
144
                 if (edge[i].flow)
145
146
                      int v = edge[i].to;
147
                      if (dis[v] > dis[u] + edge[i].cost + h[u] - h[v])
148
                      {
149
                          dis[v] = dis[u] + edge[i].cost + h[u] - h[v];
150
                          pre[v] = i;
151
                          if (!inque[v])
152
                          {
153
                              heap.push(dis[v], v);
154
                              inque[v] = 1;
                          }
155
156
                          else
157
                              heap.update(dis[v], v);
158
                      }
                 }
159
160
         }
161
162
    int mcmf(int s, int t, int &cost)
163
         int flow = 0;
164
165
         memset(h, 0, 4 * N);
166
         for (spfa(s); pre[t] != -1; dijkstra(s))
167
      {
168
         int maxs = edge[pre[t]].flow;
```

```
169
        for (int i = pre[t]; i != -1; i = pre[edge[i ^ 1].to])
170
           maxs = min(maxs, edge[i].flow);
             for (int i = pre[t]; i != -1; i = pre[edge[i ^ 1].to])
171
             {
172
173
                 edge[i].flow -= maxs;
                 edge[i ^ 1].flow += maxs;
174
175
                 cost += edge[i].cost * maxs;
176
             }
177
        flow += maxs;
      }
178
179
        return flow;
180
    int a[1000];
181
    int main()
182
183
    {
184
        int t;
        scanf("%d", &t);
185
        for (int cas = 1; cas <= t; ++cas)
186
187
         {
188
             int n;
             scanf("%d", &n);
189
190
             init(n * 2 + 3);
191
             for (int i = 0; i < n; ++i)
192
             {
193
                 int x;
                 scanf("%d", &x);
194
195
                 a[i] = x;
                 add_edge(i * 2, i * 2 + 1, 1, -1);
196
197
                 add_{edge}(i * 2 + 1, n * 2 + 1, 1, 0);
198
                 add_{edge}(n * 2 + 2, i * 2, 1, 0);
199
             for (int i = 0; i < n; ++i)
200
                 for (int j = i + 1; j < n; ++j)
201
                     if (a[i] < a[j])
202
                          add_edge(i * 2 + 1, j * 2, 1, 0);
203
204
             add_edge(n * 2, n * 2 + 2, 2, 0);
205
             int ans = 0;
206
             mcmf(n * 2, n * 2 + 1, ans);
             printf("Case_#%d: _%d\n", cas, -ans);
207
208
        return 0;
209
210 |}
    5.4
         网络单纯形
    返回 pair(流量,费用)
  1 #include <iostream>
    #include <cstdio>
  2
    #include <cstring>
    |#include <algorithm>
  5
    using namespace std;
  6
```

```
7 \mid const int N = 1100;
   const int M = 50000*2*5+2;
 9
   struct Node
10
   {
11
     int depth,pot,id;
     Node *parent,*thread,*prev,*last;
12
13
   };
   struct Arc
14
15
   {
     int tail,head,u,c;
16
   };
17
   Arc arc[M];
18
19
   int cnt_arc;
   Node nnode[N],*rec[N];
20
   int cr;
21
   const int inf = 0x222222222;
   void dfs(Node *n)
23
24
   {
25
     cr=0;
26
     rec[cr++]=n;
     while(cr)
27
28
     {
29
        Node *nn=n->thread;
30
        nn->prev=n;
31
        n=nn;
32
        int d=n->depth;
        if(d<=rec[cr-1]->depth)
33
34
        {
35
          Node *l=rec[cr-1];
36
          while(cr&&d<=rec[cr-1]->depth)
37
38
            rec[--cr]->last=l;
          }
39
40
41
        if(cr) rec[cr++]=n;
42
     }
43
   }
44
   Node*pivot(Node*n1, Node*n2, Node*n3, Node*n4)
45
   {
46
     dfs(n1);
47
     Node *n1l=n1->last,*n3l,*n3p,*end;
     if(n1l->thread==n2)
48
49
     {
50
        n2->parent=n1;
51
        dfs(n3);
52
        return n3->last->thread;
53
     if(n1l->thread!=n3)
54
55
     {
56
        dfs(n4);
57
        n3p=n3->prev;
```

```
58
         n3l=n3->last;
 59
         n3p->thread=n3l->thread;
         if(n3l==n1l)
 60
 61
           n3l->thread=n1->thread,n1->thread=n2;
 62
         else
 63
           n3l->thread=n1l->thread,n1l->thread=n2;
       }
 64
       else
 65
 66
       {
         dfs(n3);
 67
 68
         n3l=n3->last;
 69
         n1l—>thread=n2;
 70
       }
 71
       end=n3l->thread;
       Node *n2l=n2->last,*n2lp=NULL,*p2=n1,*pp=NULL;
 72
 73
       int pid;
       int first=0;
 74
 75
       while(n2!=n3)
 76
 77
         n2l=n2—>last;
         Node *xp=pp;
 78
 79
         if(n2l!=n2lp) xp=n2l,n2lp=n2l;
 80
         pp=n2->prev;
         pp->thread=xp->thread;
 81
 82
         xp->thread=n2->parent;
 83
         Node *n2n=n2->parent;
         int ppid=n2->id;
 84
         if(first) n2->id=pid^1;
 85
 86
         pid=ppid;
 87
         first++;
 88
         n2->parent=p2;
 89
         p2=n2;
 90
         n2=n2n;
 91
 92
       if(first) n2->id=pid^1;
 93
       n2->parent=p2;
 94
       return end;
 95
 96
    void update(Node *n1,Node *n2)
 97
 98
       n1=n1->thread;
       while(n1!=n2)
 99
100
       {
         Node *n1p=n1->parent;
101
         n1->depth=n1p->depth+1;
102
         n1\rightarrow pot = n1p\rightarrow pot - arc[n1\rightarrow id].c;
103
104
         n1=n1—>thread;
       }
105
106
107
    void pivot(int id)
108 | {
```

```
109
      int tail=arc[id].tail,head=arc[id].head;
110
      int u=arc[id].u,c=arc[id].c;
      Node *uu=nnode+tail,*vv=nnode+head;
111
      Node *mu=0,*mv=0;
112
      int mn_f = u;
113
      while(uu!=vv)
114
115
      {
         int nid;
116
117
         if(uu->depth>vv->depth)
           nid=uu->id,uu=uu->parent;
118
         else nid=vv->id^1,vv=vv->parent;
119
         if(arc[nid].u<mn_f) mn_f=arc[nid].u;</pre>
120
      }
121
122
      uu=nnode+tail,vv=nnode+head;
      arc[id].u=mn_f;
123
124
      arc[id^1].u+=mn_f;
      while(uu!=vv)
125
      {
126
127
         int nid;
         if(uu->depth>vv->depth)
128
129
         {
130
           nid=uu->id;
131
           arc[nid].u=mn_f;
           arc[nid^1].u+=mn_f;
132
           if(arc[nid].u==0&&mu==0)
133
134
             mu=uu, mv=0;
           uu=uu->parent;
135
136
         }
137
         else
138
         {
           nid=vv->id^1;
139
           arc[nid].u==mn_f;
140
           arc[nid^1].u+=mn_f;
141
           if(arc[nid].u==0&&mu==0)
142
143
             mv = vv;
144
           vv=vv->parent;
         }
145
146
      if(arc[id].u)
147
148
        if(mv)
149
150
         {
           int n3=mv—nnode,n4=mv—>parent—nnode;
151
           Node *nx=pivot(nnode+tail,nnode+head,mv,mv->parent);
152
           nnode[head].id=id;
153
           update(nnode+tail,nx);
154
         }
155
         else
156
157
         {
158
           int n3=mu-nnode,n4=mu->parent-nnode;
           Node *nx=pivot(nnode+head,nnode+tail,mu,mu->parent);
159
```

```
nnode[tail].id=id^1;
160
161
           update(nnode+head,nx);
         }
162
163
      }
    }
164
165
    struct List
166
    {
167
      int ∨;
168
      List *R;
169
    };
170
    List lst[M],*cl,*hd;
    pair<int,int> cost(int s,int t,int cnt_node)
171
172
    {
173
      int tmp_arc=cnt_arc;
      int i;
174
175
      int sid=-1;
      nnode[cnt_node].depth=0;
176
      nnode[cnt_node].parent=nnode+cnt_node;
177
      nnode[cnt node].pot=0;
178
      nnode[cnt_node].thread=nnode;
179
      for(i=0; i<cnt_node; i++)</pre>
180
181
      {
182
         nnode[i].depth=1;
         nnode[i].parent=nnode+cnt_node;
183
         nnode[i].thread=nnode+(i+1);
184
         nnode[i].id=tmp_arc;
185
         int pot=-inf,u=0,tot=0;
186
         if(i==s)
187
188
           pot=-pot,tot=inf,u=inf,sid=tmp_arc+1;
189
         if(i==t) tot=inf;
190
         nnode[i].pot=pot;
         arc[tmp_arc].tail=cnt_node;
191
         arc[tmp_arc].head=i;
192
         arc[tmp_arc].u=u;
193
194
         arc[tmp_arc].c=-pot;
195
         tmp_arc++;
196
         arc[tmp_arc].tail=i;
         arc[tmp_arc].head=cnt_node;
197
         arc[tmp_arc].u=tot-u;
198
199
         arc[tmp_arc].c=pot;
200
         tmp arc++;
201
      }
      while(1)
202
203
      {
         bool fd=false;
204
         int i,tot=0;
205
206
         hd=cl=lst:
         cl->R=cl++;
207
         int tail,head,c,cc;
208
209
         const int MAXQ = cnt_node/4+5;
         const int MINQ = cnt_node/10+2;
210
```

```
211
         for(i=0; i<cnt_arc; i++)
212
         {
           if(arc[i].u==0) continue;
213
           tail=arc[i].tail;
214
           head=arc[i].head,c=arc[i].c;
215
           cc=c-nnode[tail].pot+nnode[head].pot;
216
           if(cc<0)
217
218
           {
219
              fd=true;
220
              cl->v=i;
221
              cl->R=hd->R;
222
             hd->R=cl;
223
              cl++;
224
              tot++;
225
              if(tot>=MAXQ)
226
              {
227
                while(tot>MINQ)
228
229
                  List *mj=NULL,*mjp,*it=hd->R,*itp=hd;
230
                  int mp=0;
                  while(it!=hd)
231
232
                  {
233
                    int id=it->v;
                    tail=arc[id].tail,head=arc[id].head,c=arc[id].c;
234
                    cc=c-nnode[tail].pot+nnode[head].pot;
235
236
                    if(cc>=0)
237
                    {
238
                       itp->R=it->R;
239
                       tot--;
240
                    }
                    else if(cc<mp)</pre>
241
                       mp=cc,mj=it,mjp=itp;
242
                    if(itp->R==it) itp=it;
243
                    it=it->R;
244
245
246
                  if(mj==NULL) break;
247
                  pivot(mj->v);
248
                  mjp \rightarrow R = mj \rightarrow R;
249
                  tot--;
                }
250
             }
251
           }
252
         }
253
         while(tot)
254
255
           List *it=hd->R,*itp=hd;
256
           while(it!=hd)
257
258
              int id=it->v;
259
              tail=arc[id].tail,head=arc[id].head;
260
261
              c=arc[id].c;
```

```
262
             cc=c—nnode[tail].pot+nnode[head].pot;
263
             if(cc<0) pivot(id);</pre>
             itp->R=it->R;
264
265
             tot--;
266
             it=it->R;
           }
267
268
         if(!fd) break;
269
270
      }
      int sum=0;
271
272
      for(i=0; i<cnt_arc; i+=2)
273
         sum+=arc[i].c*arc[i^1].u;
274
275
276
      return pair<int,int>(arc[sid].u,sum);
277
    void add_arc(int tail,int head,int u,int c)
278
279
280
      arc[cnt_arc].tail=tail;
281
      arc[cnt_arc].head=head;
282
      arc[cnt_arc].u=u;
283
      arc[cnt_arc].c=c;
284
      cnt_arc++;
285
    }
286
    void init()
287
288
    {
289
      cnt_arc = 0;
290
    }
291
    void add_edge(int x,int y,int cap,int cost)
292
293
294
      add_arc(x,y,cap,cost);
295
      add_arc(y,x,0,-cost);
296
    }
297
298
    int main()
299
300
      int n,m,k;
301
      while (scanf("%d%d%d",&n,&m,&k)!=EOF)
302
      {
         init();
303
         add_edge(0,1,k,0);
304
         for (int i=0;i<m;i++)</pre>
305
306
307
           int u,v,a,c;
           scanf("%d%d%d%d",&u,&v,&a,&c);
308
309
           for (int j=0;j<c;j++)
310
             add_edge(u,v,1,a*(j*2+1));
311
312
         pair<int,int> ret = cost(0,n,n+1);
```

```
313
         if (ret.first == k)
314
           printf("%d\n",ret.second);
         else
315
316
           puts("-1");
      }
317
318
      return 0;
319 | }
          匈牙利
    5.5
    5.5.1
          新版, 隐式图可解
   |bool check(int u)
  2
  3
      for (int i=head[u]; i!=-1; i=edge[i].next)
  4
      {
  5
         int v=edge[i].to;
         if (matc[v]==u) continue;
  6
  7
         if (!use[v])
  8
         {
  9
           use[v]=1;
 10
           if (matc[v]==-1 || check(matc[v]))
 11
 12
             matc[v]=u;
 13
             matc[u]=v;
             return 1;
 14
 15
           }
 16
         }
 17
 18
      return 0;
 19
    int match()
 20
 21
    {
 22
      int ret=0;
 23
      memset(matc, -1, sizeof(matc));
 24
      for (int u=0; u<N; u++)
 25
         if (matc[u]!=-1) continue;
 26
 27
         memset(use,0,sizeof(use));
         if (check(u))
 28
 29
           ret++;
 30
 31
      return ret;
 32 }
    5.5.2
          邻接矩阵
    |bool check(int u)
  2
    {
  3
      for (int v=0; v<N; v++)
  4
         if (am[u][v] && !use[v])
  5
         {
```

```
use[v]=1;
 6
 7
          if (pre[v]==-1 || check(pre[v]))
 8
 9
            pre[v]=u;
10
            return 1;
          }
11
12
13
      return 0;
14
   }
15
   int match()
16
   {
17
      int ret=0;
18
      memset(pre,-1,sizeof(pre));
      for (int u=0; u<N; u++)</pre>
19
20
      {
21
        memset(use,0,sizeof(use));
22
        if (check(u))
23
          ret++;
24
25
      return ret;
26 | }
   5.5.3
         邻接表
   |bool check(int u)
 2
 3
      for (int i=head[u]; i!=-1; i=edge[i].next)
 4
        int v=edge[i].to;
 5
 6
        if (!use[v])
 7
        {
 8
          use[v]=1;
 9
          if (pre[v]==-1 || check(pre[v]))
10
11
            pre[v]=u;
12
             return 1;
          }
13
14
        }
15
      }
16
      return 0;
17
   int match()
18
19
   {
20
      int ret=0;
21
      memset(pre,-1,sizeof(pre));
22
      for (int u=1; u<=N; u++)</pre>
23
24
        memset(use,0,sizeof(use));
25
        if (check(u))
26
          ret++;
27
      }
28
      return ret;
```

29 |}

5.6 一般图最大加权匹配

注意 G 初始化

```
1 #define N 229
   int G[N][N];
   int cnt_node;
   int dist[N];
   int rec[N],cr,M[N],P[N];
   bool vst[N];
   const int inf = 0x3f3f3f3f;
 7
   bool spfa(int u)
 9
   {
       rec[cr++]=u;
10
11
       if(vst[u]) return true;
12
       vst[u]=true;
       int ∨;
13
14
       for(v=0; v<cnt_node; v++)</pre>
15
          if(v!=u&&M[u]!=v&&!vst[v])
16
17
          {
18
            int w=M[v];
19
            if(dist[w]<dist[u]+G[u][v]-G[v][w])
20
            {
                dist[w]=dist[u]+G[u][v]-G[v][w];
21
22
                if(spfa(w))
23
                {
24
                   return true;
25
                }
26
            }
          }
27
28
       }
29
       cr--;
30
       vst[u]=false;
       return false;
31
32
   }
33
   int match()
34
35
       int i;
36
       for(i=0; i<cnt_node; i++) P[i]=i;</pre>
       for(i=0; i<cnt_node; i+=2) M[i]=i+1,M[i+1]=i;</pre>
37
       int cnt=0;
38
39
       while(1)
40
       {
41
          memset(dist,0,sizeof(dist));
          cr=0;
42
43
          int i;
44
          bool fd=false;
45
          memset(vst,0,sizeof(vst));
46
          for(i=0; i<cnt_node; i++)</pre>
```

```
47
          {
48
            if(spfa(P[i]))
49
            {
50
                fd=true;
                int j;
51
52
                int nx=M[rec[cr-1]];
53
                for(j=cr-2; rec[j]!=rec[cr-1]; j---)
54
55
                   M[nx]=rec[j];
                   int tmp=nx;
56
                   nx=M[rec[j]];
57
                   M[rec[j]]=tmp;
58
59
                }
60
               M[nx]=rec[j];
61
               M[rec[j]]=nx;
62
               break;
            }
63
64
          }
          if(!fd)
65
66
          {
67
            cnt++;
68
            if(cnt>=3) break;
69
            random_shuffle(P,P+cnt_node);
          }
70
71
72
       int sum=0;
       for(i=0; i<cnt_node; i++)</pre>
73
74
       {
75
          int ∨=M[i];
76
          if(i<v)
77
78
            sum+=G[i][v];
79
          }
80
81
       return sum;
82 |}
        一般图匹配带花树
 1 | const int MaxN = 222;
 2
   int N;
   bool Graph[MaxN+1][MaxN+1];
   int Match[MaxN+1];
 5 | bool InQueue[MaxN+1], InPath[MaxN+1], InBlossom[MaxN+1];
   int Head, Tail;
   int Queue[MaxN+1];
   int Start,Finish;
   int NewBase;
   int Father[MaxN+1],Base[MaxN+1];
10
11
   int Count;
12 void CreateGraph()
```

```
13
   {
14
     int u,v;
15
     memset(Graph, false, sizeof(Graph));
     scanf("%d",&N);
16
17
     while (scanf("%d%d",&u,&v) != EOF)
        Graph[u][v] = Graph[v][u] = true;
18
19
20
   void Push(int u)
21
   {
22
     Queue[Tail] = u;
     Tail++;
23
     InQueue[u] = true;
24
25
26
   int Pop()
27
   {
28
     int res = Queue[Head];
29
     Head++;
30
     return res;
31
   int FindCommonAncestor(int u,int v)
32
33
   {
34
     memset(InPath, false, sizeof(InPath));
35
     while (true)
36
     {
37
        u = Base[u];
        InPath[u] = true;
38
        if (u == Start) break;
39
        u = Father[Match[u]];
40
41
     }
42
     while (true)
43
44
        v = Base[v];
        if (InPath[v]) break;
45
46
        v = Father[Match[v]];
47
48
     return ∨;
49
50
   void ResetTrace(int u)
51
   {
52
     int ∨;
53
     while (Base[u] != NewBase)
54
     {
55
        v = Match[u];
56
        InBlossom[Base[u]] = InBlossom[Base[v]] = true;
57
        u = Father[v];
58
        if (Base[u] != NewBase) Father[u] = v;
     }
59
60
61
   void BlossomContract(int u,int v)
62
   {
63
     NewBase = FindCommonAncestor(u,v);
```

```
64
       memset(InBlossom, false, sizeof(InBlossom));
 65
       ResetTrace(u);
       ResetTrace(v);
 66
       if (Base[u] != NewBase) Father[u] = v;
 67
       if (Base[v] != NewBase) Father[v] = u;
 68
       for (int tu = 1; tu <= N; tu++)</pre>
 69
 70
         if (InBlossom[Base[tu]])
 71
         {
 72
           Base[tu] = NewBase;
 73
           if (!InQueue[tu]) Push(tu);
 74
 75
 76
    void FindAugmentingPath()
 77
 78
       memset(InQueue, false, sizeof(InQueue));
 79
       memset(Father, 0, sizeof(Father));
       for (int i = 1; i <= N; i++)</pre>
 80
 81
         Base[i] = i;
 82
       Head = Tail = 1;
       Push(Start);
 83
 84
       Finish = 0;
 85
       while (Head < Tail)</pre>
 86
         int u = Pop();
 87
         for (int v = 1; v <= N; v++)
 88
           if (Graph[u][v] && (Base[u] != Base[v]) && (Match[u] != v))
 89
 90
           {
             if ((v == Start) ||
 91
 92
                ((Match[v] > 0) \&\& (Father[Match[v]] > 0)))
 93
                BlossomContract(u,v);
             else if (Father[v] == 0)
 94
 95
             {
                Father[v] = u;
 96
 97
                if (Match[v] > 0)
                  Push(Match[v]);
 98
 99
               else
100
                {
101
                  Finish = v;
102
                  return;
103
               }
             }
104
           }
105
106
       }
107
108
    void AugmentPath()
109
110
       int u, v, w;
       u = Finish;
111
       while (u > 0)
112
113
114
         v = Father[u];
```

