## EE24BTECH11019 - DWARAK A

**Question**: Find the values of x for which the distance between the points  $\mathbf{A}(x,2)$  and  $\mathbf{B}(9,8)$  is 10 units.

Solution: Distance formula:

Variable	Description	Value
A	First point	$\begin{pmatrix} x \\ 2 \end{pmatrix}$
В	Second point	$\binom{9}{8}$
d	Distance between <b>A</b> and <b>B</b>	10

TABLE 0: Variables Used

$$||A - B|| = d \tag{0.1}$$

$$\sqrt{\|A\|^2 - 2A^{\mathsf{T}}B + \|B\|^2} = d \tag{0.2}$$

$$||A||^2 - 2A^{\mathsf{T}}B + ||B||^2 = d^2 \tag{0.3}$$

Substituting values,

$$\begin{pmatrix} x & 2 \end{pmatrix} \begin{pmatrix} x \\ 2 \end{pmatrix} - 2 \begin{pmatrix} x & 2 \end{pmatrix} \begin{pmatrix} 9 \\ 8 \end{pmatrix} + \begin{pmatrix} 9 & 8 \end{pmatrix} \begin{pmatrix} 9 \\ 8 \end{pmatrix} = 10^2$$
 (0.4)

$$(x^2 + 4) - 2(9x + 16) + (81 + 64) = 100 (0.5)$$

$$x^2 - 18x + 17 = 0 ag{0.6}$$

$$(x-17)(x-1) = 0 (0.7)$$

$$x_1 = 17, x_2 = 1 \tag{0.8}$$

$$\implies A_1 = \begin{pmatrix} 17\\2 \end{pmatrix}, A_2 = \begin{pmatrix} 1\\2 \end{pmatrix} \tag{0.9}$$

1

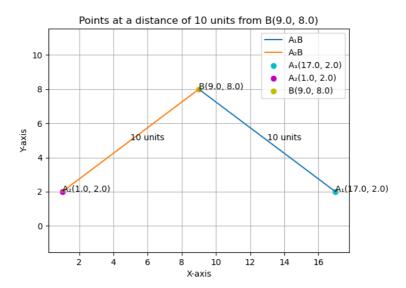


Fig. 0.1: Plot of points  $A_1$  and  $A_2$  at a distance of 10 units from B