Ch.4: User input and error handling

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Programs until now hardcode input data

$$y = v_0 t - 0.5 g t^2$$

```
v0 = 5
g = 9.81
t = 0.6
y = v0*t - 0.5*g*t**2
print y
```

Note

- Input data (v_0, t) are hardcoded (explicitly set)
- Changing input data requires editing
- This is considered bad programming (because editing programs may easily introduce errors!)
- Rule: read input from user avoid editing a correct program

How do professional programs get their input?

- Consider a web browser: how do you specify a web address?
 How do you change the font?
- You don't need to go into the program and edit it...

How can we specify input data in programs?

- Hardcode values
- Ask the user questions and read answers
- Read command-line arguments
- Read data from a file

Getting input from questions and anwsers

```
Sample program:
C = 21; F = (9.0/5)*C + 32; print F
```

Idea: let the program ask the user a question "C=?", read the user's answer, assign that answer to the variable C.

 $\begin{array}{lll} \textbf{C} = \texttt{raw_input('C=?')} & \textit{f C becomes a string} \\ \textbf{C} = \texttt{float(C)} & \textit{f convert to float so we can compute} \\ \textbf{F} = (9.75) * \textbf{C} + 32 \\ \textbf{print F} & & \\ \end{array}$

Running in a terminal window:

```
Terminal> python c2f_qa.py
C=? 21
69.8
```

Another example: print the n first even numbers

```
n = int(raw_input('n=?'))
for i in range(2, 2*n+1, 2):
    print i

# or:
print range(2, 2*n+1, 2)
# or:
for i in range(1, n+1):
    print 2*i
```

Command-line arguments are words written after the program name

Examples on command-line arguments:

Terminal> python myprog.py arg1 arg2 arg3 .. Terminal> cp -r yourdir ../mydir Terminal> ls -1

Unix programs (rm, 1s, cp, ...) make heavy use of command-line arguments, (see e.g. man 1s). We shall do the same.

How to use a command-line argument in our sample program

```
C = 21; F = (9.0/5)*C + 32; print F
```

The user wants to specify C as a *command-line argument* after the name of the program when we run the program:

```
Terminal> python c2f_cml.py 21 69.8
```

Command-line arguments are the "words" after the program name, and they are stored in the list sys.argv:

```
import sys C = float(sys.argv[1]) # read 1st command-line argument F = 9.0*C/5 + 32 print F
```

Command-line arguments are separated by blanks

```
Here is another program print_cml.py:
```

import sys; print sys.argv[1:]

Demonstrations:

```
Terminal> python print_cml.py 21 string with blanks 1.3 ['21', 'string', 'with', 'blanks', '1.3']

Terminal> python print_cml.py 21 "string with blanks" 1.3 ['21', 'string with blanks', '1.3']
```

Note 1: use quotes, as in "string with blanks", to override the rule that command-line arguments are separate by blanks.

Note 2: all list elements are surrounded by quotes, demonstrating that command-line arguments are strings.

The magic eval function turns a string into live code

eval(s) evaluates a string object s as if the string had been written directly into the program

```
>>> s = '1+2'
>>> r = eval(s)
>>> r
3
>>> type(r)
<type 'int'>
>>> r = eval('[1, 6, 7.5] + [1, 2]')
>>> r
[1, 6, 7.5, 1, 2]
>>> type(r)
<type 'list'>
```

Note: be careful with eval and string values

```
We want r = 'math programming'. Writing just
```

r = eval('math programming')

is the same as writing

r = math programming

which is an invalid expression and illegal syntax.

Remedy: must put the string inside quotes:

```
s = "'math programming'"
r = eval(s)  # r becomes 'math programming'
```

With eval, a little program (add_input.py) can do much...

D.

