# Ch.4: User input and error handling

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# Programs until now hardcode input data

$$y = v_0 t - 0.5 g t^2$$

```
v0 = 5
g = 9.81
t = 0.6
y = v0*t - 0.5*g*t**2
print y
```

### Note

- Input data (v<sub>0</sub>, t) are hardcoded (explicitly set)
- Changing input data requires editing
- This is considered bad programming (because editing programs may easily introduce errors!)
- Rule: read input from user avoid editing a correct program

# How do professional programs get their input?

- Consider a web browser: how do you specify a web address?
   How do you change the font?
- You don't need to go into the program and edit it...

# How can we specify input data in programs?

- Hardcode values
- Ask the user questions and read answers
- Read command-line arguments
- Read data from a file

# Getting input from questions and anwsers

```
Sample program:
    C = 21; F = (9.0/5)*C + 32; print F
```

Idea: let the program ask the user a question "C=?", read the user's answer, assign that answer to the variable C.

```
C = raw_input('C=?')  # C becomes a string
C = float(C)  # convert to float so we can compute
F = (9./5)*C + 32
print F
```

# Testing:

```
Terminal> python c2f_qa.py
C=? 21
69.8
```

# Another example: print the n first even numbers

```
n = int(raw_input('n=?'))
for i in range(2, 2*n+1, 2):
    print i

# or:
print range(2, 2*n+1, 2)

# or:
for i in range(1, n+1):
    print 2*i
```

# Command-line arguments are words written after the program name

# Examples on command-line arguments:

```
Terminal> python myprog.py arg1 arg2 arg3 ...
Terminal> cp -r yourdir ../mydir
Terminal> ls -l
```

Unix programs (rm, 1s, cp, ...) make heavy use of command-line arguments, (see e.g. man 1s). We shall do the same.

# How to use a command-line argument in our sample program

```
C = 21; F = (9.0/5)*C + 32; print F
```

The user wants to specify C as a command-line argument after the name of the program when we run the program:

```
Terminal> python c2f_cml_v1.py 21
```

Command-line arguments are the "words" after the program name, and they are stored in the list sys.argv:

```
C = float(sys.argv[1]) # read 1st command-line argument
print F
```

# Command-line arguments are separated by blanks

```
Here is another program print_cml.py:
```

import sys; print sys.argv[1:]

### Demonstrations:

```
Terminal> python print_cml.py 21 string with blanks 1.3
['21', 'string', 'with', 'blanks', '1.3']
Terminal> python print_cml.py 21 "string with blanks" 1.3 ['21', 'string with blanks', '1.3']
```

Note 1: use quotes, as in "string with blanks", to override the rule that command-line arguments are separate by blanks. Note 2: all list elements are surrounded by quotes, demonstrating that command-line arguments are strings.

# The magic eval function turns a string into live code

eval(s) evaluates a string object s as if the string had been written directly into the program

```
>>> s = '1+2'
>>> r = eval(s)
>>> r
>>> type(r)
<type 'int'>
>>> r = eval('[1, 6, 7.5] + [1, 2]')
>>> r
[1, 6, 7.5, 1, 2]
>>> type(r)
<type 'list'>
```

# Note: be careful with eval and string values

```
We want r = 'math programming'. Writing just
```

r = eval('math programming')

is the same as writing

r = math programming

which is an invalid expression and illegal syntax.

Remedy: must put the string inside quotes:

```
s = "'math programming'"
r = eval(s)
                                # r becomes 'math programming'
```

# With eval, a little program can do much...

# Program add\_input.py

```
i1 = eval(raw_input('Give input: '))
i2 = eval(raw_input('Give input: '))
r = i1 + i2
print '%s + %s becomes %s\nwith value %s' %
         (type(i1), type(i2), type(r), r)
```

## We can add integer and float:

```
Terminal> python add_input.py
   operand 1: 1
operand 2: 3.0
<type 'int'> + <type 'float'> becomes <type 'float'>
with value 4
or two lists:
```

