

# Machining

Cutting action involves shear deformation of work material to form a chip

- As chip is removed, a new surface is exposed

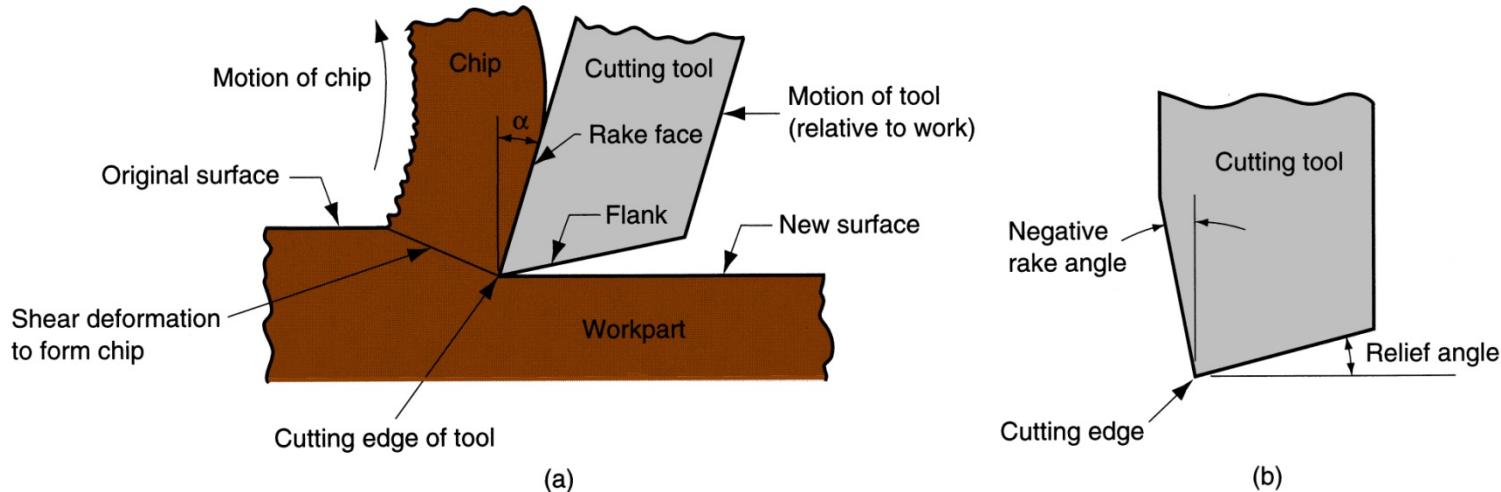


Figure 21.2 - (a) A cross-sectional view of the machining process, (b) tool with negative rake angle; compare with positive rake angle in (a)



# Why Machining is Important

- Variety of work materials can be machined
  - Most frequently applied to metals
- Variety of part shapes and special geometry features possible, such as:
  - Screw threads
  - Accurate round holes
  - Very straight edges and surfaces
- Good dimensional accuracy and surface finish



# Disadvantages with Machining

- Wasteful of material
  - Chips generated in machining are wasted material, at least in the unit operation
- Time consuming
  - A machining operation generally takes more time to shape a given part than alternative shaping processes, such as casting, powder metallurgy, or forming



# Machining in the Manufacturing Sequence

- Generally performed after other manufacturing processes, such as casting, forging, and bar drawing
  - Other processes create the general shape of the starting workpart
  - Machining provides the final shape, dimensions, finish, and special geometric details that other processes cannot create



# Cutting Tool Classification

## 1. *Single-Point Tools*

- One cutting edge
- *Turning* uses single point tools
- Point is usually rounded to form a *nose radius*

## 2. *Multiple Cutting Edge Tools*

- More than one cutting edge
- Motion relative to work usually achieved by rotating
- *Drilling* and *milling* use rotating multiple cutting edge tools.

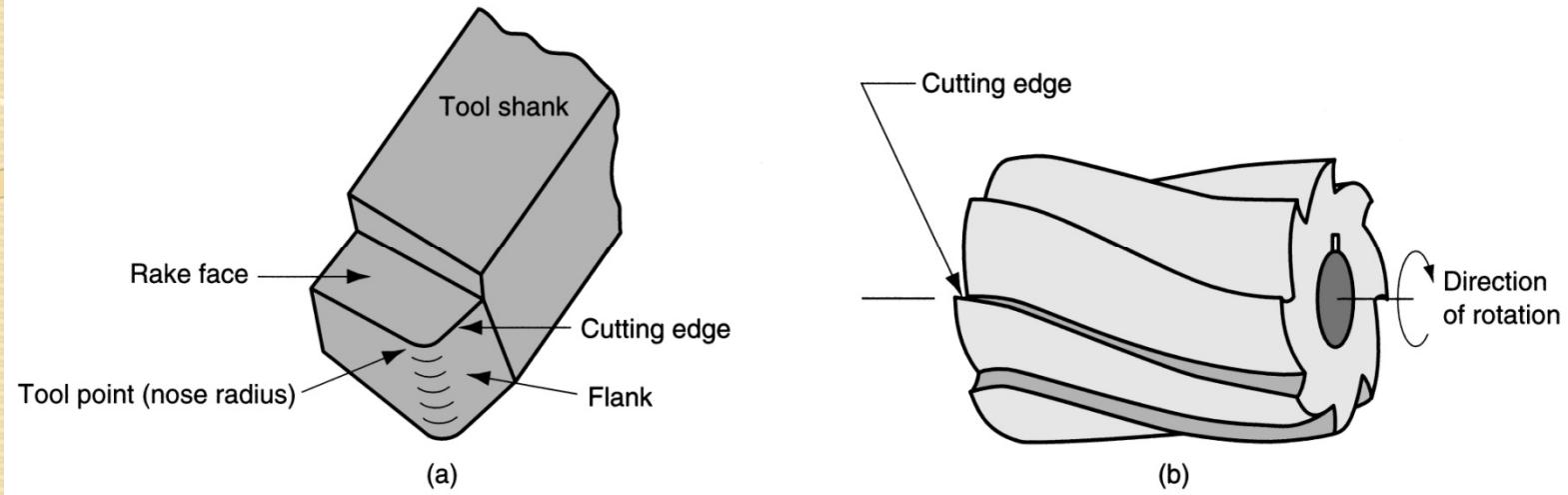


Figure 21.4 - (a) A single-point tool showing rake face, flank, and tool point; and (b) a helical milling cutter, representative of tools with multiple cutting edges