We can add integer and float:

```
Terminal> python add_input.py
operand 1: 3.0
ctype 'int'> + ctype 'float'> becomes <type 'float'>
with value 4

or two lists:

Terminal> python add_input.py
operand 1: [1,2]
operand 2: [-1,0,1]
ctype 'list'> + ctype 'list'> becomes <type 'list'>
with value [1, 2, -1, 0, 1]
```

This great flexibility also quickly breaks programs... Terminal> python add_input.py operand 1: (1,2) operand 2: (3,4) Traceback (most recent call last): File "add.input.py", line 3, in <module> r = i1 + i2 TypeError: can only concatenate tuple (not "list") to tuple Terminal> python add_input.py operand 1: one Traceback (most recent call last): File "add.input.py", line 1, in <module> ii = eval(raw.input.operand i: ')) File "sdd.input.py", line 1, in <module> NameError: name 'one' is not defined Terminal> python add_input.py operand 1: 4 operand 2: 'Hello, World!' Traceback (most recent call last): File "add.input.py", line 3, in <module> r = i1 + i2 TypeError: unsupported operand type(s) for +: 'int' and 'str'

```
    eval(s) evaluates an expression s
    eval('r = 1+1') is illegal because this is a statement, not only an expression
    ...but we can use exec to turn one or more complete statements into live code:

statement = 'r = 1+1'  # store statement in a string exec(statement)
print r  # prints 2

For longer code we can use multi-line strings:
somecode = ''''
def f(t):
    term1 = exp(-a*t)*sin(v1*x)
    term2 = 2*sin(v2*x)
    return term1 + term2
;'''
exec(somecode) # execute the string as Python code
```

```
exec can be used for building a function at run-time
   Embed user's formula in a Python function:
   formula = raw_input('Write a formula involving x: ')
   code = """
def f(x):
   return %s
    from math import * # make sure we have sin, cos, log, etc
    exec(code)
                     # turn string formula into live function
    # Ask the user for x values and evaluate f(x)
    while x is not None:
       x = eval(raw_input('Give x (None to quit): '))
if x is not None;
           y = f(x)
            print 'f(%g)=%g' % (x, y)
  While the program is running, the user types a formula, which
  becomes a function, the user gives x values until the answer is
  None, and the program evaluates the function f(x). Note: the
  programmer knows nothing about the user's choice of f(x) when
  she writes the program (!).
```

```
It is common for programs to read formulas and turn them into functions so we have made a special tool for this purpose:

>>> from scitools.std import StringFunction
>>> formula = 'exp(x)*sin(x)'
>>> f = StringFunction(formula)
>>> f(0)
0.0
>>> from math import pi
>>> f(pi)
2.838329929952166e-15
>>> print str(f)
exp(x)*sin(x)

The function can also have parameters: g(t) = Ae^{-at}\sin(\omega x)
g = StringFunction('A*exp(-a*t)*sin(omgga*x)', independent_variable='t', A=1, a=0.1, omega=pi, x=5)
print g(1.2)
g.set_parameters(A=2, x=10)
print g(1.2)
```

```
Usage:

Terminal> python diff.py 'exp(x)*sin(x)' 3.4
Numerical derivative: -36.6262969164

Differentiate e^x \sin x at x = 3.4 numerically.

Implementation:

f'(x) \approx \frac{f(x+h) - f(x-h)}{2h} \quad (h \text{ small})
import sys
from scitools.std import StringFunction
f = \text{StringFunction}(sys. \arg v[1], \text{ independent\_variable}='x')
x = f \log t(sys. \arg v[2])
def numerical_derivative(f, x, h=1E-5):
    return (f(x+h) - f(x-h))/(2+h)
print 'Numerical derivative:', numerical_derivative(f, x)
```

Example on reading 4 parameters from the command line

$$s(t) = s_0 + v_0 t + \frac{1}{2} a t^2$$

Input data: s_0 (initial location), v_0 (initial velocity), a (constant acceleration) and t (time)

Output data: s (current location)

Specify $s_0=1$ m, $v_0=1$ m/s, a=0.5 m/s², and t=3 s on the command line:

Terminal> python location_cml.py 1 1 0.5 3 6.25

Program:

```
import sys
s0 = float(sys.argv[1])
v0 = float(sys.argv[2])
a = float(sys.argv[3])
t = float(sys.argv[4])
s = s0 + v0*t + 0.5*a*t*t
print s
```

Command-line arguments with options

Many programs, especially on Unix systems, take a set of command-line arguments of the form -option value

Terminal> python location.py --v0 1 --t 3 --s0 1 --a 0.5 Terminal> python location.py --t 3

The latter run relies on default values for v0, s0, and a: we provide only the values we want to change.