```
115
        w = Match[v];
116
        Match[v] = u;
117
        Match[u] = v;
118
        u = w;
119
      }
    }
120
121
    void Edmonds()
122
123
      memset(Match,0,sizeof(Match));
124
      for (int u = 1; u <= N; u++)
        if (Match[u] == 0)
125
        {
126
127
          Start = u;
128
          FindAugmentingPath();
129
          if (Finish > 0) AugmentPath();
        }
130
131
132
    void PrintMatch()
133
134
      for (int u = 1; u <= N; u++)
135
        if (Match[u] > 0)
136
          Count++;
      printf("%d\n",Count);
137
      for (int u = 1; u <= N; u++)
138
139
        if (u < Match[u])
140
          141
142
    int main()
143
    {
144
      CreateGraph();
145
      Edmonds();
146
      PrintMatch();
147 }
        KM
    5.8
    5.8.1 最大加权匹配
  1 | bool visx[N], visy[N]; //x, y 中的点是否被访问
   |int lx[N],ly[N];//x,y 中的点的标号
    |int matchy[N];//y 中各点匹配状态
    |int map[N][N];//二分图描述 [x][y]
    bool find(int x)
  5
  6
    {
  7
      visx[x]=true;
      int t;
  8
  9
      for (int y=0;y<ycnt;y++)</pre>
 10
 11
        if (!visy[y])
 12
        {
 13
          t=lx[x]+ly[y]-map[x][y];
 14
          if (t==0)
```

```
{
15
16
            visy[y]=true;
            if (matchy[y]==-1 || find(matchy[y]))
17
18
            {
19
               matchy[y]=x;
20
               return true;
            }
21
22
23
          else if (lack>t) lack=t;
        }
24
25
26
      return false;
27
   }
28
   void KM()
29
   {
30
      memset(lx,0,sizeof(lx));
      memset(ly,0,sizeof(ly));
31
32
      memset(matchy,-1,sizeof(matchy));
      for (int i=0;i<xcnt;i++)</pre>
33
        for (int j=0;j<ycnt;j++)</pre>
34
35
          if (map[i][j]>lx[i])
36
            lx[i]=map[i][j];
37
      for (int x=0;x<xcnt;x++)</pre>
38
      {
39
        while (true)
40
          memset(visx, false, sizeof(visx));
41
          memset(visy, false, sizeof(visy));
42
43
          lack=INFI;
44
          if (find(x)) break;
          for (int i=0;i<xcnt;i++)</pre>
45
46
          {
47
            if (visx[i]) lx[i]—=lack;
48
            if (visy[i]) ly[i]+=lack;
49
50
        }
51
      }
52
      int cost=0;
      for (int i=0;i<ycnt;i++)</pre>
53
54
        cost+=map[matchy[i]][i];
55 |}
          自认为正确的 Kuhn_Munkras
   未验证
 1 | #include < cstdio >
 2
   #include<cstring>
   #include<algorithm>
 4 using namespace std;
   const int MAXN=100;
   const int inf=0x3f3f3f3f;
 7 | bool visitx[MAXN], visity[MAXN];
```

```
int labx[MAXN],laby[MAXN],matx[MAXN],maty[MAXN],slack[MAXN];
   int ma[MAXN][MAXN];
   bool check(int x,int n)
10
11
   {
12
     visitx[x]=1;
13
     for (int i=0; i<n; i++)
        if (!visity[i])
14
          if (labx[x]+laby[i]==ma[x][i])
15
16
17
            visity[i]=1;
            if (maty[i]==-1 || check(maty[i],n))
18
19
20
              matx[x]=i;
21
              maty[i]=x;
22
              return 1;
23
            }
          }
24
25
          else
26
            slack[i]=min(slack[i],labx[x]+laby[i]-ma[x][i]);
27
28
     return 0;
29
   }
30
   void maintain(int n)
31
   {
32
     int diff=inf;
     for (int i=0; i<n; i++)</pre>
33
        if (!visity[i])
34
          diff=min(diff,slack[i]);
35
36
     for (int i=0; i<n; i++)
37
     {
        if (visitx[i])
38
39
          labx[i]—=diff;
40
        if (visity[i])
41
          laby[i]+=diff;
42
        else
43
          slack[i]—=diff;
44
     }
45
46
   int Kuhn_Munkras(int n)
47
48
     for (int i=0; i<n; i++)
49
     {
50
        labx[i]=-inf;
51
        for (int j=0; j<n; j++)
52
          labx[i]=max(labx[i],ma[i][j]);
53
     }
54
     memset(laby, 0, 4*n);
     memset(matx,-1,4*n);
55
56
     memset(maty, -1, 4*n);
57
     for (int i=0; i<n; i++)
58
     {
```

```
59
        memset(visitx,0,n);
60
        memset(visity,0,n);
        memset(slack, 63, 4*n);
61
62
        while (!check(i,n))
63
        {
64
          maintain(n);
65
          memset(visitx,0,n);
66
          memset(visity,0,n);
67
        }
68
69
     int ret=0;
70
     for (int i=0;i<n;i++)
71
        ret+=labx[i]+laby[i];
72
     return ret;
73
   }
   int main()
74
75
76
     int n,m;
77
     scanf("%d%d",&m,&n);
78
     for (int i=m; i<n; i++)
        for (int j=0; j<n; j++)</pre>
79
80
          ma[i][j]=0;
     for (int i=0; i<m; i++)</pre>
81
        for (int j=0; j<n; j++)
82
          scanf("%d",&ma[i][j]);
83
     printf("%d\n",Kuhn_Munkras(n));
84
85
     printf("%d", matx[0]+1);
     for (int i=1;i<m;i++)</pre>
86
87
        printf("⊔%d",matx[i]+1);
88
     puts("");
89
     return 0;
90 }
        * 二维平面图的最大流
   5.9
   待整理
 1 | #include < iostream>
   #include <algorithm>
   #include <cstdio>
 3
   #include <cstring>
   #include <vector>
   #include <cmath>
 6
 7
   |#include <map>
   #include <queue>
 9
   using namespace std;
10
11 | const int maxn = 100100;
   const int inf = 0x3f3f3f3f;
13
   struct Point
14 | {
```

```
15
      int x,y,id;
16
      double theta;
17
      Point() {}
18
      Point(int _x,int _y)
19
      {
20
        x = _x;
21
        y = _y;
      }
22
23
      Point(Point _s,Point _e,int _id)
24
        id = _id;
25
26
        x = _s.x-_e.x;
27
        y = _s.y-_e.y;
28
        theta = atan2(y,x);
29
      }
30
     bool operator < (const Point &b)const</pre>
31
32
        return theta < b.theta;</pre>
33
      }
   };
34
35
   map<pair<int,int>,int > idmap;
37
   struct Edge
38
   {
39
      int from, to, next, cap, near, mark;
40
   };
41
   Edge edge[maxn*2];
   int head[maxn],L;
42
   int cntd[maxn];
44
   void addedge(int u,int v,int cap)
45
46
      cntd[u]++;
47
      cntd[v]++;
48
      idmap[make_pair(u,v)] = L;
49
      edge[L].from = u;
50
      edge[L].to = v;
51
      edge[L].cap = cap;
52
      edge[L].next = head[u];
     edge[L].mark = -1;
53
54
      head[u] = L++;
55
   }
56
57
   int rtp[maxn];
   |Point p[maxn],tp[maxn];
   int n,m,S,T;
59
60
   int vid;
61
62
   struct Edge2
63
   {
64
      int to,next,dis;
65 |} edge2[maxn*2];
```

```
int head2[maxn],L2;
 66
 67
 68
    void addedge2(int u,int v,int dis)
 69
    {
 70
      edge2[L2].to = v;
 71
      edge2[L2].dis = dis;
 72
      edge2[L2].next = head2[u];
 73
      head2[u] = L2++;
 74
    }
 75
 76
    |int dist[maxn];
 77 | bool inq[maxn];
    int SPFA(int s,int t)
 78
 79
    {
 80
      queue<int> Q;
      memset(inq,false,sizeof(inq));
 81
      memset(dist,63,sizeof(dist));
 82
 83
      Q.push(s);
      dist[s] = 0;
 84
      while (!Q.empty())
 85
 86
      {
 87
         int now = Q.front();
 88
         Q.pop();
         for (int i = head2[now]; i != -1; i = edge2[i].next)
 89
 90
           if (dist[edge2[i].to] > dist[now]+edge2[i].dis)
 91
           {
 92
             dist[edge2[i].to] = dist[now]+edge2[i].dis;
             if (inq[edge2[i].to] == false)
 93
 94
             {
               inq[edge2[i].to] = true;
 95
 96
               Q.push(edge2[i].to);
 97
             }
           }
 98
 99
         inq[now] = false;
100
101
      return dist[t];
102
    }
103
    int main()
104
105
106
      int totcas;
      scanf("%d",&totcas);
107
      for (int cas = 1; cas <= totcas; cas++)</pre>
108
109
      {
         idmap.clear();
110
         L = 0;
111
         scanf("%d%d",&n,&m);
112
         S = T = 0;
113
         for (int i = 0; i < n; i++)</pre>
114
115
         {
116
           head[i] = -1;
```

```
scanf("%d%d",&p[i].x,&p[i].y);
117
118
           if (p[S].x > p[i].x)
119
             S = i;
120
           if (p[T].x < p[i].x)
121
            T = i;
          cntd[i] = 0;
122
        }
123
        //源汇中间加入一个特殊节点
124
125
        head[n] = -1;
126
        n ++;
127
        addedge(S,n-1,inf);
128
        addedge(n-1,S,inf);
129
        addedge(T, n-1, inf);
130
        addedge(n-1,T,inf);
131
132
        for (int i = 0; i < m; i++)
133
134
          int u,v,cap;
          scanf("%d%d%d",&u,&v,&cap);
135
136
137
          v--;
138
          addedge(u,v,cap);
139
          addedge(v,u,cap);
        }
140
141
        for (int i = 0; i < n; i++)
142
143
        {
144
           int tot = 0:
145
           //源点汇点连到特殊点的方向需要特别考虑一下
146
           if (i == S)
147
             tp[tot++] = Point(Point(0,0), Point(-1,0), n-1);
           else if (i == T)
148
149
             tp[tot++] = Point(Point(0,0), Point(1,0), n-1);
           else if (i == n-1)
150
151
           {
152
             tp[tot++] = Point(Point(0,0),Point(1,0),S);
153
             tp[tot++] = Point(Point(0,0), Point(-1,0), T);
154
155
          if (i < n-1)
156
             for (int j = head[i]; j != -1; j = edge[j].next)
157
158
             {
               if (i == S && edge[j].to == n-1)
159
                                                   continue;
               if (i == T && edge[j].to == n-1)
160
                                                   continue;
               tp[tot++] = Point(p[i],p[edge[j].to],edge[j].to);
161
             }
162
           }
163
164
           sort(tp,tp+tot);
165
           for (int j = 0; j < tot; j++)
166
             rtp[tp[j].id] = j;
167
           for (int j = head[i]; j != -1; j = edge[j].next)
```

```
168
             edge[j].near = tp[(rtp[edge[j].to]+1)%tot].id;
169
        }
170
        vid = 0;
171
        for (int i = 0;i < L;i++)
172
           if (edge[i].mark == -1)
173
174
           {
             int now = edge[i].from;
175
             int eid = i;
176
             int to = edge[i].to;
177
             while (true)
178
179
               edge[eid].mark = vid;
180
181
               eid ^= 1;
182
               now = to;
183
               to = edge[eid].near;
184
               eid = idmap[make_pair(now,to)];
185
186
               if (now == edge[i].from)
                                          break;
             }
187
             vid++;
188
           }
189
190
191
        L2 = 0;
192
        for (int i = 0; i < vid; i++)</pre>
           head2[i] = -1;
193
        for (int i = 0; i < L; i++)
194
           addedge2(edge[i].mark,edge[i^1].mark,edge[i].cap);
195
196
        printf("%d\n",SPFA(edge[0].mark,edge[1].mark));
197
      }
198
      return 0;
199 }
    5.10
          强联通
  1 | int dfsnum[2000];
  2
    |int low[2000];
  3
    int top;
  5
    int ans;
    int an;
  6
  7
    int be[2000];
    int flag[2000];
  9
    void dfs(int x)
 10
    {
 11
      dfsnum[x] = low[x] = ans++;
 12
      stack[++top] = x;
      flag[x] = 1;
 13
      for (int i = head[x]; i != -1; i = edge[i].next)
 14
 15
      {
 16
        int y = edge[i].to;
```

```
if (dfsnum[y] == -1)
17
18
        {
          dfs(y);
19
20
          low[x] = min(low[x], low[y]);
21
        else if (flag[y] == 1)
22
23
          low[x] = min(low[x], dfsnum[y]);
24
25
      if (dfsnum[x] == low[x])
26
      {
        while (stack[top] != x)
27
28
          flag[stack[top]] = 0;
29
          be[stack[top]] = an;
30
31
          top--;
32
        }
33
        flag[x] = 0;
        be[x] = an++;
34
35
        top--;
      }
36
37 |}
   调用:
 1 void SC()
 2
   {
 3
     memset(dfsnum,-1,sizeof(dfsnum));
      memset(flag,0,sizeof(flag));
 4
 5
      top = 0;
      an = 0;
 6
 7
      ans = 0;
      for (int i = 0;i < n;i++)
 8
        if (dfsnum[i] == -1)
 9
10
          dfs(i);
11 |}
```

5.11 最大团以及相关知识

- 独立集: 独立集是指图的顶点集的一个子集,该子集的导出子图不含边.如果一个独立集不是任何一个独立集的子集,那么称这个独立集是一个极大独立集.一个图中包含顶点数目最多的独立集称为最大独立集。最大独立集一定是极大独立集,但是极大独立集不一定是最大的独立集。
- 支配集: 与独立集相对应的就是支配集,支配集也是图顶点集的一个子集,设 S 是图 G 的一个支配集,则对于图中的任意一个顶点 u,要么属于集合 s,要么与 s 中的顶点相邻。在 s 中除去任何元素后 s 不再是支配集,则支配集 s 是极小支配集。称 s 的所有支配集中顶点个数最少的支配集为最小支配集,最小支配集中的顶点个数成为支配数。
- 最小点的覆盖: 最小点的覆盖也是图的顶点集的一个子集,如果我们选中一个点,则称这个 点将以他为端点的所有边都覆盖了。将图中所有的边都覆盖所用顶点数最少,这个集合 就是最小的点的覆盖。
- 最大团: 图 G 的顶点的子集,设 D 是最大团,则 D 中任意两点相邻。若 u,v 是最大团,则 u,v 有边相连,其补图 u,v 没有边相连,所以图 G 的最大团 = 其补图的最大独立集。

给定无向图 G = (V, E),如果 U 属于 V,并且对于任意 u,v 包含于 U 有 < u,v > 包含于 E,则称 U 是 G 的完全子图,G 的完全子图 U 是 G 的团,当且仅当 U 不包含在 G 的更大的完全子图中,G 的最大团是指 G 中所含顶点数目最多的团。如果 U 属于 V,并且对于任意 u,v 包含于 U 有 < u,v > 不包含于 E,则称 U 是 G 的空子图,G 的空子图 U 是 G 的独立集,当且仅当 U 不包含在 G 的更大的独立集,G 的最大团是指 G 中所含顶点数目最多的独立集。

一些性质: 最大独立集 + 最小覆盖集 = V,最大团 = 补图的最大独立集,最小覆盖集 = 最大匹配

```
1 |#include <cstdio>
   bool am[100][100];
   int ans;
   |int c[100];
   |int U[100][100];
   int n;
 7
   bool dfs(int rest,int num)
 8
 9
      if (!rest)
10
      {
        if (num>=ans)
11
12
          return 1;
13
        else
14
          return 0;
15
      }
      int pre=-1;
16
      for (int i=0;i<rest && rest-i+num>=ans;i++)
17
18
        int idx=U[num][i];
19
20
        if (num+c[idx]<ans)</pre>
21
          return 0;
22
        int nrest=0;
23
        for (int j=i+1; j<rest; j++)</pre>
          if (am[idx][U[num][i]])
24
            U[num+1][nrest++]=U[num][j];
25
        if (dfs(nrest,num+1))
26
27
          return 1;
28
29
      return 0;
30
31
   int main()
32
33
      while (scanf("%d",&n),n)
34
35
        for (int i=0;i<n;i++)</pre>
36
          for (int j=0; j<n; j++)
            scanf("%d",&am[i][j]);
37
38
        ans=0;
39
        for (int i=n-1; i>=0; i---)
40
        {
41
          int rest=0;
42
          for (int j=i+1; j<n; j++)
```

```
43
            if (am[i][j])
44
              U[0][rest++]=j;
45
          ans+=dfs(rest,0);
46
          c[i]=ans;
47
        }
48
        printf("%d\n",ans);
49
50
     return 0;
51 |}
   5.12
          双连通分量
   标号从 0 起
 1 | #include < cstdio >
   #include<cstring>
 3 #include<stack>
   #include<queue>
 5 | #include < algorithm >
 6 using namespace std;
   const int MAXN=100000*2;
   const int MAXM=200000;
 9
   struct edges
10
   {
11
     int to,next;
12
     bool cut, visit;
13
   } edge[MAXM<<1];</pre>
   int head[MAXN],low[MAXN],dpt[MAXN],L;
   bool visit[MAXN],cut[MAXN];
16
   void init(int n)
17
   {
18
     L=0;
19
     memset(head,-1,4*n);
20
     memset(visit,0,n);
21
   }
   void add_edge(int u,int v)
22
23
24
     edge[L].cut=edge[L].visit=0;
25
     edge[L].to=v;
     edge[L].next=head[u];
26
27
     head[u]=L++;
   }
28
29
   int idx;
30
   stack<int> st;
31
   |int bcc[MAXM];
32
   void dfs(int u,int fu,int deg)
33
   {
     cut[u]=0;
34
35
     visit[u]=1;
36
     low[u]=dpt[u]=deg;
37
     int tot=0;
38
     for (int i=head[u]; i!=-1; i=edge[i].next)
```

```
39
      {
40
        int v=edge[i].to;
41
        if (edge[i].visit)
42
          continue;
43
        st.push(i/2);
44
        edge[i].visit=edge[i^1].visit=1;
45
        if (visit[v])
46
        {
47
          low[u]=dpt[v]>low[u]?low[u]:dpt[v];
48
          continue;
49
        }
        dfs(v,u,deg+1);
50
51
        edge[i].cut=edge[i^1].cut=(low[v]>dpt[u] || edge[i].cut);
        if (u!=fu) cut[u]=low[v]>=dpt[u]?1:cut[u];
52
        if (low[v]>=dpt[u] || u==fu)
53
54
        {
          while (st.top()!=i/2)
55
56
          {
57
            int x=st.top()*2,y=st.top()*2+1;
58
            bcc[st.top()]=idx;
59
            st.pop();
60
          }
61
          bcc[i/2]=idx++;
62
          st.pop();
63
64
        low[u] = low[v] > low[u] ? low[u] : low[v];
65
        tot++;
66
67
      if (u==fu && tot>1) cut[u]=1;
68
   }
69
   int main()
70
   {
71
      int n,m;
72
      while (scanf("%d%d",&n,&m)!=EOF)
73
      {
74
        init(n);
75
        for (int i=0; i<m; i++)
76
        {
77
          int u, v;
          scanf("%d%d",&u,&v);
78
79
          add_edge(u,v);
80
          add_edge(v,u);
81
        }
82
        idx=0;
83
        for (int i=0; i<n; i++)
          if (!visit[i])
84
85
            dfs(i,i,0);
86
      return 0;
87
88
   }
```

5.13 割点与桥

```
1 | #include < cstdio >
 2
   #include<cstring>
 3 const int MAXN=10000;
 4 struct edges
 5
   {
     int to,next;
 6
     bool cut, visit;
 7
     int from;
   } edge[MAXN-1<<1];</pre>
 9
   int head[MAXN],low[MAXN],dfn[MAXN],L;
11 | bool visit[MAXN], cut[MAXN];
12
   void init(int n)
13
   {
14
     L=0;
15
     memset(head, -1, 4*n);
16
     memset(cut, 0, 4*n);
17
     memset(visit,0,4*n);
18
19
   void add_edge(int u,int v)
20
21
     edge[L].from=u;
     edge[L].cut=edge[L].visit=0;
22
     edge[L].to=v;
23
     edge[L].next=head[u];
24
25
     head[u]=L++;
26
27
   int idx;
28
   void dfs(int u,int fu)
29
30
     visit[u]=1;
     low[u]=dfn[u]=idx++;
31
32
     int tot=0;
     for (int i=head[u]; i!=-1; i=edge[i].next)
33
34
     {
35
        int v=edge[i].to;
36
        if (edge[i].visit)
37
          continue;
        edge[i].visit=edge[i^1].visit=1;
38
39
        if (visit[v])
40
41
          low[u]=dfn[v]>low[u]?low[u]:dfn[v];
42
          continue;
43
        }
        dfs(v,u);
44
45
        edge[i].cut=edge[i^1].cut=low[v]>dfn[u] || edge[i].cut;
46
        if (u!=fu) cut[u]=low[v]>=dfn[u]?1:cut[u];
47
        low[u] = low[v] > low[u] ? low[u] : low[v];
48
        tot++;
49
     }
```

```
50
      if (u==fu && tot>1) cut[u]=1;
51
   }
52
   int main()
53
   {
54
      int t;
      scanf("%d",&t);
55
      while (t---)
56
57
      {
58
        int n,m;
59
        scanf("%d%d",&n,&m);
60
        init(n);
        for (int i=0; i<m; i++)
61
62
        {
63
          int u,v;
          scanf("%d%d",&u,&v);
64
          add_edge(--u,--v);
65
66
          add_edge(v,u);
67
        }
        for (int i=0; i<n; i++)</pre>
68
          if (!visit[i])
69
          {
70
71
            idx=0;
72
            dfs(i,i);
          }
73
74
75
      return 0;
76 |}
         LCA
   5.14
   在线 LCA, bfs
 1 #include<cstdio>
   #include<cstring>
 3 | #include < queue >
   using namespace std;
   const int NSIZE = 50000;
   const int DEG = 20;
 7
   struct trees
 8
   {
 9
10
      int fa[DEG];
      int head,deg;
11
   } tree[NSIZE];
13
   struct edges
14
   {
15
      int to , next;
   } edge[NSIZE];
16
17
   struct states
18
19
      int u,fu,deg;
20
   };
21 | int L;
```

