

$$\begin{matrix} x_1 & y_1 & & x_2 & y_2 \\ (0, 2) & & & (-0.667, 0) \end{matrix}$$

$$\text{slope} = \frac{\Delta y / y_2 - y_1}{\Delta x / x_2 - x_1} = \frac{0 - 2}{-0.667 - 0}$$

$$\frac{-2}{-0.667} = \sim 3$$

$$y = mx + b$$

$m \Rightarrow \text{slope}$

$b \Rightarrow \text{Intercept}$

slope \rightarrow steepness, rate of change of

$$\frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$

line of y
with respect x

Intercept \rightarrow Value of y where
line crosses the y axis

when $x=0$ what is y ?

what will happen to slope when
 \perp change and keep the Intercept constant

Angle is changed

It is going to rotate with the
intercept point as constant

What will happen when Intercept is changing
keeping the slope constant

It is going to place parallelly
with the same angle

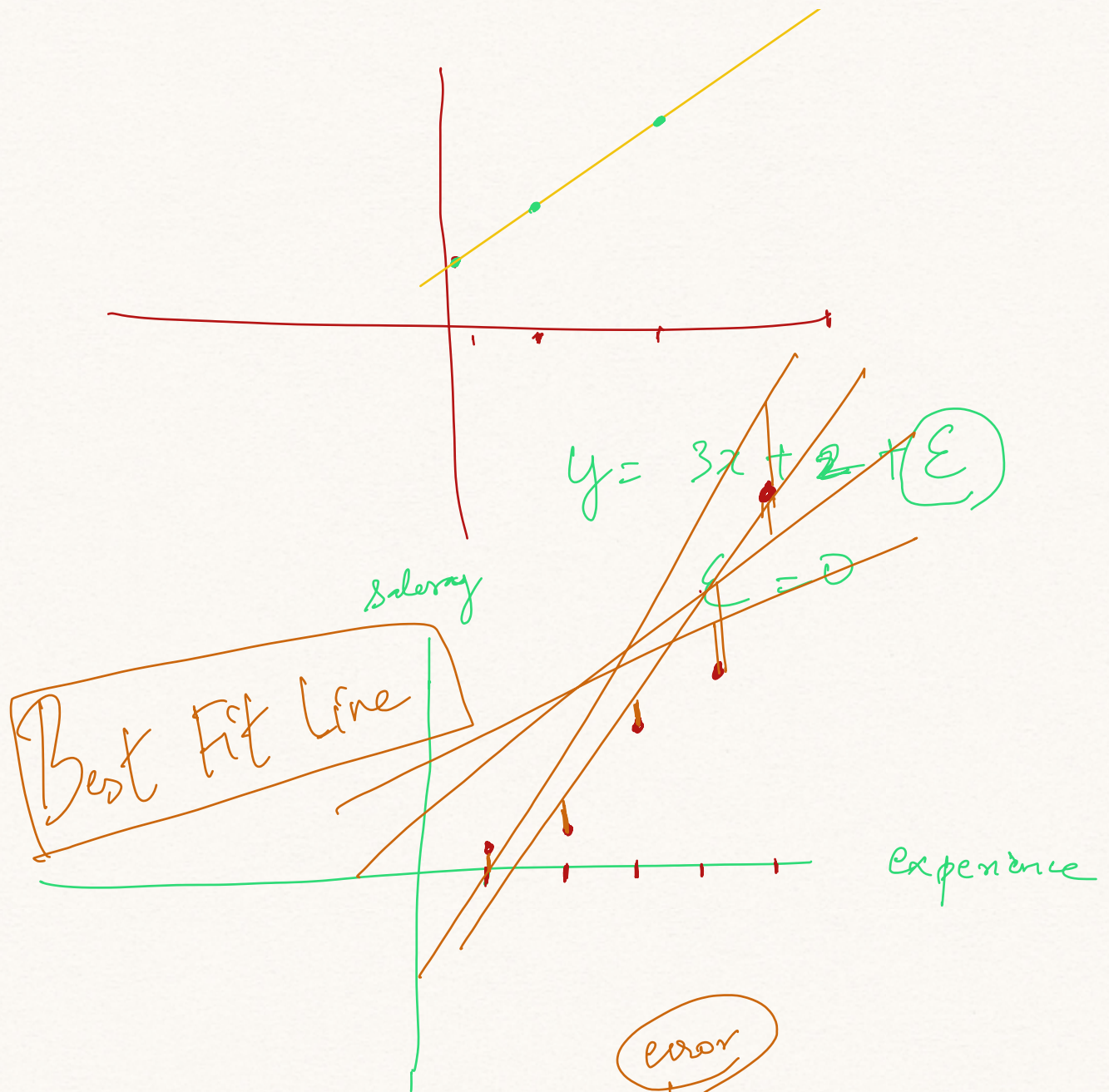
$$y = mx + b$$

$$y = ax + b$$

$$y = mx + c$$

$$y = b_1 x + b_0$$

$$y = \theta_1 x + \theta_0$$



$$y = 3x + 2 + (\epsilon)$$

$$\epsilon = 0$$

$$y = \underbrace{mx + b}_{\text{linear regression}} + (\epsilon)$$

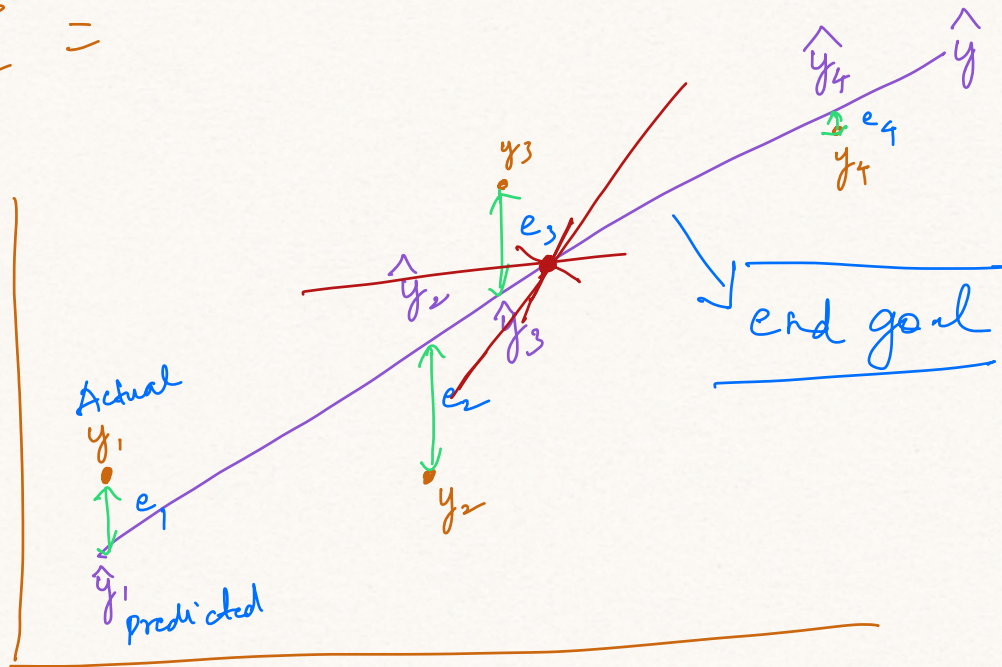
linear regression

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Objective to find m and b where

Σ is as minimum as possible

$\Sigma =$



$$\text{Mean Square Error (MSE)} = \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{n}$$

may end up zero

Find m and b where MSE is minimal

Slope

Intercept

Rule of thumb

The best fit line will cross the
Centroid

$$(x_1, y_1) \quad (x_2, y_2) \quad (x_3, y_3) \quad (x_4, y_4)$$

$$\left(\frac{x_1 + x_2 + x_3 + x_4}{4}, \frac{y_1 + y_2 + y_3 + y_4}{4} \right)$$