Such option-value pairs make it easier to understand what the input is (cf. keyword arguments).

Programming option-value pairs with the argparse module

```
import argparse
parser = argparse.ArgumentParser()

# Define command-line arguments
parser.add_argument('--v0', '--initial_velocity', type=float,
default=0.0, help='initial_velocity')

parser.add_argument('--s0', '--initial_position', type=float,
default=0.0, help='initial_position')

parser.add_argument('--a', '--acceleration', type=float,
default=1.0, help='acceleration')

parser.add_argument('--t', '--time', type=float,
default=1.0, help='initial_position')

# Read the command line and interpret the arguments
args = parser parse_args()

# Extract values
s = args.s0 + args.v0*t + 0.5*args.a*args.t**2
# or
s0 = args.s0; v0 = args.v0; a = args.a; t = args.t
s = s0 + v0*t + 0.5*a*t**2
```

The program has long and short command-line arguments

Can use short or long options:

Terminal> python location.py --v0 1.2 --t 0.2 Terminal> python location.py --initial_velocity 1.2 --time 0.2

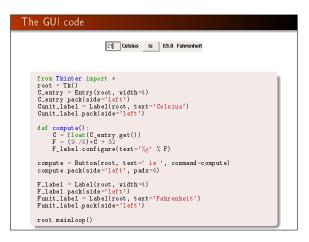
Graphical user interfaces

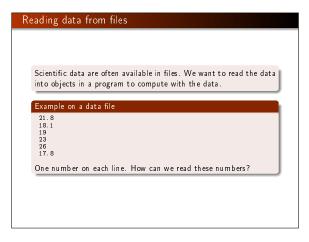
- Most programs today fetch input data from graphical user interfaces (GUI), consisting of windows and graphical elements on the screen: buttons, menus, text fields, etc.
- Why don't we learn to make such type of programs?
 - GUI demands much extra complicated programming
 - Experienced users often prefer command-line input
 - Programs with command-line or file input can easily be combined with each other, this is difficult with GUI-based programs
- Assertion: command-line input will probably fill all your needs in university courses
- But let's have a look at GUI programming!

A graphical Celsius-Fahrenheit conversion program

21 Celsius is 69.8 Fahrenheit

- The Celsius degrees can be filled in as a number in a field
- Clicking the "is" button computes the corresponding Fahrenheit temperature





```
Reading a file line by line

Basic file reading:

infile = open('data.txt', 'r')  # open file
for line in infile:
    # do something with line
infile.close()

Compute the mean values of the numbers in the file:

infile = open('data.txt', 'r')  # open file
mean = 0
for line in infile:
    number = float(line)
    mean = mean + number
mean = mean / len(lines)
print mean
```

```
File:
Line 1. Line 2. Line 3. Line 4.

Session:

>>> infile = open('tmp.txt', 'r')
>>> lines = infile readlines()  # read all lines
>>> lines
['Line 1.\n', 'Line 2.\n', 'Line 3.\n', 'Line 4.\n']
>>> infile readline()  # no more to read
>>> infile eopen('tmp.txt', 'r')
>>> infile.readline()  # read one line
'Line 1.\n'
>>> infile.readline()  # read next line
'Line 2.\n'
>>> for line in infile:  # read the next lines to the end
...
    print line
...
Line 3.
Line 4.
```