```
void add_edge(int x, int y)
23
   {
24
     edge[L].to = y;
25
     edge[L].next = tree[x].head;
26
     tree[x].head = L++;
27
28
   int Root;
29
   void BFS(int s)
30
31
     queue<states> que;
32
     states st;
33
     st.deg=0;
     st.fu=st.u=s;
34
35
     que.push(st);
36
     while(!que.empty())
37
     {
38
        states st=que.front();
39
        que.pop();
        tree[st.u].deg = st.deg;
40
41
        tree[st.u].fa[0] = st.fu;
42
        for (int i=1;i<DEG;i++)</pre>
43
          tree[st.u].fa[i]=s;
44
        for (int tmp=st.fu,num=1;tree[tmp].deg;tmp=tree[st.u].fa[num
           ++])
45
          tree[st.u].fa[num]=tree[tmp].fa[num-1];
46
        for(int i = tree[st.u].head ; <math>i != -1; i = edge[i].next)
47
        {
          int v = edge[i].to;
48
49
          if (v == st.fu) continue;
          states nst;
50
51
          nst.u=v;
52
          nst.fu=st.u;
53
          nst.deg=st.deg+1;
54
          que.push(nst);
55
        }
56
     }
57
   int LCA(int x, int y)
58
59
60
     if(tree[x].deg > tree[y].deg) swap(x,y);
61
     int hx=tree[x].deg,hy=tree[y].deg;
62
     int tx=x,ty=y;
63
     for (int det=hy-hx,i=0; det; det>>=1,i++)
64
        if (det&1)
65
          ty=tree[ty].fa[i];
     if(tx == ty) return tx;
66
67
     for (int i=DEG-1; i>=0; i---)
68
69
        if(tree[tx].fa[i] == tree[ty].fa[i])
70
          continue;
71
        tx = tree[tx].fa[i];
```

```
72
         ty = tree[ty].fa[i];
 73
 74
      return tree[tx].fa[0];
 75
 76
    int main()
 77
    {
 78
      int t;
 79
      scanf("%d",&t);
 80
      while(t---)
 81
      {
         int n;
 82
 83
         scanf("%d",&n);
 84
         L = 0;
 85
         for(int i = 0 ; i < n ; i++)
 86
           tree[i].head = -1;
 87
         for(int i = 0 ; i < n-1 ; i++)
 88
 89
           int a,b;
           scanf("%d%d",&a ,&b);
 90
 91
           add_edge(a-1,b-1);
 92
           add_edge(b-1,a-1);
 93
         }
 94
         Root=0;
 95
         BFS(Root);
 96
         int a,b;
 97
         scanf("%d%d",&a,&b);
 98
         int lca=LCA(a-1,b-1)+1;
 99
         printf("%d\n",lca);
100
      }
101
      return 0;
102 |}
           最优比例生成树
    5.15
  1 | #include < stdio.h >
    #include<string.h>
  3
    #include<math.h>
  4
    struct
  5
    {
  6
      int x,y;
  7
      double z;
    } node[1100];
  9
    struct
 10
    {
 11
      double l,c;
    } map[1100][1100];
 12
    |int n,l,f[1100],pre[1100];
    double dis[1100];
    double mst(double x)
 15
 16
    {
```

int i,j,tmp;

17

```
18
     double min,s=0,t=0;
19
     memset(f,0,sizeof(f));
20
     f[1]=1;
21
     for (i=2; i<=n; i++)
22
23
        dis[i]=map[1][i].c-map[1][i].l*x;
24
        pre[i]=1;
25
26
     for (i=1; i<n; i++)
27
     {
28
        min=1e10;
        for (j=1; j<=n; j++)
29
          if (!f[j] && min>dis[j])
30
31
32
            min=dis[j];
33
            tmp=j;
34
35
        f[tmp]=1;
36
        t+=map[pre[tmp]][tmp].l;
37
        s+=map[pre[tmp]][tmp].c;
        for (j=1; j<=n; j++)
38
39
          if (!f[j] && map[tmp][j].c-map[tmp][j].l*x<dis[j])</pre>
40
          {
41
            dis[j]=map[tmp][j].c-map[tmp][j].l*x;
42
            pre[j]=tmp;
          }
43
44
45
     return s/t;
46
   int main()
47
48
     int i,j;
49
50
     double a,b;
     scanf("%d",&n);
51
52
     while (n)
53
54
        for (i=1; i<=n; i++)
          scanf("%d%d%lf",&node[i].x,&node[i].y,&node[i].z);
55
56
        for (i=1; i<=n; i++)
57
          for (j=i+1; j<=n; j++)
58
          {
            map[j][i].l=map[i][j].l=sqrt(1.0*(node[i].x-node[j].x)*(
59
               node[i].x-node[j].x)+(node[i].y-node[j].y)*(node[i].y-
               node[j].y));
60
            map[j][i].c=map[i][j].c=fabs(node[i].z-node[j].z);
61
62
        a=0,b=mst(a);
63
        while (fabs(b-a)>1e-8)
64
        {
65
          a=b;
66
          b=mst(a);
```

```
67
       }
68
       printf("%.3f\n",b);
69
       scanf("%d",&n);
70
     }
71 |}
         生成树计数
   5.16
   根据邻接矩阵构造 Laplacian matrix。
 1 | Matrix laplacian;
 2
   laplacian.clear();
 3
   for (int i = 0;i < n;i++)
 4
     for (int j = 0; j < n; j++)
 5
     if (i != j && G[i][j])
 6
     {
 7
       laplacian.a[i][j] = -1;
 8
       laplacian.a[i][i]++;
 9
   printf("%d\n",laplacian.det(n-1));
         全局最小割
   5.17
 1 | #include < iostream>
   using namespace std;
   const int maxn=510;
   int map[maxn][maxn];
 5
   int n;
   void contract(int x,int y)
 6
 7
 8
     int i,j;
 9
     for (i=0; i<n; i++)
10
       if (i!=x) map[x][i]+=map[y][i],map[i][x]+=map[i][y];
     for (i=y+1; i<n; i++) for (j=0; j<n; j++)
11
12
       {
13
          map[i-1][j]=map[i][j];
14
         map[j][i-1]=map[j][i];
15
16
     n--;
17
18
   int w[maxn],c[maxn];
19
   int sx,tx;
20
   int mincut()
21
22
     int i,j,k,t;
23
     memset(c,0,sizeof(c));
     c[0]=1;
24
25
     for (i=0; i<n; i++) w[i]=map[0][i];</pre>
26
     for (i=1; i+1<n; i++)
27
28
       t=k=-1;
29
       for (j=0; j<n; j++) if (c[j]==0&&w[j]>k)
```

```
30
            k=w[t=j];
31
        c[sx=t]=1;
32
        for (j=0; j<n; j++) w[j]+=map[t][j];</pre>
33
34
      for (i=0; i<n; i++) if (c[i]==0) return w[tx=i];</pre>
35
36
   int main()
37
    {
38
      int i,j,k,m;
39
      while (scanf("%d%d",&n,&m)!=EOF)
40
41
        memset(map,0,sizeof(map));
42
        while (m——)
43
44
          scanf("%d%d%d",&i,&j,&k);
45
          map[i][j]+=k;
          map[j][i]+=k;
46
47
        }
48
        int mint=999999999;
        while (n>1)
49
50
        {
51
          k=mincut();
52
          if (k<mint) mint=k;</pre>
53
          contract(sx,tx);
54
55
        printf("%d\n",mint);
56
57
      return 0;
58
   }
   5.18
          欧拉路
   5.18.1 有向图
   void solve(int x)
 1
 2
   {
 3
      int i;
 4
      if (!match[x])
 5
 6
        path[++l]=x;
 7
        return ;
 8
      for (i=1; i<=n; i++)
 9
        if (b[x][i])
10
11
        {
12
          b[x][i]--;
13
          match[x]--;
14
          solve(i);
15
      path[++l]=x;
16
   }
17
```

5.18.2 无向图

```
void solve(int x)
 2
   {
 3
      int i;
 4
      if (!match[x])
 5
 6
        path[++l]=x;
 7
        return ;
 8
      }
      for (i=1; i<=n; i++)
 9
        if (b[x][i])
10
11
        {
12
          b[x][i]--;
13
          b[i][x]--;
          match[x]--;
14
15
          match[i]--;
16
          solve(i);
        }
17
18
      path[++l]=x;
19
   }
   5.18.3 混合图
   zju1992
   | int in[MAXN+100],out[MAXN+100];
 2
   int main()
 3
   {
 4
      int t;
      scanf("%d",&t);
 5
      while (t--)
 6
 7
      {
 8
        int n,m;
 9
        scanf("%d%d",&n,&m);
10
        N=n+2; L=-1;
        for (int i=0;i<N;i++)</pre>
11
12
          head[i]=-1;
13
        memset(in,0,sizeof(in));
14
        memset(out,0,sizeof(out));
15
        for (int i=0;i<m;i++)</pre>
16
17
        {
18
          int x,y,z;
          scanf("%d%d%d",&x,&y,&z);
19
20
          in[y]++;out[x]++;
21
          if (!z)
22
             add_edge(x,y,1);
        }
23
24
        int flag=1;
25
        for (int i=1;i<=n;i++)</pre>
26
        {
27
          if (in[i]—out[i]>0)
```

```
28
            add_edge(i,n+1,(in[i]-out[i])/2);
29
          else
          if (out[i]—in[i]>0)
30
31
            add_edge(0,i,(out[i]-in[i])/2);
          //printf("%d %d %d\n",i,out[i],in[i]);
32
          if ((in[i]+out[i])&1)
33
34
          {
35
            flag=0;
36
            break;
          }
37
38
        maxflow(0,n+1);
39
40
        for (int i=head[0];i!=-1;i=edge[i].next)
          if (edge[i].cap>0 && edge[i].cap>edge[i].flow)
41
42
          {
43
            flag=0;
44
            break;
45
46
        if (flag)
          puts("possible");
47
48
        else
49
          puts("impossible");
50
51
     return 0;
52 }
         K 短路
   5.19
 1 | #include < cstdio >
 2 | #include < cstring >
   #include<queue>
   using namespace std;
 5
   int K;
   class states
 6
 7
   {
   public:
 8
 9
     int cost,id;
10
   };
   int dist[1000];
11
12
   class cmp
13
   {
14
   public:
15
     bool operator ()(const states &i,const states &j)
16
17
        return i.cost>j.cost;
18
19
   };
20
   class cmp2
21
   public:
22
```

bool operator ()(const states &i,const states &j)

23

```
24
     {
25
        return i.cost+dist[i.id]>j.cost+dist[j.id];
26
27
   };
   struct edges
28
29
30
     int to,next,cost;
   } edger[100000],edge[100000];
31
   int headr[1000],head[1000],Lr,L;
   void dijkstra(int s)
33
34
   {
35
     states u;
36
     u.id=s;
37
     u.cost=0;
38
     dist[s]=0;
39
     priority_queue<states, vector<states>, cmp> q;
40
     q.push(u);
41
     while (!q.empty())
42
43
        u=q.top();
        q.pop();
44
        if (u.cost!=dist[u.id]) continue;
45
46
        for (int i=headr[u.id]; i!=-1; i=edger[i].next)
        {
47
48
          states v=u;
          v.id=edger[i].to;
49
          if (dist[v.id]>dist[u.id]+edger[i].cost)
50
51
52
            v.cost=dist[v.id]=dist[u.id]+edger[i].cost;
53
            q.push(v);
          }
54
55
        }
     }
56
57
   }
58
   int num[1000];
59
   void init(int n)
60
   {
61
     Lr=L=0;
62
     memset(head, -1, 4*n);
63
     memset(headr,-1,4*n);
64
     memset(dist,63,4*n);
65
     memset(num, 0, 4*n);
66
   }
67
   void add_edge(int u,int v,int x)
68
69
     edge[L].to=v;
70
     edge[L].cost=x;
71
     edge[L].next=head[u];
     head[u]=L++;
72
73
     edger[Lr].to=u;
74
     edger[Lr].cost=x;
```

```
75
       edger[Lr].next=headr[v];
 76
       headr[v]=Lr++;
 77
 78
    int a_star(int s,int t)
 79
 80
       if (dist[s]==0x3f3f3f3f)
 81
         return -1;
 82
       priority_queue<states, vector<states>, cmp2> q;
 83
       states tmp;
 84
       tmp.id=s;
 85
       tmp.cost=0;
       q.push(tmp);
 86
 87
       while (!q.empty())
 88
 89
         states u=q.top();
 90
         q.pop();
 91
         num[u.id]++;
 92
         if (num[t]==K)
 93
           return u.cost;
         for (int i=head[u.id]; i!=-1; i=edge[i].next)
 94
 95
         {
 96
           int v=edge[i].to;
 97
           tmp.id=v;
 98
           tmp.cost=u.cost+edge[i].cost;
 99
           q.push(tmp);
         }
100
       }
101
102
       return -1;
103
    }
104
    int main()
105
       int n,m;
106
       scanf("%d%d",&n,&m);
107
       init(n);
108
       for (int i=0; i<m; i++)
109
110
       {
111
         int u, v, x;
         scanf("%d%d%d",&u,&v,&x);
112
         add_edge(u-1,v-1,x);
113
114
       }
115
       int s,t;
       scanf("%d%d%d",&s,&t,&K);
116
       if (s==t)
117
         K++;
118
      dijkstra(t-1);
119
       printf("%d\n",a_star(s-1,t-1));
120
121 }
```

5.20 稳定婚姻

假定有 n 个男生和 个女生,理想的拍拖状态就是对于每对情侣 (a,b),找不到另一对情侣 (c,d) 使得 c 更喜欢 b,b 也更喜欢 c,同理,对 a 来说也没有 (e,f) 使得 a 更喜欢 e 而 e 更喜

欢 a_1 当然最后会有一些人落单。这样子一个状态可以称为理想拍拖状态,它也有一个专业的名词叫稳定婚姻。

求解这个问题可以用一个专有的算法,延迟认可算法,其核心就是让每个男生按自己喜欢的顺序逐个向女生表白,例如 leokan 向一个女生求爱,这个过程中,若这个女生没有男朋友,那么这个女生就暂时成为 leokan 的女朋友,或这个女生喜欢她现有男朋友的程度没有喜欢leokan 高,这个女生也暂时成为 leokan 的女朋友,而她原有的男朋友则再将就找下一个次喜欢的女生来当女朋友。

```
1 | #include < string.h >
   #include<stdio.h>
   #define N 1050
 3
   int boy[N][N];
   int girl[N][N];
   int ans[N];
   int cur[N];
 7
   int n;
   void getMarry(int g)
 9
10
11
      for (int i=ans[g]+1;i<n;i++)</pre>
12
      {
13
        int b=girl[g][i]-1;
        if (cur[b]<0)
14
15
        {
16
          ans[g]=i;
17
          cur[b]=g;
18
          return;
19
        }
20
        int og=cur[b];
        if (boy[b][og] > boy[b][g])
21
22
          cur[b]=g;
23
24
          ans[g]=i;
          getMarry(og);
25
26
          return;
27
        }
28
      }
29
   };
30
   int main()
31
   {
32
      int t,a;
33
      scanf("%d",&t);
      while(t--)
34
35
      {
        memset(girl,0,sizeof(girl));
36
37
        memset(boy,0,sizeof(boy));
        scanf("%d",&n);
38
39
        for (int i=0;i<n;i++)</pre>
40
          for (int j=0;j<n;j++)
             scanf("%d",&girl[i][j]);
41
42
        for (int i=0;i<n;i++)</pre>
43
          for (int j=0;j<n;j++)
44
          {
```

```
45
            scanf("%d",&a);
46
            boy[i][a-1]=j;
47
          }
48
        memset(cur,0xff,sizeof(cur));
49
        memset(ans,0xff,sizeof(ans));
        for (int i=0;i<n;i++)</pre>
50
51
          getMarry(i);
52
        for (int i=0;i<n;i++)
53
          printf("%d\n",girl[i][ans[i]]);
54
     }
55
     return 0;
56 |}
          最小树形图
   5.21
   const int inf = 19921005;
 2
   |int n,m,u,v,cost,dis[1001][1001],L;
 3
 4
   void init(int n)
 5
   {
 6
     L = 0;
 7
     for (int i = 0; i < n; i++)
 8
        for (int j = 0; j < n; j++)
 9
          dis[i][j] = inf;
10
   }
11
12
   struct Edge
13
14
     int u,v,cost;
15
   };
16
17
   Edge e[1001*1001];
18
19
   int pre[1001],id[1001],visit[1001],in[1001];
20
21
   int zhuliu(int root,int n,int m,Edge e[])
22
   {
23
     int res = 0,u,v;
24
     while (true)
25
        for (int i = 0; i < n; i++)
26
27
          in[i] = inf;
28
        for (int i = 0; i < m; i++)
29
          if (e[i].u != e[i].v && e[i].cost < in[e[i].v])</pre>
30
          {
            pre[e[i].v] = e[i].u;
31
32
            in[e[i].v] = e[i].cost;
          }
33
34
        for (int i = 0; i < n; i++)
35
          if (i != root)
36
            if (in[i] == inf)
                                  return -1;
```

```
37
        int tn = 0;
38
        memset(id,-1,sizeof(id));
39
        memset(visit,-1,sizeof(visit));
40
        in[root] = 0;
41
        for (int i = 0; i < n; i++)
42
43
          res += in[i];
44
          v = i;
45
          while (visit[v] != i && id[v] == -1 && v != root)
46
          {
47
            visit[v] = i;
            v = pre[v];
48
          }
49
          if(v != root \&\& id[v] == -1)
50
51
52
            for(int u = pre[v] ; u != v ; u = pre[u])
53
              id[u] = tn;
54
            id[v] = tn++;
          }
55
56
        }
57
        if(tn == 0) break;
58
        for (int i = 0; i < n; i++)
59
          if (id[i] == -1)
60
            id[i] = tn++;
61
        for (int i = 0; i < m;)
62
        {
63
          int v = e[i].v;
          e[i].u = id[e[i].u];
64
65
          e[i].v = id[e[i].v];
66
          if (e[i].u != e[i].v)
67
            e[i++].cost -= in[v];
68
          else
69
            swap(e[i],e[--m]);
70
        }
71
        n = tn;
72
        root = id[root];
73
74
     return res;
75
   }
76
77
   int main()
78
79
     freopen("in.txt","r",stdin);
80
     while (scanf("%d%d",&n,&m) != EOF)
81
82
        init(n);
83
        for (int i = 0; i < m; i++)
84
          scanf("%d%d%d",&u,&v,&cost);
85
86
          if (u == v) continue;
87
          dis[u][v] = min(dis[u][v],cost);
```

```
}
 88
         L = 0;
 89
         for (int i = 0; i < n; i++)</pre>
 90
           for (int j = 0; j < n; j++)
 91
             if (dis[i][j] != inf)
 92
 93
             {
               e[L].u = i;
 94
               e[L].v = j;
 95
               e[L++].cost = dis[i][j];
 96
 97
         printf("%d\n",zhuliu(0,n,L,e));
 98
 99
       }
      return 0;
100
101 }
```

6 计算几何

6.1 注意事项

如果用整数小心越界(多次乘法?) 如果用浮点数判断的时候一定要用 eps!

6.2 基本函数

6.2.1 Point 定义

```
struct Point
 2
   {
 3
     double x, y;
 4
     Point() {}
     Point(double _x, double _y)
 5
 6
     {
 7
        x = _x, y = _y;
 8
 9
     Point operator -(const Point &b)const
10
11
        return Point(x-b.x, y-b.y);
12
     double operator *(const Point &b)const
13
14
     {
15
        return x*b.y-y*b.x;
16
17
     double operator &(const Point &b)const
18
19
        return x*b.x+y*b.y;
20
21
     void transXY(double B)
22
23
        double tx = x, ty = y;
        x = tx*cos(B)-ty*sin(B);
24
25
        y = tx*sin(B)+ty*cos(B);
26
     }
27 | };
   6.2.2 Line 定义
   struct Line
 1
 2
   {
 3
     Point s, e;
 4
     double k;
 5
     Line() {}
 6
     Line(Point _s, Point _e)
 7
 8
        s = _s, e = _e;
 9
        k = atan2(e.y-s.y, e.x-s.x);
10
     }
```

```
Point operator &(const Line &b)const
11
12
13
       Point res = s;
       //注意: 有些题目可能会有直线相交或者重合情况
14
       //可以把返回值改成 pair<Point,int> 来返回两直线的状态。
15
       double t = ((s-b.s)*(b.s-b.e))/((s-e)*(b.s-b.e));
16
       res.x += (e.x-s.x)*t;
17
18
       res.y += (e.y-s.y)*t;
19
       return res;
20
     }
21 | };
   6.2.3 距离:点到直线距离
   result: 点到直线最近点
 1 | Point NPT(Point P, Line L)
 2
 3
     Point result;
 4
     double a, b, t;
 5
 6
     a = L.e.x-L.s.x;
 7
     b = L.e.y-L.s.y;
     t = ((P.x-L.s.x)*a+(P.y-L.s.y)*b)/(a*a+b*b);
 8
 9
10
     result.x = L.s.x+a*t;
     result.y = L.s.y+b*t;
11
12
     return dist(P, result);
13 }
   6.2.4 距离: 点到线段距离
   res: 点到线段最近点
 1 | Point NearestPointToLineSeg(Point P, Line L)
 2
   {
 3
     Point result;
 4
     double a, b, t;
 5
     a = L.e.x-L.s.x;
 6
 7
     b = L.e.y-L.s.y;
     t = ((P.x-L.s.x)*a+(P.y-L.s.y)*b)/(a*a+b*b);
 8
 9
     if (t >= 0 && t <= 1)
10
11
     {
12
       result.x = L.s.x+a*t;
13
       result.y = L.s.y+b*t;
     }
14
     else
15
16
       if (dist(P,L.s) < dist(P,L.e))</pre>
17
18
         result = L.s;
19
       else
20
         result = L.e;
```

