

## Chapter-18

① Supervised Learning: Supervised learning is a type of machine learning where the model is trained using labeled data - that means each input has a corresponding correct output (label).

labeled data example

customer-id	Age	gender	Income (Lakh)	years-employed (years)	total Lakh
1021210	27	Female	1 lakh	1	10
20306212	28	male	2 lakh	10	20

Types of algorithm used in supervised learning:

Classification

① Logistic Regression

② K-Nearest Neighbour (KNN)

③ Decision Tree Classifier

④ Random Forest classifier

⑤ Naive Bayes classifier

⑥ SVM (support vector machine)

⑦ Gradient Boosting (XGBoost, LightGBM, CatBoost)

⑧ NN (ANN, CNN, RNN)

Regression

① Linear regression

② Ridge / Lasso Regression

③ Polynomial regression

④ Decision tree Regressor

⑤ Random Forest

⑥ SVR ⑦ XGBoost, LightGBM

Unsupervised learning      Unsupervised learning is a type of machine learning where model is trained using unlabeled data - meaning there is no pre-defined output.

Examples:

- (i) Grouping customer behavior (Clustering)
- (ii) Reducing dimensions for visualization (PCA)

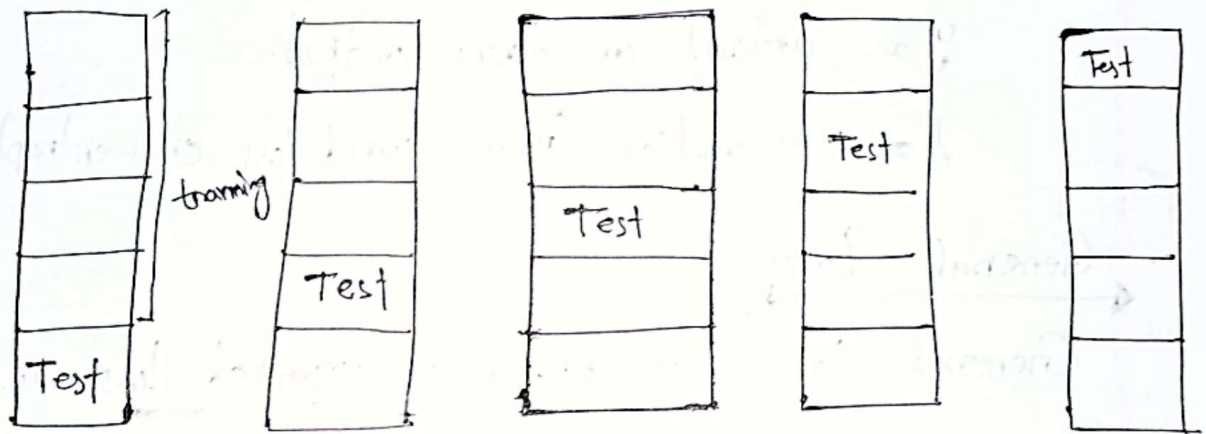
Some examples of unsupervised learning algorithms

- (i) K-mean clustering
- (ii) Hierarchical clustering
- (iii) DBSCAN (Density-Based Spatial clustering)
- (iv) GMM (Gaussian Mixture Models)

## K-Fold cross validation:

K-Fold Cross Validation is a model evaluation technique used to how well a machine learning model perform on unseen data.

It works dividing the dataset into  $K$  equal folds (parts) then training and testing the model  $K$ -times, each time using a different fold as the test set and the remaining folds as the training set. Let's assume,  $K=5$  then



Dataset



Accuracy

$a_1$

$a_2$

$a_3$

$a_4$

$a_5$

$$K\text{-Fold - cross validation score} = \frac{a_1 + a_2 + a_3 + a_4 + a_5}{5}$$



Empirical loss - also called: training loss:

Empirical loss is the average loss of a model over the training dataset. It measures how well the model fits the training data.

$$L_{\text{empirical}} = \frac{1}{n} \sum_{i=1}^n l(f(x_i), y_i)$$

$n$  = number of training sample / batch size

$f(x_i)$  = model prediction for input  $x_i$

$y$  = actual or true output.

$l$  = loss function (mean-squared loss, cross-entropy loss).

General Loss:

General loss also known as expected loss on generalization. General loss is the expected value of the loss over the entire data distribution, including unseen and future data. It measures how well a model generalizes or performs to new, unseen dataset.

