

Grid Cell Encoder

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Abstract—The HTM Spatial Pooler (operating at L2), with the extended Homeostatic Plasticity Controller (HPC) generates the Sparse Distributed Representation (SDR) for the input. But this SDR pattern is stable for a while, then changes exactly for only one input in one learning iteration, causing momentary “instability”. Thus, this problem is hereafter referred to as the “one-cycle problem” and this paper discusses what causes the one cycle problem and how it is remedied. The causes are examined from various angles – is it just the wrong feeding of values to configuration parameters for the Spatial Pooler or HPC? Or is it a fundamental execution issue? (Abstract)

Keywords—Homeostatic Plasticity, Spatial Pooler, instability, boosting, SDR, stability, Scalar Encoder

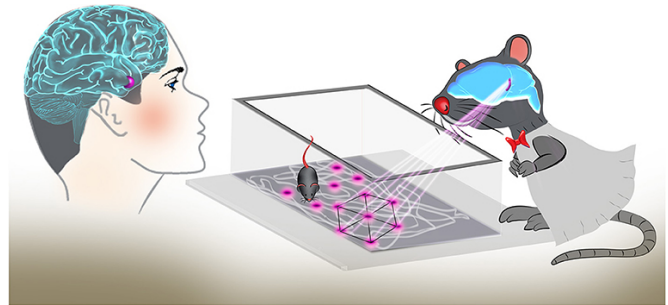


Figure 3

I. INTRODUCTION

Navigation in the environment, getting from one place to another, is one of the most fundamental and vital skills in the animal kingdom, and for humans, too. The brain has a built-in navigation system that is responsible for representing the location in the environment and for orienting so that one can successfully get from one place to another. This mental representation of the environment is often called a cognitive map. To navigate successfully, an animal needs to create an internal “cognitive map” of the outside environment. This is performed by a specific system in the brain, containing several brain regions and various cell types, each with its unique role in navigation. One of such special system of nerve cells in the brain is called grid cells.

The grid cell system is located in the middle of the brain, a bit below the ear level, in a deep brain area called the entorhinal cortex (Figure 3, purple area), which is located close to the hippocampus. A grid cell becomes active at many locations in the environment (Figure 3). According to the findings, these locations form a symmetric and extremely accurate crystal like pattern, characterized by equilateral triangles connection the centers of nearby locations. These locations, called coordinates, form a hexagonal (six-sided polygon) grid.

Each grid cell forms a unique pattern of coordinates, which is shifted with respect to the coordinates formed by other nearby grid cells. In this way, the whole environment is “filled” with grid patterns (Figure 4A). Using only one grid cell you cannot know where the animal is, because each grid cell is active in multiple locations, forming a grid. But, because of the shift in location between different grid cells,

and because of the varying scales of the grids (Figure 4C), it is possible to define the animal’s current location with great accuracy, using the overlapping grids of several cells³. These grid patterns serve as an internal map of coordinates in the brain and can also be used for measuring the distance between different points in space, a critical requirement for navigation (Figure 4B).

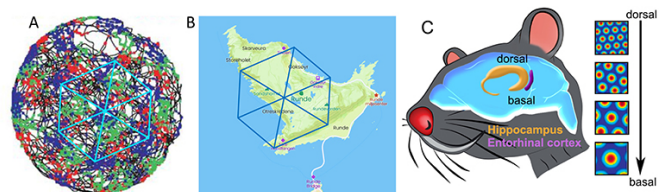


Figure 4B

Grid cells produce internal coordinate maps that allow an animal to navigate from one location to another. The grid cells work in unison with place cells and with other cell types, such as head direction cells and speed cells. This navigation system also integrates information from the senses, to calibrate the internal maps with the environment. This whole navigation system in the brain allows us to perform complex navigation tasks in a smooth and seamless manner.

A grid cell module is simply a group of grid cells sharing the same projection properties onto space. Using many grid cells, we can cover a patch of space and use it to tile over a larger space.

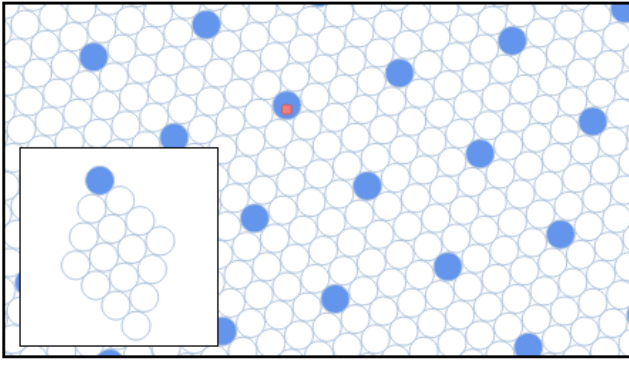


Figure 3

In figure 3, the overlay on the bottom left shows all 16 grid cells within the module, and which one is currently active in response to an object's location (red dot) in space. One grid cell module can tell us a lot more about an object's location in space than a lone grid cell. The grid cell module can show one must be within one of many locations moving across the space. But it cannot decipher an exact location. So one grid cell module is not enough to uniquely map space. But when we use many grid cell modules together, we can map a virtually infinite amount of space.