```
21
     }
22
     return result;
23 |}
   旧版
 1 | double CalcDis(Point a,Point s,Point e) //点到线段距离
 2
 3
     if (sgn((e-s)*(a-s)) < 0 \mid | sgn((s-e)*(a-e)) < 0)
 4
       return min(dist(a,s),dist(a,e));
 5
     return abs(((s-a)*(e-a))/dist(s-e));
 6
   }
         面积:多边形
   6.2.5
   点按逆时针排序。
   |double CalcArea(Point p[], int n)
 2
 3
     double res = 0;
 4
     for (int i = 0; i < n; i++)
 5
       res += (p[i]*p[(i+1) % n])/2;
 6
     return res;
   }
 7
   6.2.6 判断: 线段相交
 1 | bool inter(Line l1,Line l2)
 2
 3
     return
 4
     max(l1.s.x, l1.e.x) >= min(l2.s.x, l2.e.x) &&
     max(l2.s.x,l2.e.x) >= min(l1.s.x,l1.e.x) &&
 5
     max(l1.s.y,l1.e.y) >= min(l2.s.y,l2.e.y) &&
 6
 7
     max(l2.s.y,l2.e.y) >= min(l1.s.y,l1.e.y) &&
     sgn((l2.s-l1.s)*(l1.e-l1.s))*sgn((l2.e-l1.s)*(l1.e-l1.s)) <= 0 \&\&
 8
     sgn((l1.s-l2.s)*(l2.e-l2.s))*sgn((l1.e-l2.s)*(l2.e-l2.s)) <= 0;
 9
10 |}
   6.2.7 判断: 点在线段上
 1 bool OnSeg(Line a, Point b)
 2
 3
     return ((a.s-b)*(a.e-b) == 0 \&\&
 4
         (b.x-a.s.x)*(b.x-a.e.x) <= 0 &&
 5
         (b.y-a.s.y)*(b.y-a.e.y) <= 0);
   }
 6
   6.2.8 判断:点在多边形内
   凸包且按逆时针排序
 1 | bool inPoly(Point a,Point p[],int n)
 2
 3
     for (int i = 0; i < n; i++)
 4
       if ((p[i]-a)*(p[(i+1)%n]-a) < 0)
```

```
5
         return false;
 6
     return true;
 7
  }
   射线法、多边形可以是凸的或凹的
   poly 的顶点数目要大于等于 3
   返回值为:
   0 - 点在 poly 内
   1 - 点在 polv 边界上
   2 - 点在 poly 外
 1 | int inPoly(Point p,Point poly[], int n)
 2
   {
 3
     int i, count;
 4
     Line ray, side;
 5
 6
     count = 0;
 7
     ray.s = p;
 8
     ray.e.y = p.y;
 9
     ray.e.x = -1;//-INF, 注意取值防止越界!
10
     for (i = 0; i < n; i++)
11
12
13
       side.s = poly[i];
14
       side.e = poly[(i+1)\%n];
15
16
       if(OnSeg(p, side))
17
         return 1;
18
19
       // 如果平行轴则不作考虑sidex
       if (side.s.y == side.e.y)
20
21
         continue;
22
23
       if (OnSeg(side.s, ray))
24
       {
25
         if (side.s.y > side.e.y) count++;
       }
26
27
       else if (OnSeg(side.e, ray))
28
29
         if (side.e.y > side.s.y) count++;
30
31
       else if (inter(ray, side))
32
       {
33
         count++;
34
       }
35
36
     return ((count % 2 == 1) ? 0 : 2);
37 |}
```

6.2.9 判断: 两凸包相交

需要考虑这几个:一个凸包的点在另外一个图包内(包括边界);一个凸包的某条边与另一个 凸包某条边相交;如果凸包可能退化成点线还需要判断点在线段上和点和点重合。

6.2.10 排序: 叉积极角排序

```
|bool cmp(const Point& a,const Point& b)
 2
   {
 3
     if (a.y*b.y <= 0)
 4
 5
       if (a.y > 0 || b.y > 0) return a.y < b.y;
 6
       if (a.y == 0 && b.y == 0) return a.x < b.x;</pre>
 7
 8
     return a*b > 0;
 9 |}
   6.3 三维几何
   6.3.1 Point 定义
 1 | struct Point3D
 2
   {
 3
     double x,y,z;
 4
     Point3D() {}
     Point3D(double _x,double _y,double _z)
 5
 6
     {
 7
       x = _x;
 8
       y = _y;
 9
       z = _z;
10
     }
11
     Point3D operator -(const Point3D& b)const
12
13
       return Point3D(x-b.x,y-b.y,z-b.z);
     }
14
     Point3D operator *(const Point3D& b)const
15
16
17
       return Point3D(y*b.z-z*b.y,z*b.x-x*b.z,x*b.y-y*b.x);
18
     }
     double operator &(const Point3D& b)const
19
20
21
       return x*b.x+y*b.y+z*b.z;
22
     }
23
   };
   //模
25
   double Norm(Point3D p)
26
27
     return sqrt(p&p);
28
   }
   //绕单位向量 V 旋转 \theta 角度
   Point3D Trans(Point3D pa,Point3D V,double theta)
30
31
     double s = sin(theta);
32
33
     double c = cos(theta);
34
     double x,y,z;
35
     x = V.x;
     y = V.y;
36
```

```
37
       z = V.z;
38
       Point3D pp =
39
       Point3D(
40
          (x*x*(1-c)+c)*pa.x+(x*y*(1-c)-z*s)*pa.y+(x*z*(1-c)+y*s)*pa.z,
41
          (y*x*(1-c)+z*s)*pa.x+(y*y*(1-c)+c)*pa.y+(y*z*(1-c)-x*s)*pa.z,
          (x*z*(1-c)-y*s)*pa.x+(y*z*(1-c)+x*s)*pa.y+(z*z*(1-c)+c)*pa.z);
42
43
       return pp;
44 }
    6.3.2 经度纬度转换
    直角坐标系与极坐标系转换:
       \begin{cases} x = r \times \sin\theta \times \cos\varphi \\ y = r \times \sin\theta \times \sin\varphi \\ z = r \times \cos\theta \end{cases} \begin{cases} r = \sqrt{x \times 2 + y \times 2 + z \times 2} \\ \varphi = \arctan(\frac{y}{x}) \\ \theta = \arccos(\frac{z}{r}) \end{cases} \qquad r \in [0, +\infty), \varphi \in [0, 2\pi], \theta \in [0, \pi] 
    经度维度转换(lat1 \in (-\frac{\pi}{2}, \frac{\pi}{2}), lng1 \in (-\pi, \pi))
 1 | Point3D getPoint3D(double lat,double lng,double r)
 2
 3
       lat += pi/2;
 4
      lng += pi;
 5
       return
         Point3D(r*sin(lat)*cos(lng),r*sin(lat)*sin(lng),r*cos(lat));
 6
 7 |}
    6.3.3 判断: 直线相交
 1 | bool LineIntersect(Line3D L1, Line3D L2)
 2
 3
       Point3D s = L1.s-L1.e;
       Point3D e = L2.s-L2.e;
 4
       Point3D p = s*e;
 5
       if (ZERO(p)) return false; //是否平行
 6
       p = (L2.s-L1.e)*(L1.s-L1.e);
 7
       return ZERO(p&L2.e); //是否共面
 8
 9 | }
    6.3.4 判断:线段相交
    需要先判断是否在一个平面上:
 1 | bool inter(Point a, Point b, Point c, Point d)
 2
    {
 3
       Point ret = (a-b)*(c-d);
       Point t1 = (b-a)*(c-a);
 4
       Point t2 = (b-a)*(d-a);
 5
 6
       Point t3 = (d-c)*(a-c);
 7
       Point t4 = (d-c)*(b-c);
       return sgn(t1&ret)*sgn(t2&ret) < 0 &&</pre>
 8
 9
                sgn(t3\&ret)*sgn(t4\&ret) < 0;
10 }
```

```
6.3.5 判断:三维向量是否为 0
  inline bool ZERO(Point3D p)
2
   {
3
     return (ZERO(p.x) && ZERO(p.y) && ZERO(p.z));
4 | }
   6.3.6 判断: 点在直线上
1 | bool OnLine(Point3D p, Line3D L)
2
3
     return ZERO((p-L.s)*(L.e-L.s));
   }
   6.3.7 判断: 点在线段上
1 | bool OnSeg(Point3D p, Line3D L)
2
3
     return (ZERO((L.s-p)*(L.e-p)) \&\&
4
       EQ(Norm(p-L.s)+Norm(p-L.e),Norm(L.e-L.s)));
5 | }
   6.3.8 距离: 点到直线
1 | double Distance(Point3D p, Line3D L)
2
3
     return (Norm((p-L.s)*(L.e-L.s))/Norm(L.e-L.s));
4 | }
   6.3.9 夹角
   返回值是 [0,\pi] 之间的弧度
1 | double Inclination(Line3D L1, Line3D L2)
2
3
     Point3D u = L1.e - L1.s;
     Point3D v = L2.e - L2.s;
5
     return acos( (u & v) / (Norm(u)*Norm(v)) );
6 |}
   6.4
        员
   6.4.1 面积:两圆相交
   圆不可包含
1 | double dis(int x,int y)
2
   {
3
     return sqrt((double)(x*x+y*y));
   double area(int x1,int y1,int x2,int y2,double r1,double r2)
6
7
     double s=dis(x2-x1,y2-y1);
     if(r1+r2<s) return 0;</pre>
8
     else if(r2-r1>s) return PI*r1*r1;
9
10
     else if(r1-r2>s) return PI*r2*r2;
```

```
double q1=acos((r1*r1+s*s-r2*r2)/(2*r1*s));
11
12
     double q2=acos((r2*r2+s*s-r1*r1)/(2*r2*s));
     return (r1*r1*q1+r2*r2*q2-r1*s*sin(q1));
13
14 | }
   6.4.2 三角形外接圆
   void CircumscribedCircle()
 2
 3
     for (int i = 0; i < 3; i++)
 4
       scanf("%lf%lf",&p[i].x,&p[i].y);
     tp = Point((p[0].x+p[1].x)/2,(p[0].y+p[1].y)/2);
 5
     l[0] = Line(tp,Point(tp.x-(p[1].y-p[0].y),tp.y+(p[1].x-p[0].x)));
 6
 7
     tp = Point((p[0].x+p[2].x)/2,(p[0].y+p[2].y)/2);
     l[1] = Line(tp, Point(tp.x-(p[2].y-p[0].y), tp.y+(p[2].x-p[0].x)));
 8
 9
     tp = LineToLine(l[0],l[1]);
     r = Point(tp,p[0]).Length();
10
     printf("(\%.6f,\%.6f,\%.6f)\n",tp.x,tp.y,r);
11
12 | }
   6.4.3 三角形内切圆
 1 | void InscribedCircle()
 2
   {
 3
     for (int i = 0; i < 3; i++)
 4
       scanf("%lf%lf",&p[i].x,&p[i].y);
 5
     if (xmult(Point(p[0],p[1]),Point(p[0],p[2])) < 0)</pre>
 6
       swap(p[1],p[2]);
 7
     for (int i = 0; i < 3; i++)
       len[i] = Point(p[i],p[(i+1)%3]).Length();
 8
     tr = (len[0] + len[1] + len[2])/2;
 9
     r = sqrt((tr-len[0])*(tr-len[1])*(tr-len[2])/tr);
10
11
     for (int i = 0; i < 2; i++)
12
13
       v = Point(p[i], p[i+1]);
       tv = Point(-v.y, v.x);
14
15
       tr = tv.Length();
16
       tv = Point(tv.x*r/tr,tv.y*r/tr);
       tp = Point(p[i].x+tv.x,p[i].y+tv.y);
17
18
       l[i].s = tp;
19
       tp = Point(p[i+1].x+tv.x,p[i+1].y+tv.y);
20
       l[i].e = tp;
     }
21
22
     tp = LineToLine(l[0], l[1]);
23
     printf("(\%.6f,\%.6f,\%.6f)\n",tp.x,tp.y,r);
24 | }
   6.4.4 点对圆的两个切点
  void calc_qie(Point poi,Point o,double r,Point &result1,Point &
      result2)
 2 | {
```

```
3
     double line = sqrt((poi.x-o.x)*(poi.x-o.x)+(poi.y-o.y)*(poi.y-o.y
        ));
     double angle = acos(r/line);
 4
     Point unitvector, lin;
 5
     lin.x = poi.x-o.x;
 6
 7
     lin.y = poi.y-o.y;
     unitvector.x = lin.x/sqrt(lin.x*lin.x+lin.y*lin.y)*r;
 8
     unitvector.y = lin.y/sqrt(lin.x*lin.x+lin.y*lin.y)*r;
 9
10
     result1 = unitvector.Rotate(-angle);
     result2 = unitvector.Rotate(angle);
11
12
     result1.x += o.x;
     result1.y += o.y;
13
     result2.x += o.x;
14
15
     result2.y += o.y;
16 | }
         两圆公切点
   6.4.5
 1 void Gao()
 2
   {
 3
     tn = 0;
     Point a,b,vab;
 4
 5
     double tab,tt,dis,theta;
     for (int i = 0; i < tc; i++)</pre>
 6
       for (int j = 0; j < tc; j++)
 7
          if (i != j)
 8
 9
10
            a = c[i];
            b = c[j];
11
            vab = Point(a,b);
12
            tab = atan2(vab.y,vab.x);
13
            dis = sqrt(vab.x*vab.x+vab.y*vab.y);
14
            if (b.r > a.r)
15
              tt = asin((b.r-a.r)/dis);
16
17
            else
              tt = -asin((a.r-b.r)/dis);
18
19
            theta = tab+pi/2+tt;
            tp[tn++] = Point(a.x+a.r*cos(theta),a.y+a.r*sin(theta));
20
            tp[tn++] = Point(b.x+b.r*cos(theta),b.y+b.r*sin(theta));
21
22
          }
23 |}
   6.4.6 两圆交点
  |lab = Point(p[j].x-p[i].x,p[j].y-p[i].y);
 2
   AB = lab.Length();
 3 | AC = cr[i];
   BC = cr[j];
 5
   |if (cmp(AB+AC,BC) <= 0) continue;//包含
 6
   if (cmp(AB+BC,AC) <= 0) continue;</pre>
 7
 8
   if (cmp(AB,AC+BC) > 0)
                             continue;//相离
 9
```

6.5 三角形相关

- 费马点: 在 $\triangle ABC$ 内求一点 P, 使 PA + PB + PC 之值为最小的点。当三角形有一个内角大于或等于 120 的时候,费马点就是该内角的顶点若没有,则费马点就是使得该点至三角形三顶点的连线两两夹角为 120 度的点.
- 等角共轭点: 对于三角形内任意一点 P, 过 A 做直线 L_1 与 AP 关于角 A 的角平分线对称, 同样过 B,C 分别做 L_2 , L_3 . 这三条直线交于 P_1 , 则 P_1 是 P 的等角共轭点. 重心的等角共轭点到三边距离的平方和最小的点.
- 6.6 矩阵
- 6.6.1 基本矩阵

按向量 (x,y,z) 平移:

$$\begin{pmatrix} 1 & 0 & 0 & x \\ 0 & 1 & 0 & y \\ 0 & 0 & 1 & z \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

按比例 (x,y,z) 缩放:

$$\begin{pmatrix} x & 0 & 0 & 0 \\ 0 & y & 0 & 0 \\ 0 & 0 & z & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

绕单位向量 (x,y,z) 旋转 angle 角度:

$$\begin{pmatrix} x^2 \times (1-c) + c & x \times y \times (1-c) - z \times s & x \times z \times (1-c) + y \times s & 0 \\ y \times x \times (1-c) + z \times s & y^2 \times (1-c) + c & y \times z \times (1-c) - x \times s & 0 \\ x \times z \times (1-c) - y \times s & y \times z \times (1-c) + x \times s & z^2 \times (1-c) + c & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{cases} s = sin(angle) \\ c = cos(angle) \end{cases}$$

以上矩阵变换都把点当作列向量,旋转角度的正负由右手定则决定

6.6.2 刘汝佳的几何教室

```
const double pi = acos(-1.0);
 2
 3
   int n,m,q;
 4
   struct Point
 5
 6
     double a,b,c,d;
   };
 7
 8
   Point p[50000],f[50000];
   double a,b,c,theta,mt[4][4],tmp[4][4],tmt[4][4],rmt[4][8];
10
11
   char com[20];
12
13
   void TRANSLATE()
14
15
     memset(tmt,0,sizeof(tmt));
16
     tmt[0][0] = tmt[1][1] = tmt[2][2] = tmt[3][3] = 1;
17
     tmt[3][0] = a;
18
     tmt[3][1] = b;
19
     tmt[3][2] = c;
     memset(tmp,0,sizeof(tmp));
20
     for (int i = 0; i < 4; i++)
21
22
       for (int j = 0; j < 4; j++)
23
          for (int k = 0; k < 4; k++)
            tmp[i][j] += mt[i][k]*tmt[k][j];
24
25
     for (int i = 0; i < 4; i++)
26
       for (int j = 0; j < 4; j++)
27
         mt[i][j] = tmp[i][j];
28
   }
29
   void ROTATE()
30
31
32
     theta = -theta*pi/180;
33
     memset(tmt,0,sizeof(tmt));
34
     tmt[3][3] = 1;
35
     tmt[0][0] = cos(theta)+(1-cos(theta))*a*a;
36
     tmt[1][0] = (1-cos(theta))*a*b+c*sin(theta);
37
     tmt[2][0] = (1-cos(theta))*a*c-b*sin(theta);
     tmt[0][1] = (1-cos(theta))*a*b-c*sin(theta);
38
39
     tmt[1][1] = cos(theta)+(1-cos(theta))*b*b;
40
     tmt[2][1] = (1-cos(theta))*b*c+a*sin(theta);
41
     tmt[0][2] = (1-cos(theta))*a*c+b*sin(theta);
42
     tmt[1][2] = (1-cos(theta))*b*c-a*sin(theta);
43
     tmt[2][2] = cos(theta)+(1-cos(theta))*c*c;
44
     memset(tmp,0,sizeof(tmp));
45
     for (int i = 0; i < 4; i++)
46
       for (int j = 0; j < 4; j++)
         for (int k = 0; k < 4; k++)
47
48
            tmp[i][j] += mt[i][k]*tmt[k][j];
     for (int i = 0; i < 4; i++)
49
50
       for (int j = 0; j < 4; j++)
51
         mt[i][j] = tmp[i][j];
```

```
52
    }
 53
 54
    void SCALE()
 55
    {
 56
      memset(tmt,0,sizeof(tmt));
 57
      tmt[0][0] = a;
 58
      tmt[1][1] = b;
 59
      tmt[2][2] = c;
 60
      tmt[3][3] = 1;
 61
      memset(tmp,0,sizeof(tmp));
 62
      for (int i = 0; i < 4; i++)
 63
        for (int j = 0; j < 4; j++)
 64
           for (int k = 0; k < 4; k++)
             tmp[i][j] += mt[i][k]*tmt[k][j];
 65
 66
      for (int i = 0; i < 4; i++)
        for (int j = 0; j < 4; j++)
 67
 68
           mt[i][j] = tmp[i][j];
 69
    }
 70
 71
    void solvep(Point p)
 72
    {
 73
      memset(tmt,0,sizeof(tmt));
 74
      tmt[0][0] = p.a;
 75
      tmt[0][1] = p.b;
 76
      tmt[0][2] = p.c;
 77
      tmt[0][3] = 1;
 78
      memset(tmp,0,sizeof(tmp));
 79
      for (int i = 0; i < 1; i++)
 80
        for (int j = 0; j < 4; j++)
 81
           for (int k = 0; k < 4; k++)
             tmp[i][j] += tmt[i][k]*mt[k][j];
 82
 83
      printf("%.2f_\%.2f\\n",tmp[0][0],tmp[0][1],tmp[0][2]);
    }
 84
 85
 86
    void solvef(Point f)
 87
 88
      memset(tmt,0,sizeof(tmt));
 89
      tmt[0][0] = f.a;
 90
      tmt[1][0] = f.b;
 91
      tmt[2][0] = f.c;
 92
      tmt[3][0] = 0;
      memset(tmp,0,sizeof(tmp));
 93
 94
      for (int i = 0; i < 4; i++)
        for (int j = 0; j < 1; j++)
 95
 96
           for (int k = 0; k < 4; k++)
             tmp[i][j] += mt[i][k]*tmt[k][j];
 97
 98
      tmp[3][0] += f.d;
 99
      double kk = tmp[0][0]*tmp[0][0]+tmp[1][0]*tmp[1][0]+tmp[2][0]*tmp
         [2][0];
100
      kk = sqrt(1/kk);
101
      for (int i = 0; i < 4; i++)
```