File with data about rainfall: Average rainfall (in mm) in Rome: 1188 months between 1782 and 1970 Jan 81. 2 Feb 63. 2 Mar 70. 3 Apr 65. 7 May 53. 0 Jun 36. 4 Jul 17. 5 Aug 27. 5 Sep 60. 9 Oct 117. 7 Nov 111. 0 Dec 97. 9 Year 792. 9 How do we read such a file?


```
def extract_data(filename):
    infile = open(filename, 'r')
    infile readline() # skip the first line
    months = []
    rainfall = []
    for line in infile:
        words = line split()
        # words(0]: month, words(1]: rainfall
        months.append(words[0])
        rainfall append(words[0])
        rainfall append(words[1]))
    infile close()
    months = months[:-1] # Brop the "Fear" entry
    annual_avg = rainfall[-1] # Store the annual average
    rainfall = rainfall[:-1] # Redefine to contain monthly data
    return months, rainfall, annual_avg

months, values, avg = extract_data('rainfall.dat')
    print 'The average rainfall for the months:'
    for month, value in zip(months, values):
        print month, value
    print 'The average rainfall for the year:', avg
```

```
Basic pattern:

outfile = open(filename, 'w')  # 'w' for writing

for data in somelist:
   outfile.write(sometext + '\n')

outfile.close()

Can append text to a file with open(filename, 'a').
```

```
Example: Writing a table to file
  We have a nested list (rows and columns):
   data = \
   Write these data to file in tabular form
  Solution:
   outfile = open('tmp_table.dat', 'w')
for row in data:
   for column in row:
           outfile.write('%14.8f' % column)
       outfile.write('\n')
   outfile.close()
   Resulting file:
       0.75000000 0.29619813 -0.29619813 -0.75000000
       0.29619813
                    0.11697778 -0.11697778 -0.29619813
                   -0.11697778
                                0.11697778
      -0.75000000 -0.29619813
                                0.29619813
                                             0.75,000,000
```

```
♦ A file is a sequence of characters
♦ For simple text files, each character is one byte (=8 bits, a bit is 0 or 1), which gives 2<sup>8</sup> = 256 different characters
♦ (Text files in, e.g., Chinese and Japanese need several bytes for each character)
♦ Save the text "ABCD" to file in Gedit/Emacs and OpenOffice/Word and examine the file!
♦ File reading in Python is about either reading all characters (read) or reading line by line (readline, readlines, for line in fileobj)
```

Code: import sys C = float(sys.argv[1]) F = 5,/9*C + 32 print F Next topic: How to handle wrong input from the user?

Our program stops with a strange error message if the command-line argument is missing

A user can easily use our program in a wrong way, e.g.,

Terminal> python c2f_cml.py
Traceback (most recent call last):
File "c2f_cml.py", line 2, in ?
C = float(sys.argv[1])
IndexError: list index out of range

Why?

- The user forgot to provide a command-line argument
- sys.argv has then only one element, sys.argv [0], which is the program name (c2f_cml.py)
- Index 1, in sys.argv [1], points to a non-existing element in the sys.argv list
- Any index corresponding to a non-existing element in a list leads to IndexError

We should handle errors in input!

How can we take control, explain what was wrong with the input, and stop the program without strange Python error messages?

```
# Program c2f_cml_if.py
import sys
if len(sys.argv) < 2:
    print 'You failed to provide a command-line arg.!'
    sys.exit(!) # abort
    F = 9.0*C/5 + 32
    print '%gC is %.1fF' % (C, F)
Terminal> python c2f_cml_if.py
You failed to provide a command-line arg.!
```

Exceptions as an alternative to if tests

- Rather than test if something is wrong, recover from error, else do what we indended to do, it is common in Python (and many other languages) to try to do what we indend to, and if it fails, we recover from the error
- This principle makes use of a try-except block

If something goes wrong in the try block, Python raises an exception and the execution jumps immediately to the except block.

