

MATGEO PRESENTATION

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Problem Statement

Find a relation between x and y such that the point (x, y) is equidistant from the points $(3, 6)$ and $(-3, 4)$.

Variables Used

Variable	Description	Value
A	First point	$\begin{pmatrix} 3 \\ 6 \end{pmatrix}$
B	Second point	$\begin{pmatrix} -3 \\ 4 \end{pmatrix}$
C	Mid-point of A and B	$\left(\frac{\mathbf{A+B}}{2}\right)$
X	Set of points equidistant from A and B	$\begin{pmatrix} x \\ y \end{pmatrix}$

Equidistant Point Condition

If \mathbf{X} is equidistant from points \mathbf{A} and \mathbf{B}

$$\|\mathbf{A} - \mathbf{X}\| = \|\mathbf{B} - \mathbf{X}\| \quad (3.1)$$

$$\|\mathbf{A} - \mathbf{X}\|^2 = \|\mathbf{B} - \mathbf{X}\|^2 \quad (3.2)$$

Expanding the squared norms:

$$\|\mathbf{A}\|^2 - 2\mathbf{A}^\top \mathbf{X} + \|\mathbf{X}\|^2 = \|\mathbf{B}\|^2 - 2\mathbf{B}^\top \mathbf{X} + \|\mathbf{X}\|^2 \quad (3.3)$$

Perpendicular Bisector Equation

The equation simplifies to

$$(\mathbf{A} - \mathbf{B})^T \mathbf{X} = \frac{\|\mathbf{A}\|^2 - \|\mathbf{B}\|^2}{2} \quad (3.4)$$

Substituting the \mathbf{A} and \mathbf{B} values, (3.4) can be derived as follows

$$\begin{pmatrix} 6 \\ 2 \end{pmatrix}^T \mathbf{X} = \frac{\left\| \begin{pmatrix} 3 \\ 6 \end{pmatrix} \right\|^2 - \left\| \begin{pmatrix} -3 \\ 4 \end{pmatrix} \right\|^2}{2} \quad (3.5)$$

$$\begin{pmatrix} 6 \\ 2 \end{pmatrix}^T \mathbf{X} = 10 \quad (3.6)$$

$$\Rightarrow \begin{pmatrix} 3 \\ 1 \end{pmatrix}^T \mathbf{X} = 5 \quad (3.7)$$

Final Line Equation

Thus, from (3.7) the line equation representing points equidistant from **A**(3, 6) and **B**(−3, 4) is:

$$3x + y = 5 \tag{3.8}$$

The code below verifies (3.7)

C Code I

```
1 #include <math.h>
2 #include <stdio.h>
3 #include <stdlib.h>
4 #include <string.h>
5 #include <sys/socket.h>
6 #include <netinet/in.h>
7 #include <unistd.h>
8
9 #include "libs/matfun.h"
10 #include "libs/geofun.h"
11
12 void line_gen(FILE *fptr, double **A, double **dir_vector, int no_rows,
13               int no_cols, int num_points_1, int num_points_2) {
14     double **output;
15     for (int i = -num_points_1; i <= num_points_2; i++) {
16         output = Matadd(A, Matscale(dir_vector, no_rows, no_cols, (double)i
17                                     / (num_points_1 + num_points_2)), no_rows, no_cols);
18         fprintf(fptr, "%lf %lf\n", output[0][0], output[1][0]);
19         freeMat(output, no_rows);
20     }
21 }
```


C Code II

```
18     }
19 }
20
21 int main(){
22     double x1 = 3.0, y1 = 6.0, x2 = -3.0, y2 = 4.0;
23     int m = 2, n = 1;
24     int k1 = 10, k2 = 10;
25     double **A, **B, **mid_point, **s_ab, **bisectorABMidpoint;
26
27     A = createMat(m, n);
28     B = createMat(m, n);
29     mid_point = createMat(m, n);
30
31     A[0][0] = x1;
32     A[1][0] = y1;
33     B[0][0] = x2;
34     B[1][0] = y2;
35
36     // Calculate the midpoint of AB
37     mid_point = Matscale(Matadd(A, B, m, n), m, n, 0.5);
```