# This great flexibility also quickly breaks programs... Terminal> python add\_input.py operand 1: (1,2) operand 2: [3,4] Traceback (most recent call last): File "add,input.py", line 3, in <module> r = ii + i2 TypeError: can only concatenate tuple (not "list") to tuple Terminal> python add\_input.py operand 1: one Traceback (most recent call last): File "add,input.py", line 1, in <module> ii = eval (rax\_input('operand 1: ')) File "sdr(rax\_input('operand 1: ')) File "string>", line 1, in <module> NameError: name 'one' is not defined Terminal> python add\_input.py operand 1: 'Hello, World!' Traceback (most recent call last): File "add\_input.py", line 3, in <module> r = ii + i2 TypeError: unsupported operand type(s) for +: 'int' and 'str'

```
• eval(s) evaluates an expression s
• eval('r = 1+1') is illegal because this is a statement, not only an expression
• ...but we can use exec to turn one or more complete statements into live code:

statement = 'r = 1+1'  # store statement in a string exec(statement)  # prints 2

For longer code we can use multi-line strings:

somecode = ''' def f(t):
    term1 = exp(-2*t)*sin(w1*x)
    term2 = 2*sin(w2*x)
    return term1 + term2
'''
exec(somecode) # execute the string as Python code

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```

```
exec can be used for building a function at run-time
   Embed user's formula in a Python function:
       formula = raw_input('Write a formula involving x: ')
      code = """
def f(x):
      return %s
       exec(code) # turn string formula into live function
       while x is not None:
          x = eval(raw_input('Give x (None to quit): '))
          if x is not None:
              y = f(x)
              print 'f(%g)=%g' % (x, y)
   While the program is running, the user types a formula, which
   becomes a function, the user gives x values until the answer is
   None, and the program evaluates the function f(x). Note: the
   programmer knows nothing about the user's choice of f(x) when
   she writes the program (!).
```

```
It is common for programs to read formulas and turn them into functions so we have made a special tool for this purpose:

>>> from scitools.std import StringFunction
>>> formula = 'exp(x)*sin(x)'
>>> f = StringFunction(formula)
>>> f(0)
0.0
0.0
>>> f(pi)
2.8338239229952166e-15
>>> print str(f)
exp(x)*sin(x)

The function can also have parameters: g(t) = Ae^{-at}\sin(\omega x)
g = StringFunction('Aeexp(-a*t)*sin(omega*x)', independent_variable='t', A=1, a=0.1, omega=pi, x=5)
print <math>g(1.2)
g.set_parameters(A=2, x=10)
print g(1.2)
```

```
Usage:

Terminal> python diff.py 'exp(x)*sin(x)' 3.4
Numerical derivative: -36.6262969164

Differentiate e^x \sin x at x = 3.4 numerically.

Implementation:

f'(x) \approx \frac{f(x+h) - f(x-h)}{2h} \quad (h \text{ small})
import sys
from scitools.std import StringFunction
f = \text{StringFunction}(\text{sys.argv}[1], \text{ independent\_variable='x'})
x = float(\text{sys.argv}[2])
def numerical_derivative(f, x, h=1E-5):
    return (f(x+h) - f(x-h))/(2+h)
print 'Numerical derivative:', numerical_derivative(f, x)
```

```
Can we extend the program to also include symbolic differentiation? (Yes, but the code is advanced...)

Terminal> python diff.py 'exp(x)*sin(x)' 3.4

Numerical derivative: -36.6262969164

Exact derivative: -36.626296916476 (error=9.390E-10)

Formula for the derivative: exp(x)*sin(x) + exp(x)*cos(x)

Program extension:

# Import all sin, cos, exp, ... functions from sympy such that # we can build a sympy expression out of str(f)

from sympy import*
x_value = x # store the value of x, x will be used as symbol x = sympy.symbols(x'x) # need x as symbol for the next statement # Turn the string formula in f into a sympy expression formula = eval(str(f)) # ex: eval('exp(x)*sin(x)')

# Differentiate formula wrt symbol x dfdx = diff(formula, x)
# Substitute symbol x by x_value dfdx, value = dfdx.subs(x, x_value)

print 'Exact derivative:', dfdx_value, '(error=%.3E)' % \ (dfdx_value - numerical_derivative(f, x_value))

print 'Formula for the derivative:', dfdx
```

# Example on reading 4 parameters from the command line

$$s(t) = s_0 + v_0 t + \frac{1}{2} a t^2$$

Input data:  $s_0$  (initial location),  $v_0$  (initial velocity), a (constant acceleration) and t (time)

Output data: s (current location)