The temperature conversion program with try-except

Try to read ${\tt C}$ from the command-line, if it fails, tell the user, and abort execution:

```
abort execution:

import sys
try:
    C = float(sys.argv[i])
except:
    print 'You failed to provide a command-line arg.!'
    sys.exit(1) # abort
F = 9.0 eC/5 + 32
print '%gC is %.ifF' % (C, F)

Execution:

Terminal> python c2f_cml_except1.py
You failed to provide a command-line arg.!

Terminal> python c2f_cml_except1.py 21C
You failed to provide a command-line arg.!
```

It is good programming style to test for specific exceptions

It is good programming style to test for specific exceptions:

try:
 C = float(sys.argv[1])
except IndexError:
 print 'You failed to provide a command-line arg.!'

If we have an index out of bounds in sys.argy, an IndexError exception is raised, and we jump to the except block.

If any other exception arises, Python aborts the execution:

Terminal> python c2f_cml_tmp.py 21C
Traceback (most recent call last):

Traceback (most recent call last):
File "tmp.py", line 3, in <module>
C = float(sys.argv[i])
ValueError: invalid literal for float(): 21C

improvement: test for IndexError and ValueError exceptions import sys try: C = float(sys.argv[1]) except IndexError: print 'No command-line argument for C!' sys.exit(1) # abort execution except ValueError: print 'C must be a pure number, not "%s"' % sys.argv[1] sys.exit(1) F = 9.0*c/5 + 32 print 'MgC is %.1fF' % (C, F) Executions: Terminal python c2f_cml_v3.py No command-line argument for C! Terminal python c2f_cml_v3.py 21C Celsius degrees must be a pure number, not "21C"

```
The programmer can raise exceptions
```

- Instead of just letting Python raise exceptions, we can raise our own and tailor the message to the problem at hand
- We provide two examples on this:
 - catching an exception, but raising a new one with an improved (tailored) error message
 - raising an exception because of wrong input data
- Baisc syntax: raise ExceptionType(message)

Examples on re-raising exceptions with better messages

```
def read_C():
    try:
        C = float(sys.argv[i])
    except IndexError:
        # re-raise, but with specific explanation:
        raise IndexError(
            'Celsius degrees must be supplied on the command line')
    except ValueError:
        # re-raise, but with specific explanation:
        raise ValueError(
            'Degrees must be number, not "%s", % sys.argv[i])

# C is read correctly as a number, but can have wrong value:
    if C < -273.15:
        raise ValueError('C-%g is a non-physical value!', % C)
    return C</pre>
```

Calling the previous function and running the program

```
try:

c = read_C()

except (IndexError, ValueError) as e:
    # print exception message and stop the program
    print e
    sys exit(1)

Executions:

Terminal> c2f_cml.py
Celsius degrees must be supplied on the command line

Terminal> c2f_cml.py 21C
Celsius degrees must be a pure number, not "21C"

Terminal> c2f_cml.py -500
C=-500 is a non-physical value!

Terminal> c2f_cml.py 21
21C is 69.8F
```

Making your own modules

We have frequently used modules like math and sys:

```
from math import log r = \log(6) \quad \text{# call log function in math module} import sys x = \text{eval(sys.argv[!])} \quad \text{# access list argu in sys module}
```

Characteristics of modules:

- Collection of useful data and functions (later also classes)
- Functions in a module can be reused in many different programs
- If you have some general functions that can be handy in more than one program, make a module with these functions
- It's easy: just collect the functions you want in a file, and that's a module!

Case on making our own module

Here are formulas for computing with interest rates:

$$A = A_0 \left(1 + \frac{p}{360 \cdot 100} \right)^n, \tag{1}$$

$$A_0 = A \left(1 + \frac{p}{360 \cdot 100} \right)^{-n}, \tag{2}$$

$$n = \frac{\ln \frac{A}{A_0}}{\ln \left(1 + \frac{P}{360 \cdot 100}\right)},\tag{3}$$

$$p = 360 \cdot 100 \left(\left(\frac{A}{A_0} \right)^{1/n} - 1 \right). \tag{4}$$

 A_0 : initial amount, p: percentage, n: days, A: final amount

We want to make a module with these four functions.

