

MATGEO PRESENTATION

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Problem Statement

Find a relation between x and y such that the point (x, y) is equidistant from the points $(3, 6)$ and $(-3, 4)$.

Variables Used

Variable	Description	Value
A	First point	$\begin{pmatrix} 3 \\ 6 \end{pmatrix}$
B	Second point	$\begin{pmatrix} -3 \\ 4 \end{pmatrix}$
C	Mid-point of A and B	$\left(\frac{\mathbf{A}+\mathbf{B}}{2}\right)$
X	Set of points equidistant from A and B	$\begin{pmatrix} x \\ y \end{pmatrix}$

Equidistant Point Condition

If \mathbf{X} is equidistant from points \mathbf{A} and \mathbf{B}

$$\|\mathbf{A} - \mathbf{X}\| = \|\mathbf{B} - \mathbf{X}\| \quad (3.1)$$

$$\|\mathbf{A} - \mathbf{X}\|^2 = \|\mathbf{B} - \mathbf{X}\|^2 \quad (3.2)$$

Expanding the squared norms:

$$\|\mathbf{A}\|^2 - 2\mathbf{A}^\top \mathbf{X} + \|\mathbf{X}\|^2 = \|\mathbf{B}\|^2 - 2\mathbf{B}^\top \mathbf{X} + \|\mathbf{X}\|^2 \quad (3.3)$$

Perpendicular Bisector Equation

The equation (3.3) simplifies to

$$(\mathbf{A} - \mathbf{B})^T \mathbf{X} = \frac{\|\mathbf{A}\|^2 - \|\mathbf{B}\|^2}{2} \quad (3.4)$$

Substituting the \mathbf{A} and \mathbf{B} values, (3.4) can be derived as follows

$$\begin{pmatrix} 3 - (-3) \\ 6 - 4 \end{pmatrix}^T \mathbf{X} = \frac{\left\| \begin{pmatrix} 3 \\ 6 \end{pmatrix} \right\|^2 - \left\| \begin{pmatrix} -3 \\ 4 \end{pmatrix} \right\|^2}{2} \quad (3.5)$$

$$\begin{pmatrix} 6 \\ 2 \end{pmatrix}^T \mathbf{X} = 10 \quad (3.6)$$

$$\Rightarrow \begin{pmatrix} 3 \\ 1 \end{pmatrix}^T \mathbf{X} = 5 \quad (3.7)$$

Final Line Equation

Thus, from (3.7) the line equation representing points equidistant from **A**(3, 6) and **B**(−3, 4) is:

$$3x + y = 5 \tag{3.8}$$

The code below verifies (3.7)

C Code I

```
1 #include <math.h>
2 #include <stdio.h>
3 #include <stdlib.h>
4 #include <string.h>
5 #include <sys/socket.h>
6 #include <netinet/in.h>
7 #include <unistd.h>
8
9 #include "libs/matfun.h"
10 #include "libs/geofun.h"
11
12 void line_gen(FILE *fptr, double **A, double **dir_vector, int no_rows,
13               int no_cols, double num_units_1, double num_units_2, int num_points)
14 {
15     double **output;
16     double **unit_dir_vector = Matscale(dir_vector, no_rows, no_cols, 1/
17     Matnorm(dir_vector, no_rows));
18     for (double i = -num_units_1; i <= num_units_2; i += (num_units_1 +
19     num_units_2)/num_points) {
```


C Code II

```
16     output = Matadd(A, Matscale(unit_dir_vector,no_rows,no_cols, i),
17     no_rows, no_cols);
18     fprintf(fptr, "%lf %lf\n", output[0][0], output[1][0]);
19     freeMat(output, no_rows);
20 }
21 }
22 int main(){
23     double x1 = 3.0, y1 = 6.0, x2 = -3.0, y2 = 4.0;
24     int m = 2, n = 1;
25     int k1 = 4, k2 = 4, res = 20;
26     double **A, **B, **mid_point, **m_ab, **n_ab;
27
28     A = createMat(m, n);
29     B = createMat(m, n);
30     mid_point = createMat(m, n);
31
32     A[0][0] = x1;
33     A[1][0] = y1;
34     B[0][0] = x2;
```