# Cutting Conditions in Machining

- The three dimensions of a machining process:
  - Cutting speed  $v$  – primary motion
  - Feed  $f$  – secondary motion
  - Depth of cut  $d$  – penetration of tool below original work surface
- For certain operations, material removal rate can be found as

$$MRR = v f d$$

where  $v$  = cutting speed;  $f$  = feed;  $d$  = depth of cut

# Machining Calculations: Turning

- Spindle Speed - N (rpm)
  - $v$  = **cutting speed**
  - $D_o$  = **outer diameter**
- Feed Rate -  $f_r$  (mm/min -or- in/min)
  - $f$  = **feed per rev**
- Depth of Cut -  $d$  (mm/rev -or- in/rev)
  - $D_o$  = **outer diameter**
  - $D_f$  = **final diameter**
- Machining Time -  $T_m$  (min)
  - $L$  = **length of cut**
- Mat'l Removal Rate - MRR (mm<sup>3</sup>/min -or- in<sup>3</sup>/min)

# Cutting Conditions for Turning

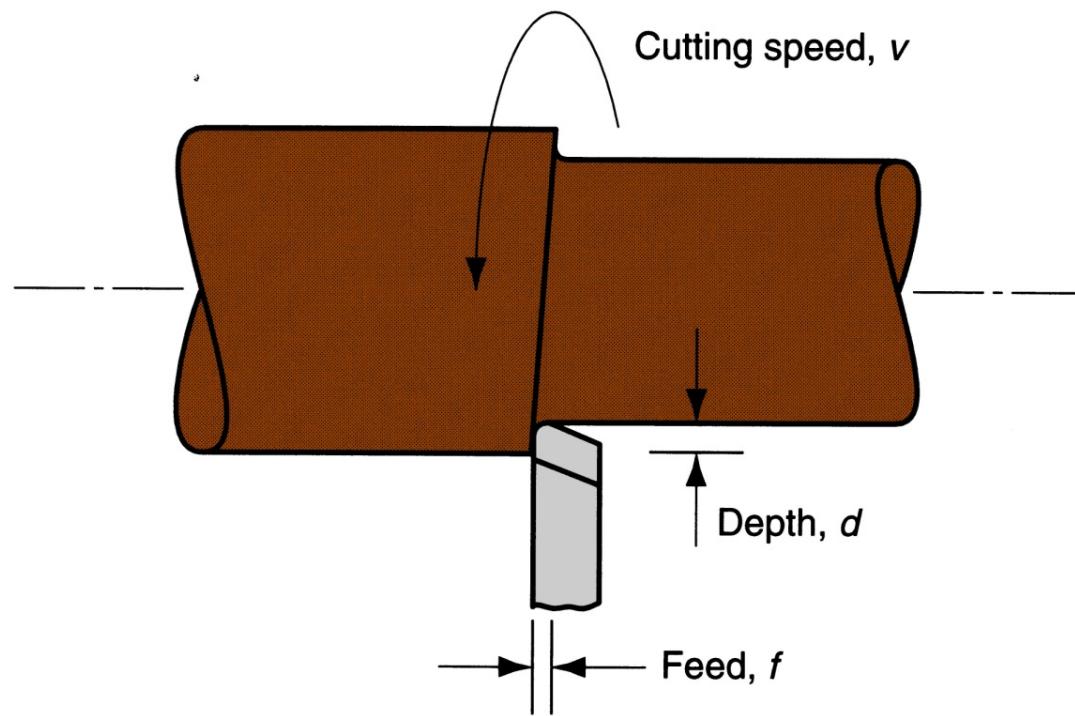
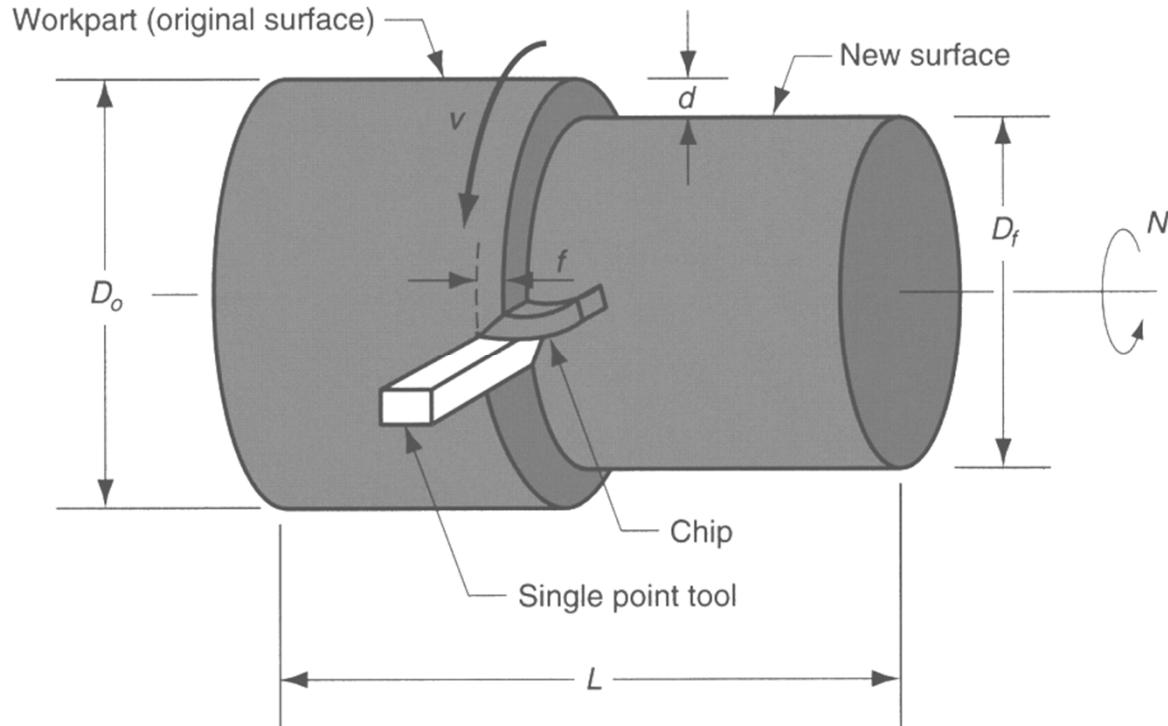


