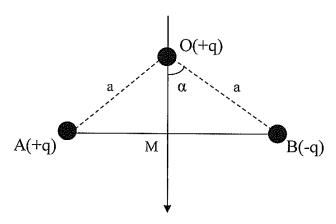
GROUP:....

Physics Midterm 1 (Duration:1h30)

Calculator and documents not allowed.

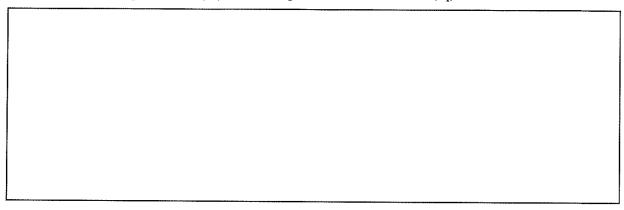
Exercise 1 Discrete distribution (4 points)

We consider three pointlike charges +q, +q and -q respectively located at points O, A and B. Point M belongs to AB bisector. Let's denote OA = OB = a.



- 1-a) Sketch in picture above the vectors describing the electrostatic fields generated at point M by the three charges and the total field $\vec{E}(M)$.
 - b) Write the norms $E_O(M)$, $E_A(M)$ and $E_B(M)$ as function of k, q, a and α . Deduce then the norm of the total field : E(M).

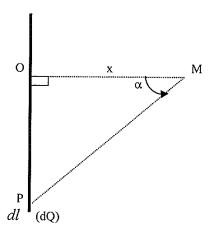
2- Write the electric potential V(M) created at point M as function of k, q, a and $\alpha.$



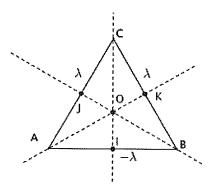
Exercise 2 Continuous distribution

(4 points)

We remind you that a linear element with charge dQ located at point P, which belongs to a wire with constant lineic charge λ , generates an elementary electric field $dE_x(M) = \frac{k.\lambda}{x} \cos(\alpha) d\alpha$ where α is defined as follows:



1-By using this result compute the norms of vectors $\overrightarrow{E_{AC}}(O)$, $\overrightarrow{E_{CB}}(O)$ and $\overrightarrow{E_{BA}}(O)$ respectively created at point O by the following continuous charge distributions. Sketch those vectors.

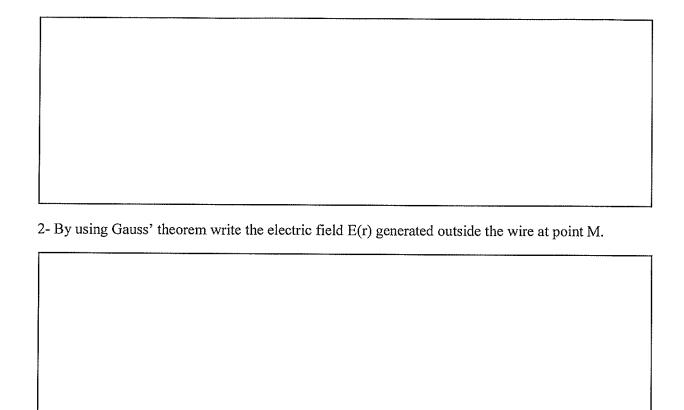


carrying a lineic ch	quilateral triangle w narge density λ and [hose edge length equals [AB] a negative density	to 2a. Lines [AC] an – λ.	d [BC] are
) Deduce from it t	he expression of the	total field created at po	int O as function of k	, λ and a.

Exercise 3 Gauss' theorem (6 points)

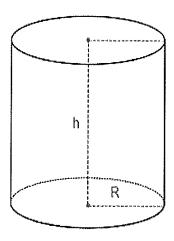
A wire of infinite length h is carrying a uniformly distributed positive charge Q of constant density.

1- Use symmetries and invariances to find the direction of the electric field vector which is generated by the wire at any exterior point M. One assumes that the wire is along (Oz)-axis.



3- From now on this wire with charge Q is surrounded by a hollow cylinder of same (Oz)-axis, of length h, radius R and such that its lateral surface is charged with a constant positive density σ .

a) Give the expression of the electric field E(r) in domains $r \le R$ and r > R.



o) Deduce from i	t the expression of th	he electric poten	tial V(r) in dom	ains r < R and r > R	
	•				
····	Electrokinetics	Part A	(3 points)		
t's consider a criable density	cylindrical conducto $I(r) = J_0 \frac{r^2}{R^2}, \text{ where}$	or of axis <i>Oz</i> and Jo and R are con	nd radius R which ristants.	ch is crossed by a	current I with
Write the total	current I crossing the $R = 3$ mm. Use the a	e conductor as f	unction of R and	l $J_{\scriptscriptstyle 0}$. Compute it ex	xplicitly for

2- Write the current I' which is crossing a section of radius $r < R$ as function of r.
Part B (3 points)
A conducting copper wire with conductivity $\gamma = 10^8 \Omega^{-1}$.m ⁻¹ , length L = 1m and radius R=1 mm is crossed by a current I with uniform density \vec{J} equals to $J = 2.10^7 \text{A/m}^2$. You will use the approximation $\pi \approx 3$.
Compute:
1- The current I crossing the conductor.
2- The electric field inside the conductor. Draw the quantities I, \vec{J} and \vec{E} .
3- The potential difference U between terminals of the conductor.
4- The conductor resistance R.
5- The electronic density n_{e-} . We have assumed that the mean velocity of charges is:
$V_{mean} = 0.2 m. s^{-1}$. Given data: $q_{e-} = -1.6.10^{-19} C$.

Useful formulas

1-Gauss' theorem :
$$\Phi(\vec{E}) = \iint_{S_g} \vec{E} . d\vec{S} = \frac{Q_{\text{int}}}{\varepsilon_0}$$

2- Lateral surface element of a cylinder of radius r and height h: $dS_{lat} = rd\theta.dz$

3- Gradient components in cylindrical coordinates

$$gra\vec{d} = \left(\frac{\partial}{\partial r}, \frac{1}{r}, \frac{\partial}{\partial \theta}, \frac{\partial}{\partial z}\right)$$