C Code III

```
35 B[1][0] = y2;
36
37 // Calculate the midpoint of AB
38 mid_point = Matscale(Matadd(A, B, m, n), m, n, 0.5);
39
40 // Calculate the vector AB and then the perpendicular bisector
  vector
41 m_ab = Matsub(B, A, m, n);
42 n_ab = normVec(m_ab);
43
44 // Open file to write points
45 FILE *fptr;
46 fptr = fopen("points.dat", "w");
47 if (fptr == NULL) {
48     printf("Error opening file!\n");
49     return 1;
50 }
51
52 fprintf(fptr, "%lf %lf\n", x1, y1);
53 fprintf(fptr, "%lf %lf\n", x2, y2);
```

C Code IV

```
54     fprintf(fp_ptr, "%lf %lf\n", mid_point[0][0], mid_point[1][0]);
55
56     // Generate points on the perpendicular bisector
57     line_gen(fp_ptr, mid_point, n_ab, m, n, k1, k2, res);
58
59     // Close the file
60     fclose(fp_ptr);
61
62     // Free all allocated memory
63     freeMat(A,m);
64     freeMat(B,m);
65     freeMat(mid_point,m);
66     freeMat(m_ab,m);
67     freeMat(n_ab,m);
68     return 0;
69 }
```

Python Code I

```
1 import numpy as np
2 import matplotlib.pyplot as plt
3
4 # Load the points from the .dat file
5 points = np.loadtxt('points.dat', max_rows = 3)
6 data = np.loadtxt('points.dat', skiprows = 3)
7
8 # Extract the x and y coordinates
9 x = data[:, 0]
10 y = data[:, 1]
11
12 # Define the points A, B, and (0,9)
13 [A, B, C] = np.array(points)
14 txtA, txtB, txtC =
15     'A'+str(tuple(A)), 'B'+str(tuple(B)), 'C'+str(tuple(C))
16
17 # Plot the locus of X
18 plt.figure()
```

Python Code II

```
18 plt.plot(x, y, label = 'Locus of X')
19 plt.plot(points[:, 0], points[:, 1], label = 'AB')
20 plt.scatter(A[0], A[1], c = 'c', label = txtA)
21 plt.scatter(B[0], B[1], c = 'm', label = txtB)
22 plt.scatter(C[0], C[1], c = 'y', label = txtC)
23
24 # Annotate the points
25 plt.annotate(txtA, xy = A)
26 plt.annotate(txtB, xy = B)
27 plt.annotate(txtC, xy = C)
28
29 # Plot Specs
30 plt.xlabel('X-axis')
31 plt.ylabel('Y-axis')
32 plt.title('Plot of Locus of X')
33 plt.axis('equal')
34 plt.grid(True)
35 plt.legend()
```

Python Code III

```
36 plt.tight_layout()
37
38 # Save and Display plot
39 plt.savefig("../figs/plot.png")
40 plt.show()
```

Plot

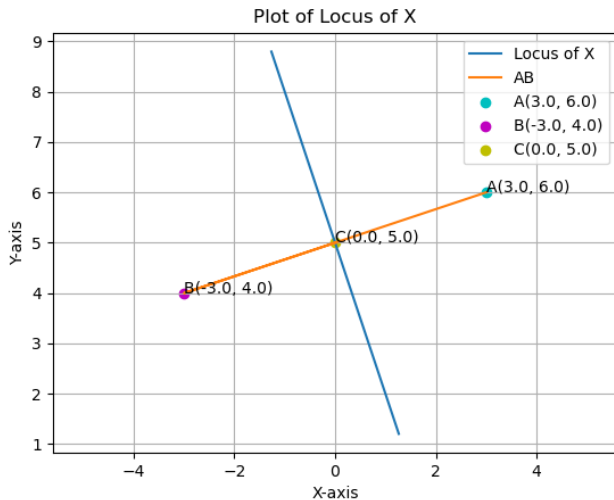


Figure: Locus of point X, equidistant from **A** and **B**