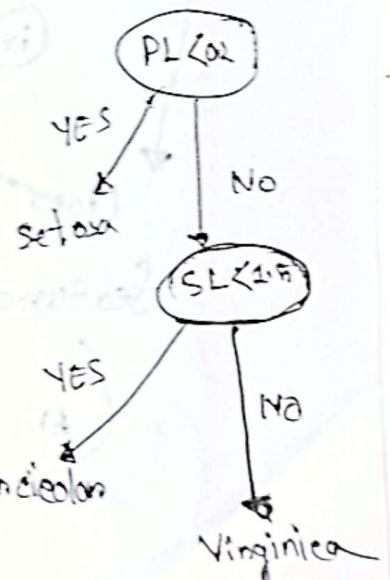
$$L_{\text{general}} = \mathbb{E}_{(x,y) \sim P_{\text{data}}} [l(f(x), y)]$$

## Difference

Aspect	Empirical loss	General (Expected) Loss
Based on	Training data	
Measures	Model fit training data	
Formula	$\frac{1}{n} \sum_{i=1}^n l(f(x_i), y_i)$	$E_{(x,y)} [l(f(x), y)]$
Depends on	The specific training data	Real-world data distribution
Risk	Low empirical loss may cause overfitting	Low general loss means good generalization

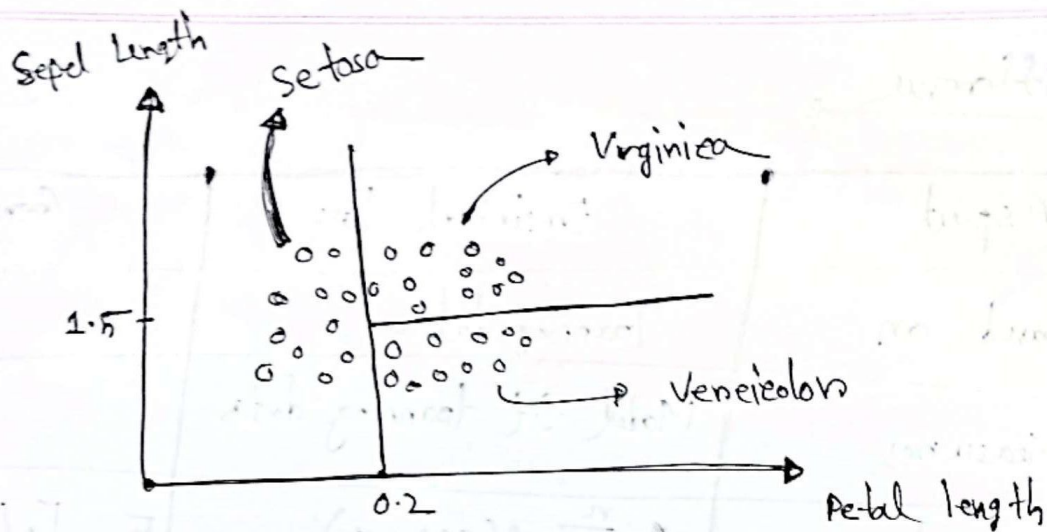
## Decision Tree (classification Problem)

Petal Length (PL)	Sepal Length (SL)	Type
1.34	0.34	Setosa
3.45	1.45	Versicolour
1.67	0.98	Setosa
2.56	1.79	Versicolour
3.00	1.13	Versicolour
1.3	0.28	Setosa



Decision tree model is nothing more than a collection of nested if-else statement.



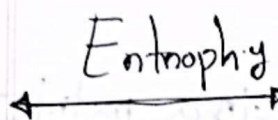


Decision tree steps

- (i) Dataset
- (ii) Best features (Previous problem 1st PL than SL)
- (iii) Split data base on best features
- (iv) Repeat (1, 2, 3)

Now our question is how to find the best features?

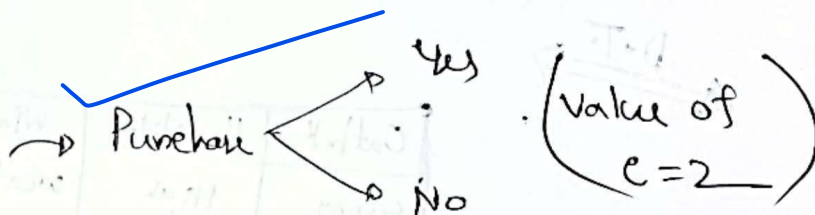
ANS [with entropy and information gain.]


 Entropy is nothing but the measure of disorderness or the measure of impurity. The mathematical formula of entropy is

$$E(s) = \sum_{i=1}^c -P_i \log_2 P_i$$

$P_i$  is the frequency probability of an element/class in our data.