```
102
        103
      printf("\n");
104
    }
105
106
    void solvermt()
107
108
      memset(rmt,0,sizeof(rmt));
109
      for (int i = 0; i < 4; i++)
         for (int j = 0; j < 4; j++)
110
111
           rmt[i][j] = mt[i][j];
112
      rmt[0][4] = rmt[1][5] = rmt[2][6] = rmt[3][7] = 1;
      for (int i = 0; i < 4; i++)
113
114
      {
        for (int j = i; j < 4; j++)
115
116
           if (fabs(rmt[j][i]) > 1e-8)
117
           {
             for (int k = i; k < 8; k++)
118
119
               swap(rmt[i][k],rmt[j][k]);
120
             break;
           }
121
        double tt = rmt[i][i];
122
        for (int j = i; j < 8; j++)
123
124
           rmt[i][j] /= tt;
125
         for (int j = 0; j < 4; j++)
126
           if (i != j)
127
           {
128
             tt = rmt[j][i];
             for (int k = i; k < 8; k++)
129
130
               rmt[i][k] -= rmt[i][k]*tt;
           }
131
132
      for (int i = 0; i < 4; i++)
133
134
        for (int j = 0; j < 4; j++)
135
           mt[i][j] = rmt[i][4+j];
136
    }
137
138
    int main()
139
140
      scanf("%d%d%d",&n,&m,&q);
141
      for (int i = 0; i < n; i++)
         scanf("%lf%lf%lf",&p[i].a,&p[i].b,&p[i].c);
142
      for (int i = 0; i < m; i++)</pre>
143
144
        scanf("%lf%lf%lf%lf",&f[i].a,&f[i].b,&f[i].c,&f[i].d);
      memset(mt,0,sizeof(mt));
145
146
      mt[0][0] = mt[1][1] = mt[2][2] = mt[3][3] = 1;
147
      for (int i = 0; i < q; i++)
148
      {
        scanf("%s",com);
149
150
        if (strcmp(com,"TRANSLATE") == 0)
151
         {
           scanf("%lf%lf%lf",&a,&b,&c);
152
```

```
}
         else if (strcmp(com,"ROTATE") == 0)
155
156
         {
           scanf("%lf%lf%lf%lf",&a,&b,&c,&theta);
157
158
           ROTATE();
         }
159
         else if (strcmp(com, "SCALE") == 0)
160
161
           scanf("%lf%lf%lf",&a,&b,&c);
162
163
           SCALE();
         }
164
      }
165
      //处理点
166
167
      for (int i = 0; i < n; i++)
168
         solvep(p[i]);
      //处理面
169
      solvermt();
170
      for (int i = 0; i < m; i++)
171
172
         solvef(f[i]);
173
      return 0;
174 |}
         重心
    6.7
   |Point CenterOfPolygon(Point poly[], int n)
  2
    {
  3
      Point p, p0, p1, p2, p3;
  4
      double m, m0;
      p1 = poly[0];
  5
      p2 = poly[1];
  6
  7
      p.x = p.y = m = 0;
      for (int i = 2; i < n; i++)
  8
  9
      {
 10
         p3 = poly[i];
 11
         p0.x = (p1.x + p2.x + p3.x) / 3.0;
         p0.y = (p1.y + p2.y + p3.y) / 3.0;
 12
 13
         m0 = p1.x*p2.y+p2.x*p3.y+p3.x*p1.y-p1.y*p2.x-p2.y*p3.x-p3.y*p1.
           х;
 14
         if (cmp(m + m0, 0.0) == 0)
         m0 += eps;
 15
 16
         p.x = (m * p.x + m0 * p0.x) / (m + m0);
 17
         p.y = (m * p.y + m0 * p0.y) / (m + m0);
 18
         m = m + m0;
 19
         p2 = p3;
 20
 21
      return p;
 22 | }
```

6.8 KD 树

153

154

TRANSLATE();

查找某个点距离最近的点,基本思想是每次分治把点分成两部分,建议按照坐标规模决定是 垂直划分还是水平划分,查找时先往分到的那一部分查找,然后根据当前最优答案决定是否

去另一个区间查找。

```
1 |bool Div[MaxN];
   |void BuildKD(int deep,int l, int r, Point p[])\\记得备份一下 P
 2
 3
   {
 4
     if (l > r) return;
 5
     int mid = l + r >> 1;
 6
     int minX, minY, maxX, maxY;
 7
     minX = min_element(p + l, p + r + 1, cmpX) -> x;
     minY = min_element(p + l, p + r + 1, cmpY)->y;
 8
 9
     maxX = max\_element(p + l, p + r + 1, cmpX) -> x;
     maxY = max_element(p + l, p + r + 1, cmpY) -> y;
10
     Div[mid] = (maxX - minX >= maxY - minY);
11
     nth_element(p + l, p + mid, p + r + 1, Div[mid] ? cmpX : cmpY);
12
     BuildKD(l, mid -1, p);
13
14
     BuildKD(mid + 1, r, p);
   }
15
16
17
   long long res;
   void Find(int l, int r, Point a, Point p[])\\查找
18
19
   {
20
     if (l > r) return;
21
     int mid = l + r >> 1;
     long long dist = dist2(a, p[mid]);
22
     if (dist > 0)//如果有重点不能这样判断
23
24
       res = min(res, dist);
25
     long long d = Div[mid] ? (a.x - p[mid].x) : (a.y - p[mid].y);
26
     int l1, l2, r1, r2;
     l1 = l, l2 = mid + 1;
27
28
     r1 = mid - 1, r2 = r;
     if (d > 0)
29
       swap(l1, l2), swap(r1, r2);
30
31
     Find(l1, r1, a, p);
32
     if (d * d < res)
33
       Find(l2, r2, a, p);
34 |}
```

6.8.1 例题

查询一个点为中心的给定正方形内所有点并删除(2012 金华网赛 A)

```
#include <iostream>
#include <cstdio>
#include <cstring>
#include <algorithm>
#include <algorithm>
#include <cmath>
#include <queue>
#include <queue>
#include <algorithm>
#
```

```
11
   {
12
     int x,y,r;
13
     int id;
14
     bool del;
15
   };
16
   int cmpTyp;
17
18
   bool cmp(const Point& a,const Point& b)
19
20
     if (cmpTyp == 0)
21
        return a.x < b.x;</pre>
22
     else
23
        return a.y < b.y;</pre>
   }
24
25
26
   int cnt[MaxN];
   bool Div[MaxN];
27
   | int minX[MaxN],minY[MaxN],maxX[MaxN],maxY[MaxN];
29
   void BuildKD(int l,int r,Point p[])
30
31
     if (l > r)
                  return;
32
     int mid = l+r>>1;
33
     cmpTyp = 0;
     minX[mid] = min_element(p+l,p+r+1,cmp)->x;
34
35
     maxX[mid] = max_element(p+l,p+r+1,cmp)->x;
     cmpTyp = 1;
36
37
     minY[mid] = min_element(p+l,p+r+1,cmp)->y;
     maxY[mid] = max_element(p+l,p+r+1,cmp)->y;
38
39
40
     cnt[mid] = r-l+1;
     cmpTyp = Div[mid] = (maxX[mid]-minX[mid] < maxY[mid]-minY[mid]);</pre>
41
     nth_element(p+l,p+mid,p+r+1,cmp);
42
43
     BuildKD(l,mid-1,p);
44
     BuildKD(mid+1,r,p);
45
   }
46
47
   queue<int> Q;
   int Find(int l,int r,Point a,Point p[])
48
49
   {
50
     if (l > r) return 0;
     int mid = l+r>>1;
51
     if (cnt[mid] == 0) return 0;
52
53
54
     if (maxX[mid] < a.x—a.r ||
55
          minX[mid] > a.x+a.r ||
56
          maxY[mid] < a.y-a.r | |
57
          minY[mid] > a.y+a.r)
58
        return 0;
59
60
     int totdel = 0;
61
```

```
62
       if (p[mid].del == false)
 63
         if (abs(p[mid].x-a.x) <= a.r && abs(p[mid].y-a.y) <= a.r)
 64
 65
           p[mid].del = true;
           Q.push(p[mid].id);
 66
 67
           totdel++;
         }
 68
 69
 70
       totdel += Find(l,mid-1,a,p);
 71
       totdel += Find(mid+1,r,a,p);
 72
 73
       cnt[mid] -= totdel;
 74
 75
       return totdel;
 76
    }
 77
 78
    Point p[MaxN], tp[MaxN];
 79
    int n;
 80
 81
    int main()
 82
    {
 83
       int cas = 1;
 84
       while (true)
 85
       {
         scanf("%d",&n);
 86
 87
         if (n == 0) break;
 88
 89
         for (int i = 0; i < n; i++)
 90
         {
 91
           p[i].id = i;
 92
           int tx,ty;
           scanf("%d%d%d",&tx,&ty,&p[i].r);
 93
 94
           p[i].x = tx-ty;
 95
           p[i].y = tx+ty;
 96
           p[i].del = false;
 97
           tp[i] = p[i];
 98
         }
 99
         BuildKD(0, n-1, tp);
100
101
         printf("Case<sub>□</sub>#%d:\n",cas++);
         int q;
102
         scanf("%d",&q);
103
104
         for (int i = 0; i < q; i++)
105
         {
           int id;
106
           scanf("%d",&id);
107
           int res = 0;
108
           id--;
109
           Q.push(id);
110
111
           while (!Q.empty())
112
           {
```

```
int now = Q.front();
113
114
             Q.pop();
             if (p[now].del == true) continue;
115
             p[now].del = true;
116
             res += Find(0,n-1,p[now],tp);
117
          }
118
119
          printf("%d\n",res);
        }
120
121
122
      return 0;
123 |}
        半平面交
    6.9
    直线左边代表有效区域。
  1 bool HPIcmp(Line a, Line b)
  2
    {
  3
      if (fabs(a.k - b.k) > eps) return a.k < b.k;
      return ((a.s - b.s) * (b.e-b.s)) < 0;
    }
  5
  7
    Line Q[100];
  8
    void HPI(Line line[], int n, Point res[], int &resn)
 9
      int tot = n;
 10
 11
      sort(line, line + n, HPIcmp);
 12
      tot = 1;
      for (int i = 1; i < n; i++)
 13
        if (fabs(line[i].k - line[i - 1].k) > eps)
 14
          line[tot++] = line[i];
 15
 16
      int head = 0, tail = 1;
      Q[0] = line[0];
 17
      Q[1] = line[1];
 18
      resn = 0;
 19
20
      for (int i = 2; i < tot; i++)
 21
        if (fabs((Q[tail].e-Q[tail].s)*(Q[tail - 1].e-Q[tail - 1].s)) <</pre>
 22
23
             fabs((Q[head].e-Q[head].s)*(Q[head + 1].e-Q[head + 1].s)) < 0
                 eps)
 24
           return;
 25
        while (head < tail && (((Q[tail] \& Q[tail - 1]) - line[i].s) * (
           line[i].e-line[i].s)) > eps)
 26
           tail——;
 27
        while (head < tail && (((Q[head]&Q[head + 1]) - line[i].s) * (
           line[i].e-line[i].s)) > eps)
 28
          head++;
 29
        Q[++tail] = line[i];
 30
 31
      while (head < tail && (((Q[tail] & Q[tail - 1]) - Q[head].s) * (Q[
         head].e-Q[head].s)) > eps)
```

```
32
       tail—;
33
     while (head < tail && (((Q[head]&Q[head + 1]) - Q[tail].s) * (Q[
        tail].e-Q[tail].s)) > eps)
       head++;
34
35
     if (tail <= head + 1) return;</pre>
     for (int i = head; i < tail; i++)</pre>
36
37
       res[resn++] = Q[i] & Q[i + 1];
38
     if (head < tail + 1)
39
       res[resn++] = Q[head] & Q[tail];
40 }
   6.10 凸包
   得到的凸包按照逆时针方向排序。
  //判断是否是共点或者共线用
   bool conPoint(Point p[], int n)
 2
 3
 4
     for (int i = 1; i < n; i++)
 5
       if (p[i].x != p[0].x || p[i].y != p[0].y)
 6
          return false;
 7
     return true;
 8
9
   bool conLine(Point p[],int n)
10
11
     for (int i = 2;i < n;i++)
12
       if ((p[i]-p[0])*(p[1]-p[0]) != 0)
13
         return false;
14
     return true;
15
   }
16
17
   bool GScmp(Point a, Point b)
18
19
     if (fabs(a.x - b.x) < eps)
20
       return a.y < b.y - eps;
21
     return a.x < b.x - eps;
   }
22
23
24
   void GS(Point p[],int n,Point res[],int &resn)
25
   {
26
     resn = 0;
27
     int top = 0;
28
     sort(p,p+n,GScmp);
29
30
     if (conPoint(p,n))
31
     {
32
       res[resn++] = p[0];
33
       return;
     }
34
     if (conLine(p,n))
35
36
     {
37
       res[resn++] = p[0];
```

```
38
        res[resn++] = p[n-1];
39
        return;
40
     }
41
42
     for (int i = 0; i < n;)
        if (resn < 2 ||
43
          (res[resn-1]-res[resn-2])*(p[i]-res[resn-1]) > 0)
44
          res[resn++] = p[i++];
45
46
        else
47
         --resn;
48
     top = resn-1;
49
     for (int i = n-2; i >= 0;)
        if (resn < top+2 ||
50
          res[resn-1]-res[resn-2])*(p[i]-res[resn-1]) > 0)
51
52
          res[resn++] = p[i--];
53
        else
54
          --resn;
55
     resn--;
56 }
```

6.11 直线与凸包求交点

复杂度 $O(\log n)$ 。 需要先预处理几个东西。

```
|//二分 [la,lb] 这段区间那条边与 line 相交
   int Gao(int la,int lb,Line line)
 3
   {
     if (la > lb)
 4
 5
       lb += n;
 6
     int l = la,r = lb,mid;
 7
     while (l < r)
 8
     {
       mid = l+r+1>>1;
 9
       if (cmp((line.e-line.s)*(p[la]-line.s),0)*cmp((line.e-line.s)*(
10
          p[mid]-line.s),0) >= 0)
         l = mid;
11
12
       else
13
         r = mid-1;
14
15
     return l%n;
16
   //求 l 与凸包的交点
17
18
   //先调用 Gettheta 预处理出凸包每条边的斜率, 然后处理成升序排列
19
20
   double theta[maxn];
21
   void Gettheta()
22
23
24
     for (int i = 0; i < n; i++)
25
     {
```

```
Point v = p[(i+1)\%n]-p[i];
26
27
       theta[i] = atan2(v.y,v.x);
     }
28
     for (int i = 1; i < n; i++)
29
       if (theta[i-1] > theta[i]+eps)
30
31
         theta[i] += 2*pi;
   }
32
33
34
   double Calc(Line l)
35
36
     double tnow;
     Point v = l.e-l.s;
37
     tnow = atan2(v.y,v.x);
38
     if (cmp(tnow,theta[0]) < 0) tnow += 2*pi;</pre>
39
     int pl = lower_bound(theta,theta+n,tnow)—theta;
40
     tnow = atan2(-v.y,-v.x);
41
     if (cmp(tnow,theta[0]) < 0) tnow += 2*pi;</pre>
42
     int pr = lower_bound(theta,theta+n,tnow)—theta;
43
     //pl 和 pr 是在 l 方向上距离最远的点对
44
45
     pl = pl%n;
     pr = pr%n;
46
47
48
     if (cmp(v*(p[pl]-l.s),0)*cmp(v*(p[pr]-l.s),0) >= 0)
49
       return 0.0;
50
51
     int xa = Gao(pl,pr,l);
     int xb = Gao(pr,pl,l);
52
53
54
     if (xa > xb)
                    swap(xa,xb);
55
     //与 [xa,xa+1] 和 [xb,xb+1] 这两条线段相交
56
     if (cmp(v*(p[xa+1]-p[xa]),0) == 0)
57
                                           return 0.0;
     if (cmp(v*(p[xb+1]-p[xb]),0) == 0) return 0.0;
58
59
     Point pa,pb;
60
61
     pa = Line(p[xa], p[xa+1]) \& l;
62
     pb = Line(p[xb], p[xb+1])&l;
     //题目: 求直线切凸包得到的两部分的面积
63
64
     double area0 = sum[xb] - sum[xa+1] + (pa*p[xa+1])/2.0 + (p[xb]*pb)
        /2.0+(pb*pa)/2.0;
     double areal = sum[xa+n]-sum[xb+1]+(pb*p[xb+1])/2.0+(p[xa]*pa)
65
        /2.0+(pa*pb)/2.0;
66
67
     return min(area0, area1);
68 |}
```

6.12 点对凸包的两切点

过了 sgu500 的前七组数据,用前需谨慎,虽然我不认为这个有问题。

```
1 | double theta[MaxN];
2 | void Gettheta(Point p[],int n)
```

```
3
   {
 4
     for (int i = 0;i < n;i++)
 5
 6
        Point v = p[(i+1)\%n]-p[i];
 7
        theta[i] = atan2(v.y,v.x);
 8
     for (int i = 1; i < n; i++)
 9
        if (theta[i-1] > theta[i]+eps)
10
11
          theta[i] += 2*pi;
12
13
   int cmp(double a,double b)
14
15
     if (fabs(a-b) < eps) return 0;</pre>
     if (a < b)
16
                 return -1;
17
     return 1;
18
   int Gao(int la,int lb,Line line,Point p[],int n)
19
20
21
     if (la > lb)
22
       lb += n;
23
     int l = la,r = lb,mid;
24
     while (l < r)
25
     {
        mid = l+r+1>>1;
26
        if (cmp((line.e-line.s)*(p[la%n]-line.s),0)*cmp((line.e-line.s)
27
           *(p[mid\%n]-line.s),0) >= 0)
          l = mid;
28
29
        else
30
          r = mid-1;
31
     }
32
     return l%n;
33
   int Gao(int la,int lb,int dir,Point s,Point p[],int n)
34
35
36
     if (la > lb)
37
       lb += n;
38
     if (la == lb) return la;
39
40
     int l = la+1,r = lb,mid;
41
     while (l < r)
42
43
     {
44
       mid = l+r+1>>1;
45
        int ret = cmp((p[mid%n]-s)*(p[(mid-1)%n]-s),0);
46
47
        if (dir*ret < 0)
          l = mid;
48
49
        else if (dir*ret > 0)
          r = mid-1;
50
51
        else
52
        {
```

```
53
          if (dir == 1)
54
            l = mid;
55
          else
56
            r = mid-1;
       }
57
     }
58
59
     int ret = cmp((p[l\%n]-s)*(p[(l-1)%n]-s),0);
60
61
     if (dir*ret < 0)
        return l%n;
62
     else if (dir*ret > 0)
63
64
        return (l-1)%n;
65
     else
66
        if (dir == 1)
67
68
          return l%n;
69
        else
70
          return (l-1)%n;
71
     }
72
   }
73
   //Gettheta(p,n) first!
   //返回 S 对于 p[] 的两个切点 p[pl],p[pr]
75
   void Calc(Point s,Point p[],int n,int& pl,int& pr)
76
   {
77
     Line l = Line(s,p[0]);
     Point v = l.e-l.s;
78
     double tnow = atan2(v.y,v.x);
79
     if (tnow < theta[0]-eps)</pre>
80
                                 tnow += 2*pi;
81
     int tpl = lower_bound(theta,theta+n,tnow)—theta;
82
     tnow = atan2(-v.y,-v.x);
     if (tnow < theta[0]-eps)</pre>
83
                                 tnow += 2*pi;
     int tpr = lower_bound(theta,theta+n,tnow)—theta;
84
85
     pl = tpl = tpl%n;
86
87
     pr = tpr = tpr%n;
88
89
     int px = Gao(pr,pl,l,p,n);
90
      //printf("pr = %d \rightarrow px = %d\n",tpr,px);
91
     //printf("px = %d -> pl = %d\n",px,tpl);
92
     //pr -> px
93
     //px \rightarrow pl
94
95
     pl = Gao(tpr,px,1,s,p,n);
96
     pr = Gao(px,tpl,-1,s,p,n);
97
98 |}
```

6.13 三维凸包

暴力写法

1 | #define eps 1e-7

```
#define MAXV 505
 3
 4
   struct pt
 5
   {
 6
     double x, y, z;
 7
     pt() {}
     pt(double _x, double _y, double _z): x(_x), y(_y), z(_z) {}
 8
 9
     pt operator — (const pt p1)
10
11
        return pt(x - p1.x, y - p1.y, z - p1.z);
12
13
     pt operator * (pt p)
14
15
        return pt(y*p.z-z*p.y, z*p.x-x*p.z, x*p.y-y*p.x);
16
17
     double operator ^ (pt p)
18
19
        return x*p.x+y*p.y+z*p.z;
     }
20
21
   };
22
   struct _3DCH
23
   {
24
     struct fac
25
26
        int a, b, c;
27
        bool ok;
28
     };
29
     int n;
30
     pt P[MAXV];
31
     int cnt;
32
     fac F[MAXV*8];
     int to[MAXV][MAXV];
33
34
     double vlen(pt a)
35
     {
36
        return sqrt(a.x*a.x+a.y*a.y+a.z*a.z);
37
38
     double area(pt a, pt b, pt c)
39
40
        return vlen((b-a)*(c-a));
41
42
     double volume(pt a, pt b, pt c, pt d)
43
     {
44
        return (b-a)*(c-a)^(d-a);
45
46
     double ptof(pt &p, fac &f)
47
        pt m = P[f.b]-P[f.a], n = P[f.c]-P[f.a], t = p-P[f.a];
48
49
        return (m * n) ^ t;
50
51
     void deal(int p, int a, int b)
52
     {
```

