Selected Slides from Prof Goldsman

Source: https://www2.isye.gatech.edu/~sman/courses/6644/

Estimation of π



Let's Make Some Pi

- Use Monte Carlo simulation to estimate π.
- Idea:
 - Area of a unit square is 1.
 - Area of an inscribed circle is $\pi/4$.
 - Probability that a dart thrown at the square will land in the circle is $\pi/4$.
 - Throw lots of darts. Proportion that will land in circle should approach π/4.
 - Multiply proportion by 4 to estimate π.



Monte Carlo Simulation **Monte Carlo Simulation** 500 500 Number of Points ? Points Plotted: START 573737 3.14159 Random Seed? Real Value of Pi: BACK 3.176 Animation Delay (1-100) ? Estimator for Pi: 3.14159

Yesterday, $\sqrt{-1} \ 2^3 \ \Sigma \ \pi$, and it was really tasty!

Monte Carlo Integration

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Fun With Calculus

- Use simulation to integrate $f(x) = \sin(\pi x)$ over [0,1].
- Idea:
 - Sample n rectangles.
 - Each is centered randomly on [0,1] and has width 1/n and height f(x).
 - Add up areas.
 - Make n really, really big.
 - Sum of areas approaches integral of f(x).



Monte Carlo Integration Monte Carlo Integration Points Plotted: 64 64 1. Number of Points: Y 567893 2. Enter Seed: 3. Animation Delay: ESTIMATE INTEGRAL 0.6366 Actual Result: 0.5886 Estimator: BACK \mathbf{X}