

Theory - hw2

November 12, 2017

1 1

$X_1, X_2, \dots, X_n \quad y_1, y_2, \dots, y_n.$

$$M = \frac{1}{n} \sum_{i=1}^n y_i.$$

- $\xi \quad y_1, y_2, \dots, y_n.$

MSE, \hat{y} , :

$$E(\sum_{i=1}^n (\hat{y} - y_i)^2) = \sum_{i=1}^n E(\hat{y} - y_i)^2 = \sum_{i=1}^n E y_i^2 - 2 \sum_{i=1}^n E y_i \hat{y} + \sum_{i=1}^n E \hat{y}^2 \quad 1- 2- :$$

1- ,

$$2- \quad EM = M, \quad E \frac{1}{n} \sum_{i=1}^n y_i = EM = M$$

$$3-e \quad : EM^2 = M^2, \quad E \xi^2, \quad E \xi^2 \geq (E \xi)^2 = M^2,$$

MSE , , .

2 2

, MSE, , . , MSE , , MSE , , , () , scipy.optimize .