

# 1.9.19

EE24BTECH11019 - DWARAK A

**Question:** Find the values of  $x$  for which the distance between the points  $\mathbf{A}(x, 2)$  and  $\mathbf{B}(9, 8)$  is 10 units.

**Solution:** Distance formula :

Variable	Description	Value
<b>A</b>	First point	$\begin{pmatrix} x \\ 2 \end{pmatrix}$
<b>B</b>	Second point	$\begin{pmatrix} 9 \\ 8 \end{pmatrix}$
$d$	Distance between <b>A</b> and <b>B</b>	10

TABLE 0: Variables Used

$$d = \|A - B\| \quad (0.1)$$

$$d = \sqrt{\|A\|^2 - 2A^\top B + \|B\|^2} \quad (0.2)$$

$$d^2 = \|A\|^2 - 2A^\top B + \|B\|^2 \quad (0.3)$$

Substituting values,

$$10^2 = \begin{pmatrix} x & 2 \end{pmatrix} \begin{pmatrix} x \\ 2 \end{pmatrix} - 2 \begin{pmatrix} x & 2 \end{pmatrix} \begin{pmatrix} 9 \\ 8 \end{pmatrix} + \begin{pmatrix} 9 & 8 \end{pmatrix} \begin{pmatrix} 9 \\ 8 \end{pmatrix} \quad (0.4)$$

$$100 = (x^2 + 4) - 2(9x + 16) + (81 + 64) \quad (0.5)$$

Rearranging terms,

$$x^2 - 18x + 17 = 0 \quad (0.6)$$

$$(x - 17)(x - 1) = 0 \quad (0.7)$$

So,

$$x_1 = 17, x_2 = 1 \quad (0.8)$$

Finally,

$$A_1 = \begin{pmatrix} 17 \\ 2 \end{pmatrix}, A_2 = \begin{pmatrix} 1 \\ 2 \end{pmatrix} \quad (0.9)$$

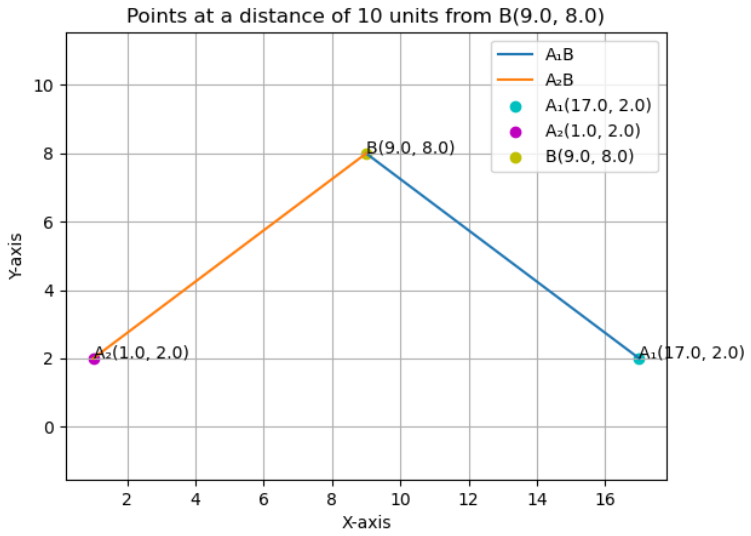


Fig. 0.1: Plot of points  $A_1$  and  $A_2$  at a distance of 10 units from  $B$