Salary	Age	Purchase
20000	21	Yes
10000	45	No
60000	27	Yes
15000	31	No
12000	18	No



$$E(d) = \sum_{i=1}^2 -P_i \log_2 P_i$$

$$= -P_{Yes} \log_2(P_{Yes}) - P_{No} \log_2(P_{No})$$

$$= -\left(\frac{2}{5}\right) \log_2\left(\frac{2}{5}\right) - \left(\frac{3}{5}\right) \log_2\left(\frac{3}{5}\right)$$

$$= 0.97$$

## Information Gain

Information gain is a metric used to train Decision Trees. Information gain is used in decision trees to find the best attributes/column to split the data at each node. Formula

$$\text{Information Gain} = \text{Entropy} - \text{Weighted Entropy}$$

↓  
Parent's on target column entropy  
eg. 0.9, 0.1

D.T.

Outlook	Humidity	Wind	Play tennis
sunny	High	weak	No
sunny	High	strong	No
Rain	High	strong	No
Rain	Normal	weak	Yes
Rain	Normal	strong	No
sunny	Normal	strong	Yes



Step: 1

$$\text{entropy of PlayTennis} = -P_{\text{No}} \log_2 P_{\text{No}} - P_{\text{Yes}} \log_2 P_{\text{Yes}}$$

$$= -\frac{4}{6} \log_2 \left(\frac{4}{6}\right) - \frac{2}{6} \log_2 \left(\frac{2}{6}\right) = 0.92$$

1. outlook column

$$E_{\text{sunny}} = -\frac{2}{3} \log_2 \left(\frac{2}{3}\right) - \frac{1}{3} \log_2 \left(\frac{1}{3}\right) = 0.92$$

$$E_{\text{rain}} = -\frac{2}{3} \log_2 \left(\frac{2}{3}\right) - \frac{1}{3} \log_2 \left(\frac{1}{3}\right) = 0.92$$

$$\text{Weighted } E = \left(\frac{3}{6} \times 0.92\right) + \left(\frac{3}{6} \times 0.92\right) = 0.92$$

$$IG_{\text{outlook}} = 0.92 - 0.92 = 0$$

2. Humidity

$$E_{\text{high}} = -\frac{3}{3} \log_2 \left(\frac{3}{3}\right) - \frac{0}{3} \log_2 \left(\frac{0}{3}\right) = 0$$

$$E_{\text{normal}} = -\frac{2}{3} \log_2 \left(\frac{2}{3}\right) - \frac{1}{3} \log_2 \left(\frac{1}{3}\right) = 0.92$$

$$\text{Weighted } E = \left(\frac{3}{6} \times 0\right) + \left(\frac{3}{6} \times 0.92\right) = 0.46$$

$$IG_{\text{humidity}} = 0.92 - 0.46 = 0.46$$

3. Wind

$$E_{\text{weak}} = -\frac{1}{2} \log_2 \left(\frac{1}{2}\right) - \frac{1}{2} \log_2 \left(\frac{1}{2}\right) = 1$$

