## Supplementary material: Chemical kinetics and transport properties [1]

## A Chemistry reduction and validation<sup>1</sup>

The Analytically Reduced Chemistry (ARC) used in this study was derived to achieve an accurate description of the combustion process of methane/air/hydrogen flames for several mixing conditions. The reduction was carried out with the ARCANE code co-developed by CERFACS and Cornell University [2]. It is a fully automatic multi-step reduction tool relying on DRGEP [3], chemical lumping [4] and Quasi-Steady State assumption [5].

The well known GRI-Mech 3.0 scheme [6] was chosen as detailed reference mechanism. This scheme comprises 53 species and 325 reactions.

To guarantee the accuracy of the mechanism, several canonical cases were included in the sampled data needed for the reduction. These cases and the thresholds errors associated on interest quantities are detailed in Tab. A.1.

| Reactor type              | Isochoric 0D reactor | Freely propagating premixed flame |
|---------------------------|----------------------|-----------------------------------|
| Temperature [K]           | 1000                 | 300                               |
| Pressure [bar]            | 1                    | 1                                 |
| Equivalence ratio         | 1                    | 0.6, 1, 1.5                       |
| Error threshold on        | 5%                   | /                                 |
| auto-ignition delay time  | 970                  | /                                 |
| Error threshold on        | /                    | 5%                                |
| laminar flame speed       | /                    | 370                               |
| Error threshold on        | /                    | 5%                                |
| maximum heat release rate | /                    | 370                               |
| Error threshold on        | 1%                   | 1%                                |
| maximum temperature       | 1/0                  | 1/0                               |

Table A.1: Table summarizing the cases used for the reduction and the associated threshold errors.

For each target case, three fuel compositions were considered: pure hydrogen, pure methane and a blend of 50% of hydrogen and 50% of methane in terms of mole fractions. For all cases air was considered as oxidizer. Consequently, the entire reduction database comprises 12 cases, i.e., 4

<sup>&</sup>lt;sup>1</sup>For addition information on the ARC mechanism and its reduction procedure please contact Q. Cazères. *Email address*: cazeres@cerfacs.fr (personal adress: quentin.cazeres@gmail.com)

operating conditions multiplied by 3 different fuels. To improve precision, different targets were set for each fuel as indicated in Tab. A.2.

| Fuels   | Hydrogen (H <sub>2</sub> )                           | Methane (CH <sub>4</sub> )                                | Blend (50% $H_2 + 50\% \text{ CH}_4$ )                                     |
|---------|--|---|--|
| Targets | H <sub>2</sub> , H <sub>2</sub> O, Heat release rate | CH <sub>4</sub> , CO, CO <sub>2</sub> , Heat release rate | H <sub>2</sub> , CH <sub>4</sub> , CO, CO <sub>2</sub> , Heat release rate |

Table A.2: Table summarizing the target quantities used for the reduction for each fuel.

The reduced ARC mechanism generated by ARCANE comprises 20 transported species, 166 reactions and 9 species in Quasi-Steady State:

- The transported species are H<sub>2</sub>, H, O, O<sub>2</sub>, OH, H<sub>2</sub>O, HO<sub>2</sub>, H<sub>2</sub>O<sub>2</sub>, CH<sub>3</sub>, CH<sub>4</sub>, CO, CO<sub>2</sub>, CH<sub>2</sub>O, CH<sub>3</sub>O, CH<sub>3</sub>OH, C<sub>2</sub>H<sub>2</sub>, C<sub>2</sub>H<sub>4</sub>, C<sub>2</sub>H<sub>6</sub>, CH<sub>2</sub>CO, N<sub>2</sub>.
- The Quasi-Steady State species are CH, CH<sub>2</sub>, CH<sub>2</sub>(S), HCO, CH<sub>2</sub>OH, C<sub>2</sub>H<sub>3</sub>, C<sub>2</sub>H<sub>5</sub>, HCCO, CH<sub>2</sub>CHO.

A compleate description of the reactions is given in Tab. A.3 and in the attached ARC.csv file.

The mechanism was validated on a broader operability spectrum compared to reduction cases. Results of the validation are displayed in Fig. A.1 showing a really good agreement between the ARC and the detailed mechanism with the maximum error on interest quantities being less than 5%. An additional validation specific for the MIRADAS test rig studied in this work was also performed. Indeed, as discussed in the manuscript, the flame developed inside this system is characterized by the presence of a hydrogen/methane-air burnt premix diffusion branch. This is here represented by a counter-flow diffusion flame with pure hydrogen at room temperature coming from one side and equilibrium products of  $\phi = 0.8$  mixture of methane and air at adiabatic flame temperature on the other side. The same solution is presented in the manuscript (Fig. 2) considering, however, preheating of the hydrogen. Temperature and heat release rate profiles predicted by the ARC mechanism are found in excellent agreement with the ones obtained with the detailed mechanism as shown in Fig. A.2(a-b).

