EE24BTECH11019 - DWARAK A

Question: Find the values of x for which the distance between the points $\mathbf{A}(x,2)$ and $\mathbf{B}(9,8)$ is 10 units.

Solution: Distance formula:

Variable	Description	Value
A	First point	$\begin{pmatrix} x \\ 2 \end{pmatrix}$
В	Second point	$\binom{9}{8}$
d	Distance between A and B	10

TABLE 0: Variables Used

$$d = ||A - B|| \tag{0.1}$$

$$d = \sqrt{\|A\|^2 - 2A^{\top}B + \|B\|^2}$$
 (0.2)

$$d^2 = ||A||^2 - 2A^{\mathsf{T}}B + ||B||^2 \tag{0.3}$$

Substituting values,

$$10^{2} = \begin{pmatrix} x & 2 \end{pmatrix} \begin{pmatrix} x \\ 2 \end{pmatrix} - 2 \begin{pmatrix} x & 2 \end{pmatrix} \begin{pmatrix} 9 \\ 8 \end{pmatrix} + \begin{pmatrix} 9 & 8 \end{pmatrix} \begin{pmatrix} 9 \\ 8 \end{pmatrix}$$
 (0.4)

$$100 = (x^2 + 4) - 2(9x + 16) + (81 + 64)$$
(0.5)

$$x^2 - 18x + 17 = 0 ag{0.6}$$

$$(x-17)(x-1) = 0 (0.7)$$

$$x_1 = 17, x_2 = 1 \tag{0.8}$$

$$\implies A_1 = \begin{pmatrix} 17\\2 \end{pmatrix}, A_2 = \begin{pmatrix} 1\\2 \end{pmatrix} \tag{0.9}$$

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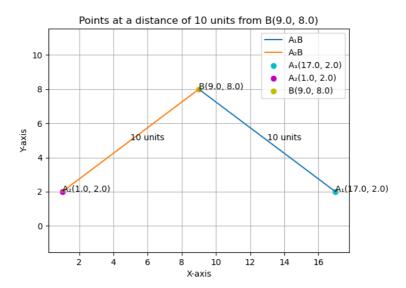


Fig. 0.1: Plot of points A_1 and A_2 at a distance of 10 units from B