First we make Python functions for the formuluas from math import log as ln def present_amount(AO, p, n): return AO*(1 + p/(360.0*100))**n def initial_amount(A, p, n): return A*(1 + p/(360.0*100))**(-n) def days(AO, A, p): return ln(A/AO)/ln(1 + p/(360.0*100)) def annual_rate(AO, A, n): return 360*100*((A/AO)**(1.0/n) - 1)

```
Then we can make the module file

• Collect the 4 functions in a file interest.py
• Now interest.py is actually a module interest (!)

Example on use:

# How long time does it take to double an amount of money?

from interest import days
A0 = 1; A = 2; p = 5
n = days(A0, 2, p)
years = n/365.0
print 'Money has doubled after %.1f years' % years
```

• Module files can have an if test at the end containing a test block for testing or demonstrating the module • The test block is not executed when the file is imported as a module in another program • The test block is executed only when the file is run as a program if __name__ == '__main__': # this test defineds the test block oblock of statements' In our case: if __name__ == '__main__': # a = 2.213398305326669 Ao = 2.0 p = 6 n = 730 print 'A='% (%) A0-% (%.1f) n=¼i (%d) p=% (%.1f)' % \ (present_amount(A0, p, n), A, initial_amount(A, p, n), A0, days(A0, A, p), n, annual_rate(A0, A, n), p) • Module files can have an if test at the end containing a test block oblock of the state of the

```
Let's make a real test function for what we had in the test block:

def test_all_functions():

# Define compatible values
A = 2.213389365266689; A0 = 2.0; p = 5; n = 730

# Given three of these, compute the remaining one
# and compare with the correct value (in parenthesis)
A.computed = present amount (A0, p, n)
AO_computed = initial_amount(A, p, n)
n.computed = days(A0, A, p)
p.computed = annual_rate(A0, A, n)
def float_ag(A, b, tolerance=1E-12):
    ""Return True if a == b within the tolerance."""
    return abs(a - b) < tolerance

success = float_ag(A_computed, A) and \
    float_ag(A_computed, A) and \
    float_ag(A_computed, A) and \
    float_ag(A_computed, A)
    assert success # could add message here if desired

if __name__ == '__main__':
    test_all_functions()
```

```
■ If the module is in the same folder as the main program, everything is simple and ok
■ Home-made modules are normally collected in a common folder, say /Users/hp1/lib/python/mymods
■ In that case Python must be notified that our module is in that folder

Technique 1: add folder to PYTHONPATH:/Users/hp1/lib/python/mymods

Technique 2: add folder to sys.path in the program:
sys.path.insert(0, '/Users/hp1/lib/python/mymods')

Technique 3: move the module file in a directory that Python already searches for libraries.
```

```
Question and answer input:

var = raw_input('Give value: ')  # var is string!

# if var needs to be a number:
var = float(var)
# or in general:
var = eval(var)

Command-line input:
import sys
parameter1 = eval(sys.argv[1])
parameter3 = sys.argv[3]
parameter2 = eval(sys.argv[2])

Recall: sys.argv[0] is the program name
```