```
Specify s_0=1 m, \nu_0=1 m/s, a=0.5 m/s², and t=3 s on the command line:
```

Terminal> python location\_cml.py 1 1 0.5 3

## Program:

```
import sys
s0 = float(sys.argv[1])
v0 = float(sys.argv[2])
a = float(sys.argv[3])
t = float(sys.argv[4])
s = s0 + v0*t + 0.5*a*t*t
print s
```

# Command-line arguments with options

Many programs, especially on Unix systems, take a set of command-line arguments of the form --option value

```
Terminal> python location.py --v0 1 --t 3 --s0 1 --a 0.5 Terminal> python location.py --t 3
```

The latter run relies on default values for v0, s0, and a: we provide only the values we want to change.

Such option-value pairs make it easier to understand what the input is (cf. keyword arguments).

# Programming option-value pairs with the argparse module

# The program has long and short command-line arguments

# Can use short or long options:

Terminal> python location.py --v0 1.2 --t 0.2 Terminal> python location.py --initial\_velocity 1.2 --time 0.2

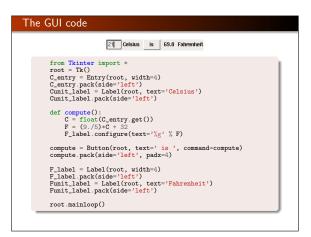
# Graphical user interfaces

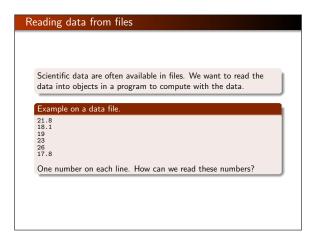
- Most programs today fetch input data from graphical user interfaces (GUI), consisting of windows and graphical elements on the screen: buttons, menus, text fields, etc.
- Why don't we learn to make such type of programs?
  - GUI demands much extra complicated programming
  - Experienced users often prefer command-line input
  - Programs with command-line or file input can easily be combined with each other, this is difficult with GUI-based programs
- Assertion: command-line input will probably fill all your needs in university courses
- But let's have a look at GUI programming!

# A graphical Celsius-Fahrenheit conversion program

21 Celsius is 69.8 Fahrenheit

- The Celsius degrees can be filled in as a number in a field
- Clicking the "is" button computes the corresponding Fahrenheit temperature





```
Basic file reading:

infile = open('data.txt', 'r')  # open file
for line in infile:
  # do something with line
infile.close()  # close file

Compute the mean values of the numbers in the file:

infile = open('data.txt', 'r')  # open file
mean = 0
for line in infile:
  number = float(line)  # line is string
mean = mean + number
mean = mean + number
```

```
Read all lines at ones into a list of strings (lines):

lines = infile.readlines()
for line in lines:
    # process line

The modern with statement:

with open('data.txt', 'r') as infile:
    for line in infile:
    # process line

The old-fashioned while construction:

while True:
    line = infile.readline()
    if not line:
        break
    # process line

Reading the whole file into a string:
    text = infile.read()
    # process the string text
```

```
Data about rainfall:

Average rainfall (in mm) in Rome: 1188 months between 1782 and 1970
Jan 81.2
Feb 63.2
Mar 70.3
Apr 55.7
May 53.0
Jun 36.4
Jul 17.5
Aug 27.5
Sep 60.9
Oct 117.7
Nov 111.0
Dec 97.9
Year 792.9
How do we read such a file?
```

```
The key idea to process each line is to split the line into words:

months = []
values = []
for line in infile:
    words = line.split()  # split into words
    if words[0]!= 'Vear':
        months.append(words[0])
        values.append(float(words[1]))

Can split with respect to any string s: line.split(s)

>>> line = 'Values: 1.2, 1.4, 2.7'
>>> line.split()
['Values:', '1.2, '1.4, '2.7']
>>> line.split(',')
['Values', '1.2, 1.4, 2.7']
>>> values = line.split(',')
['1.2', '1.4', '2.7']
>>> values = float(v) for v in values.split(',')]
>>> values
[1.2, 1.4, 2.7]
```

# def extract\_data(filename): infile = open(filename, 'r') infile.readline() # skip the first line months = [] rainfall = [] for line in infile: words [0]: month, words[i]: rainfall months = sppen(words[0]) rainfall.append(float(words[i])) infile.close() months = months[:-1] # Drop the "Year" entry annual\_avg = rainfall[:-1] # Store the annual average rainfall = rainfall[:-1] # Redefine to contain monthly data return months, rainfall, annual\_avg months, values, avg = extract\_data('rainfall.dat') print 'The average rainfall for the months:' for month, value in zip(months, values): print month, value print 'The average rainfall for the year:', avg