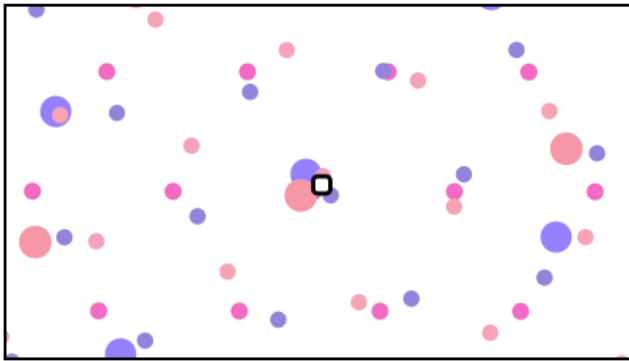


Figure 4: 6 Grid cell modules

When grid cell modules work together, they can uniquely map space by combining their representations. Each cell in a grid cell module is like a bit in a Sparse Distributed Representation (SDR). As shown in Figure 4, this space is being mapped with 6 grid cell modules each with 16 cells (96 grid cells).

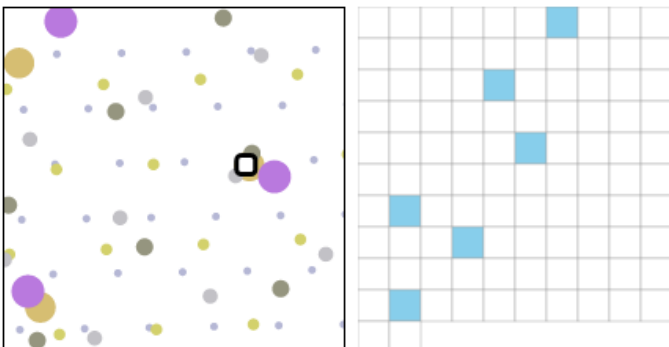


Figure 5: Grid Cell Modules as SDR

Grid cell module activations are SDRs (Figure 5), and can be used to represent semantic location information in many ways in the brain. Many grid cell modules' SDR representations can be used to create unique binary representations of space.

II.METHODS

A. GridCell Encoder constructor

```
public GridCellEncoder(int size, double sparsity = 0.15)
{
    this.size = size;
    this.sparsity = sparsity;

    // should be passed as input
    for (var i = 0; i < 5; i++)
    {
        periods[i] = 6 * Math.Pow(Math.Pow(2, 0.5), i);
    }

    var partitions = np.linspace(0, size, periods.Length + 1);
    for (var i = 0; i < partitions.size - 1; i++)
    {
        this.partitions.Add(new int[2] {
            (int) ((float) partitions[i].GetValue()), (int)
            ((float) partitions[i+1].GetValue()),
        });
    }

    // Assign each module a random offset and orientation.
    var rng = np.random.RandomState(23);
    offsets_ = rng.uniform(0, periods.Max() * 9, new int[]
    { size, 2 });

    foreach (var period in periods)
    {
        var angle = rng.uniform(0, 1, np.float32) * 2 * Math.PI;
        var c = Math.Cos(angle);
        var s = Math.Sin(angle);

        Tuple<double, double>[] sdist = {
            Tuple.Create(c, -s),
            Tuple.Create(s, c)
        };

        rotationMatrix.Add(sdist);
    }
}
```

The constructor takes two arguments as input. The size argument defines the length of the SDR whereas the sparsity refers to the percentage of neurons being active at any given time.

The periods array is a list of distances. The length of this list defines the number of distinct grid cell modules. In the sample code the periods is of length 5 which represents a total of 5 grid cell modules. The period of a module is the distance between the centers of a grid cell receptive fields.

Each grid cells modules are of the same size but are slightly of different orientation and offsets. The "offsets" property is a two dimensional (size, 2) list of random values generated between 0 and maximum value in the periods list. Each row in the offset represents the x and y offset for the location.

