

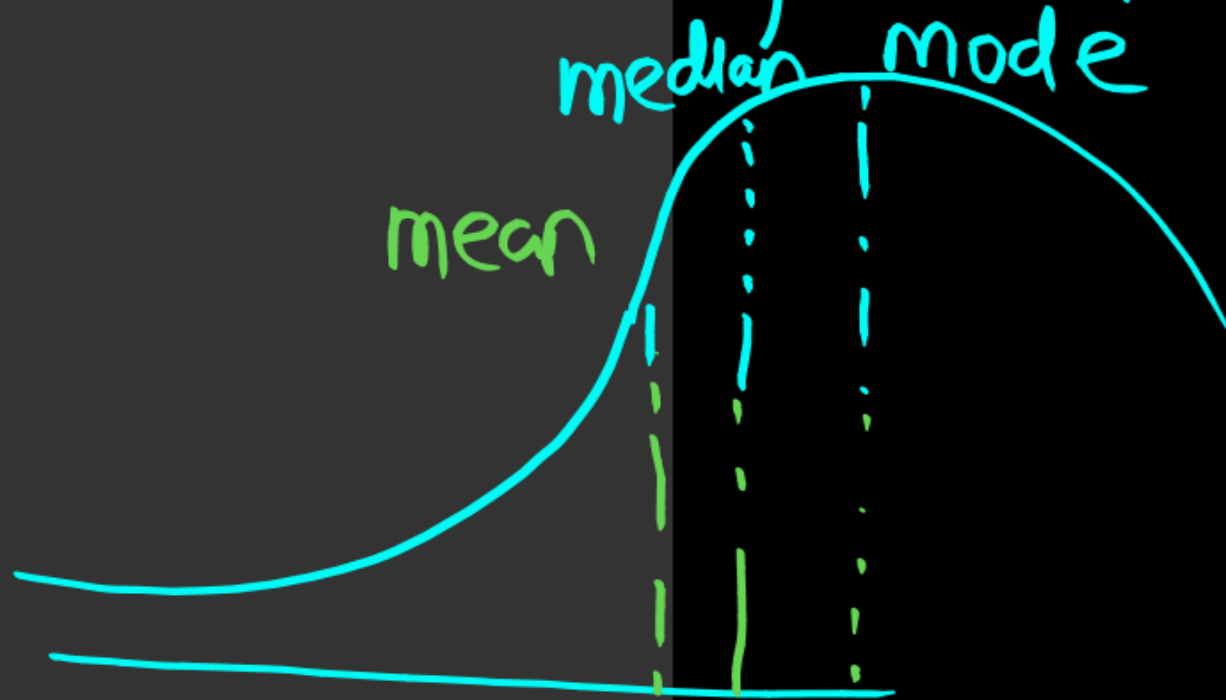
**Mode- most common no. of data
(Most frequently occurring value in the list)**

$\Rightarrow \text{Mode} = 3.\text{median} - 2.\text{mean}$

$$\text{mode} - \text{median} = 2(\text{median} - \text{mean})$$

$$\frac{\text{mode} - \text{median}}{\text{median} - \text{mean}} = 2$$

negatively Skewed frequency distribution



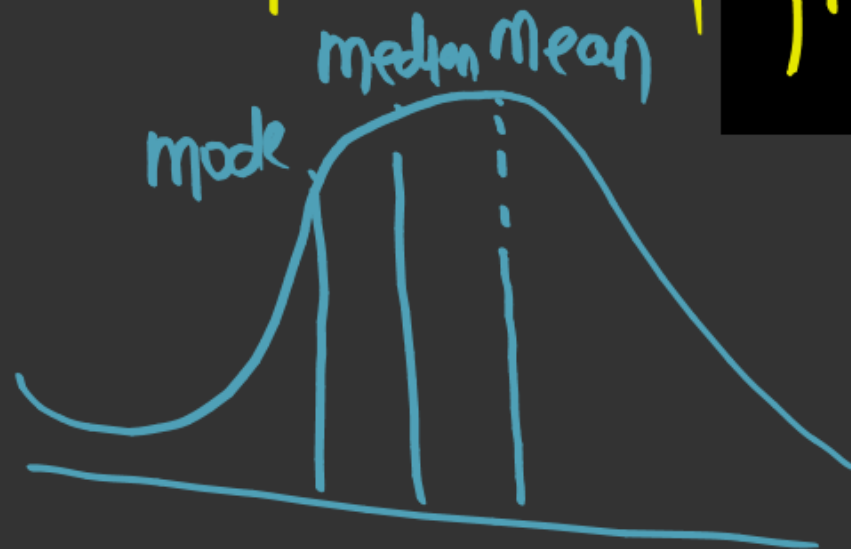
Which relation can be true between Mode, Median and Arithmetic Mean ?