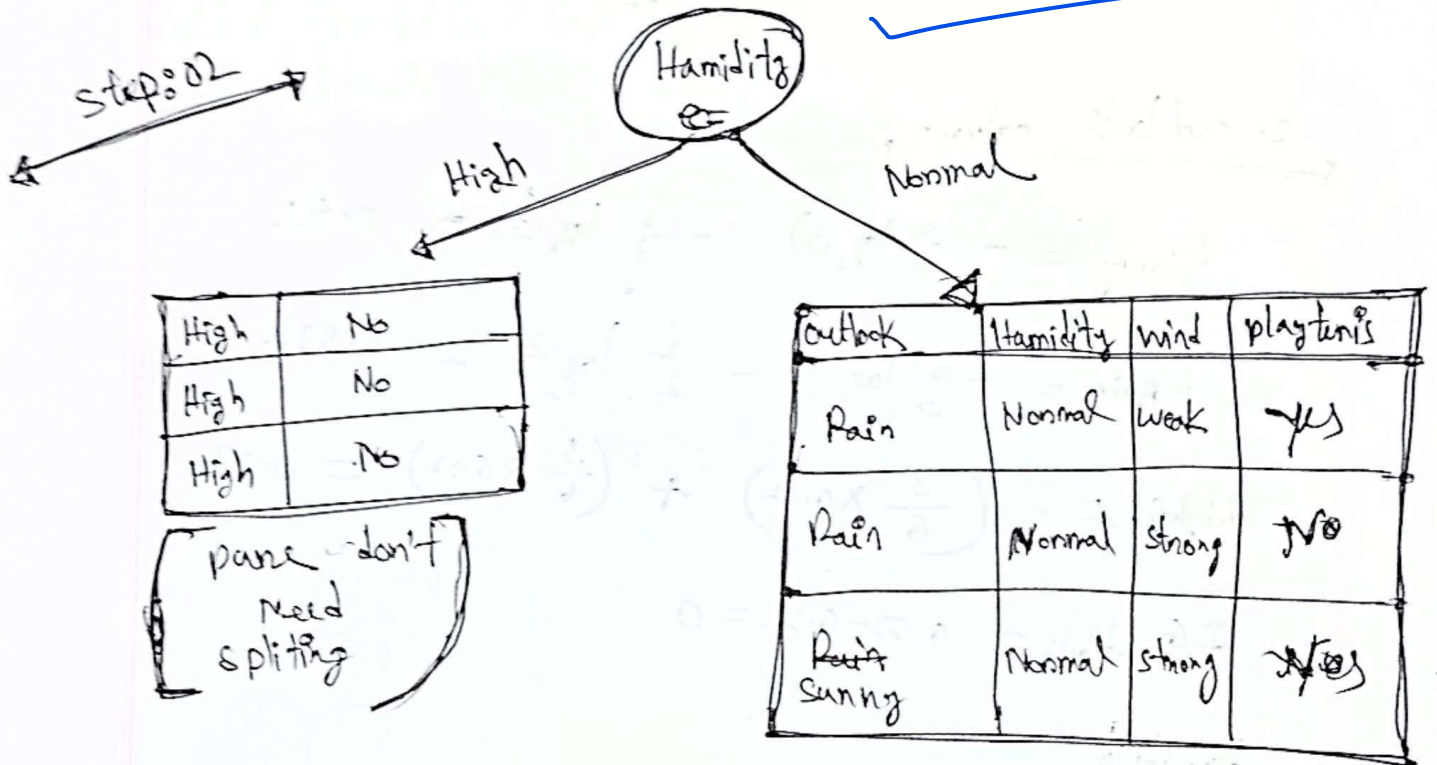
$$E_{\text{no}} = -\frac{3}{4} \log_2 \left(\frac{3}{4}\right) - \frac{1}{4} \log_2 \left(\frac{1}{4}\right) = 0.811$$

$$\text{Weighted } E = \frac{2}{6} \times 1 + \frac{4}{6} \times 0.811 = 0.874$$

$$IG_{\text{wind}} = 0.92 - 0.874 = 0.046$$

$$IG_{\text{Humidity}} > IG_{\text{wind}} > IG_{\text{outlook}}$$

∴ Root Node: (Humidity)



$$E_{\text{normal}} = 0.92 \quad (\text{from previous})$$

Winds:

$$E_{\text{strong}} = 0 - \frac{1}{2} \log \frac{1}{2} - \frac{1}{2} \log \frac{1}{2} = 1$$

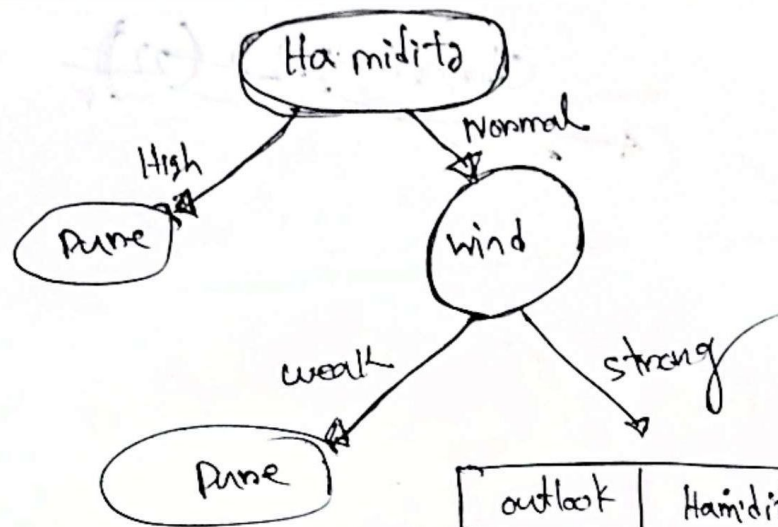
$$E_{\text{weak}} = 0$$

$$\text{weighted entropy} = \left( \frac{1}{3} \times 0 \right) + \left( \frac{2}{3} \times 1 \right) = 0.67$$

$$IG_{\text{wind}} = 0.92 - 0.67 = 0.25$$

(highest  $IG_{\text{Grain}}$ ) [split base on this]

value may be same take anyone



outlook	Humidity	wind	play
Rain	Normal	strong	No
Sunny	Normal	strong	Yes