```
53
         int f = to[a][b];
 54
         fac add;
 55
         if (F[f].ok)
 56
         {
           if (ptof(P[p], F[f]) > eps)
 57
 58
             dfs(p, f);
 59
           else
 60
           {
 61
             add.a = b, add.b = a, add.c = p, add.ok = 1;
             to[p][b] = to[a][p] = to[b][a] = cnt;
 62
             F[cnt++] = add;
 63
           }
 64
         }
 65
 66
 67
      void dfs(int p, int cur)
 68
      {
 69
         F[cur].ok = 0;
 70
         deal(p, F[cur].b, F[cur].a);
 71
         deal(p, F[cur].c, F[cur].b);
 72
         deal(p, F[cur].a, F[cur].c);
 73
      }
 74
      bool same(int s, int t)
 75
         pt a = P[F[s].a], &b = P[F[s].b], &c = P[F[s].c];
 76
 77
         return fabs(volume(a, b, c, P[F[t].a])) < eps && fabs(volume(a,
 78
             P[F[t].b]) < eps && fabs(volume(a, b, c, P[F[t].c])) < eps
 79
      }
 80
      void construct()
 81
 82
         cnt = 0;
         if (n < 4)
 83
 84
           return;
 85
         bool sb = 1;
 86
         for (int i = 1; i < n; i++)
 87
 88
           if (vlen(P[0] - P[i]) > eps)
 89
           {
 90
             swap(P[1], P[i]);
 91
             sb = 0;
 92
             break;
 93
           }
 94
         }
 95
         if (sb)return;
         sb = 1;
 96
 97
         for (int i = 2; i < n; i++)
 98
           if (Vlen((P[0] - P[1]) * (P[1] - P[i])) > eps)
 99
100
           {
101
             swap(P[2], P[i]);
```

```
102
             sb = 0;
103
             break;
104
           }
105
106
         if (sb)return;
107
         sb = 1;
         for (int i = 3; i < n; i++)</pre>
108
109
110
           if (fabs((P[0] - P[1]) * (P[1] - P[2]) ^ (P[0] - P[i])) > eps
              )
111
           {
112
             swap(P[3], P[i]);
113
             sb = 0;
114
             break;
           }
115
116
         if (sb)return;
117
118
         fac add;
         for (int i = 0; i < 4; i++)
119
120
           add.a = (i+1)\%4, add.b = (i+2)\%4, add.c = (i+3)\%4, add.ok =
121
              1;
           if (ptof(P[i], add) > 0)
122
123
             swap(add.b, add.c);
124
           to[add.a][add.b] = to[add.b][add.c] = to[add.c][add.a] = cnt;
125
           F[cnt++] = add;
         }
126
         for (int i = 4; i < n; i++)
127
128
129
           for (int j = 0; j < cnt; j++)
130
131
             if (F[j].ok && ptof(P[i], F[j]) > eps)
132
133
               dfs(i, j);
134
               break;
135
             }
           }
136
137
138
         int tmp = cnt;
139
         cnt = 0;
         for (int i = 0; i < tmp; i++)</pre>
140
141
         {
142
           if (F[i].ok)
143
           {
144
             F[cnt++] = F[i];
145
           }
         }
146
147
148
    //表面积
149
       double area()
150
       {
```

```
151
         double ret = 0.0;
152
         for (int i = 0; i < cnt; i++)
153
154
           ret += area(P[F[i].a], P[F[i].b], P[F[i].c]);
155
         }
156
         return ret / 2.0;
157
       }
    //体积
158
      double volume()
159
160
      {
161
         pt 0(0, 0, 0);
         double ret = 0.0;
162
         for (int i = 0; i < cnt; i++)
163
164
           ret += volume(0, P[F[i].a], P[F[i].b], P[F[i].c]);
165
166
         }
         return fabs(ret / 6.0);
167
168
       }
    //表面三角形数
169
170
      int facetCnt_tri()
171
      {
172
         return cnt;
173
       }
    //表面多边形数
174
175
      int facetCnt()
176
         int ans = 0;
177
         for (int i = 0; i < cnt; i++)</pre>
178
179
         {
180
           bool nb = 1;
           for (int j = 0; j < i; j++)
181
182
             if (same(i, j))
183
184
             {
185
               nb = 0;
186
               break;
187
             }
           }
188
189
           ans += nb;
190
         }
191
         return ans;
192
      }
193
194
      pt Fc[MAXV*8];
195
      double V[MAXV*8];
196
      pt Center()//重心
197
198
         pt 0(0,0,0);
199
         for (int i = 0; i < cnt; i++)
200
         {
           Fc[i].x = (0.x+P[F[i].a].x+P[F[i].b].x+P[F[i].c].x)/4.0;
201
```

```
Fc[i].y = (0.y+P[F[i].a].y+P[F[i].b].y+P[F[i].c].y)/4.0;
202
203
           Fc[i].z = (0.z+P[F[i].a].z+P[F[i].b].z+P[F[i].c].z)/4.0;
           V[i] = volume(0,P[F[i].a],P[F[i].b],P[F[i].c]);
204
         }
205
         pt res = Fc[0], tmp;
206
         double m = V[0];
207
         for (int i = 1; i < cnt; i++)
208
209
         {
210
           if (fabs(m+V[i]) < eps)</pre>
211
             V[i] += eps;
           tmp.x = (m*res.x+V[i]*Fc[i].x)/(m+V[i]);
212
           tmp.y = (m*res.y+V[i]*Fc[i].y)/(m+V[i]);
213
           tmp.z = (m*res.z+V[i]*Fc[i].z)/(m+V[i]);
214
           m += V[i];
215
216
           res = tmp;
217
         }
218
         return res;
219
      }
220
    };
221
222
    _3DCH hull;
223
224
    int main()
225
226
      while (scanf("%d",&hull.n) != EOF)
227
         for (int i = 0; i < hull.n; i++)</pre>
228
           scanf("%lf%lf%lf",&hull.P[i].x,&hull.P[i].y,&hull.P[i].z);
229
230
         hull.construct();
231
      }
232
      return 0;
233 |}
    6.14
           旋转卡壳
    "对踵"
    6.14.1 单个凸包
    void solve(Point p[],int n)
  1
  2
    {
  3
      Point v;
      int cur = 1;
  4
      for (int i = 0;i < n;i++)</pre>
  5
  6
  7
         v = p[i]-p[(i+1)%n];
  8
         while (v*(p[(cur+1)%n]-p[cur]) < 0)
  9
           cur = (cur+1)%n;
         //p[cur] -> p[i]
 10
 11
         //p[cur] -> p[i+1]
```

```
//p[cur] -> (p[i],p[i+1])
12
13
     }
14 }
   6.14.2 两个凸包
   注意初始点的选取,代码只是个示例。
   有时候答案需要取 solve(p0,n,p1,m) 和 solve(p1,m,p0,n) 的最优值。
   何老鱼说我的是错的。。
   void solve(Point p0[],int n,Point p1[],int m)
 2
   {
 3
     Point v;
     int cur = 0;
 4
 5
     for (int i = 0;i < n;i++)</pre>
 6
 7
       v = p0[i]-p0[(i+1)%n];
 8
       while (v*(p1[(cur+1)%m]-p1[cur]) < 0)
 9
          cur = (cur+1)%m;
10
       //p1[cur] -> p0[i]
       //p1[cur] -> p0[i+1]
11
12
       //p1[cur] -> (p0[i],p0[i+1])
13
     }
14 | }
   6.14.3 外接矩形
 1 void solve()
 2
   {
 3
     resa = resb = 1e100;
 4
     double dis1,dis2;
 5
     Point xp[4];
     Line l[4];
 6
 7
     int a,b,c,d;
 8
     int sa,sb,sc,sd;
 9
     a = b = c = d = 0;
10
     sa = sb = sc = sd = 0;
     Point va, vb, vc, vd;
11
12
     for (a = 0; a < n; a++)
13
14
       va = Point(p[a],p[(a+1)%n]);
15
       vc = Point(-va.x, -va.y);
16
       vb = Point(-va.y,va.x);
17
       vd = Point(-vb.x,-vb.y);
18
       if (sb < sa)
19
       {
20
          b = a;
21
          sb = sa;
22
       while (xmult(vb,Point(p[b],p[(b+1)%n])) < 0)
23
24
       {
25
          b = (b+1)\%n;
```

```
26
          sb++;
27
        }
        if (sc < sb)
28
29
        {
          c = b;
30
          sc = sb;
31
32
       while (xmult(vc,Point(p[c],p[(c+1)%n])) < 0)
33
34
35
          c = (c+1)%n;
36
          sc++;
        }
37
        if (sd < sc)
38
39
          d = c;
40
41
          sd = sc;
42
43
        while (xmult(vd,Point(p[d],p[(d+1)%n])) < 0)
44
45
          d = (d+1)%n;
46
          sd++;
47
        }
48
49
        //卡在 p[a],p[b],p[c],p[d] 上
50
        sa++;
51
     }
52 |}
         三角形内点个数
   6.15
         无三点共线
   6.15.1
 1 | Point p[1000], tp[2000], base;
 2
 3
   bool cmp(const Point &a, const Point &b)
 4
   {
 5
     return a.theta < b.theta;</pre>
   }
 6
 7
   int cnt[1000][1000];
 8
 9
   int cntleft[1000][1000];
10
   int n, m;
11
   int calc(int a, int b, int c)
12
13
   {
14
     Point p1 = p[b] - p[a], p2 = p[c] - p[a];
15
     if (atan2(p1.y, p1.x) > atan2(p2.y, p2.x))
16
        swap(b, c);
17
     if ((p[b] - p[a]) * (p[c] - p[a]) > 0)
18
        return cnt[a][c] - cnt[a][b] - 1;
19
     else
        return n - 3 - (cnt[a][c] - cnt[a][b] - 1);
20
```

```
21
         }
22
23
           int main(int argc, char const *argv[])
24
           {
25
                  int totcas;
26
                  scanf("%d", &totcas);
27
                  for (int cas = 1; cas <= totcas; ++cas)</pre>
28
29
                        scanf("%d", &n);
30
                        for (int i = 0; i < n; ++i)
31
32
                               scanf("%lld%lld", &p[i].x, &p[i].y);
33
                               p[i].id = i;
34
35
                        for (int i = 0; i < n; ++i)
36
                        {
37
                               m = 0;
38
                               base = p[i];
                                for (int j = 0; j < n; ++j)</pre>
39
                                      if (i != j)
40
41
                                      {
42
                                             tp[m] = p[j];
43
                                             Point v = tp[m]-base;
44
                                             tp[m++].theta = atan2(v.y,v.x);
45
                                      }
46
                                sort(tp, tp + m, cmp);
47
                                for (int j = 0; j < m; ++j)</pre>
48
49
                                      tp[m + j] = tp[j];
50
                                //calc cnt
51
                                for (int j = 0; j < m; ++j)
52
                                      cnt[i][tp[j].id] = j;
53
54
                               //calc cntleft
55
56
                                for (int j = 0, k = 0, tot = 0; j < m; ++j)
57
58
                                     while (k == j \mid | (k < j + m \& (tp[j] - base) * (tp[k] - base) * (tp[k
                                               base) > 0)
                                             k++, tot++;
59
                                      cntleft[i][tp[j].id] = --tot;
60
61
                               }
62
                        }
63
                        printf("Case_\%d:\n", cas);
64
65
                        int q;
                        scanf("%d", &q);
66
67
                        for (int i = 0; i < q; ++i)
68
                        {
69
                                int x, y, z;
                                scanf("%d%d%d", &x, &y, &z);
70
```

```
71
          if ((p[z] - p[x]) * (p[y] - p[x]) > 0)
72
            swap(y, z);
          int res = cntleft[x][z] + cntleft[z][y] + cntleft[y][x];
73
74
          res += calc(x, y, z) + calc(y, z, x) + calc(z, x, y);
75
          res -= 2 * (n - 3);
76
          printf("%d\n", res);
77
       }
78
     }
79
     return 0;
80
   6.15.2 有三点共线且点有类别之分
   | int n,n0,n1,m;
 2
   Point p[3000], tp[3000], base;
 3
   bool cmp(const Point &a, const Point &b)
 5
 6
     if ((a-base)*(b-base) == 0)
 7
 8
       return (a-base).getMol() < (b-base).getMol();</pre>
 9
10
     return a.theta < b.theta;</pre>
11
12
13
   int cnt[100][100];
14
   int cntleft[100][100];
15
   int calc(int a,int b,int c)
16
17
     Point p1 = p[b]-p[a],p2 = p[c]-p[a];
18
19
     if (atan2(1.0*p1.y,1.0*p1.x) > atan2(1.0*p2.y,1.0*p2.x))
20
       swap(b,c);
21
     int res = cnt[a][c]-cnt[a][b];
22
     if ((p[b]-p[a])*(p[c]-p[a]) > 0)
23
       return res;
24
     else
25
       return n1—res;
26
   }
27
28
   int main()
29
   {
30
     int cas = 0;
     while (scanf("%d%d",&n0,&n1) != EOF)
31
32
     {
33
       n = n1+n0;
34
       for (int i = 0; i < n; i++)
35
          scanf("%I64d%I64d",&p[i].x,&p[i].y);
36
37
          p[i].id = i;
       }
38
39
       for (int i = 0; i < n0; ++i)
```

```
{
40
41
                               m = 0;
42
                               base = p[i];
43
                               for (int j = 0; j < n; ++j)
44
                                      if (i != j)
45
                                      {
46
                                             tp[m] = p[j];
47
                                             Point v = tp[m]-base;
48
                                            tp[m++].theta = atan2(1.0*v.y,1.0*v.x);
                                      }
49
50
                               sort(tp, tp + m, cmp);
51
                               for (int j = 0; j < m; ++j)
52
53
                                      tp[m + j] = tp[j];
54
55
                               for (int j = 0, tot = 0; j < m; ++j)
56
57
                                      if (tp[j].id < n0)
                                            cnt[i][tp[j].id] = tot;
58
59
                                      else
60
                                            tot++;
                               }
61
62
                               for (int j = 0, k = 0, tot = 0; j < m; ++j)
63
64
                                     while (k == j \mid | (k < j + m \& (tp[j] - base) * (tp[k] - base) * (tp[k
65
                                               base) > 0)
66
67
                                             if (tp[k].id >= n0)
68
                                                   tot++;
69
                                            k++;
70
                                      if (tp[j].id >= n0)
71
72
                                            tot--;
73
                                      else
74
                                            cntleft[i][tp[j].id] = tot;
75
                               }
                        }
76
77
                        int ans = 0;
78
79
                         for (int i = 0; i < n0; i++)
                               for (int j = i+1; j < n0; j++)</pre>
80
81
                                      for (int k = j+1; k < n0; k++)
82
                                      {
83
                                             int x = i, y = j, z = k;
84
85
                                             if ((p[z] - p[x]) * (p[y] - p[x]) > 0)
86
                                                   swap(y, z);
                                             int res = cntleft[x][z] + cntleft[z][y] + cntleft[y][x];
87
88
89
                                             res += calc(x, y, z) + calc(y, z, x) + calc(z, x, y);
```

```
90
 91
               res -= 2 * n1;
 92
 93
               //printf("%d %d %d \n",x,y,z,res);
 94
 95
               if (res%2 == 1)
 96
                 ans++;
 97
 98
         printf("Case_\%d:\\\n",++cas,ans);
 99
100
      return 0;
101 |}
    6.16
           最近点对
    6.16.1 类快排算法
    double calc_dis(Point &a ,Point &b) {
  2
      return sqrt((a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y));
  3
    }
    //别忘了排序
  4
  5
    bool operator<(const Point &a ,const Point &b) {</pre>
  6
      if(a.y != b.y) return a.x < b.x;</pre>
  7
      return a.x < b.x;</pre>
  8
    }
  9
    double Gao(int l ,int r ,Point pnts[]) {
      double ret = inf;
 10
 11
      if(l == r) return ret;
      if(l+1 ==r) {
 12
 13
         ret = min(calc_dis(pnts[l],pnts[l+1]) ,ret);
 14
         return ret;
 15
      }
      if(l+2 ==r) {
 16
 17
         ret = min(calc_dis(pnts[l],pnts[l+1]) ,ret);
         ret = min(calc_dis(pnts[l],pnts[l+2]) ,ret);
 18
         ret = min(calc_dis(pnts[l+1],pnts[l+2]) ,ret);
 19
 20
         return ret;
      }
 21
 22
 23
      int mid = l+r>>1;
 24
      ret = min (ret ,Gao(l ,mid,pnts));
 25
      ret = min (ret , Gao(mid+1, r,pnts));
 26
      for(int c = l ; c<=r; c++)</pre>
 27
         for(int d = c+1; d <=c+7 && d<=r; d++) {
 28
 29
           ret = min(ret , calc_dis(pnts[c],pnts[d]));
 30
         }
 31
      return ret;
 32 | }
    6.16.2 随机增量法
```

1 | **#include** < iostream>

```
2 | #include <cstdio>
 3
   #include <cstring>
   #include <map>
   #include <vector>
 5
 6 | #include < cmath>
 7
   #include <algorithm>
   #define Point pair<double,double>
   using namespace std;
10
   const int step[9][2] =
11
      \{\{-1,-1\},\{-1,0\},\{-1,1\},\{0,-1\},\{0,0\},\{0,1\},\{1,-1\},\{1,0\},\{1,1\}\}\};
   int n,x,y,nx,ny;
12
13 |map<pair<int,int>,vector<Point > > g;
   vector<Point > tmp;
15 | Point p[20000];
16
   double tx,ty,ans,nowans;
17
   vector<Point >::iterator it,op,ed;
   pair<int,int> gird;
18
19
   bool flag;
20
21
   double Dis(Point p0,Point p1)
22
23
     return sqrt((p0.first-p1.first)*(p0.first-p1.first)+
            (p0.second-p1.second) * (p0.second-p1.second));
24
25
   }
26
27
   double CalcDis(Point p0,Point p1,Point p2)
28
29
     return Dis(p0,p1)+Dis(p0,p2)+Dis(p1,p2);
   }
30
31
   void build(int n,double w)
32
33
   {
34
     g.clear();
35
     for (int i = 0; i < n; i++)
36
        g[make_pair((int)floor(p[i].first/w),(int)floor(p[i].second/w))
           ].push_back(p[i]);
37
   }
38
   int main()
39
40
   {
41
     int t;
42
     scanf("%d",&t);
43
     for (int ft = 1;ft <= t;ft++)
44
45
        scanf("%d",&n);
        for (int i = 0; i < n; i++)
46
47
          scanf("%lf%lf",&tx,&ty);
48
49
          p[i] = make_pair(tx,ty);
50
        }
```

```
random_shuffle(p,p+n);
51
52
       ans = CalcDis(p[0], p[1], p[2]);
       build(3,ans/2.0);
53
54
       for (int i = 3;i < n;i++)
55
          x = (int)floor(2.0*p[i].first/ans);
56
          y = (int)floor(2.0*p[i].second/ans);
57
          tmp.clear();
58
59
          for (int k = 0; k < 9; k++)
60
          {
61
            nx = x+step[k][0];
            ny = y+step[k][1];
62
            gird = make_pair(nx,ny);
63
            if (g.find(gird) != g.end())
64
65
66
              op = g[gird].begin();
              ed = g[gird].end();
67
68
              for (it = op;it != ed;it++)
69
                tmp.push back(*it);
            }
70
          }
71
72
          flag = false;
          for (int j = 0;j < tmp.size();j++)</pre>
73
            for (int k = j+1;k < tmp.size();k++)
74
75
76
              nowans = CalcDis(p[i],tmp[j],tmp[k]);
77
              if (nowans < ans)</pre>
78
79
                ans = nowans;
80
                flag = true;
81
              }
82
          if (flag == true)
83
84
            build(i+1,ans/2.0);
85
          else
86
            g[make_pair((int)floor(2.0*p[i].first/ans),(int)floor(2.0*p
               [i].second/ans))].push_back(p[i]);
87
       }
88
       printf("%.3f\n",ans);
89
     }
   }
90
          多圆面积并
   6.17
          去重
   6.17.1
   有时候可能需要去掉不需要的圆
 1 | for (int i = 0; i < n; i++)
 2
 3
     scanf("%lf%lf",&c[i].c.x,&c[i].c.y,&c[i].r);
     del[i] = false;
 4
 5
   }
```

```
for (int i = 0; i < n; i++)</pre>
 7
     if (del[i] == false)
 8
 9
        if (c[i].r == 0.0) del[i] = true;
        for (int j = 0; j < n; j++)
10
          if (i != j)
11
            if (del[j] == false)
12
              if (cmp(Point(c[i].c,c[j].c).Len()+c[i].r,c[j].r) <= 0)</pre>
13
14
                del[i] = true;
15
     }
16
   tn = n;
   n = 0;
17
   for (int i = 0; i < tn; i++)
18
     if (del[i] == false)
19
20
        c[n++] = c[i];
   6.17.2 圆并
   ans[i] 表示被覆盖 i 次的面积
 1 | const double pi = acos(-1.0);
   const double eps = 1e-8;
 3
   struct Point
 4
   {
 5
     double x,y;
 6
     Point(){}
     Point(double _x,double _y)
 7
 8
        {
 9
          x = _x;
10
          y = _y;
11
        }
12
     double Length()
13
        {
14
          return sqrt(x*x+y*y);
15
        }
16
   };
17
   struct Circle
18
   {
19
     Point c;
20
     double r;
21
   };
22
   struct Event
23
   {
24
     double tim;
25
     int typ;
26
     Event(){}
     Event(double _tim,int _typ)
27
28
        {
29
          tim = _tim;
30
          typ = _typ;
31
        }
32 | };
```