मोड, माध्यिका और अंकगणितीय माध्य के बीच कौन सा संबंध सही हो सकता है? (SSC 10 + 2)

- (a) Mean > Median > Mode
- (b) Mean > Mode > Median
- (c) Mean < Mode < Median
- (d) Mode < Mean < Median

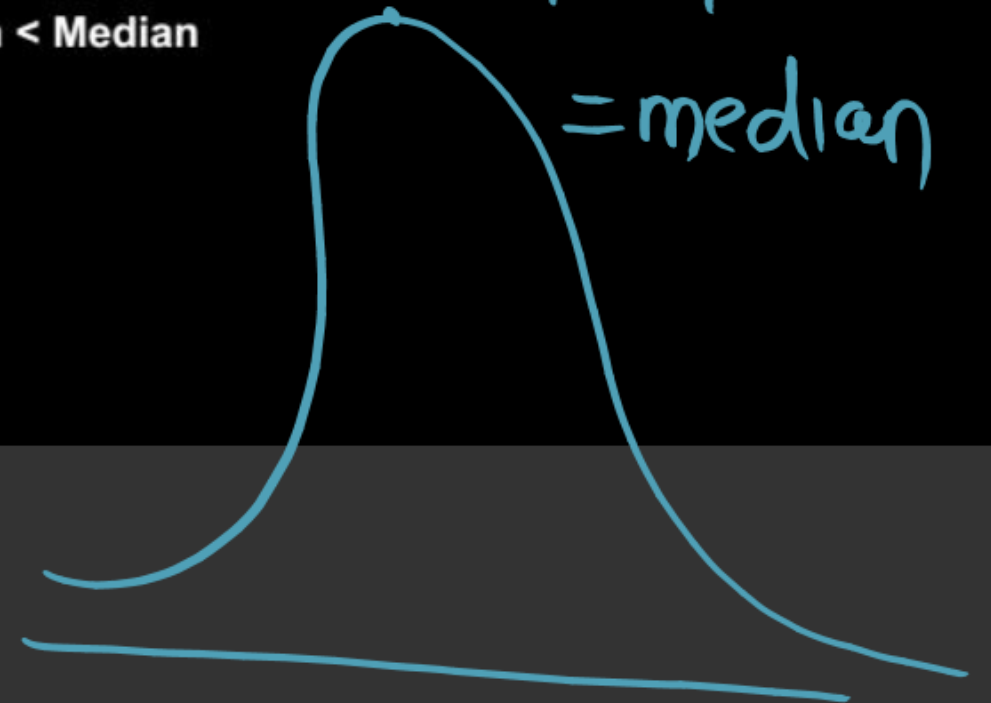
mean < median < mode

positively Skewed frequency distribution



mean > median > mode

mean = mode
= median



**Mode- most common no. of data
(Most frequently occurring value in the list)**

$$\text{Mode} = 3.\text{median}-2.\text{mean}$$

✓ **Mode for grouped data –**

$$\text{Mode} = \text{L} + h \left(\frac{f_m - f_1}{2f_m - (f_1 + f_2)} \right)$$

जिसकी frequency max है।
modal

f_1 - frequency of class preceding of the median class

f_2 - frequency of class succeeding of the median class


f_m - frequency of the modal class

L- lower limit of the mode class

h- size of class interval

there is a 15 Students in the class. and weight are

39	40	45	50	51	52	53	60
1	1	2	1	5	2	1	1

Find mode  $51 = \underline{\underline{\text{mode}}}$

S1
S2
S3
S1
S1
40
39
51
45
45
50
60
61
S2

Find mode

$$40 < \text{mode} < 50$$

Score	no. of Students
20-30	4
30-40	28 = f_1
40-50	42 = modal class = f_m
50-60	20 = f_2
60-70	6

$$l = 40$$

$$h = 10$$

$$\text{mode} = 40 + 10 \left(\frac{14}{84 - 48} \right)$$

$$= 40 + \frac{140}{36} = 35$$

$$= 43.9$$

$$\begin{aligned} \text{mode} &= 25 + \frac{5(2)}{3} \\ &= 25 + 3.33 = \underline{\underline{28.33}} \end{aligned}$$

Find the mode for the given distribution (rounded off to two decimal places).