The “rotationMatrix” contains the orientation angle for the each grid modules. For 5 grid modules, the “rotationMatrix” will be a size of 5.

B. Grid Cell Encoder Algorithm

Step 1: Calculate displacement

- Apply offsets to the location i.e. (x, y)
- Then, apply rotation

Step 2: Find radius of grid cell in each grid module

Step 3: Convert the displacement into and out of hexagonal coordinates

Step 4: Calculate difference between the result of Step 3 with Step 1.

Step 5: Find the distance (hypotenuse) between the location (result from Step 4) and the RF center.

Step 6: Get SDR by activating the closest grid cells in each module based on sparsity.

a) Step 1: Calculate displacement

```
var location = np.ndarray((1,2));
location[0][0] = x;
location[0][1] = y;

var displacement = location - offsets_;

for (var i = 0; i < partitions.Count; i++) {
    var start = partitions[i][0];
    var stop = partitions[i][1];

    var r = rotationMatrix[i];

    var rr = np.ndarray((2,2));
    rr[0][0] = r[0].Item1;
    rr[0][1] = r[0].Item2;
    rr[1][0] = r[1].Item1;
    rr[1][1] = r[1].Item2;

    displacement["{start}:{stop}"] =
    rr.dot(displacement["{start}:{stop}"].T).T;
}
```

The x and y are the location for which the SDR is to be calculated. A 1x2 NDAarray (location) is created from the x and y coordinate. As resulted the “offsets” which is a (size x 2) NDAarray can be easily subtracted from the location.

The partition groups the displacement as per the number of grid cell modules. For example, for a SDR of size 100 and 5 grid cell modules, there will be 100 displacements and 5 partitions in the range of 0-20, 20-40, 40-60, 60-80 and 80-100. So, displacement from the range 0-20 belongs to the first grid cell module, displacement from the range 20-40 belongs to the second grid cell module and so on. So the appropriate rotation is applied to the each cells in the particulate grid cell module.

b) Step 2: Find radius of grid cell in each grid module

```
var radius = np.empty(size);
for (var i = 0; i < periods.Length; i++) {
    var start = partitions[i][0];
    var stop = partitions[i][1];

    radius["{start}:{stop}"] = periods[i] / 2;
}
```

For each grid cell module the radius is calculated which is the half of the period value of that module.

c) Step 3: Convert the displacement into and out of hexagonal coordinates

```
NDAarray nearestArray = np.ndarray((size, 2));
for (var i = 0; i < size; i++)
{
    var grid = new
    HexagonalGrid(HexagonalGridType.PointyEven,
    (float)radius[i].GetValue<Double>());

    var x = displacement[i][0].GetValue<Double>();
    var y = displacement[i][1].GetValue<Double>();

    var nearest = grid.ToPoint2(grid.ToCubic(x, y));
    nearestArray[i][0] = nearest.X;
    nearestArray[i][1] = nearest.Y;
}
```

Each of the displacement (x,y) is converted to cubic and back to (x,y) which rounds to the nearest hexagonal center.

d) Step 4: Calculate difference between the result of Step 3 with Step 1.

```
var nearestMinusDisplacement = nearestArray -
displacement;
```

e) Step 5: Find the distance between the result from Step 4 and the hexagonal center

```
var distances = new double[size];
for (var i = 0; i < size; i++)
{
    var x = nearestMinusDisplacement[i][0];
    var y = nearestMinusDisplacement[i][1];
    var hypot = Math.Sqrt(Math.Pow(x, 2) +
    Math.Pow(y, 2));

    distances[i] = hypot;
}
```

The hypotenuse is calculated ($h = \sqrt{p^2 + b^2}$) where h gives the distance from the point to the center of the hexagon and p and b is the value from the Step 4.

f) Step 6: Get SDR by activating the closest grid cells in each module based on sparsity

```
var activatedCells = new List<int>();
foreach (var partition in partitions)
{
    var start = partition[0];
    var stop = partition[1];
    var z = (int) (Math.Round(sparsity * (stop - start)));

    var indexes = distances[start..stop]
        .Select((x, i) => new KeyValuePair<double, int>(x, i))
        .OrderBy(x => x.Key)
        .Take(z)
        .Select((x, i) => x.Value + start)
        .ToList();

    activatedCells.AddRange(indexes);
}

activatedCells.Sort();
```

The “start” and “stop” variable gives the range to get distances (from step 5) for each module which is then sorted in ascending order of value and the first “z” number of distances which is calculated based on sparsity is taken. The index of these selected distances is the active index in the SDR.