C Code III

```
38 // Calculate the vector AB and then the perpendicular bisector
39 vector
40 s_ab = Matsub(B, A, m, n);
41 bisectorABMidpoint = normVec(s_ab);
42
43 // Open file to write points
44 FILE *fptr;
45 fptr = fopen("points.dat", "w");
46 if (fptr == NULL) {
47     printf("Error opening file!\n");
48     return 1;
49 }
50
51 fprintf(fptr, "%lf %lf\n", x1, y1);
52 fprintf(fptr, "%lf %lf\n", x2, y2);
53 fprintf(fptr, "%lf %lf\n", mid_point[0][0], mid_point[1][0]);
54
55 // Generate points on the perpendicular bisector
56 line_gen(fptr, mid_point, bisectorABMidpoint, m, n, 10, 10);
```

C Code IV

```
57  
58 // Close the file  
59 fclose(fptr);  
60  
61 // Free all allocated memory  
62 freeMat(A,m);  
63 freeMat(B,m);  
64 freeMat(mid_point,m);  
65 freeMat(s_ab,m);  
66 freeMat(bisectorABMidpoint,m);  
67 return 0;  
68 }
```

Python Code I

```
1 import numpy as np
2 import matplotlib.pyplot as plt
3
4 # Load the points from the .dat file
5 points = np.loadtxt('points.dat', max_rows = 3)
6 data = np.loadtxt('points.dat', skiprows = 3)
7
8 # Extract the x and y coordinates
9 x = data[:, 0]
10 y = data[:, 1]
11
12 # Define the points A, B, and (0,9)
13 [A, B, C] = np.array(points)
14 txtA, txtB, txtC =
15     'A'+str(tuple(A)), 'B'+str(tuple(B)), 'C'+str(tuple(C))
16
17 # Plot the locus of X
18 plt.figure()
```

Python Code II

```
18 plt.plot(x, y, label = 'Locus of X')
19 plt.plot(points[:, 0], points[:, 1], label = 'AB')
20 plt.scatter(A[0], A[1], c = 'c', label = txtA)
21 plt.scatter(B[0], B[1], c = 'm', label = txtB)
22 plt.scatter(C[0], C[1], c = 'y', label = txtC)
23
24 # Annotate the points
25 plt.annotate(txtA, xy = A)
26 plt.annotate(txtB, xy = B)
27 plt.annotate(txtC, xy = C)
28
29 # Plot specs
30 plt.xlabel('X-axis')
31 plt.ylabel('Y-axis')
32 plt.title('Plot of Locus of X')
33 plt.axis('equal')
34 plt.grid(True)
35 plt.legend(loc = 'upper left')
```

Python Code III

```
36  
37 # Save and Display plot  
38 plt.savefig("../figs/plot.png")  
39 plt.show()
```

Plot

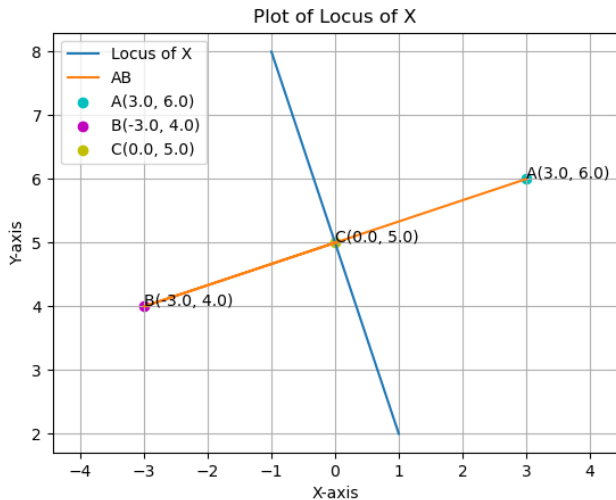


Figure: Locus of point X, equidistant from **A** and **B**