-option value pairs with the aid of argparse: import argparse parser = argparse.ArgumentParser() parser.add_argument(\frac{1}{2}-p1\frac{1}{2}, \frac{1}{2}-p1\frac{1}{2} targarse parser = argparse.ArgumentParser() parser.add_argument(\frac{1}{2}-p1\frac{1}{2}, \frac{1}{2}-p1\frac{1}{2} targarse default=0.0, help=\frac{1}{2}\targarse parameter() args = parser.parse_args() p1 = args.p1 p2 = args.p2 On the command line we can provide any or all of these options: Terminal> program prog.py --parameter_1 2.1 --p2 -9

```
Evaluating string expressions with eval:

>>> x = 20
>>> r = eval('x + 1.1')
>>> r
21.1
>>> type(r)
<type 'float'>

Executing strings with Python code, using exec:

exec("""

def f(x):
    return %s
""" % sys. argv[1])
```

```
infile = open(filename, 'x')  # read
outfile = open(filename, 'w')  # write
outfile = open(filename, 'w')  # write
outfile = open(filename, 'a')  # oppend

# Reading
line = infile.readline()  # read the next line
filestr = infile.readline()  # read rest of file into string
lines = infile.readlines()  # read rest of file into list
for line in infile:  # read rest of file line by line

# Writing
outfile.write(s)  # add \n if you need it

# Closing
infile.close()
outfile.close()
```

```
A summarizing example: solving f(x)=0

Nonlinear algebraic equations like

x=1+\sin x
\tan x+\cos x=\sin 8x
x^5-3x^3=10
are usually impossible to solve by pen and paper, but can be solved by numerical methods. To this end, rewrite any equation as

f(x)=0
For the above we have (put everything on the left-hand side)

f(x)=x-1-\sin x
f(x)=\tan x+\cos x-\sin 8x
f(x)=x^5-3x^3-10
```

```
We shall learn about a method for solving f(x) = 0

A solution x of f(x) = 0 is called a root of f(x)

Outline of the next slides:

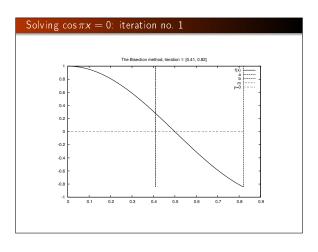
• Formulate a method for finding a root

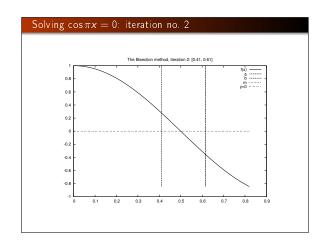
• Translate the method to a precise algorithm

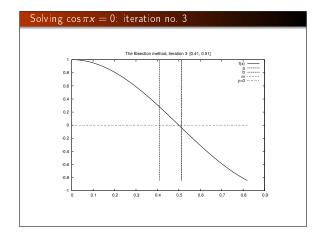
• Implement the algorithm in Python

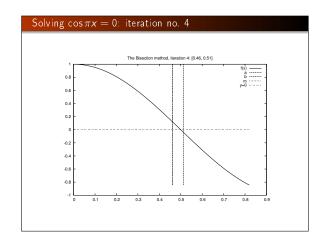
• Test the implementation
```

The Bisection method • Start with an interval [a,b] in which f(x) changes sign • Then there must be (at least) one root in [a,b]• Halve the interval: • m = (a+b)/2; does f change sign in left half [a,m]? • Yes: continue with left interval [a,m] (set b=m) • No: continue with right interval [m,b] (set a=m) • Repeat the procedure • After halving the initial interval [p,q] n times, we know that f(x) must have a root inside a (small) interval $2^{-n}(q-p)$ • The method is slow, but very safe • Other methods (like Newton's method) can be faster, but may also fail to locate a root - bisection does not fail









```
From method description to a precise algorithm

• We need to translate the mathematical description of the Bisection method to a Python program

• An important intermediate step is to formulate a precise algorithm

• Algorithm = detailed, code-like formulation of the method

for i in range(0, n+1):
    m = (a + b)/2
    if f(a)*f(m) <= 0:
        b = if root is in left half
    else:
        a = m # root is in right half

# f(m) has a root in [a, b]
```

The algorithm can be made more efficient

- f(a) is recomputed in each if test
- This is not necessary if a has not changed since last pass in the loop
- On modern computers and simple formulas for f(x) these extra computations do not matter
- However, in science and engineering one meets f functions that take hours or days to evaluate at a point, and saving some f(a) evaluations matters!
- Rule of thumb: remove redundant computations (unless the code becomes much more complicated, and harder

```
New, more efficient version of the algorithm
   Idea: save f(x) evaluations in variables
    f_a = f(a)
for i in range(0, n+1):
m = (a + b)/2
f_m = f(m)
if f_a*f_m <= 0:
             b = m # root is in left half
         else:
             a = m # root is in right half
f_a = f_m
     # f(x) has a root in [a, b]
```

