JEE MAINS 2020

EE24BTECH11019 - Dwarak A

JANUARY 7 SHIFT-2

- 1) If $3x + 4y = 12\sqrt{2}$ is a tangent to the ellipse $\left(\frac{x^2}{a^2}\right) + \left(\frac{y^2}{9}\right) = 1$ for some $a \in \mathbb{R}$, then the distance between the foci of the ellipse is:
 - a) $2\sqrt{5}$
 - b) $2\sqrt{7}$
 - c) $2\sqrt{2}$
 - d) 4
- 2) Let A, B, C and D be four non-empty sets. The Contrapositive statement of "If $A \nsubseteq B$ and B $\not\subseteq$ D then A $\not\subseteq$ C" is :
 - a) If $A \subseteq C$, then $B \subset A$ or $D \subset B$
 - b) If $A \nsubseteq C$, then $A \subseteq B$ and $B \subseteq D$
 - c) If $A \nsubseteq C$, then $A \nsubseteq B$ and $B \subseteq D$
 - d) If $A \nsubseteq C$, then $A \nsubseteq B$ or $B \nsubseteq D$
- 3) The coefficient of x^7 in the expression $(1+x)^{10}$ + $x(1+x)^9 + x^2(1+x)^8 + \dots + x^{10}$ is:
 - a) 420
 - b) 330
 - c) 210
 - d) 120
- 4) In a workshop, there are five machines and the probability of any one of them to be out of service on a day is $\frac{1}{4}$. If the probability that at most two machines will be out of service on the same day is $\left(\frac{3}{4}\right)^3 k$, then k is equal to:
 - a) $\frac{17}{2}$ b) 4

 - c) $\frac{17}{\cdot}$
- 5) The locus of mid points of the perpendiculars drawn from points on the line x = 2y to the line x = y is:
 - a) 2x 3y = 0
 - b) 3x 2y = 0
 - c) 5x 7y = 0
 - d) 7x 5y = 0
- 6) The value of α for which $4\alpha \int_{-1}^{2} e^{-\alpha |x|} dx = 5$
 - a) $\log_e 2$

- b) $\log_e \sqrt{2}$
- c) $\log_e\left(\frac{4}{3}\right)$
- d) $\log_e\left(\frac{3}{2}\right)$
- 7) If the sum of the first 40 terms of the series, 3+4+8+9+13+14+18+19+... is (102)m, then *m* is equal to :
 - a) 10
 - b) 25
 - c) 5
 - d) 20
- 8) If $\frac{3+i\sin\theta}{4-i\cos\theta}$, $\theta \in [0,2\pi]$ is a real number, then the argument of $\sin \theta + i \cos \theta$ is :
 - a) $\pi \tan^{-1}\left(\frac{4}{3}\right)$
 - b) $-\tan^{-1}\left(\frac{3}{4}\right)$
 - c) $\pi \tan^{-1}\left(\frac{3}{4}\right)$
 - d) $tan^{-1}\left(\frac{4}{3}\right)$
- 9) Let $A = [a_{ij}]$ and $B = [b_{ij}]$ be two 3×3 real matrices such that $b_{ij} - (3)^{(i+j-2)} a_{ji}$, where i, j =1, 2, 3. If the determinant of B is 81, then the determinant of A is:

 - a) $\frac{1}{9}$ b) $\frac{1}{81}$ c) $\frac{1}{3}$ d) 3
- 10) Let f(x) be a polynomial of degree 5 such that $x = \pm 1$ are its critical points. If $\lim_{x\to 0} \left(2 + \frac{f(x)}{x^3}\right) = 4$ then which of the following is not true?
 - a) f(1) 4f(-1) = 4
 - b) x = 1 is a point of maxima and x = -1 is a point of minima of f.
 - c) f is an odd function
 - d) x = 1 is a point of minima and x = -1 is a point of maxima of f.
- 11) The number of ordered pairs (r, k) for which $6 \cdot {}^{35}C_r = (k^2 - 3) \cdot {}^{36}C_{r+1}$, where k is an integer, is:
 - a) 4
 - b) 6
 - c) 2

- d) 3
- 12) Let $a_1, a_2, a_3,...$ be a G.P. such that $a_1 < 0$, $a_1 + a_2 = 4$ and $a_3 + a_4 = 16$. If $\sum_{i=1}^{9} a_i = 4\lambda$ then λ is equal to :
 - a) 171

 - b) $\frac{511}{3}$ c) -171
 - d) -513
- 13) Let **a**, **b**, **c** be three unit vectors such that $\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c} = 0$. If $\lambda = \overrightarrow{a} \cdot \overrightarrow{b} + \overrightarrow{b} \cdot \overrightarrow{c} + \overrightarrow{c} \cdot \overrightarrow{a}$ and $\overrightarrow{d} = \overrightarrow{a} \times \overrightarrow{b} + \overrightarrow{b} \times \overrightarrow{c} + \overrightarrow{c} \times \overrightarrow{a}$, then the ordered pair $(\lambda, \overrightarrow{d})$ is equal to:
 - a) $\left(\frac{3}{2}, 3\mathbf{a} \times \mathbf{c}\right)$

 - b) $\left(\frac{-3}{2}, 3\mathbf{c} \times \mathbf{b}\right)$ c) $\left(\frac{-3}{2}, 3\mathbf{a} \times \mathbf{b}\right)$
 - d) $\left(\frac{3}{2}, 3\mathbf{b} \times \mathbf{c}\right)$
- 14) Let y = y(x) be the solution curve of the differential equation $(y^2 - x) \left(\frac{dy}{dx}\right) = 1$ satisfying y(0) = 1 This curve intersects the x-axis at a point whose abscissa is:
 - a) 2 + e
 - b) 2
 - c) 2 e
 - d) −*e*
- 15) If θ_1 and θ_2 be respectively the smallest and largest values of θ in $(0, 2\pi) - \{\pi\}$ which satisfy the equation $2 \cot^2 \theta - \frac{5}{\sin \theta} + 4 = 0$ then $\int_{\theta_1}^{\theta_2} \cos^2 3\theta \, d\theta$ is equal to:
 - a) $\frac{2\pi}{3}$ b) $\frac{\pi}{3}$

 - c) $\left(\frac{\pi}{3}\right) + \left(\frac{1}{6}\right)$ d) $\frac{\pi}{9}$