```
33
34
   int cmp(const double& a,const double& b)
35
36
     if (fabs(a-b) < eps) return 0;</pre>
37
     if (a < b)
                 return -1;
38
     return 1;
   }
39
40
41
   bool Eventcmp(const Event& a,const Event& b)
42
43
     return cmp(a.tim,b.tim) < 0;</pre>
44
   }
45
46
   double Area(double theta,double r)
47
48
     return 0.5*r*r*(theta-sin(theta));
49
   }
50
51
   double xmult(Point a,Point b)
52
53
     return a.x*b.y—a.y*b.x;
54
   }
55
56
   |int n,cur,tote;
57
   Circle c[1000];
   double ans[1001],pre[1001],AB,AC,BC,theta,fai,a0,a1;
58
59
   Event e[4000];
60
   Point lab;
61
62
   int main()
63
64
     while (scanf("%d",&n) != EOF)
65
66
        for (int i = 0; i < n; i++)
67
          scanf("%lf%lf",&c[i].c.x,&c[i].c.y,&c[i].r);
68
        for (int i = 1; i <= n; i++)
69
          ans[i] = 0.0;
70
        for (int i = 0; i < n; i++)
71
        {
72
          tote = 0;
73
          e[tote++] = Event(-pi,1);
          e[tote++] = Event(pi,-1);
74
          for (int j = 0; j < n; j++)
75
76
            if (j != i)
            {
77
              lab = Point(c[j].c.x-c[i].c.x,c[j].c.y-c[i].c.y);
78
79
              AB = lab.Length();
80
              AC = c[i].r;
              BC = c[j].r;
81
82
              if (cmp(AB+AC,BC) <= 0)
83
              {
```

```
e[tote++] = Event(-pi,1);
 84
 85
                 e[tote++] = Event(pi,-1);
                 continue;
 86
 87
               }
               if (cmp(AB+BC,AC) <= 0) continue;</pre>
 88
               if (cmp(AB,AC+BC) > 0) continue;
 89
               theta = atan2(lab.y,lab.x);
 90
               fai = acos((AC*AC+AB*AB-BC*BC)/(2.0*AC*AB));
 91
 92
               a0 = theta—fai;
               if (cmp(a0,-pi) < 0) a0 += 2*pi;
 93
 94
               a1 = theta+fai;
                                     a1 -= 2*pi;
 95
               if (cmp(a1,pi) > 0)
 96
               if (cmp(a0,a1) > 0)
 97
 98
                 e[tote++] = Event(a0,1);
 99
                 e[tote++] = Event(pi,-1);
100
                 e[tote++] = Event(-pi,1);
101
                 e[tote++] = Event(a1,-1);
               }
102
               else
103
104
               {
105
                 e[tote++] = Event(a0,1);
106
                 e[tote++] = Event(a1,-1);
107
               }
             }
108
109
           sort(e,e+tote,Eventcmp);
110
           cur = 0;
           for (int j = 0; j < tote; j++)</pre>
111
112
           {
113
             if (cur != 0 && cmp(e[j].tim,pre[cur]) != 0)
114
               ans[cur] += Area(e[j].tim-pre[cur],c[i].r);
115
116
               ans[cur] += xmult(Point(c[i].c.x+c[i].r*cos(pre[cur]),c[i
                  ].c.y+c[i].r*sin(pre[cur])),
                          Point(c[i].c.x+c[i].r*cos(e[j].tim),c[i].c.y+c[
117
                             i].r*sin(e[j].tim)))/2.0;
118
             }
119
             cur += e[j].typ;
120
             pre[cur] = e[j].tim;
           }
121
122
         for (int i = 1; i < n; i++)
123
           ans[i] = ans[i+1];
124
         for (int i = 1; i <= n; i++)
125
           printf("[%d]_=_%.3f\n",i,ans[i]);
126
127
128
      return 0;
129 |}
```

6.18 一个圆与多边形面积交

```
|bool InCircle(Point a, double r)
 2
   {
 3
     return cmp(a.x*a.x+a.y*a.y,r*r) <= 0;
 4
     //这里判断的时候 EPS 一定不要太小!!
   }
 5
 6
 7
   double CalcArea(Point a,Point b,double r)
 8
9
     Point p[4];
10
     int tot = 0;
     p[tot++] = a;
11
12
13
     Point tv = Point(a,b);
     Line tmp = Line(Point(0,0),Point(tv.y,-tv.x));
14
15
     Point near = LineToLine(Line(a,b),tmp);
16
     if (cmp(near.x*near.x+near.y*near.y,r*r) <= 0)</pre>
17
18
       double A,B,C;
19
       A = near.x*near.x+near.y*near.y;
20
       C = r;
21
       B = C * C - A;
22
       double tvl = tv.x*tv.x+tv.y*tv.y;
23
       double tmp = sqrt(B/tvl); //这样做只用一次开根
24
       p[tot] = Point(near.x+tmp*tv.x,near.y+tmp*tv.y);
25
       if (OnSeg(Line(a,b),p[tot]) == true) tot++;
26
       p[tot] = Point(near.x-tmp*tv.x,near.y-tmp*tv.y);
27
       if (OnSeg(Line(a,b),p[tot]) == true) tot++;
28
29
     if (tot == 3)
30
     {
31
       if (cmp(Point(p[0],p[1]).Length(),Point(p[0],p[2]).Length()) >
          0)
32
          swap(p[1],p[2]);
33
34
     p[tot++] = b;
35
36
     double res = 0.0,theta,a0,a1,sgn;
37
     for (int i = 0; i < tot-1; i++)
38
     {
39
       if (InCircle(p[i],r) == true && InCircle(p[i+1],r) == true)
40
       {
41
          res += 0.5*xmult(p[i],p[i+1]);
42
       }
43
       else
44
45
         a0 = atan2(p[i+1].y,p[i+1].x);
46
         a1 = atan2(p[i].y,p[i].x);
47
         if (a0 < a1)
                        a0 += 2*pi;
48
         theta = a0-a1;
49
         if (cmp(theta,pi) >= 0) theta = 2*pi-theta;
50
          sgn = xmult(p[i],p[i+1])/2.0;
```

```
51
         if (cmp(sgn,0) < 0) theta = -theta;
52
         res += 0.5*r*r*theta;
       }
53
54
55
     return res;
56 }
   调用
1 | area2 = 0.0;
  |for (int i = 0;i < resn;i++) //遍历每条边,按照逆时针
     area2 += CalcArea(p[i],p[(i+1)%resn],r);
   6.19
         精度问题
```

6.19.1 浮点数为啥会有精度问题

浮点数 (以 C/C++ 为准), 一般用的较多的是 float、double。

	占字节数	数值范围	十进制精度位数
float	4	$-3.4e - 38 \sim 3.4e38$	$6 \sim 7$
double	8	$\begin{vmatrix} -3.4e - 38 \sim 3.4e38 \\ -1.7e - 308 \sim 1.7e308 \end{vmatrix}$	$14 \sim 15$

如果内存不是很紧张或者精度要求不是很低,一般选用 double。14 位的精度 (是有效数字位,不是小数点后的位数) 通常够用了。注意,问题来了,数据精度位数达到了 14 位,但有些浮点运算的结果精度并达不到这么高,可能准确的结果只有 $10 \sim 12$ 位左右。那低几位呢?自然就是不可预料的数字了。这给我们带来这样的问题:即使是理论上相同的值,由于是经过不同的运算过程得到的,他们在低几位有可能 (一般来说都是) 是不同的。这种现象看似没太大的影响,却会一种运算产生致命的影响:==。恩,就是判断相等。注意,C/C++ 中浮点数的 == 需要完全一样才能返回 true。

6.19.2 eps

eps 缩写自 epsilon,表示一个小量,但这个小量又要确保远大于浮点运算结果的不确定量。 eps 最常见的取值是 1e-8 左右。引入 eps 后,我们判断两浮点数 a、b 相等的方式如下:

1 | int sgn(double a) {return a < -eps ? -1 : a < eps ? 0 : 1;}

这样,我们才能把相差非常近的浮点数判为相等;同时把确实相差较大 (差值大于 eps) 的数判为不相等。

养成好习惯,尽量不要再对浮点数做 == 判断。

6.19.3 eps 带来的函数越界

如果 sqrt(a), asin(a), acos(a) 中的 a 是你自己算出来并传进来的,那就得小心了。 如果 a 本来应该是 0 的,由于浮点误差,可能实际是一个绝对值很小的负数(比如 -1e-12),

这样 $\operatorname{sqrt}(a)$ 应得 0 的,直接因 a 不在定义域而出错。

类似地,如果 a 本来应该是 ± 1 ,则 asin(a)、acos(a) 也有可能出错。

因此,对于此种函数,必需事先对 a 进行校正。

6.19.4 输出陷阱 I

现在考虑一种情况,题目要求输出保留两位小数。有个 case 的正确答案的精确值是 0.005, 按理应该输出 0.01, 但你的结果可能是 0.00500000001(恭喜),也有可能是 0.004999999999(悲剧),如果按照 printf("%.2lf",a) 输出,那你的遭遇将和括号里的字相同。解决办法是,如果 a 为正,则输出 a+eps,否则输出 a-eps

6.19.5 输出陷阱 II

ICPC 题目输出有个不成文的规定 (有时也成文),不要输出:-0.000 那我们首先要弄清,什么时候按 printf("%.3lf",a) 输出会出现这个结果。直接给出结果好了: $a \in (-0.000499999 \cdots, -0.000 \cdots 1)$ 所以,如果你发现 a 落在这个范围内,请直接输出 0.000。更保险的做法是用 sprintf 直接判断输出结果是不是 -0.000 再予处理。

6.19.6 范围越界

请注意,虽然 double 可以表示的数的范围很大,却不是不穷大,上面说过最大是 1e308。所以有些时候你得小心了,比如做连乘的时候,必要的时候要换成对数的和。

6.19.7 关于 set

经观察,set 不是通过 == 来判断相等的,是通过 < 来进行的,具体说来,只要 a < b 和 b < a 都不成立,就认为 a 和 b 相等,可以发现,如果将小于定义成:

1 | bool operator < (const Dat dat)const{return val < dat.val − eps;} 就可以解决问题了。(基本类型不能重载运算符,所以封装了下)

6.19.8 输入值波动过大

这种情况不常见,不过可以帮助你更熟悉 eps。假如一道题输入说,给一个浮点数 a, 1e-20 < a < 1e20。那你还敢用 1e-8 做 eps 么? 合理的做法是把 eps 按照输入规模缩放到合适大小。

6.19.9 一些建议

容易产生较大浮点误差的函数有 asin、acos。欢迎尽量使用 atan2。 另外,如果数据明确说明是整数,而且范围不大的话,使用 int 或者 long long 代替 double 都是极佳选择,因为就不存在浮点误差了

7 搜索

7.1 Dancing Links

7.1.1 估价函数

```
| int h()
 1
 2
   {
 3
      bool vis[100];
 4
      memset(vis, false, sizeof(vis));
 5
      int i,j,k,res=0,mi,col;
      while(1)
 6
 7
      {
 8
        mi=inf;
 9
        for(i=R[head]; i!=head&&i<=2*n; i=R[i])</pre>
          if(mi>nk[i]&&!vis[i])
10
11
            mi=nk[i];
12
13
            col=i;
14
          }
15
        if(mi==inf)
16
          break;
17
        res++;
        vis[col]=true;
18
19
        for(j=D[col]; j!=col; j=D[j])
          for(k=R[j]; k!=j; k=R[k])
20
21
          {
22
             if(C[k]>2*n)
23
               continue;
24
            vis[C[k]]=true;
25
          }
26
      }
27
      return res;
   }
28
   7.1.2 DLX
 1 | void remove1(int col)
 2
   {
 3
      int i,j;
      L[R[col]]=L[col];
 4
 5
      R[L[col]]=R[col];
 6
      for(i=D[col];i!=col;i=D[i])
 7
 8
        L[R[i]]=L[i];
 9
        R[L[i]]=R[i];
      }
10
11
12
   void remove2(int col)
13
   {
14
      int i,j;
15
      L[R[col]]=L[col];
```

```
16
      R[L[col]]=R[col];
17
      for(i=D[col];i!=col;i=D[i])
18
19
        for(j=R[i];j!=i;j=R[j])
20
21
          U[D[j]]=U[j];
22
          D[U[j]]=D[j];
23
          --nk[C[j]];
24
        }
      }
25
26
27
   void resume1(int col)
28
   {
29
      int i,j;
30
      for(i=U[col];i!=col;i=U[i])
31
32
        L[R[i]]=i;
33
        R[L[i]]=i;
34
      }
35
      L[R[col]]=col;
36
      R[L[col]]=col;
37
38
   void resume2(int col)
39
   {
40
      int i,j;
41
      for(i=U[col];i!=col;i=U[i])
42
43
        for(j=L[i];j!=i;j=L[j])
44
        {
45
          ++nk[C[j]];
46
          U[D[j]]=j;
47
          D[U[j]]=j;
        }
48
49
50
      L[R[col]]=col;
51
      R[L[col]]=col;
52
   }
53
   int h()
54
   {
55
      bool vis[100];
56
      memset(vis, false, sizeof(vis));
57
      int i,j,k,res=0,mi,col;
58
      while(1)
59
      {
60
        mi=inf;
61
        for(i=R[head];i!=head&&i<=2*n;i=R[i])</pre>
          if(mi>nk[i]&&!vis[i])
62
63
64
            mi=nk[i];
65
            col=i;
          }
66
```

```
67
         if(mi==inf)
 68
           break;
 69
         res++; vis[col]=true;
         for(j=D[col];j!=col;j=D[j])
 70
 71
           for(k=R[j];k!=j;k=R[k])
 72
           {
 73
              if(C[k]>2*n)
 74
                continue;
 75
             vis[C[k]]=true;
           }
 76
 77
       }
 78
       return res;
 79
 80
    bool DLX(int d,int deep)
 81
 82
       if(d+h()>deep) return false;
 83
       if(R[head] == head | | R[head] > 2*n)
 84
         return true;
 85
       if(d>=deep)
 86
         return false;
       int col,ma=inf;
 87
 88
       int i,j;
 89
       for(i=R[head];i!=head&&i<=2*n;i=R[i])</pre>
 90
         if(nk[i]<ma)
 91
         {
 92
           col=i;
 93
           ma=nk[i];
 94
 95
       remove1(col);
 96
       for(i=D[col];i!=col;i=D[i])
 97
 98
         int flag=1;
 99
         for(j=R[i];;j=R[j])
100
101
           if(j==R[i]&&!flag)
102
             break;
103
           U[D[j]]=U[j];
104
           D[U[j]]=D[j];
105
           if(C[j]>2*n)
106
              remove2(C[j]);
107
           else
              remove1(C[j]);
108
109
           flag=0;
         }
110
111
         if(DLX(d+1,deep))
112
           return true;
113
         flag=1;
114
         for(j=L[i];;j=L[j])
115
         {
           if(j==L[i]&&!flag)
116
117
              break;
```

```
if(C[j]>2*n)
118
119
             resume2(C[j]);
           else
120
             resume1(C[j]);
121
           U[D[j]]=j;
122
123
           D[U[j]]=j;
           flag=0;
124
        }
125
      }
126
      resume1(col);
127
      return false;
128
129 }
```

8 动态规划

8.1 斜率优化

```
1 | #include < cstdio >
   #include<algorithm>
 3 using namespace std;
   |int a[1000],sum[1001],dp[1000][1000];
   | int deque[1000];
   const int inf=0x7fffffff;
   int N,s,t;
 7
   |int calc(int i,int l,int j)//决策值计算
 9
10
     return dp[j][l-1]-(sum[i]-sum[j])*(sum[N]-sum[i]);
   }
11
   bool check(int i,int l)//尾端判断
12
13
     int k1=deque[t-1],k2=deque[t-2];
14
15
     return (long long)(dp[k1][l]-dp[k2][l])*(sum[i]-sum[k1])>(long
        long) (dp[i][l]-dp[k1][l])*(sum[k1]-sum[k2]);
16
   int main()
17
18
19
     int n,m;
20
     while (scanf("%d%d",&n,&m),n)
21
22
       for (int i=0; i<n; i++)
          scanf("%d",&a[i]);
23
       N=n;
24
25
       sum[0]=0;
       for (int i=0; i<n; i++)</pre>
26
27
          sum[i+1]=sum[i]+a[i];
       dp[0][0]=0;
28
29
       for (int i=0; i<n; i++)</pre>
          for (int j=i+1; j<n; j++)
30
31
            dp[0][0]+=a[i]*a[j];
32
       for (int i=1; i<n; i++)
          dp[i][0]=inf;
33
34
       for (int i=1; i<n; i++)
35
36
          dp[i][1]=inf;
37
          for (int j=0; j<i; j++)
38
            dp[i][1]=min(dp[i][1],calc(i,1,j));
39
       }
40
       for (int l=2; l<=m; l++)
41
42
          s=t=0;//双端队列清空
43
          for (int i=l; i<n; i++)
44
          {
            while (t-s>1 && check(i-1,l-1)) t--;
45
            deque[t++]=i-1;//决策加入
46
```

```
47
            while (t-s>1 && calc(i,l,deque[s])>calc(i,l,deque[s+1])) s
            dp[i][l]=calc(i,l,deque[s]);
48
          }
49
        }
50
        int ans=0x7fffffff;
51
        for (int i=m; i<n; i++)</pre>
52
53
          ans=min(ans,dp[i][m]);
54
        printf("%d\n",ans);
55
56
     return 0;
   }
57
   8.2
        RMQ 二版
   void init()
 1
 2
   {
 3
     int i,j;
 4
     int n=N,k=1,l=0;
 5
     for (i=0; i<n; i++)
 6
 7
        f[i][0]=ele[i].num;
 8
        if (i+1>k*2)
 9
        {
          k*=2;
10
11
          l++;
12
13
        lent[i+1]=l;
14
15
     for (j=1; (1<< j)-1< n; j++)
16
        for (i=0; i+(1<<j)-1<n; i++)
17
          f[i][j]=max(f[i][j-1],f[i+(1<<(j-1))][j-1]);
18
19
   int fint(int x,int y)
20
   {
21
     int k=lent[y-x+1];
22
     return max(f[x][k],f[y-(1<<k)+1][k]);
23 |}
   8.3
        二维 LIS
 1 | #include < cstdio >
   |#include<map>
   using namespace std;
   map<int,int> mp[100001];
 5
   bool check(int idx,int x,int y)
 6
 7
     if (!idx) return 1;
     if (mp[idx].begin()->first>=x) return 0;
 8
 9
     map<int,int> ::iterator it=mp[idx].lower_bound(x);
10
     it---;
     if (it->second<y) return 1;</pre>
11
```

```
12
     else return 0;
13
14
   int main()
15
   {
16
     int n;
     scanf("%d",&n);
17
     int l=0, r=0;
18
     for (int i=0;i<n;i++)</pre>
19
20
21
       int x,y;
       scanf("%d%d",&x,&y);
22
23
       int tl=l,tr=r;
       while (tl<tr)</pre>
24
25
26
          int mid=(tl+tr+1)/2;
27
          if (check(mid,x,y))
28
            tl=mid;
29
          else
30
            tr=mid-1;
       }
31
       if (tl==r) r++;
32
33
       int idx=tl+1;
       map<int,int> ::iterator itl=mp[idx].lower_bound(x),itr=itl;
34
       while (itr!=mp[idx].end() && itr->second>y) itr++;
35
36
       if (mp[idx].find(x)!=mp[idx].end())
37
          y=min(y,mp[idx][x]);
       if (itl!=itr) mp[idx].erase(itl,itr);
38
39
       if (mp[idx].find(x)==mp[idx].end() || mp[idx][x]>y)
40
         mp[idx][x]=y;
41
     printf("%d\n",r);
42
43
     return 0;
44 | }
        插头 DP
   8.4
   Tower Defence 独立插头 + 构造解
   构造解的时候保存的是在 hash map 的 ele 数组的下标位置
   没想清楚千万别去写
   |int bit[12];
 1
 2
   inline int getbit(long long sta,int pos)
 3
 4
   {
 5
     return sta/bit[pos]%bit[1];
   }
 6
 7
 8
   inline long long setbit(long long sta,int pos,int val)
 9
10
     return sta/bit[pos+1]*bit[pos+1]+val*bit[pos]+sta%bit[pos];
11
12
```

```
13 | int n,m,mp[30][10];
14
   char buf[30][10];
15
   hash_map dp[2];
16
   bool flag;
   int key,val,upd,l,u,res,msk,cov,now,pr,resnow,resmsk,pru;
17
18
   int w[15],s[15],top;
19
   int pre[210][10007],preuse[210][10007];
20
21
   void decode(int msk,int& key,int& cov)
22
   {
23
     int tmp;
24
     key = cov = 0;
25
     for (int i = 0; i < m+1; i++)</pre>
26
27
        tmp = getbit(msk,i);
28
        if (tmp > 0)
29
30
          key = setbit(key,i,tmp-1);
31
          cov = setbit(cov,i,1);
32
        }
33
      }
34
   }
35
   int encode(int key,int cov)
36
37
38
     int res = 0,tmp;
39
     for (int i = 0; i < m+1; i++)
40
41
        tmp = getbit(cov,i);
42
        if (tmp > 0)
43
44
          tmp = getbit(key,i);
45
          res = setbit(res,i,tmp+1);
46
        }
47
48
     return res;
49
   }
50
51
   void update(int a,int key,int cov,int val)
52
53
     int msk = encode(key,cov);
54
     int pos;
55
     if (dp[a][msk] < val)
56
     {
57
        dp[a][msk] = val;
        pos = dp[a].fint(msk);
58
59
        pre[now][pos] = pr;
60
        preuse[now][pos] = pru;
61
     }
62
   }
63
```