दिए गए बंटन का बहुलक ज्ञात कीजिए (दो दशमलव स्थान तक पूर्णांकित)।

$$h = 5$$

Class Interval	5-10	10-15	15-20	20-25	25-30	30-35
Frequency	8	7	6	9	11	10

(a) 40.25

(b) 28.33

(c) 30.33

(d) 35.25

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$$25-30$$

$\text{Range} = \text{largest observation} - \text{smallest observation}$

Range - difference b/w largest and smallest no. in data.

frequency — 1, 0, 2, 3, 8, 3, 4, 5

3-2, frequency

mean deviation. (about the mean (\bar{x})) = $\frac{|x_i - \bar{x}|}{n}$

\bar{x} - mean

mean deviation (about the median (m)) = $\frac{|x_i - m|}{n}$

m - median

mean deviation for discrete frequency distribution—

data— $x_1, x_2, x_3, \dots, x_n$ — observations occurring with frequency
 $f_1, f_2, f_3, \dots, f_n$

$$M.D(\bar{x}) = \frac{f_i |x_i - \bar{x}|}{\sum f_i = N}$$

$$M.D(M) = \frac{f_i |x_i - M|}{\sum f_i = N}$$

Find the mean deviation about the mean -

Size(x) 1 3 5 7 9 11 13 15

frequency(f) 3 3 4 14 7 4 3 4

avg $\bar{x} = \text{mean} = \frac{1 \cdot 3 + 3 \cdot 3 + 5 \cdot 4 + 7 \cdot 14 + 9 \cdot 7 + 11 \cdot 4 + 13 \cdot 3 + 15 \cdot 4}{3 + 3 + 4 + 14 + 7 + 4 + 3 + 4} = \frac{336}{42}$

$MD(\bar{x}) = \frac{\sum f_i |x_i - \bar{x}|}{\sum f_i} = \frac{3(7) + 3(5) + 4(3) + 14(1) + 7(1) + 4(3) + 3(5) + 4(7)}{42} = \frac{124}{42} = 2.95$

$f_1 + f_2 \dots$

Variance $\rightarrow x_1, x_2, x_3, \dots, x_n$ are n observations.

$$\bar{x} - \text{mean} = \frac{x_1 + x_2 + \dots + x_n}{n}$$

σ - Standard deviation
मानक विचलन

$$\sigma^2 = \frac{1}{n} (x_i - \bar{x})^2 = \text{variance}$$

mean

$$\sigma = \sqrt{\text{variance}}$$

Standard deviation for discrete frequency —

$$\sigma = \sqrt{\frac{1}{N} \sum f_i (x - \bar{x})^2}$$

$$\text{Coefficient of variation} = \frac{\text{Standard deviation}}{\text{mean}} \times 100$$

Find the variance and standard deviation -

57, 64, 43, 67, 49, 59, 44, 47, 61, 59

$$\text{mean} = \frac{57+64+43+67+49+59+44+47+61+59}{10}$$

$$\begin{aligned}\text{variance} = \sigma^2 &= \frac{1}{10} (4^2 + 9^2 + 12^2 + 12^2 + 6^2 + 4^2 + 11^2 + 8^2 + 6^2 + 4^2) \\ &= \frac{662}{10} = 66.2\end{aligned}$$

σ = Standard deviation

$$= \sqrt{\text{variance}} = \sqrt{66.2} = 8.2$$

Calculate variance

	mean	Class interval	-frequency
x_1	6	4-8	3
x_2	10	8-12	6
x_3	14	12-16	4
x_4	18	16-20	7

$$\bar{x} = \frac{3 \cdot 6 + 6 \cdot 10 + 4 \cdot 14 + 7 \cdot 18}{3 + 6 + 4 + 7} = 13$$

$$\sigma^2 = \frac{1}{20} (3 \cdot (7)^2 + 6 \cdot (3)^2 + 4 \cdot (1)^2 + 7 \cdot (5)^2)$$

$$= \frac{1}{20} (147 + 54 + 4 + 175)$$

$$= 3 \frac{80}{20} = 19$$

$$\bar{x} = \text{mean} = \frac{5+3+4+7}{4} = \frac{19}{4}$$

Find the standard deviation of the following data (rounded off to two decimal places).

निम्नलिखित आंकड़ों का मानक विचलन ज्ञात कीजिए (दो दशमलव स्थान तक पूर्णांकित)।

$$5, 3, 4, 7 = x_1, x_2, x_3, x_4$$

- (a) 1.48 (b) 4.12 (c) 2.45 (d) 3.21

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$$\text{Variance} = \sigma^2 = \frac{1}{n} (x_i - \bar{x})^2$$

$$\sigma^2 = \frac{140}{4} = \frac{1}{4} \left(\frac{1}{16} + \frac{49}{16} + \frac{9}{16} + \frac{81}{16} \right)$$

$$\sigma = \text{Standard deviation} = \frac{\sqrt{140}}{2} = \frac{11.8}{2} = 5.9$$