Figure 21.5 - Cutting speed, feed, and depth of cut for a turning operation

# Cutting Conditions for Turning



Turning Parameters Illustrated

# Machining Operations & Parameters

<i>Operation Type</i>	<i>Speed</i>	<i>Feed</i>	<i>Depth of Cut</i>
<b>Turning:</b> work piece rotates single point cutting	Surface speed (periphery) of workpiece	Parallel to the work piece axis* <small>(*except parting/grooving)</small>	Tool penetration below original work surface
<b>Drilling:</b> tool rotates single pass cutting	Surface speed (periphery) of tool	Parallel to the tool axis	Tool penetration below original work surface <b>(depth of hole)</b>
<b>Milling:</b> tool rotates multi-point cutting	Surface speed (periphery) of tool	Perpendicular to the tool axis	Tool penetration below original work surface



# Roughing vs. Finishing in Machining

In production, several roughing cuts are usually taken on the part, followed by one or two finishing cuts

- *Roughing* - removes large amounts of material from the starting workpart
  - Creates shape close to desired geometry, but leaves some material for finish cutting
  - High feeds and depths, **low speeds**
- *Finishing* - completes part geometry
  - Achieves final dimensions, tolerances, and finish
  - Low feeds and depths, **high cutting speeds**

# Cut Types: Roughing & Finishing

<i>Cut Type</i>	<i>Number of Passes</i>	<i>Speed</i>	<i>Feed</i>	<i>Depth of Cut</i>
<b>Roughing:</b> removes large amounts to get close to shape	1 +	Low	High 0.4 - 1.25 mm/ .015 - .050 in/	High 2.5 - 20 mm .100 - .750 in
<b>Finishing:</b> achieves final dimensions, tolerances, and finish	1 - 2	High	Low 0.125 - 0.4 mm/ .005 - .015 in/	Low 0.75 - 2.0 mm .030 - .075 in



# Why cutting analysis is important

- To determine the power consumption-  
Motor selection
- Maximize the productivity
- Determine tool life
- Excellent dimensional tolerance



# THEORY OF METAL MACHINING

- Theory of Chip Formation in Metal Machining
- Force Relationships and the Merchant Equation
- Power and Energy Relationships in Machining
- Cutting Temperature

## Orthogonal Cutting Model

A simplified 2-D model of machining that describes the mechanics of machining fairly accurately

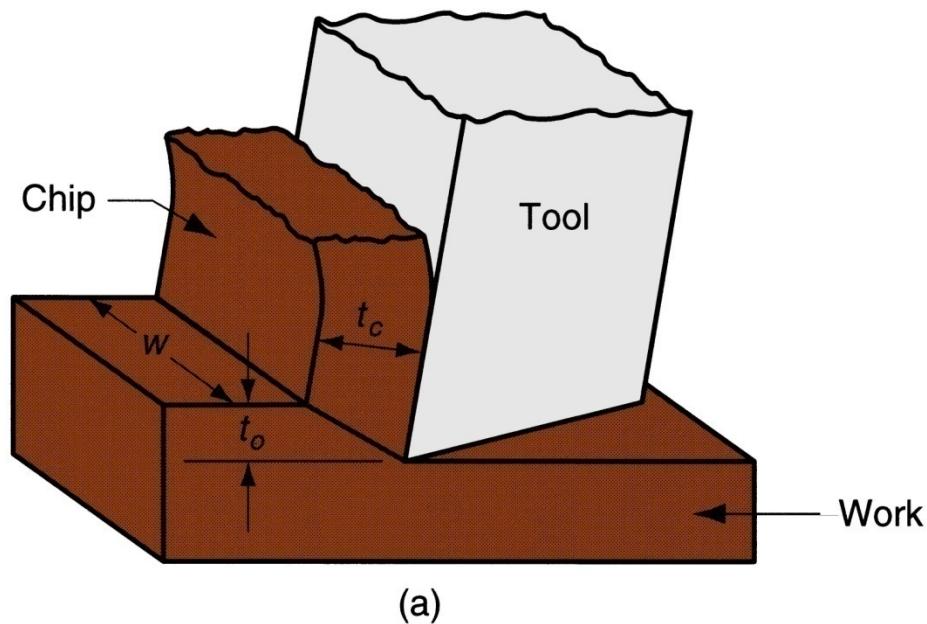
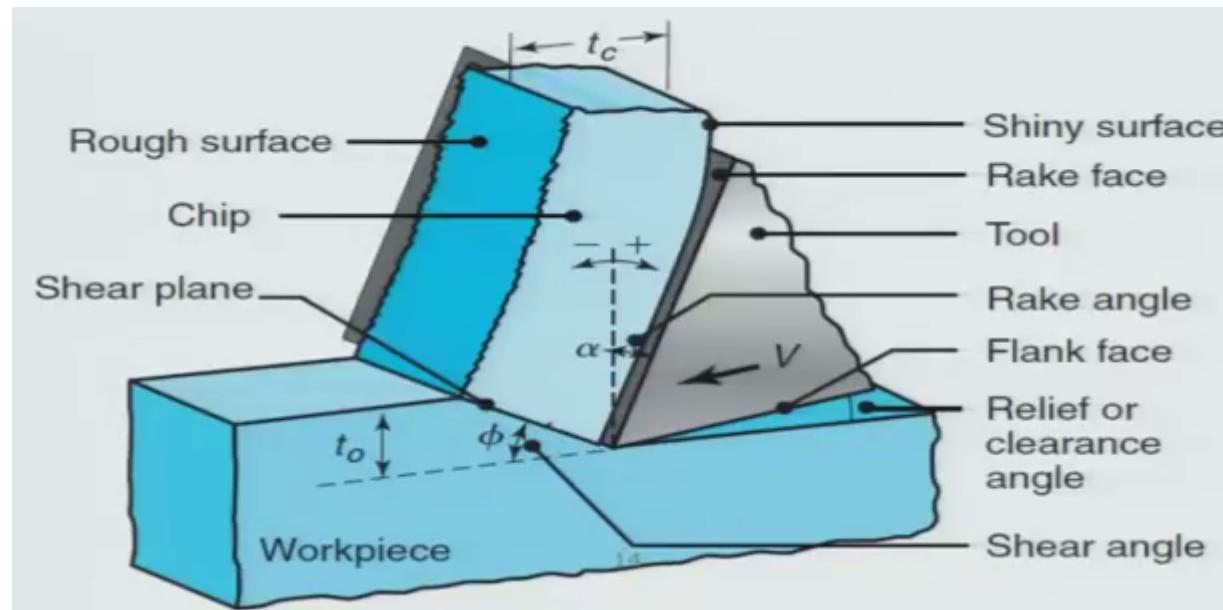