Concluding, the afore discussed validations give confidence to the authors in the capabilities of the derived ARC mechanism to represent correctly the complex combustion process of the investigated system.

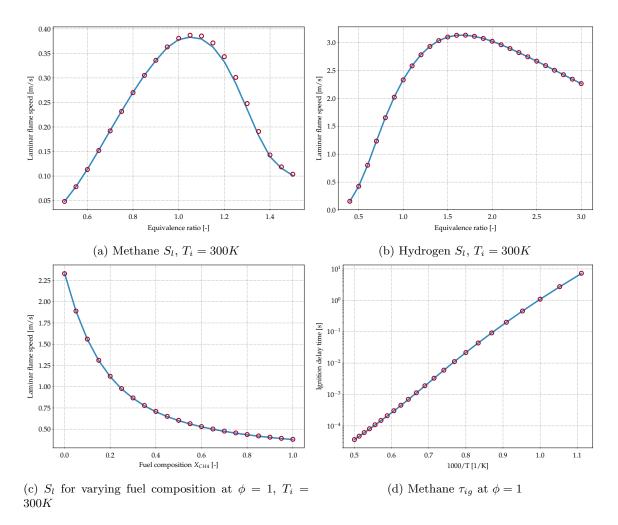


Figure A.1: Validation of the ARC mechanism on canonical cases. Laminar flame speed  $S_l$  as function of the equivalence ratio  $\phi$  for pure methane/air (a) and pure hydrogen/air (b) flames. (c)  $S_l$  for varying fuel composition at  $\phi = 1$ . (d) Methane auto-ignition delay time  $\tau_{ig}$  at  $\phi = 1$ . In all plots, blue line refers to results obtained with the GRI-Mech 3.0 mechanism while ARC predictions are indicated by the red circles. For all cases, the pressure is 1 bar.

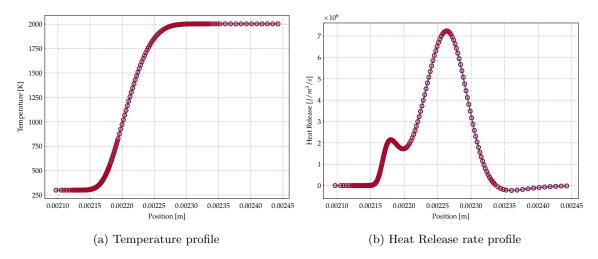


Figure A.2: Validation of the mechanism on canonical cases. Temperature (a) and heat release rate (b) profiles for a counterflow diffusion flame of H<sub>2</sub> ( $T_{\rm H_2}^i=300$  K) against the equilibrium burnt gases from lean ( $\phi=0.8$ ) CH<sub>4</sub>/Air premixed flame ( $T_{\rm g}^i=2000$  K). Blue line refers to results obtained with the GRI-Mech 3.0 mechanism while ARC predictions are indicated by the red circles. Width between the two inlets is 0.04 m but plots are zoomed to show the reactive zone.

Table A.3: List of reactions with A the pre-exponential factor in  $m^{3(n-1)}/\text{kmol}^{n-1}/\text{s}$  with n the order of the reaction, b the temperature exponent and Ea the activation energy in J/kmol. In the case of fall-off reactions, two sets of Arrhenius coefficients are specified, the first one being the low temperature set and the second one the high temperature set.