```
Basic pattern:

outfile = open(filename, 'w') # 'w' for writing

for data in somelist:
    outfile.write(sometext + '\n')

outfile.close()

Can append text to a file with open(filename, 'a').
```

```
Example: Writing a table to file
  Problem
  We have a nested list (rows and columns):
  Write these data to file in tabular form
  Solution:
     outfile = open('tmp_table.dat', 'w')
     for row in data:
        for column in row:
           outfile.write('%14.8f' % column)
     outfile.write('\n')
outfile.close()
  Resulting file:
        0.75000000 0.29619813 -0.29619813 -0.75000000
        -0.11697778
        -0.75000000
                  -0.29619813
                             0.29619813
```

```
A user can easily use our program in a wrong way, e.g.,

Terminal> python c2f_cml_v1.py
Traceback (most recent call last):
File "c2f_cml_v1.py", line 2, in ?
C = float(sys.argv[1])
IndexError: list index out of range

(the user forgot to provide a command-line argument...)
How can we take control, explain what was wrong with the input, and stop the program without strange Python error messages?

if len(sys.argv) < 2:
    print 'You failed to provide a command-line arg.!'
    sys.exit(1) # abort
F = 9.0*c/5 + 32
    print '%c is %.iff' % (C, F)

Terminal> python c2f_cml_v2.py
You failed to provide arg.!
```

```
Try to read C from the command-line, if it fails, tell the user, and abort execution:

import sys
try:
    C = float(sys.argv[1])
except:
    print 'You failed to provide a command-line arg.!'
    sys.exit(1) # abort
    F = 9.0e(75 + 32
    print 'WgC is %.1fF' % (C, F)

Execution:

Terminal> python c2f_cml_except1.py
You failed to provide a command-line arg.!

Terminal> python c2f_cml_except1.py 21C
You failed to provide a command-line arg.!
```

# It is good programming style to test for specific exceptions It is good programming style to test for specific exceptions: C = float(sys.argv[1]) except IndexError: print 'You failed to provide a command-line arg.!' If we have an index out of bounds in sys.argv, an IndexError exception is raised, and we jump to the except block. If any other exception arises, Python aborts the execution: Terminal>> python c2f\_cml\_tmp.py 21C Traceback (most recent call last): File "tmp.py", line 3, in <module> C = float(sys.argv[1]) ValueError: invalid literal for float(): 21C

```
Improvement: test for IndexError and ValueError
exceptions
        import sys
        try:
    C = float(sys.argv[1])
        except IndexError:
    print 'No command-line argument for C!'
             sys.exit(1) # abort execution
        except ValueError:
            print 'C must be a pure number, not "%s"' % sys.argv[1]
             sys.exit(1)
        F = 9.0*C/5 + 32
        print '%gC is %.1fF' % (C, F)
   Executions:
        Terminal> python c2f_cml_v3.py
No command-line argument for C!
        Terminal> python c2f_cml_v3.py 21C
Celsius degrees must be a pure number, not "21C"
```

## The programmer can raise exceptions

- Instead of just letting Python raise exceptions, we can raise our own and tailor the message to the problem at hand
- We provide two examples on this:
  - catching an exception, but raising a new one with an improved (tailored) error message
  - raising an exception because of wrong input data
- Baisc syntax: raise ExceptionType(message)

# Examples on re-raising exceptions with better messages

```
def read_C():
   try:
    C = float(sys.argv[1])
    except IndexError:
    # re-raise, but with specific explanation:
        raise IndexError(
          'Celsius degrees must be supplied on the command line')
    except ValueError:
        # re-raise, but with specific explanation:
        raise ValueError(
'Degrees must be number, not "%s", % sys.argv[1])
    # C is read correctly as a number, but can have wrong value:
       raise ValueError('C=%g is a non-physical value!' % C)
    return C
```

# Calling the previous function and running the program