How to choose n? That is, when to stop the iteration

- \bullet We want the error in the root to be ϵ or smaller
- After n iterations, the initial interval [a, b] is halved n times and the current interval has length $2^{-n}(b-a)$. This is sufficiently small if $2^{-n}(b-a) = \epsilon$ \Rightarrow $n = -\frac{\ln \epsilon - \ln(b-a)}{\ln 2}$
- A simpler alternative: just repeat halving until the length of the current interval is $<\epsilon$
- This is easiest done with a while loop: while b-a <= epsilon:
- We also add a test to check if f really changes sign in the initial inverval [a, b]

Final version of the Bisection algorithm

```
f_a=f(a)
if f_a*f(b) > 0:
   # error: f does not change sign in [a,b]
while b-a > epsilon:
   i = i + 1

m = (a + b)/2
    f m = f(m)
   if f_a*f_m <= 0:
        b = m # root is in left half
   b - m
else:
   a = m # root is in right half
f_a = f_m
# if x is the real root, |x-m| < epsilon
```

Python implementation of the Bisection algorithm

```
def f(x):
     return 2*x - 3 # one root x=1.5
eps = 1E-5
a, b = 0, 10
fa = f(a)
if fa*f(b) > 0:
     print 'f(x) does not change sign in [%g, %g].' % (a, b)
      sys.exit(1)
 i = 0 # iteration counter
 while b-a > eps:
    i += 1

m = (a + b)/2.0
     fm = f(m)
if fa*fm <= 0:
          b = m # root is in left half of [a, b]
          is:
    a = m  # root is in right half of [a, b]
    fa = fm
    # this is the approximate root
```

Implementation as a function (more reusable!)

```
def bisection(f, a, b, eps):
    fa = f(a)
if fa*f(b) > 0:
         return None, 0
         # Alternative: raise ValueError(
# 'No change of sign in [%g, %g]' % (a, b))
    i = 0 # iteration counter
     while b-a > eps:
         i += 1

m = (a + b)/2.0

fm = f(m)

if fa*fm <= 0:
             b = m # root is in left half of [a, b]
             a = m # root is in right half of [a, b]
fa = fm
print bisection(f=lambda x: 2*x-3, a=0, b=10, eps=1E-5)
```

```
• If we put the bisection function in a file bisection.py, we automatically have a module, and the bisection function can easily be imported in other programs to solve f(x) = 0
• We should make a test function too
def test_bisection():
def t(x):
    return 2*x - 3 # only one root x=1.5
eps = 1E.5
    x, iter = bisection(f, a=0, b=10, eps=eps)
    success = abs(x - 1.5) < eps # test_within eps tolerance assert success, 'found x=/% != 1.5' % x</pre>
if __name__ == ',__main__':
    test_bisection()
```

```
To the point of this lecture: get input!

We want to provide an f(x) formula at the command line along with a and b (3 command-line args)

Usage:

Terminal> python bisection.py 'sin(pi*x**3)-x**2' -1 3.5

Reading input:

def get input():
    """det f, a, b, eps from the command line."""
    from scitools.std import StringFunction
    f = StringFunction(sys.argv[1])
    a = float(sys.argv[2])
    b = float(sys.argv[3])
    eps = float(sys.argv[4])
    return f, a, b, eps

# Usage:
f, a, b, eps = get_input()
    x, iter = bisection(f, a, b, eps)
    print 'Found root x=%g in %d iterations' % (x, iter)
```

```
def get_input():
    """Get f, a, b, eps from the command line."""
    from scitcols.std import StringFunction
    try:
        a = float(sys.argv[2])
        b = float(sys.argv[3])
        eps = float(sys.argv[4])
    except IndexError:
        print 'Usage %s: f a b eps' % sys.argv[0]
        sys.exit(1)
    return f, a, b, eps
```

Applications of the Bisection method Two examples: tanh x = x and $tanh x^5 = x^5$: Terminal> python bisection_plot.py "x-tanh(x)" -1 1 Terminal> python bisection_plot.py "x**5-tanh(x**5)" -1 1 The first equation is easy to treat, but the second leads to much less accurate results. Why??