

Question no.1:

Multiple choice question (MCQs)

1. What is the use of random signal?
  - a) Test dynamic response statistically
  - b) Time duration
  - c) Impulse response
  - d) Both a, b.**
2. When we use DFT?
  - a) When signal is periodic**
  - b) When signal is Aperiodic
  - c) Both a, b.
  - d) None of the above
3. What do you mean by aliasing in DSP?
  - a) Through which different signals become indistinguishable.
  - b) Distortion in the reconstructed signal when it is reconstructed from the original continuous signal.
  - c) Both a, b.**
  - d) None of the above
4. What is microprocessor?
  - a) Process control oriented tasks.**
  - b) High performance and repetitive
  - c) Intensive task
  - d) All of the above.
5. What is convolution?
  - a) Technique of adding two signals in time domain.
  - b) Through FFT it is easy to change domain.
  - c) Both a, b**
  - d) Technique of adding two signals in frequency domain.

6. What is FFT?
- a) Fast way to measure DFT.
  - b) It is much efficient then DFT.
  - c) This technique is feasible.
  - d) All of the above**
7. What is the advantage of a direct form II FIR over form I?
- a) Requires half the number of delay units.**
  - b) It is in  $-\infty \geq \beta \geq \frac{\pi c o}{\sin \alpha}$  range
  - c) Both a, b
  - d) None of the above
8. What is interpolation?
- a) Decreasing the sample rate in DSP.
  - b) Increasing the sample rate in DSP.**
  - c) Same as Decimation
  - d) All of the above
9. How many complex multiplications are required to compute  $X(k)$ ?
- a)  $N(N + 1)$
  - b)  $\frac{N(N-1)}{2}$
  - c)  $N^2/2$
  - d)  $N(N+1)/2$**
- 10.
- The total number of complex multiplications required to compute N point DFT by radix-2 FFT is?
- a)  $\frac{N}{2} \log N$
  - b)  $n \log_2 N$
  - c)  $\frac{n}{2} \log_2 N$**
  - d) *all of the above*
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Question no.2:

**Classify the following signal if it is power signal.**

**a.  $f(t) = 1 - \cos t$**

Solution:

$$P = \frac{1}{T} \int_0^T |f(t)|^2 dt$$

We are taking T in between 0 to  $2\pi$

$$P = \frac{1}{2\pi} \int_0^{2\pi} \left[ \left( \frac{1}{2} - \cos t \right) \right]^2 dt$$

$$P = \frac{1}{2\pi} \left[ \int_0^{2\pi} \left( \frac{1}{2} \right)^2 dt - \int_0^{2\pi} (\cos t)^2 dt \right]$$

Solving the integral, respectively.

$$P = \frac{1}{2\pi} \left[ \frac{1}{4} \times \int_0^{2\pi} dt - \left[ \frac{(\sin t)^3}{3} \right]_0^{2\pi} \right]$$

Where  $\int dt = t$ , so  $\int_0^{2\pi} dt = 2\pi - 0$

Power signal becomes,

$$P = \frac{1}{2\pi} \left[ \frac{1}{4} \times 2\pi - \frac{\sin(2\pi)^3}{3} \right]$$

Solve it further, we will get

$P=0.2499999$  this value lies in between  $0 < \int_{-\infty}^{\infty} |f(t)|^2 dt < +\infty$ , so it is a power signal.

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Question no.3:

Use the graphical interpretation of convolution to find the output  $y[n]$  for the input  $x[n]$  and impulse response  $h[n]$ .

$$x[n] = 0 \ 0 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 0 \ 0$$

$$h[n] = 1 \ 1 \ 1 \ 0 \ 0 \ 1 \ 0 \ 1 \ 0 \ 1$$

It is important question!