```
C = read_C()
except (IndexError, ValueError) as e:
# print exception message and stop the program
            print e
            sys.exit(1)
Executions:
      Terminal> c2f_cml.py
Celsius degrees must be supplied on the command line
      Terminal> c2f_cml.py 21C
Celsius degrees must be a pure number, not "21C"
      Terminal> c2f_cml.py -500
C=-500 is a non-physical value!
      Terminal> c2f_cml.py 21 21C is 69.8F
```

# Making your own modules

```
We have frequently used modules:
    from math import log

r = log(6) # call log function in math module
     \begin{array}{ll} \text{import sys} \\ x = eval(\text{sys.argv[1]}) & \text{\# access list argu in sys module} \end{array} 
Characteristics of modules:
  · Collection of useful data and functions
     (later also classes)
  • Functions in a module can be reused in many different
     programs
  • If you have some general functions that can be handy in more
     than one program, make a module with these functions
  • It's easy: just collect the functions you want in a file, and
     that's a module!
```

# Case on making our own module

Here are formulas for computing with interest rates:

$$A = A_0 \left( 1 + \frac{p}{360 \cdot 100} \right)^n, \tag{1}$$

$$A_0 = A \left( 1 + \frac{p}{360 \cdot 100} \right)^{-n}, \tag{2}$$

$$n = \frac{\ln \frac{A}{A_0}}{\ln \left(1 + \frac{P}{360 \cdot 100}\right)},\tag{3}$$

$$p = 360 \cdot 100 \left( \left( \frac{A}{A_0} \right)^{1/n} - 1 \right). \tag{4}$$

Ao: initial amount, p: percentage, n: days, A: final amount

We want to make a module with these four functions.

# First we make Python functions for the formuluas

```
from math import log as ln

def present_amount(A0, p, n):
    return A0*(1 + p/(360.0*100))**n

def initial_amount(A, p, n):
    return A*(1 + p/(360.0*100))**(-n)

def days(A0, A, p):
    return ln(A/A0)/ln(1 + p/(360.0*100))

def annual_rate(A0, A, n):
    return 360*100*((A/A0)**(1.0/n) - 1)
```

# Then we can make the module file

- Collect the 4 functions in a file interest.py
- Now interest.py is actually a module interest (!)

### Example on use:

```
# How long time does it take to double an amount of money? from interest import days AO = 1; A = 2; p = 5 n = days AO = 2; A = 2; P = 5 n = days AO = 2; AO = 20 years = 1/365. O print 'Money has doubled after %.1f years' % years
```

# Adding a test block in a module file

- Module files can have an if test at the end containing a test block for testing or demonstrating the module
- The test block is not executed when the file is imported as a module in another program
- The test block is executed only when the file is run as a program

# Test blocks are often collected in functions

```
Let's make a real test function:

def test_all_functions():
    #Define compatible values
    A = 2.2133983053266699; AO = 2.0; p = 5; n = 730
    # Given three of these, compute the remaining one
# and compare with the correct value (in parenthesis)
A_computed = present_amount(AO, p, n)
AO_computed = days(AO, A, p)
p_computed = days(AO, A, p)
p_computed = annual_rate(AO, A, n)
def float_eq(A, b, tolerance=1E-14):
    """Return True if a == b within the tolerance."""
    return abs(a - b) < tolerance

success = float_eq(A_computed, AO) and \
    float_eq(AO_computed, AO) and \
    float_eq(A_computed, D) and \
    float_eq(A_computed, D)
    assert success # could add message here if desired

if __name__ == '__main__':
    test_all_functions()
```

# How can Python find our new module?

- If the module is in the same folder as the main program, everything is simple and ok
- Home-made modules are normally collected in a common folder, say /Users/hpl/lib/python/mymods
- In that case Python must be notified that our module is in that folder

Technique 1: add folder to PYTHONPATH in .bashrc: export PYTHONPATH=\$PYTHONPATH:/Users/hpl/lib/python/mymods

Technique 2: add folder to sys.path in the program:

sys.path.insert(0, '/Users/hpl/lib/python/mymods')

Technique 3: move the module file in a directory that Python already searches for libraries.

# Question and answer input: var = raw\_input('Give value: ') # var is string! # if var needs to be a number: var = float(var) # or in general: var = eval(var) Command-line input: import sys parameter1 = eval(sys.argv[1]) parameter3 = sys.argv[3] # string is ok parameter2 = eval(sys.argv[2]) Recall: sys.argv[0] is the program name

# --option value pairs with the aid of argparse: import argparse parser = argparse.ArgumentParser() parser.add\_argument('--p1', '--parameter\_1', type=float, default=0.0, help='1st parameter') parser.add\_argument('--p2', type=float, default=0.0, help='2nd parameter') args = parser.parse\_args() p1 = args.p1 p2 = args.p2 On the command line we can provide any or all of these options: Terminal> program prog.py --parameter\_1 2.1 --p2 -9