```
int count3(int sta)
 65
    {
 66
      int res = 0;
 67
      for (int i = 0; i < m+1; i++)
         if (getbit(sta,i) == 3)
 68
 69
           res++;
 70
      return res;
 71
    }
 72
 73
    void expand(int sta)
 74
 75
      top = 0;
 76
      for (int i = 0; i < m+1; i++)
 77
         if (getbit(sta,i) == 1)
 78
           s[top++] = i;
 79
         else if (getbit(sta,i) == 2)
 80
 81
           w[s[top-1]] = i;
           w[i] = s[top-1];
 82
 83
           top--;
 84
         }
 85
    }
 86
 87
    int main()
 88
 89
      //freopen("TD.in","r",stdin);
 90
       //freopen("TDM.out","w",stdout);
 91
      bit[0] = 1;
 92
      for (int i = 1; i < 12; i++) bit[i] = bit[i-1]*5;</pre>
 93
      int t;
      scanf("%d",&t);
 94
 95
      dp[0].init();
 96
      dp[1].init();
      for (int ft = 1; ft <= t; ft++)
 97
 98
      {
 99
         scanf("%d%d",&n,&m);
100
         res = 0;
         memset(mp,0,sizeof(mp));
101
         memset(pre,0,sizeof(pre));
102
103
         memset(preuse,0,sizeof(preuse));
         for (int i = 0; i < n; i++)
104
105
         {
           scanf("%s",buf[i]);
106
           for (int j = 0; j < m; j++)
107
             if (buf[i][j] == '.')
108
               mp[i][j] = 1;
109
             else if (buf[i][j] != 'B')
110
               mp[i][j] = 2;
111
112
         }
113
         dp[0].clear();
         dp[1].clear();
114
```

```
115
        flag = 0;
116
        dp[flag][0] = 0;
117
        int res = 0;
118
        now = 0;
        for (int i = 0; i < n; i++)
119
120
          for (int j = 0; j < m; j++)
121
122
          {
123
            dp[!flag].clear();
             for (int k = 0; k < dp[flag].N; k++)</pre>
124
125
               msk = dp[flag].ele[k].key;
126
127
               pr = k;
               val = dp[flag].ele[k].val;
128
129
               decode(msk,key,cov);
130
               l = getbit(key,j);
131
               u = getbit(key,j+1);
132
               if (mp[i][j] == 0)//是障碍
133
                 if (l == 0 && u == 0)
134
135
                 {
136
                   pru = 0;
137
                   update(!flag,key,setbit(setbit(cov,j,0),j+1,0),val);
138
139
               }
140
               else
141
               {
                 if (mp[i][i] == 1 && l == 0 && u == 0)//不要插头
142
143
144
                   pru = 1;
                   update(!flag,key,setbit(setbit(cov,j,0),j+1,0),val);
145
146
147
                 if (getbit(cov,j) == 1 && l == 0)
                                                      continue; / /不可以在
                    这里搞插头
148
                 if (getbit(cov,j+1) == 1 && u == 0) continue;
149
                 cov = setbit(setbit(cov,j,1),j+1,1);//更新覆盖情况
150
                 upd = setbit(setbit(key,j,0),j+1,0);
151
                 pru = 2;
                 if (mp[i][j] == 2)
152
153
                   if (l == 0 && u == 0)
154
155
                   {
156
                     if (count3(key) < 2)//可以新建独立插头
157
                     {
158
                       if (mp[i][j+1] != 0)
159
                         update(!flag,setbit(setbit(key,j,0),j+1,3),cov,
                            val+1);
                       if (mp[i+1][j] != 0)
160
161
                         update(!flag,setbit(setbit(key,j,3),j+1,0),cov,
                            val+1);
162
                     }
```

```
}
163
164
                  else if (l == 0 || u == 0)
165
                     if (l+u < 3 && count3(key) < 2)//可以用一个独立插头来
166
                       结束这条路径
                     {
167
168
                       expand(key);
169
                       if (l > 0)
170
                         update(!flag,setbit(upd,w[j],3),cov,val+1);
171
                       else
172
                         update(!flag,setbit(upd,w[j+1],3),cov,val+1);
173
                     }
                     else if (l+u == 3 && upd == 0)//路径的一端
174
175
176
                       if (res < val+1)
177
                       {
178
                         res = val+1;
179
                         resnow = now-1;
                         resmsk = k;
180
                       }
181
                     }
182
                  }
183
184
                }
                else if (l == 0 && u == 0)
185
186
                  if (mp[i][j+1] != 0 && mp[i+1][j] != 0)//可以新建插头
187
                     update(!flag,setbit(setbit(key,j,1),j+1,2),cov,val
188
                       +1);
189
                }
190
                else if (l == 0 || u == 0)
191
                  if (mp[i][j+1]!= 0)//可以延续插头
192
                     update(!flag,setbit(upd,j+1,l+u),cov,val+1);
193
                  if (mp[i+1][j] != 0)//可以延续插头
194
                     update(!flag,setbit(upd,j,l+u),cov,val+1);
195
196
                }
197
                else if (l == u)
198
                  if (l < 3) //合并两个相同的括号
199
200
201
                     expand(key);
202
                     if (l == 1)
203
                      update(!flag,setbit(upd,w[j+1],1),cov,val+1);
204
                     else
                       update(!flag,setbit(upd,w[j],2),cov,val+1);
205
206
                  }
                  else if (upd == 0)//合并两个独立插头
207
208
209
                     if (res < val+1)
210
211
                       res = val+1;
```

```
212
                        resnow = now-1;
213
                        resmsk = k;
                      }
214
215
                    }
                 }
216
                 else if (l == 3 || u == 3)//合并独立插头与括号
217
218
219
                   expand(key);
220
                   if (l == 3)
                      update(!flag,setbit(upd,w[j+1],3),cov,val+1);
221
222
                   else
223
                      update(!flag,setbit(upd,w[j],3),cov,val+1);
224
                 }
225
                 else if (l == 2 || u == 1) //合并)(
226
                   update(!flag,upd,cov,val+1);
227
               }
228
229
             flag = !flag;
230
             now++;
231
           if (i+1 == n)
232
                            break;
233
234
           dp[!flag].clear();
           for (int k = 0; k < dp[flag].N; k++)</pre>
235
236
           {
             msk = dp[flag].ele[k].key;
237
238
             pr = k;
             val = dp[flag].ele[k].val;
239
240
             pru = 0;
241
             decode(msk,key,cov);
242
             update(!flag,key*bit[1],cov*bit[1],val);
           }
243
244
           now++;
245
           flag = !flag;
246
         }
247
248
         printf("Case_wd:_wd\n",ft,res);
249
         for (int i = resnow; i >= 0; i—)
250
         {
251
           if (preuse[i][resmsk] == 1)
252
             buf[i/(m+1)][i\%(m+1)] = 'W';
253
           resmsk = pre[i][resmsk];
254
         for (int i = 0; i < n; i++)</pre>
255
256
           printf("%s\n",buf[i]);
         printf("\n");
257
258
      }
259
      return 0;
260 |}
```

9 杂物

9.1 高精度数

支持乘以整数和加法。

```
struct BigInt
 2
   {
 3
     const static int mod = 1000000000;
 4
     int a[600],len;
 5
     BigInt (){}
 6
     BigInt (int v)
 7
        len = 0;
 8
 9
        do
10
        {
          a[len++] = v mod;
11
12
          v /= mod;
13
        }while(v);
14
     BigInt operator *(const int& b) const
15
16
17
        BigInt res;
        res.len = len;
18
        for (int i = 0; i <= len; ++i)</pre>
19
20
          res.a[i] = 0;
21
        for (int i = 0; i < len; ++i)
22
          res.a[i] += a[i]*b;
23
24
          res.a[i+1] += res.a[i]/mod;
          res.a[i] %= mod;
25
        }
26
27
        if (res.a[len] > 0) res.len++;
28
        return res;
29
     }
     BigInt operator +(const BigInt& b) const
30
31
        BigInt res;
32
33
        res.len = max(len,b.len);
34
        for (int i = 0; i <= res.len; ++i)</pre>
35
          res.a[i] = 0;
        for (int i = 0; i < res.len; ++i)
36
37
38
          res.a[i] += ((i < len)?a[i]:0)+((i < b.len)?b.a[i]:0);
39
          res.a[i+1] += res.a[i]/mod;
40
          res.a[i] %= mod;
41
        }
42
        if (res.a[res.len] > 0) res.len++;
43
        return res;
44
45
     void output()
```

```
46
     {
47
       printf("%d",a[len-1]);
       for (int i = len-2; i >= 0; —-i)
48
49
          printf("%08d",a[i]);
       printf("\n");
50
51
52 | };
   9.2
        整数外挂
   int wg;
 2
   char ch;
 3
   bool ng;
 4
   inline int readint()
 5
 6
   {
 7
     ch = getchar();
     while (ch != '-' && (ch < '0' || ch > '9')) ch = getchar();
 8
 9
     if (ch == '-')
10
11
       ng = true;
12
       ch = getchar();
13
     }
14
     else
15
       ng = false;
16
     wg = ch-'0';
     ch = getchar();
17
     while (ch >= '0' && ch <= '9')
18
19
20
       wg = wg*10+ch-'0';
21
       ch = getchar();
22
23
     if (ng == true) wg = -wg;
24
     return wg;
25 }
   9.3
        Java
   9.3.1 文件操作
 1 | import java.io.∗;
   import java.util.*;
 2
   import java.math.*;
 4
   import java.text.*;
 5
 6
   public class Main
 7
 8
 9
     public static void main(String args[]) throws
        FileNotFoundException, IOException
10
     {
11
       Scanner sc = new Scanner(new FileReader("a.in"));
```

```
12
       PrintWriter pw = new PrintWriter(new FileWriter("a.out"));
13
       int n,m;
       n=sc.nextInt();//读入下一个INT
14
15
       m=sc.nextInt();
16
17
       for(ci=1; ci<=c; ++ci)
18
         pw.println("Case_#"+ci+":_easy_for_output");
19
20
       }
21
       pw.close();//关闭流并释放,这个很重要,否则是没有输出的
22
23
       sc.close();//关闭流并释放
24
     }
25 | }
   9.3.2 优先队列
   PriorityQueue queue = new PriorityQueue( 1, new Comparator()
 1
 2
 3
     public int compare( Point a, Point b )
 4
 5
     if( a.x < b.x || a.x == b.x && a.y < b.y )
 6
       return -1;
 7
     else if( a.x == b.x && a.y == b.y )
 8
       return 0;
 9
     else
10
       return 1;
11
     }
12 | });
   9.3.3 Map
 1 | Map map = new HashMap();
   map.put("sa","dd");
 2
 3
   |String str = map.get("sa").toString;
 4
 5
   for(Object obj : map.keySet()){
 6
     Object value = map.get(obj );
  |}
 7
   9.3.4 sort
  static class cmp implements Comparator
 2
 3
     public int compare(Object o1,Object o2)
 4
     BigInteger b1=(BigInteger)o1;
 5
 6
     BigInteger b2=(BigInteger)o2;
 7
     return b1.compareTo(b2);
 8
 9
   public static void main(String[] args) throws IOException
11 |{
```

```
12
     Scanner cin = new Scanner(System.in);
13
     int n;
     n=cin.nextInt();
14
15
     BigInteger[] seg = new BigInteger[n];
     for (int i=0;i<n;i++)
16
17
     seg[i]=cin.nextBigInteger();
18
     Arrays.sort(seg,new cmp());
19 | }
   9.4
        hashmap
 1
   struct hash_map
 2
 3
     const static int mod=10007;
 4
     int head[mod];
     struct hash_tables
 5
 6
     {
 7
        int key;
 8
        int val;
 9
        int next;
     } ele[10007];
10
     int N;
11
     int getHash(int x)
12
13
     {
14
        return x%mod; //小心负数
15
     void init()
16
17
        memset(head, 255, sizeof(head));
18
19
        N=0;
20
     }
21
     void clear()
22
        for (int i = 0; i < N; i++)</pre>
23
          head[getHash(ele[i].key)] = -1;
24
25
        N = 0;
26
     int fint(int x)
27
28
29
        for (int i=head[getHash(x)]; i!=-1; i=ele[i].next)
30
          if (ele[i].key==x) return i;
31
        return -1;
32
33
     void insert(int x)
34
35
        int tmp=getHash(x);
36
        ele[N].key=x;
37
        ele[N].val=0;
38
        ele[N].next=head[tmp];
        head[tmp]=N++;
39
40
41
     int& operator [](int x)
```

```
42
     {
43
        int tmp=fint(x);
        if (tmp==-1)
44
45
        {
46
          insert(x);
47
          return ele[N-1].val;
        }
48
49
        else
50
          return ele[tmp].val;
51
     }
52 | };
        C++&STL 常用函数
   9.5
   9.5.1 lower_bound/upper_bound
   不解释
 1 | iterator lower_bound(const key_type &key )
   \\返回一个迭代器, 指向键值 >= key 的第一个元素。
 2
   iterator upper_bound(const key_type &key )
   \\返回一个迭代器, 指向键值 > key 的第一个元素。
 5
   #include <iostream>
 7
   #include <algorithm>
   #include <vector>
 9
   using namespace std;
10
11
   int main () {
12
     int myints[] = {10,20,30,30,20,10,10,20};
     vector<int> v(myints,myints+8);
13
     // 10 20 30 30 20 10 10 20
14
     vector<int>::iterator low,up;
15
16
17
     sort (v.begin(), v.end());
     // 10 10 10 20 20 20 30 30
18
19
20
     low=lower_bound (v.begin(), v.end(), 20);
21
     // 10 10 10 20 20 20 30 30
22
23
     up= upper_bound (v.begin(), v.end(), 20);
24
      // 10 10 10 20 20 20 30 30
25
     //
26
     cout << "lower_bound<sub>□</sub>at<sub>□</sub>position<sub>□</sub>" << int(low— v.begin()) << endl
27
28
     cout << "upper_bound_{\square}at_{\square}position_{\square}" << int(up - v.begin()) << endl
         ;
29
30
     return 0;
31 |}
```

Output:

```
1 |lower_bound at position 3
2 upper_bound at position 6
  9.5.2 rotate
  把数组后一半搬到前面
 template <class ForwardIterator>
2
    void rotate ( ForwardIterator first, ForwardIterator middle,
3
                  ForwardIterator last );
  9.5.3 nth element
 template <class RandomAccessIterator>
1
    void nth_element ( RandomAccessIterator first,
2
       RandomAccessIterator nth,
3
                       RandomAccessIterator last );
4
  template <class RandomAccessIterator, class Comapre>
5
    void nth_element ( RandomAccessIterator first,
6
       RandomAccessIterator nth,
7
                       RandomAccessIterator last, Compare comp );
  9.5.4 bitset
  取用
1 | bitset<4> mybits;
2
                          // 0010
3 |mybits[1]=1;
                           // 0110
4 | mybits[2] = mybits[1];
  翻转
1 | bitset<4> mybits (string("0001"));
2
 4 | cout << mybits.flip() << endl;</pre>
                                     // 1010
  运算
1 | bitset<4> first (string("1001"));
  bitset<4> second (string("0011"));
2
3
  cout << (first^=second) << endl;</pre>
                                            // 1010 (XOR,assign)
  cout << (first&=second) << endl;</pre>
                                            // 0010 (AND,assign)
  cout << (first|=second) << endl;</pre>
                                            // 0011 (OR,assign)
7
 cout << (first<<=2) << endl;</pre>
                                            // 1100 (SHL,assign)
```

```
cout << (first>>=1) << endl;
                                                 // 0110 (SHR,assign)
10
   cout << (~second) << endl;</pre>
                                                 // 1100 (NOT)
11
   cout << (second<<1) << endl;</pre>
                                                 // 0110 (SHL)
12
   cout << (second>>1) << endl;</pre>
                                                 // 0001 (SHR)
13
14
15
   cout << (first==second) << endl;</pre>
                                                 // false (0110==0011)
16 | cout << (first!=second) << endl;</pre>
                                                 // true (0110!=0011)
17
18 | cout << (first&second) << endl;</pre>
                                                 // 0010
   cout << (first|second) << endl;</pre>
                                                // 0111
19
20 | cout << (first^second) << endl;</pre>
                                                 // 0101
   9.5.5 multimap
   遍历
 1 |multimap<char,int> mymm;
 2 |multimap<char,int>::iterator it;
 3
   char c;
   mymm.insert(pair<char,int>('x',50));
 6 mymm.insert(pair<char,int>('y',100));
   mymm.insert(pair<char,int>('y',150));
 7
   mymm.insert(pair<char,int>('y',200));
   mymm.insert(pair<char,int>('z',250));
 9
   mymm.insert(pair<char,int>('z',300));
10
11
   for (c='x'; c<='z'; c++)
12
13
   {
     cout << "There are (int) mymm.count(c);</pre>
14
     cout << "__elements__with__key__" << c << ":";</pre>
15
     for (it=mymm.equal_range(c).first; it!=mymm.equal_range(c).second
16
         ; ++it)
17
        cout << "" << (*it).second;
18
     cout << endl;</pre>
19
   }
20
   /*
21 Output:
22
23
   There are 1 elements with key x: 50
24 There are 3 elements with key y: 100 150 200
25
   There are 2 elements with key z: 250 300
26 | * /
   二分查找
 1 |multimap<char,int> mymultimap;
   multimap<char,int>::iterator it,itlow,itup;
 2
 3
 4 | mymultimap.insert(pair<char,int>('a',10));
```

```
mymultimap.insert(pair<char,int>('b',121));
   mymultimap.insert(pair<char,int>('c',1001));
   mymultimap.insert(pair<char,int>('c',2002));
   mymultimap.insert(pair<char,int>('d',11011));
   mymultimap.insert(pair<char,int>('e',44));
9
10
   itlow=mymultimap.lower_bound ('b'); // itlow points to b
11
   itup=mymultimap.upper_bound ('d'); // itup points to e (not d)
12
13
   // print range [itlow,itup):
14
15
   for ( it=itlow ; it != itup; it++ )
     cout << (*it).first << "_=>_" << (*it).second << endl;
16
17
   /*
18
19
   Output:
20
21 |b => 121
22
   c => 1001
23
   c => 2002
24 | d => 11011
25 | */
   删除
 1 |multimap<char,int> mymultimap;
 2
   |multimap<char,int>::iterator it;
 3
 4
   // insert some values:
   |mymultimap.insert(pair<char,int>('a',10));
   mymultimap.insert(pair<char,int>('b',20));
   mymultimap.insert(pair<char,int>('b',30));
   mymultimap.insert(pair<char,int>('c',40));
   mymultimap.insert(pair<char,int>('d',50));
   mymultimap.insert(pair<char,int>('d',60));
   mymultimap.insert(pair<char,int>('e',70));
   mymultimap.insert(pair<char,int>('f',80));
12
13
   it=mymultimap.find('b');
14
15
   mymultimap.erase (it);
   // erasing by iterator (1 element)
16
17
18
   mymultimap.erase ('d');
19
   // erasing by key (2 elements)
20
21
   it=mymultimap.find ('e');
   mymultimap.erase ( it, mymultimap.end() );
23
   // erasing by range
24
25
   // show content:
   for ( it=mymultimap.begin() ; it != mymultimap.end(); it++ )
26
     cout << (*it).first << "□=>□" << (*it).second << endl;
27
28
```

9.6 位运算

9.6.1 基本操作

注意括号

	示例	位运算
去掉最后一位	$(101101 \rightarrow 10110)$	x shr 1
在最后加一个 0	$(101101 \rightarrow 1011010)$	x shl 1
在最后加一个 1	$(101101 \rightarrow 1011011)$	x shl 1+1
把最后一位变成 1	(101100 o 101101)	x or 1
把最后一位变成 0	(101101 o 101100)	x or 1-1
最后一位取反	(101101 o 101100)	x xor 1
把右数第 k 位变成 1	$(101001 \rightarrow 101101, k = 3)$	x or (1 shl (k-1))
把右数第 k 位变成 0	$(101101 \rightarrow 101001, k = 3)$	x and not $(1 shl (k-1))$
右数第 <i>k</i> 位取反	$(101001 \rightarrow 101101, k = 3)$	x xor (1 shl (k-1))
取末三位	$(1101101 \to 101)$	x and 7
取末 <i>k</i> 位	$(1101101 \rightarrow 1101, k = 5)$	x and $(1 shl k-1)$
取右数第 <i>k</i> 位	$(1101101 \rightarrow 1, k = 4)$	x shr (k-1) and 1
把末 <i>k</i> 位变成 1	$(101001 \rightarrow 101111, k = 4)$	x or (1 shl k-1)
末 k 位取反	$(101001 \rightarrow 100110, k = 4)$	x xor (1 shl k-1)
把右边连续的 1 变成 0	$(100101111 \rightarrow 100100000)$	x and $(x+1)$
把右起第一个 0 变成 1	$(1001011111 \rightarrow 1001111111)$	x or (x+1)
把右边连续的 0 变成 1	(11011000 o 11011111)	x or (x-1)
取右边连续的 1	$(1001011111 \rightarrow 1111)$	(x xor (x+1)) shr 1
去掉右起第一个 1 的左边	$(100101000 \to 1000)$	\mid x and (x xor (x-1))

9.6.2 枚举长为 n 含 k 个 1 的 01 串

```
1 | int n = 5, k = 3;
   for (int s = (1 << k)-1, u = 1 << n; s < u;)
2
3
     for (int i = 0;i < n;i++)</pre>
4
5
        printf("%d",(((s>>(n-1-i))&1) == 1));
     printf("\n");
6
7
     int b = s \& -s;
8
9
     s = (s+b) | (((s^{(s+b))})>2)/b);
10 |}
```

9.7 其它

9.7.1 对跑脚本

```
while true; do
    ./gen > input
    ./sol < input > output.sol
    ./bf < input > output.bf

diff output.sol output.bf

if [ $? -ne 0 ]; then break; fi

done
```