Figure 21.6 - Orthogonal cutting: (a) as a three-dimensional process

# Cutting Analysis

In idealized model, a cutting tool moves to the left along the workpiece at a constant velocity,  $V$ , and a depth of cut,  $t_o$ . Chip thickness,  $t_c$



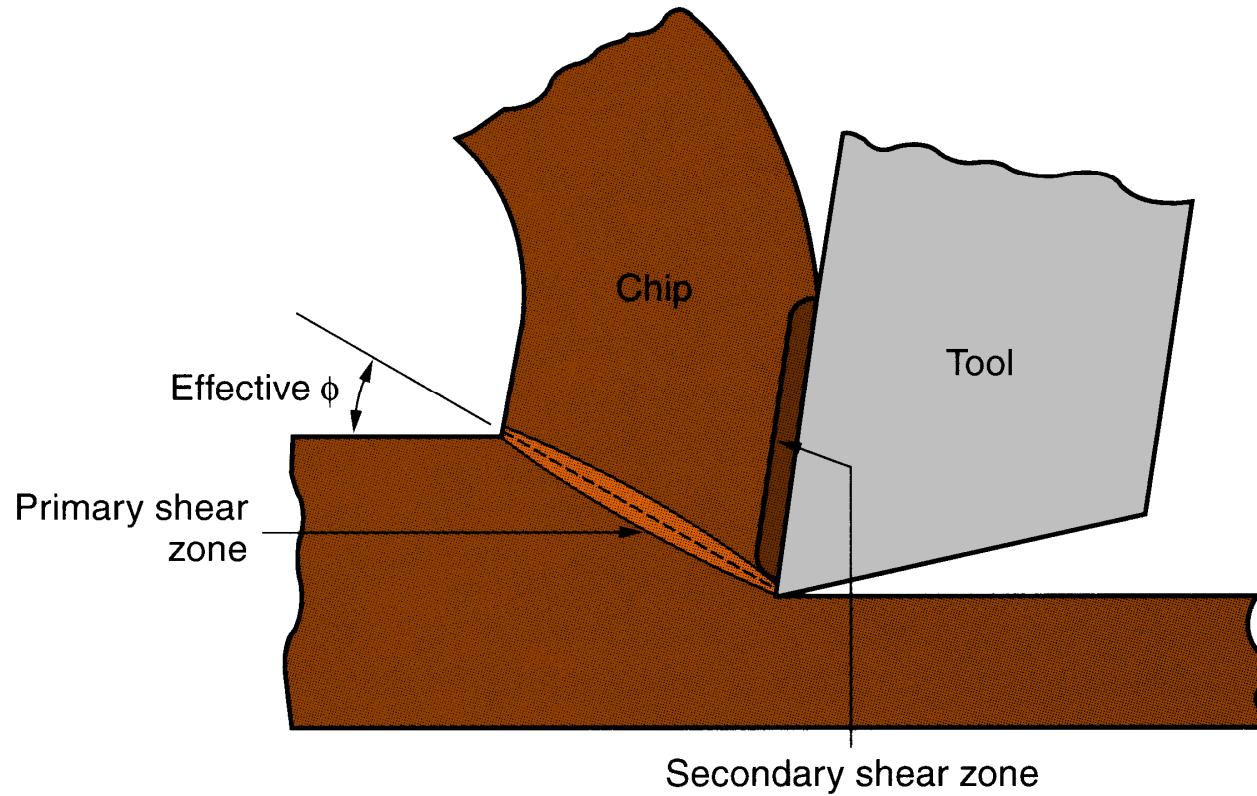


Figure 21.8 - More realistic view of chip formation, showing shear zone rather than shear plane. Also shown is the secondary shear zone resulting from tool-chip friction

# Chip Thickness Ratio

$$r = \frac{t_o}{t_c}$$

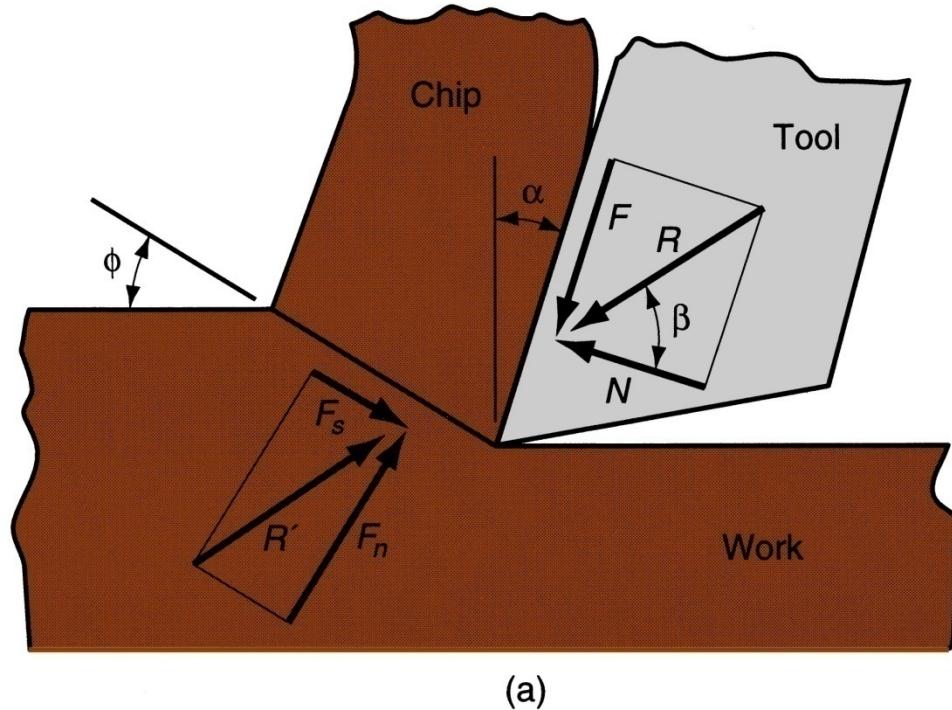
where  $r$  = *chip thickness ratio*;  $t_o$  = thickness of the chip prior to chip formation; and  $t_c$  = chip thickness after separation

- Chip thickness after cut is always greater than before, so chip ratio is always less than 1.0