III.RESULTS

For this experiment, we take three input coordinates and generate the resulting SDR. We also find the similarity matrix to find the similarity between these computed SDR. The size of the SDR is 100 for this experiment.

A. SDR Output

```
var coordinates = new double[,] {
    {100, 100},
    {100, 100.50},
    {5000, 400}
};
```

a) 100,100

The SDR for the coordinate (100,100) is as follow:

1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1,
0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 1, 0, 0, 0, 0,
0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0,
1, 0, 0, 0, 0,

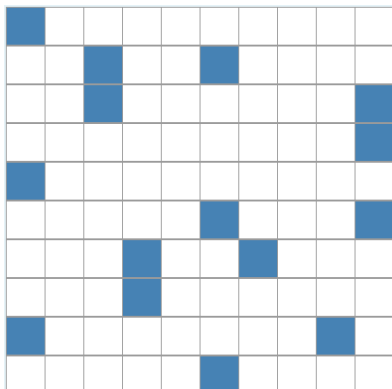


Figure X: SDR visualization for coordinate 100,100

b) 100,100.50

The SDR for the coordinate (100,100.50) is as follow:

1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1,
0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 1, 0, 0, 0, 0,
0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0,
1, 0, 0, 0, 0,

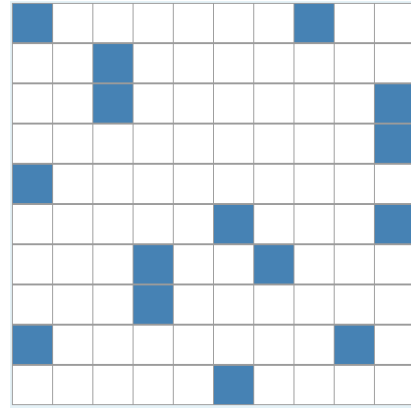


Figure XX: SDR visualization for coordinate 100,100.5

a) 5000,400

The SDR for the coordinate (100,100.50) is as follow:

1, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0,
1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0,

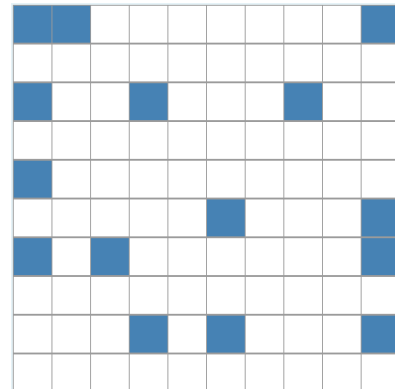


Figure XX: SDR visualization for coordinate 5000, 400

B. Similarity Matrix

Coordinates (x,y)	100 x 100	100 x 100.5	5000 x 400
100 x 100	100	93.33	26.67
100 x 100.5	93.33	100	26.67
5000 x 400	26.67	26.67	100

From the similarity matrix of the resulting SDR for three coordinates in this experiment we can observe that the similarity for the coordinate 100x100 and 100x100.5 is quite similar at 93.33%.

The similarity of the SDR 5000x400 with respect to the other two coordinates is at 26.67%.

IV. CONCLUSION

Thus, one part of the problem with the Homeostatic Plasticity Controller arises due to threading issues. In the future, speed will be of the utmost importance and more modules like the initialization of Spatial Pooler will be multithreaded too. While undertaking such steps, behaviour of threads in sync with each other must be taken care of to avoid problems.

However, there is another problem that could arise due to threading that is completely from another angle. Random number generators are only pseudo random and this is because, the CPU clock has finite resolution. The synapses between the Columns and the Input bits are fixed in a random fashion. When there is a large number of inputs

(>100) and multiple threads running simultaneously to create a random connection, it must be ensured that threads do not access the same random value, that is tied to the same clock instance. As shown in [13], creating different Random objects in close succession creates random number generators that produce identical sequences of random numbers. Ways to avoid this can be found in detail in [13] and can be taken advantage of in future parallel implementations.

REFERENCES

The main source that has served as ground zero is the paper mentioned in [1].

Further References [2],[5],[6],[9],[10] contain source code for the experiments stated above and also some of them [8] provide more information on some functions in C#. Whereas the references [3],[4],[7] are detailed observations made on each module.

1. *How grid cells map space* (2021) Numenta. Available at: <https://www.numenta.com/blog/2018/05/25/how-grid-cells-map-space/> (Accessed: November 21, 2022).
2. Authors Dori Derdikman *et al.* (no date) *How do we find our way? grid cells in the brain*, *Frontiers for Young Minds*. Available at: <https://kids.frontiersin.org/articles/10.3389/frym.2021.678725> (Accessed: November 21, 2022).
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