```
Evaluating string expressions with eval:

>>> x = 20
>>> r = eval('x + 1.1')
>>> type(r)
<type 'float'>

Executing strings with Python code, using exec:

exec("""
def f(x):
    return %s
    """ % sys.argv[1])
```

```
infile = open(filename, 'r')  # read
outfile = open(filename, 'v')  # write
outfile = open(filename, 'v')  # append

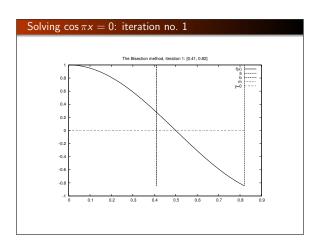
# Reading
line = infile.readline()  # read the next line
filestr = infile.read()  # read rest of file into string
lines = infile.read()  # read rest of file into list
for line in infile:
    # writing
outfile.write(s)  # add \n if you need it

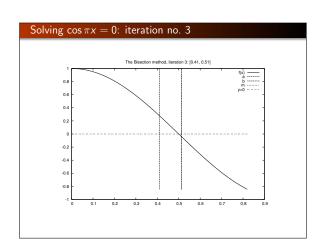
# Closing
infile.close()
outfile.close()
```

```
A summarizing example: solving f(x)=0

Nonlinear algebraic equations like x=1+\sin x
\tan x + \cos x = \sin 8x
x^5-3x^3=10
are usually impossible to solve by pen and paper, but can be solved by numerical methods. To this end, rewrite any equation as f(x)=0
For the above we have (put everything on the left-hand side) f(x)=x-1-\sin x
f(x)=\tan x+\cos x-\sin 8x
f(x)=x^5-3x^3-10
```

# We shall learn about a method for solving f(x) = 0A solution x of f(x) = 0 is called a *root* of f(x)Outline of the next slides: • Formulate a method for finding a root • Translate the method to a precise algorithm • Implement the algorithm in Python • Test the implementation

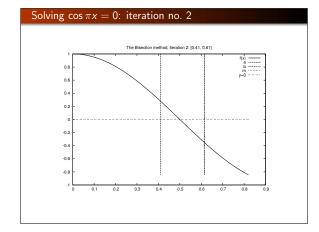


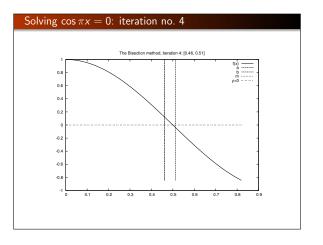


# The Bisection method

- Start with an interval [a, b] in which f(x) changes sign
- Then there must be (at least) one root in [a, b]
- Halve the interval:
  - m = (a + b)/2; does f change sign in left half [a, m]? Yes: continue with left interval [a, m] (set b = m)

  - No: continue with right interval [m, b] (set a = m)
- Repeat the procedure
- After halving the initial interval [p, q] n times, we know that f(x) must have a root inside a (small) interval  $2^{-n}(q-p)$
- The method is slow, but very safe
- Other methods (like Newton's method) can be faster, but may also fail to locate a root - bisection does not fail





# From method description to a precise algorithm

- We need to translate the mathematical description of the Bisection method to a Python program
- An important intermediate step is to formulate a precise algorithm
- Algorithm = detailed, code-like formulation of the method

```
for i = 0,1,2, ..., n:

m = (a + b)/2

if f(a)*f(m) <= 0:

b = m # root is in left half

else:

a = m # root is in right half

# f(x) has a root in [a,b]
```

# The algorithm can be made more efficient

- f(a) is recomputed in each if test
- This is not necessary if a has not changed since last pass in the loop
- On modern computers and simple formulas for f(x) these extra computations do not matter
- However, in science and engineering one meets f functions that take hours or days to evaluate at a point, and saving some f(a) evaluations matters!
- Rule of thumb: remove redundant computations
   (unless the code becomes much more complicated, and harder to verify)

# New, more efficient version of the algorithm

Idea: save f(x) evaluations in variables