## Forces Acting on Chip

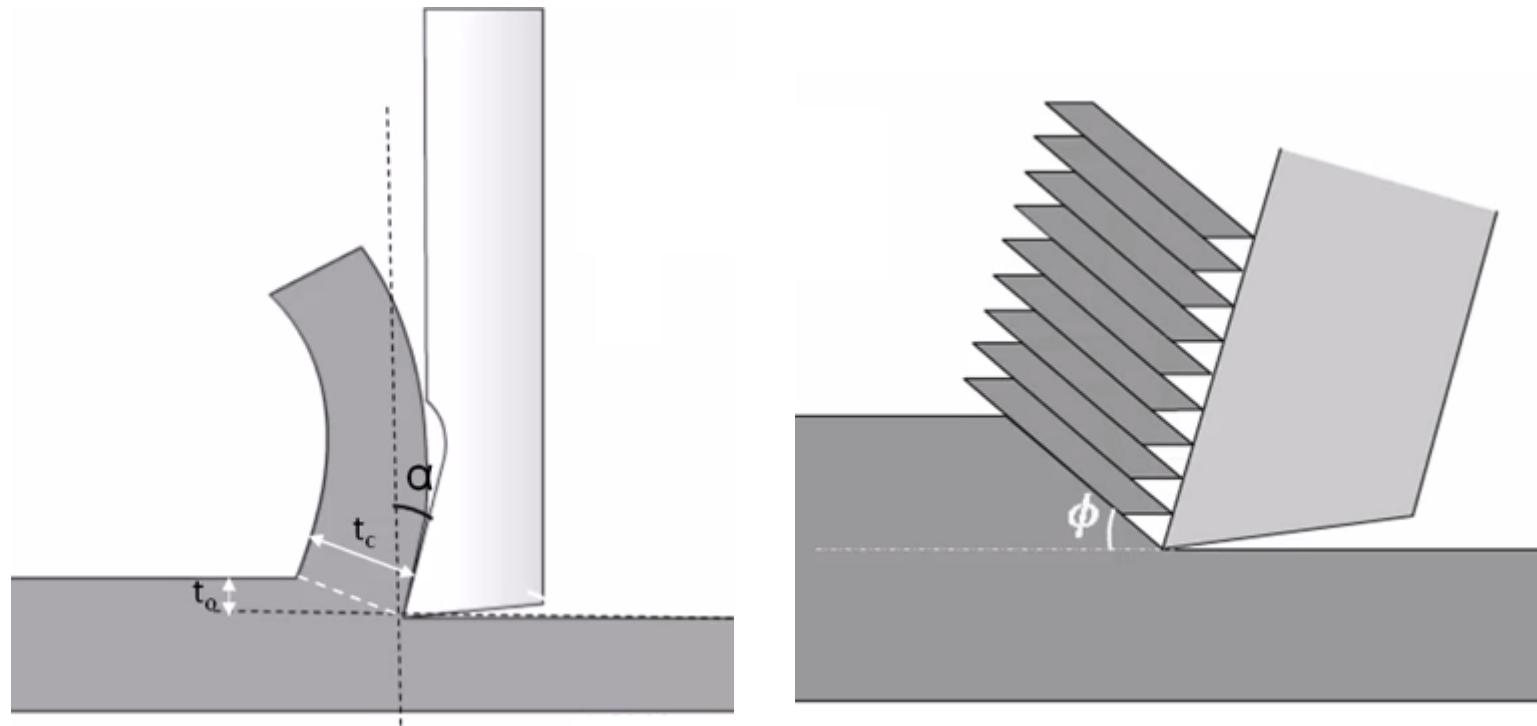
- Friction force  $F$  and Normal force to friction  $N$
- Shear force  $F_s$  and Normal force to shear  $F_n$

Figure 21.10 -  
Forces in metal  
cutting: (a) forces  
acting on the chip  
in orthogonal  
cutting