Linear Algebra ✓

$$\begin{array}{r} x + 2y = 5 \\ (7) \quad x + 3y = 10 \\ \hline -y = -5 \\ y = 5 \end{array}$$

x , and y $y = 5$

$$x + 2y = 5$$

$$\begin{array}{r} x + 2y + 3z + 5k = 6 \\ x + y - z + k = 10 \\ 2x + 3y + z + 2k = 15 \end{array}$$

$y = 5$ and $z = 1$

$$x + 2(5) = 5$$

$$x + 10 = 5$$

$$\boxed{x = -5}$$

$$x + 2y = 5$$

$$2x + y = 10$$

$$\begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 5 \\ 10 \end{bmatrix}$$

$$\boxed{X \theta = y}$$

$$\cancel{X^T \cdot X} \theta = \cancel{y} \cancel{X^T}$$

$$\theta = \frac{1}{X^T X} y X^T$$

Linear
Algebra

$$\theta = (X^T X)^{-1} y^T X^T$$

Normal Equation

X	Y
1	2
2	3
3	5

$$y = \underline{mx} + \underline{b}$$

$$X = \begin{bmatrix} 1 & x_1 \\ 1 & x_2 \\ 1 & x_3 \end{bmatrix}$$

$$y = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & x_1 \\ 1 & x_2 \\ 1 & x_3 \end{bmatrix} \begin{bmatrix} b \\ m \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 \\ 1 & 2 \\ 1 & 3 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} b \\ m \end{bmatrix} = \begin{bmatrix} 2 \\ 3 \\ 5 \end{bmatrix}$$

$$X \theta = Y$$

multiply $X^T = X$ transpose in both side

$$\begin{bmatrix} 1 & 1 \\ 1 & 2 \\ 1 & 3 \end{bmatrix}^T \Rightarrow \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 3 \end{bmatrix} X^T$$

$$(X^T \cdot X) \theta = y \cdot X^T$$

$$\theta = \frac{1}{(X^T \cdot X)} \cdot (y \cdot X^T)$$

$$\frac{1}{5} = 5^{-1}$$

1×2

$2 \times$

$$\theta \Rightarrow (\underline{X^T \cdot X})^{-1} (X^T \cdot y)$$

$$X = \begin{bmatrix} 1 & 1 \\ 1 & 2 \\ 1 & 3 \end{bmatrix}$$

$$X^T = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 3 \end{bmatrix}$$

$$y = \begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$$

$$\theta = \begin{bmatrix} b \\ m \end{bmatrix}$$

$$\left(\begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 3 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & 2 \\ 1 & 3 \end{bmatrix} \right)^{-1}$$

2×3

$$\left(\begin{array}{ccc|c} 1 & 1 & 1 & 2 \\ 1 & 2 & 3 & 3 \\ & & & 5 \end{array} \right)$$

$$3 \times 2 \quad 2 \times$$

$$\text{max } p \times q$$

$$\begin{bmatrix} 1+1+1 & 1+2+3 \\ 1+2+3 & 1+4+9 \end{bmatrix}$$

$$\begin{bmatrix} 3 & 6 \\ 6 & 14 \end{bmatrix}$$

$$\begin{array}{r} 1 \\ 4 \times 2 = 8 \\ \hline 6 \end{array}$$

$$\frac{1}{|A|} \quad (\text{adj } A)$$

$$\frac{1}{6} \quad \begin{bmatrix} 14 & -6 \\ -6 & 3 \end{bmatrix} \quad \begin{matrix} \leftarrow \\ \leftarrow \end{matrix} \quad \begin{matrix} 2 \times 2 \\ 2 \times 2 \end{matrix}$$

$$\begin{bmatrix} 2.3 & -1 \\ -1 & 0.5 \end{bmatrix}$$

X	Y	\hat{Y}	$(y - \hat{y})$
1	2	1.83	0.17
2	3	3.33	-0.33
3	5	4.83	0.17

$$(y - \hat{y})^2$$

$$0.0289$$

$$0.1089$$

$$0.0289$$

$$SSE \Rightarrow \sum (y - \hat{y})^2 = 0.1667$$

$$MSE = \frac{\sum (y - \hat{y})^2}{n} = \frac{0.1667}{3}$$

$$MSE \boxed{= 0.05}$$