```
 f_{-a} = f(a) \\ for i = 0,1,2, ..., n; \\ m = (a + b)/2 \\ f_{-m} = f(m) \\ if f_{-a} = f_{-m} < 0; \\ b = m  # root is in left half \\ else: \\ a = m  # root is in right half \\ f_{-a} = f_{-m} \\ # f(x) has a root in [a,b]
```

# How to choose n? That is, when to stop the iteration

- ullet We want the error in the root to be  $\epsilon$  or smaller
- After n iterations, the initial interval [a,b] is halved n times and the current interval has length  $2^{-n}(b-a)$ . This is sufficiently small if  $2^{-n}(b-a) = \epsilon \implies n = -\frac{\ln \epsilon \ln(b-a)}{\ln 2}$
- $\bullet$  A simpler alternative: just repeat halving until the length of the current interval is  $\leq \epsilon$
- This is easiest done with a while loop:
   while b-a <= epsilon:</li>
- We also add a test to check if f really changes sign in the initial inverval [a, b]

# Final version of the Bisection algorithm

```
f_a=f(a)
if f_a=f(b) > 0:
    # error: f does not change sign in [a,b]

i = 0
while b-a > epsilon:
    i = i + 1
    m = (a + b)/2
    f_m = f(m)
    if f_a=f(m) <= 0:
        b = m # root is in left half
    else:
        a = m # root is in right half
    f_a = f_m

# if x is the real root, |x-m| < epsilon</pre>
```

# Python implementation of the Bisection algorithm

```
def f(x):
    return 2*x - 3  # one root x=1.5

eps = 1E-5
a, b = 0, 10

fa = f(a)
    if fa*f(b) > 0:
        print 'f(x) does not change sign in [%g, %g].' % (a, b)
        sys.exit(1)

i = 0  # iteration counter
while b-a > eps:
    i += 1
    m = (a + b)/2.0
    fm = f(m)
    if fa*fm <= 0:
        b = m # root is in left half of [a, b]
    else:
        a = m # root is in right half of [a, b]
    fa = fm
x = m # this is the approximate root</pre>
```

# 

# • If we put the bisection function in a file bisection.py, we automatically have a module, and the bisection function can easily be imported in other programs to solve f(x) = 0 • We should make a test function too def test\_bisection(): def f(x): return 2\*x - 3 # only one root z=1.5 eps = 1E-5 x, iter = bisection(f, a=0, b=10, eps=eps) success = abs(x - 1.5) < eps # test within eps tolerance assert success, 'found x='kg != 1.5' % x</li> if \_\_name\_\_ == '\_\_main\_\_': test\_bisection()

```
To the point of this lecture: get input!

We want to provide an f(x) formula at the command line along with a and b (3 command-line args)

Usage:

Terminal> python bisection.py 'sin(pi*x**3)-x**2' -1 3.5

Reading input:

def get_input():
    """Oet f, a, b, eps from the command line."""
    from scitools.std import StringFunction
    f = StringFunction(sys.argv[1])
    a = float(sys.argv[2])
    b = float(sys.argv[3])
    eps = float(sys.argv[3])
    return f, a, b, eps

# Usage:
    f, a, b, eps = get_input()
    x, iter = bisection(f, a, b, eps)
    print 'Found root x=%g in %d iterations' % (x, iter)
```

```
def get_input():
    """Get f, a, b, eps from the command line."""
    from scitcols.std import StringFunction
    try:
        a = float(sys.argy[2])
        b = float(sys.argy[3])
        eps = float(sys.argy[4])
    except IndexError:
        print 'Usage '%: f a b eps' % sys.argv[0]
        sys.exit(1)
    return f, a, b, eps
```

```
Applications of the Bisection method

Two examples: tanh x = x and tanh x<sup>5</sup> = x<sup>5</sup>:

Terminal> python bisection_plot.py "x-tanh(x)" -1 1
Terminal> python bisection.plot.py "x**5-tanh(x**5)" -1 1

The first equation is easy to treat, but the second leads to much less accurate results. Why??
```