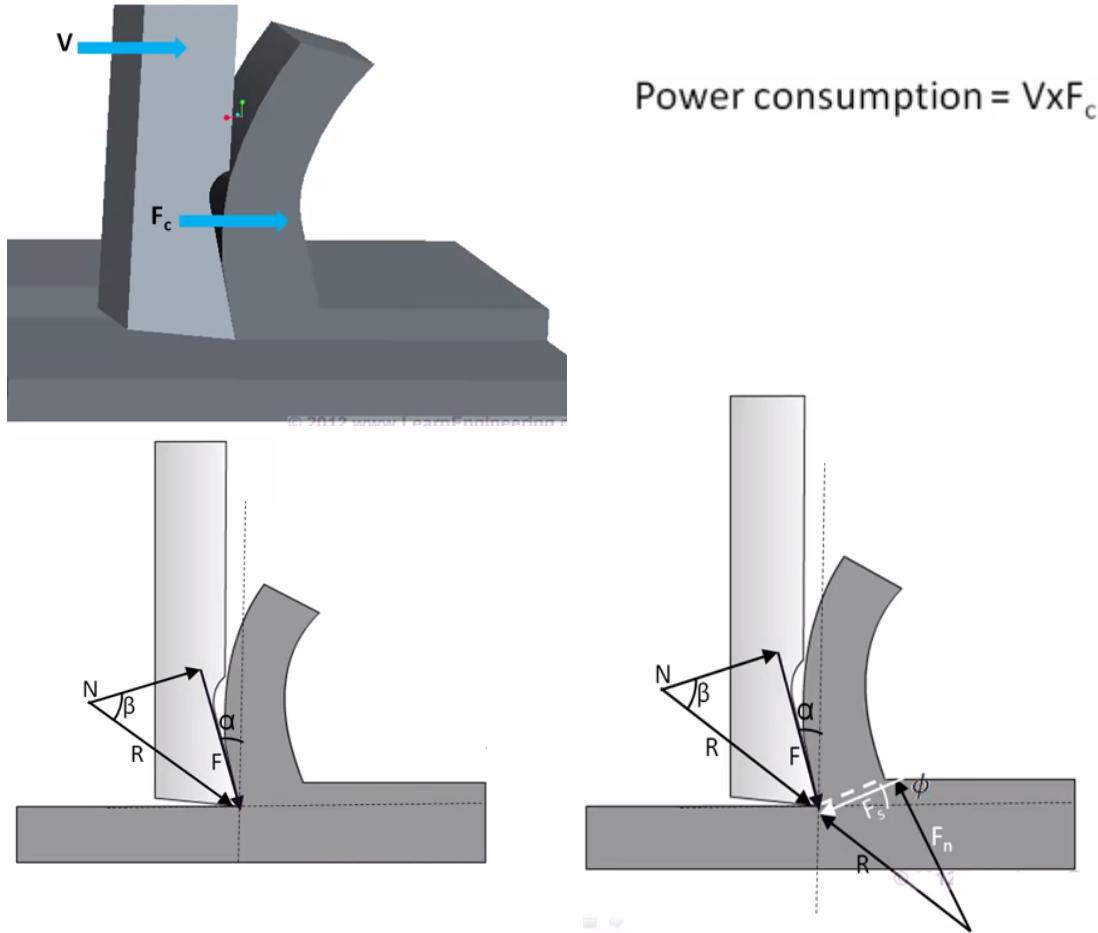


# SHEAR PLANE THEORY

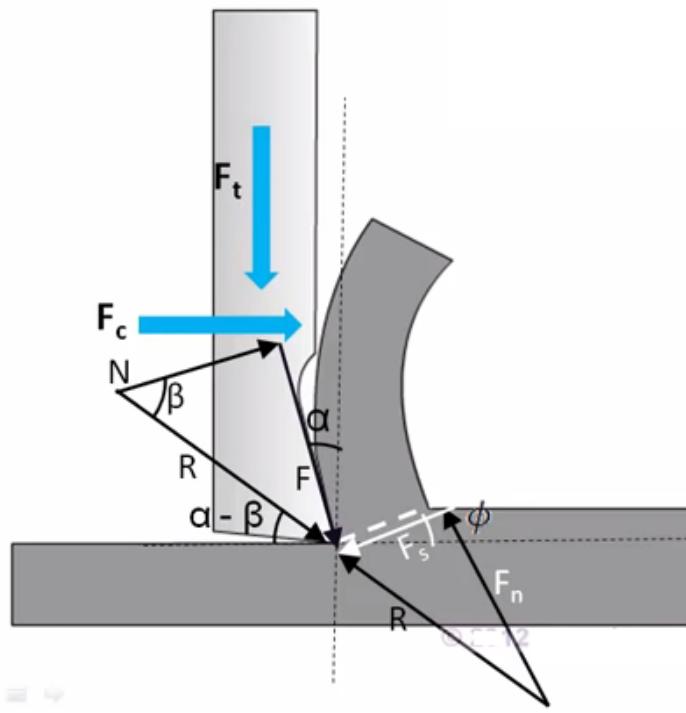
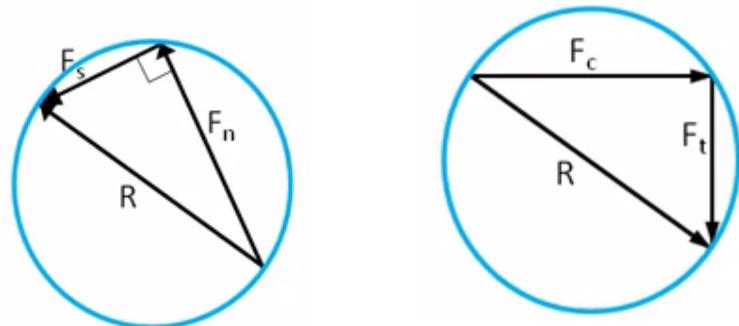
$$\frac{t_o}{t_c} = \frac{\sin \phi}{\cos(\phi - \alpha)}$$



# Cutting Analysis



# MERCHANT CIRCLE DIAGRAM



# Determining Shear Plane Angle

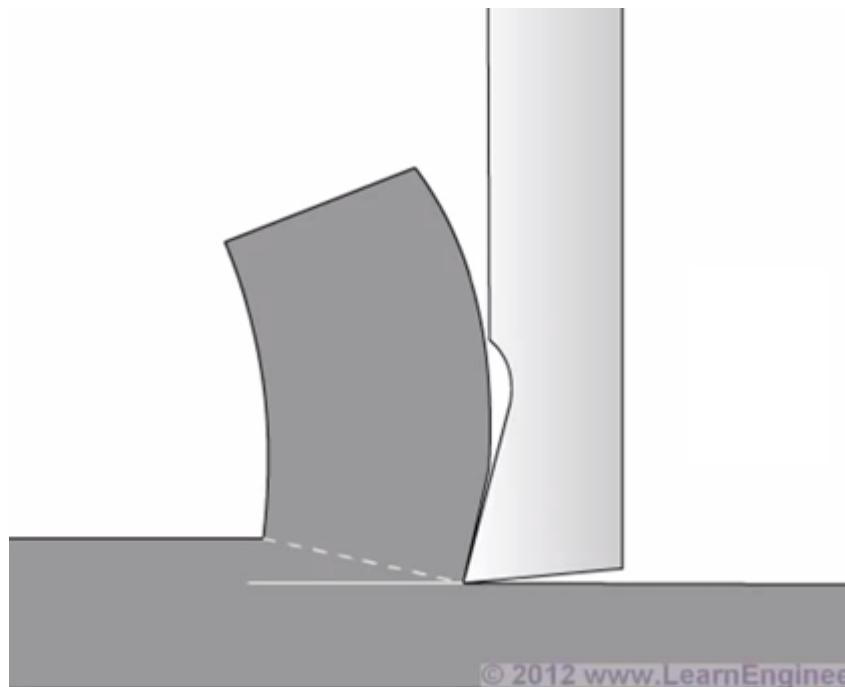
- Based on the geometric parameters of the orthogonal model, the shear plane angle  $\phi$  can be determined as:

$$\tan \phi = \frac{r \cos \alpha}{1 - r \sin \alpha}$$

where  $r$  = chip ratio, and  $\alpha$  = rake angle

# HOW TO PREDICT $\phi$

## Merchant Equation



$$\tau = \frac{F_c \cos \phi - F_t \sin \phi}{t_o W / \sin \phi}$$

$$\frac{d\tau}{d\phi} = 0$$

$$\phi = 45^\circ + \frac{\alpha}{2} - \frac{\beta}{2}$$

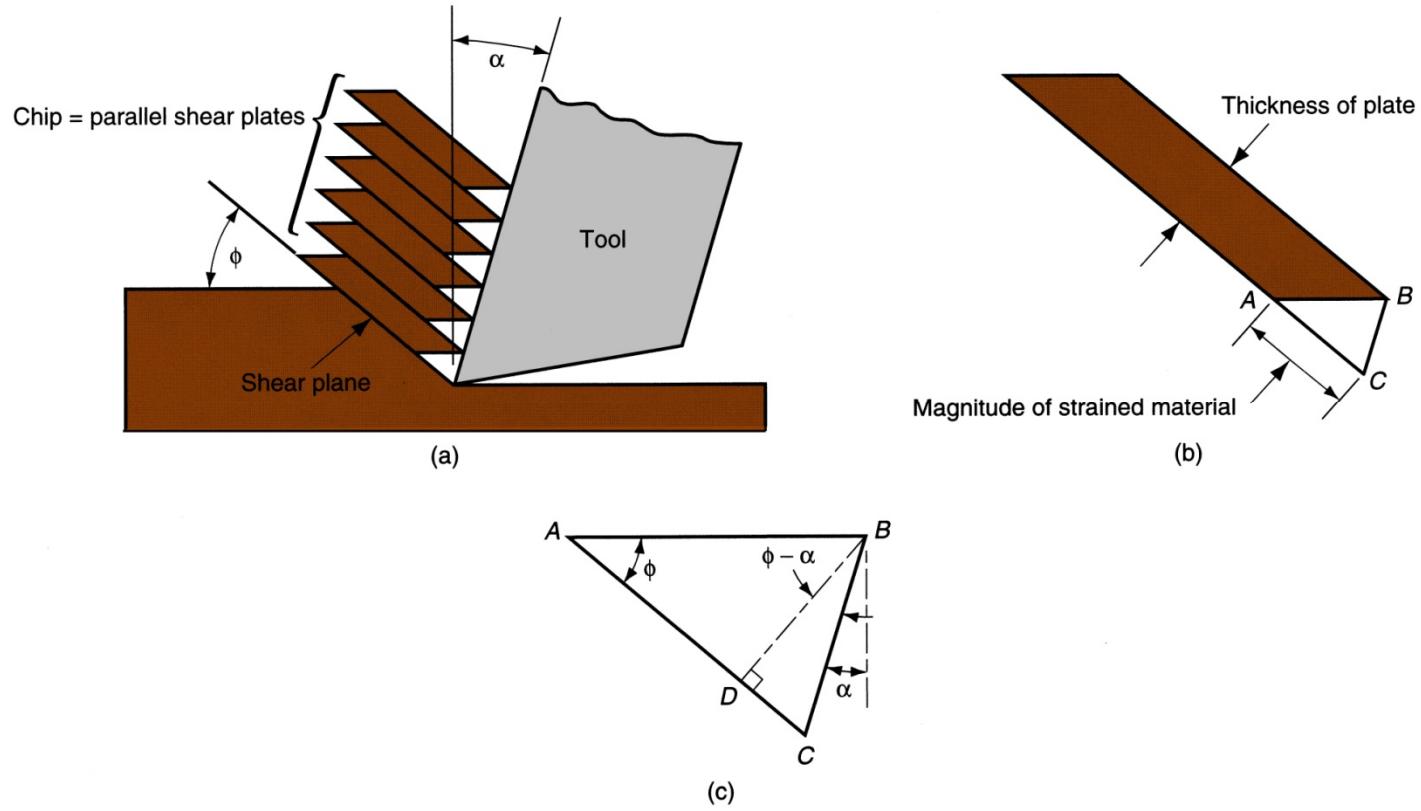


Figure 21.7 - Shear strain during chip formation: (a) chip formation depicted as a series of parallel plates sliding relative to each other, (b) one of the plates isolated to show shear strain, and (c) shear strain triangle used to derive strain equation

# Shear Strain

Shear strain in machining can be computed from the following equation, based on the preceding parallel plate model:

$$\gamma = \tan(\phi - \alpha) + \cot \phi$$

where  $\gamma$  = shear strain,  $\phi$  = shear plane angle, and  $\alpha$  = rake angle of cutting tool



# Resultant Forces

- Vector addition of  $F$  and  $N$  = resultant  $R$
- Vector addition of  $F_s$  and  $F_n$  = resultant  $R'$
- Forces acting on the chip must be in balance:
  - $R'$  must be equal in magnitude to  $R$
  - $R'$  must be opposite in direction to  $R$
  - $R'$  must be collinear with  $R$



# Coefficient of Friction

Coefficient of friction between tool and chip:

$$\mu = \frac{F}{N}$$

Friction angle related to coefficient of friction as follows:

$$\mu = \tan \beta$$

# Shear Stress

Shear stress acting along the shear plane:

$$S = \frac{F_s}{A_s}$$

where  $A_s$  = area of the shear plane

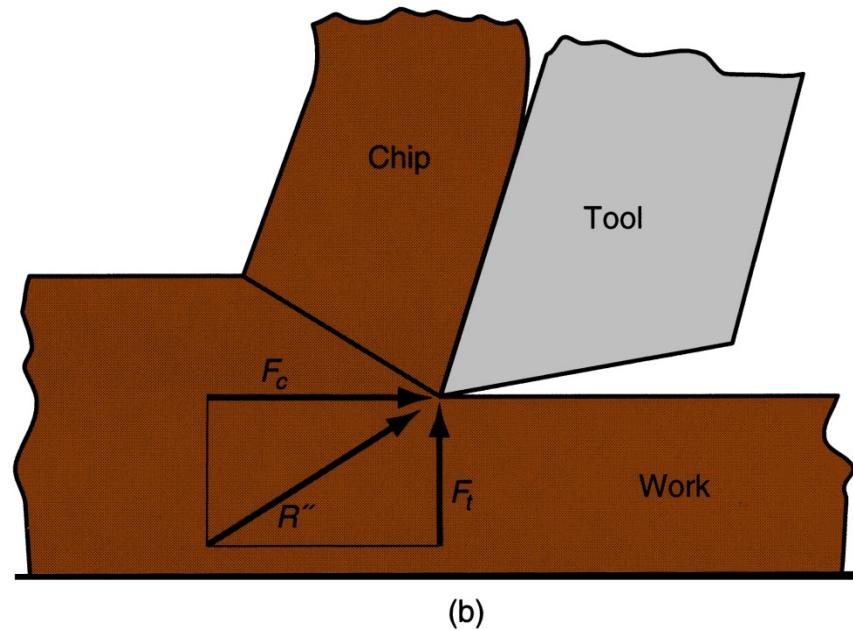
$$A_s = \frac{t_o w}{\sin \phi}$$

Shear stress = shear strength of work material during cutting

## Cutting Force and Thrust Force

- Forces  $F$ ,  $N$ ,  $F_s$ , and  $F_n$  cannot be directly measured
- Forces acting on the tool that can be measured:
  - *Cutting force  $F_c$  and Thrust force  $F_t$*

