

* Simplify the Boolean function

$F(w, x, y, z) = \sum (1, 3, 7, 11, 15)$ which has don't care conditions $d(w, x, y, z) = \sum (0, 2, 5)$ and show "An expression with the minimum number of literals is not necessarily unique".

Sub $w'x'w = 0$ $xy'x = 0$ $xyz'x = 0$ $xyz'x = 0$

w\y\z	z			
	00	01	11	10
00	X	1	1	X
01		X	1	
11			1	
10			1	

$$F = w'z + yz$$

We can also find another minimal expression by choosing different grouping

w\y\z	z			
	00	01	11	10
00	X	1	1	X
01		X	1	
11			1	
10			1	

$$F = w'x' + yz$$

Since, we have two different minimal expressions with the same numbers of literals, this demonstrates that "An expression with the minimum number of literals is not necessarily unique".

$$\therefore F = w'z + yz \text{ or } F = w'n' + yz$$

Both are valid minimal expressions.

X	1	1	X
	1	X	
	1		
	1		