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Question no.4:

Find the linear convolution between

$$x(n) = 1, 2, 3, 4 \quad n \geq 0$$

$$h(n) = 4, 3, 2, 1 \quad n \geq 0$$

**Solution:**

**Example:** Find the linear convolution between

$$x(n) = 1, 2, 3, 4 \quad n \geq 0$$

$$h(n) = 4, 3, 2, 1 \quad n \geq 0$$

**Solution:**

$N_1 = 4, N_2 = 4$ , and  $N_1 + N_2 - 1 = 7$  ( $y(0)$  to  $y(7)$ )

$$y(n) = \sum_{m=0}^7 x(m) \cdot h(n-m)$$

$$y(0) = \sum_{m=0}^7 x(m) \cdot h(-m) \\ = x(0)h(0) + x(1)h(-1) + x(2)h(-2) + x(3)h(-3) + x(4)h(-4) \\ + x(5)h(-5) + x(6)h(-6) + x(7)h(-7) = 1 \cdot 4 + 0 = 4$$

$$y(1) = \sum_{m=0}^7 x(m) \cdot h(1-m) \\ = x(0)h(1) + x(1)h(0) + x(2)h(-1) + x(3)h(-2) + x(4)h(-3) \\ + x(5)h(-4) + x(6)h(-5) + x(7)h(-6) = 1 \cdot 3 + 2 \cdot 4 + 0 = 11$$

$$y(2) = \sum_{m=0}^7 x(m) \cdot h(2-m) = 20$$

$$y(3) = \sum_{m=0}^7 x(m) \cdot h(3-m) = 1 + 4 + 9 + 16 = 30$$

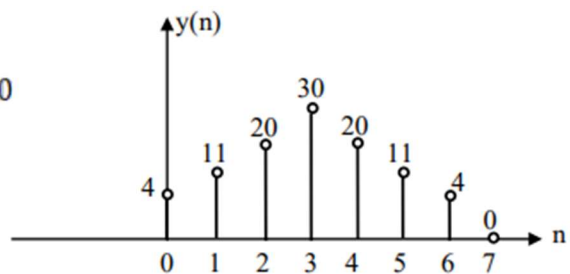
$$y(4) = \sum_{m=0}^7 x(m) \cdot h(4-m) = 2 + 6 + 12 = 20$$

$$y(5) = \sum_{m=0}^7 x(m) \cdot h(5-m) = 1 \cdot 0 + 2 \cdot 0 + 3 \cdot 1 + 4 \cdot 2 = 11$$

$$y(6) = \sum_{m=0}^7 x(m) \cdot h(6-m) = 4 \cdot 1 = 4$$

$$y(7) = \sum_{m=0}^7 x(m) \cdot h(7-m) = 0$$

$$y(n) = 4, 11, 20, 30, 20, 11, 4, 0$$



Question no.5:

Find the circular convolution between

$$x[n] = 1, 2, 3, 4 \geq 0$$

$$h[n] = 4, 3, 2, 1 \ n \geq 0$$

Solution:

**Example:** Find the Circular convolution between

$$x[n] = 1, 2, 3, 4 \ n \geq 0$$

$$h[n] = 4, 3, 2, 1 \ n \geq 0$$

**Solution:**

$$N = 4$$

$$y[n] = \sum_{m=0}^3 h(n-m).x(m)$$

$$\begin{aligned} y[0] &= \sum_{m=0}^3 h(-m).x(m) = x(0)h(0) + x(1)h(-1) + x(2)h(-2) + x(3)h(-3) \\ &= 1*4 + 2*1 + 3*2 + 4*3 = 24 \end{aligned}$$

$$\begin{aligned} y[1] &= \sum_{m=0}^3 h(1-m).x(m) = x(0)h(1) + x(1)h(0) + x(2)h(-1) + x(3)h(-2) \\ &= 1*3 + 2*4 + 3*1 + 4*2 = 22 \end{aligned}$$

$$\begin{aligned} y[2] &= \sum_{m=0}^3 h(2-m).x(m) = x(0)h(2) + x(1)h(1) + x(2)h(0) + x(3)h(-1) \\ &= 1*2 + 2*3 + 3*4 + 4*1 = 24 \end{aligned}$$

$$\begin{aligned} y[3] &= \sum_{m=0}^3 h(3-m).x(m) = x(0)h(3) + x(1)h(2) + x(2)h(1) + x(3)h(0) \\ &= 1*1 + 2*2 + 3*3 + 4*4 = 30 \end{aligned}$$