Figure 21.10 - Forces in metal cutting: (b) forces acting on the tool that can be measured





# Forces in Metal Cutting

- Equations can be derived to relate the forces that cannot be measured to the forces that can be measured:

$$F = F_c \sin\alpha + F_t \cos\alpha$$

$$N = F_c \cos\alpha - F_t \sin\alpha$$

$$F_s = F_c \cos\phi - F_t \sin\phi$$

$$F_n = F_c \sin\phi + F_t \cos\phi$$

- Based on these calculated force, shear stress and coefficient of friction can be determined

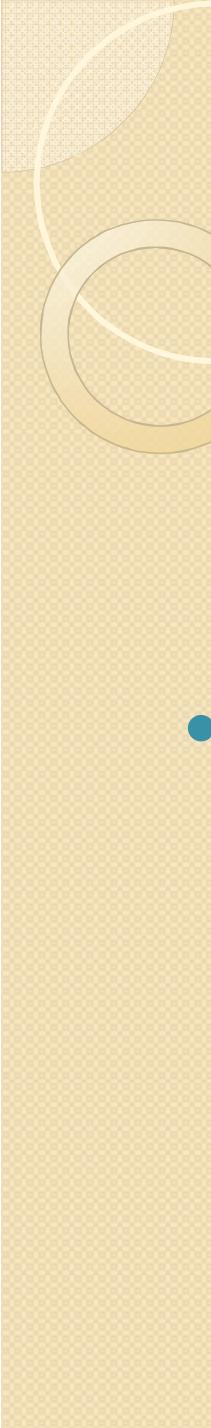


# The Merchant Equation

- Of all the possible angles at which shear deformation could occur, the work material will select a shear plane angle  $\phi$  which minimizes energy, given by

$$\phi = 45 + \frac{\alpha}{2} - \frac{\beta}{2}$$

- Derived by Eugene Merchant
- Based on orthogonal cutting, but validity extends to 3-D machining



# What the Merchant Equation Tells Us

$$\phi = 45 + \frac{\alpha}{2} - \frac{\beta}{2}$$

- To increase shear plane angle
  - Increase the rake angle
  - Reduce the friction angle (or coefficient of friction)

- Higher shear plane angle means smaller shear plane which means lower shear force
- Result: lower cutting forces, power, temperature, all of which mean easier machining

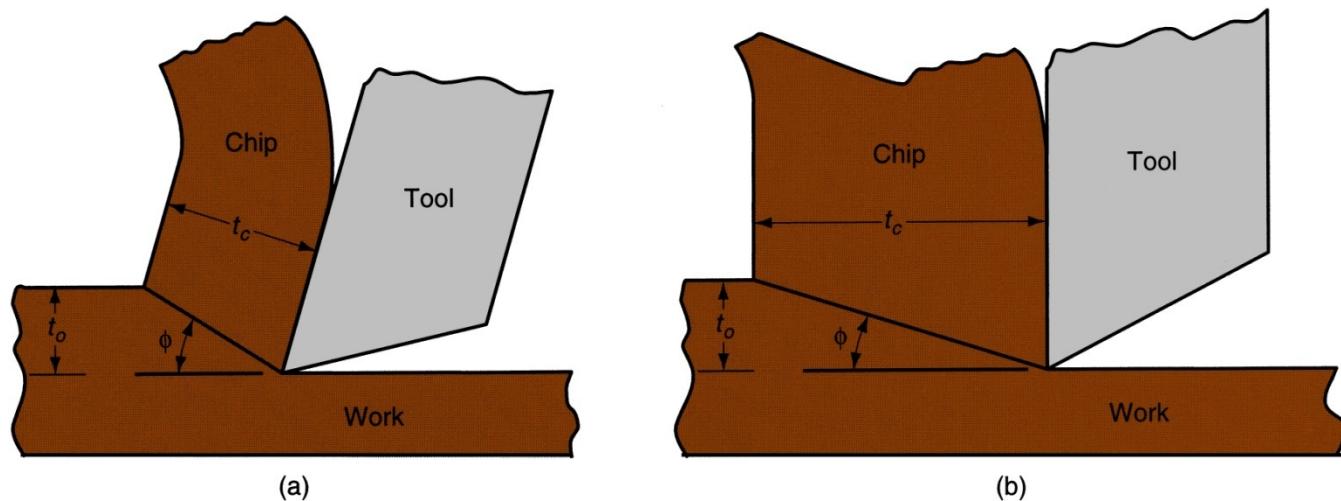


Figure 21.12 - Effect of shear plane angle  $\phi$  : (a) higher  $\phi$  with a resulting lower shear plane area; (b) smaller  $\phi$  with a corresponding larger shear plane area. Note that the rake angle is larger in (a), which tends to increase shear angle according to the Merchant equation



# Power and Energy Relationships

- A machining operation requires power

The power to perform machining can be computed from:

$$P_c = F_c v$$

where  $P_c$  = cutting power;  $F_c$  = cutting force; and  $v$  = cutting speed

# Power and Energy Relationships

In U.S. customary units, power is traditionally expressed as horsepower (dividing ft-lb/min by 33,000)

$$HP_c = \frac{F_c v}{33,000}$$

where  $HP_c$  = cutting horsepower, hp

# Power and Energy Relationships

Gross power to operate the machine tool  $P_g$  or  $HP_g$  is given by

$$P_g = \frac{P_c}{E} \quad \text{or} \quad HP_g = \frac{HP_c}{E}$$

where  $E$  = mechanical efficiency of machine tool

Typical  $E$  for machine tools = ~ 90%

# Unit Power in Machining

- Useful to convert power into power per unit volume rate of metal cut
- Called the *unit power*,  $P_u$  or *unit horsepower*,  $HP_u$

$$P_u = \frac{P_c}{MRR} \quad \text{or} \quad HP_u = \frac{HP_c}{MRR}$$

where  $MRR$  = material removal rate

# Specific Energy in Machining

Unit power is also known as the *specific energy*  $U$

$$U = P_u = \frac{P_c}{MRR} = \frac{F_c v}{v t_o w} = \frac{F_c}{t_o w}$$

Units for specific energy are typically N-m/mm<sup>3</sup> or J/mm<sup>3</sup> (in-lb/in<sup>3</sup>)



# Cutting Temperature

- Approximately 98% of the energy in machining is converted into heat
- This can cause temperatures to be very high at the tool-chip
- The remaining energy (about 2%) is retained as elastic energy in the chip



Thank You