| No.      | Reaction  | A               | 9             | $E_{a}$        |
|----------|---|-----------------|---------------|----------------|
| -        | $H + O + M \longleftrightarrow OH + M$  | 5.000000E+11    | -1.000000E+00 | 0.000000E±00   |
| 1        | C2H6:3.00E+00 CH4:2.00E+00 CO:1.50E+00 CO2:2.00E+00 H2:2.00E+00 H2O:6.00E+00      |                 |               |                |
| 2        | $H2 + O \longleftrightarrow H + OH$   | 3.870000E+01    | 2.700000E+00  | 2.619184E+07   |
| 3        | $HO2 + O \longleftrightarrow O2 + OH$   | 2.000000E+10    | 0.0000000E+00 | 0.0000000E+00  |
| 4        | $H2O2 + O \longleftrightarrow HO2 + OH$   | 9.630000E + 03  | 2.000000E+00  | 1.673600E + 07 |
| ರ        | $CH + O \longleftrightarrow CO + H$   | 5.700000E+10    | 0.0000000E+00 | 0.0000000E+00  |
| 9        | $CH2 + O \longleftrightarrow H + HCO$   | 8.000000E+10    | 0.0000000E+00 | 0.0000000E+00  |
| 2        | $CH2(S) + O \longleftrightarrow CO + H2$  | 1.500000E + 10  | 0.000000E+00  | 0.0000000E+00  |
| $\infty$ | $CH2(S) + O \longleftrightarrow H + HCO$  | 1.500000E+10    | 0.0000000E+00 | 0.0000000E+00  |
| 6        | $CH3 + O \longleftrightarrow CH2O + H$  | 5.0600000E + 10 | 0.0000000E+00 | 0.0000000E+00  |
| 10       | $CH4 + O \longleftrightarrow CH3 + OH$  | 1.020000E + 06  | 1.500000E+00  | 3.598240E + 07 |
| 11       | $CO + O(+M) \longleftrightarrow CO2(+M)$  | 6.020000E + 08  | 0.0000000E+00 | 1.255200E+07   |
|          |   | 1.800000E+07    | 0.0000000E+00 | 9.978840E+06   |
|          | C2H6:3.0E+00 CH4:2.0E+00 CO:1.5E+00 CO2:3.5E+00 H2:2.0E+00 H2O:6.0E+00 O2:6.0E+00 |                 |               |                |
| 12       | $HCO + O \longleftrightarrow CO + OH$   | 3.0000000E+10   | 0.000000E+00  | 0.000000E+00   |
| 13       | 1   | 3.000000E+10    | 0.0000000E+00 | 0.0000000E+00  |
| 14       |   | 3.900000E+10    | 0.0000000E+00 | 1.481136E+07   |
| 15       | $CH2OH + O \longleftrightarrow CH2O + OH$   | 1.000000E+10    | 0.0000000E+00 | 0.0000000E+00  |
| 16       | $CH3O + O \longleftrightarrow CH2O + OH$  | 1.000000E+10    | 0.0000000E+00 | 0.0000000E+00  |
| 17       | <b>↓</b> 0  | 3.880000E + 02  | 2.500000E+00  | 1.297040E+07   |
| 18       | ~   | 1.300000E + 02  | 2.500000E+00  | 2.092000E+07   |
| 19       | <b>+</b>  | 1.350000E+04    | 2.000000E+00  | 7.949600E+06   |
| 20       | $\downarrow$  | 6.940000E+03    | 2.000000E+00  | 7.949600E+06   |
| 21       | $\downarrow \hspace*{0.2cm}$  | 3.000000E+10    | 0.0000000E+00 | 0.0000000E+00  |
| 22       | $\downarrow \hspace{0.25cm}$  | 1.250000E+04    | 1.830000E+00  | 9.204800E + 05 |
| 23       | $\uparrow$  | 2.240000E+10    | 0.0000000E+00 | 0.0000000E+00  |
| 24       | $\uparrow$  | 8.980000E+04    | 1.920000E+00  | 2.380696E+07   |
| 22       | 1   | 1.000000E+11    | 0.0000000E+00 | 0.0000000E+00  |
| 56       |   | 1.000000E+10    | 0.0000000E+00 | 3.347200E+07   |
| 27       | $CH2CO + O \longleftrightarrow CH2 + CO2$   | 1.750000E+09    | 0.0000000E+00 | 5.648400E+06   |
| 28       | $\overline{}$   | 2.500000E + 09  | 0.0000000E+00 | 1.999952E+08   |
| 56       | $CH2O + O2 \longleftrightarrow HCO + HO2$   | 1.000000E+11    | 0.0000000E+00 | 1.673600E + 08 |
| 30       |   | 2.800000E+12    | -8.600000E-01 | 0.0000000E+00  |
|          | C2H6:1.50E+00 CO:7.50E-01 CO2:1.50E+00 H2O:0.00E+00 N2:0.00E+00 O2:0.00E+00       |                 |               |                |
| 31       | $H + 2.02 \longleftrightarrow H02 + 02$   | 2.080000E+13    | -1.240000E+00 | 0.0000000E+00  |
| 32       |   | 1.126000E + 13  | -7.600000E-01 | 0.0000000E+00  |
| 33       |   | 2.600000E + 13  | -1.240000E+00 | 0.0000000E+00  |
| 34       | $H + O2 \longleftrightarrow O + OH$   | 2.650000E + 13  | -6.707000E-01 | 7.129954E+07   |
| 35       | $2~\mathrm{H} + \mathrm{M} \longleftrightarrow \mathrm{H2} + \mathrm{M}$          | 1.000000E+12    | -1.000000E+00 | 0.000000E+00   |
|          | C2H0:3.UUE+UU CH4:2.UUE+UU CO2:U.UUE+UU H2:U.UUE+UU H2O:U.UUE+UU                  |                 |               |                |

| No. | Reaction   | A                     | b             | $E_a$           |
|-----|--|-----------------------|---------------|-----------------|
| 36  | $2 \text{ H} + \text{H2} \longleftrightarrow 2 \text{ H2}$   | 9.000000E+10          | -6.000000E-01 | 0.0000000E+00   |
| 37  | $2 \text{ H} + \text{H2O} \longleftrightarrow \text{H2} + \text{H2O}$  | 6.000000E+13          | -1.250000E+00 | 0.0000000E+00   |
| 38  | $\mathrm{H}+\mathrm{OH}+\mathrm{M} \longleftrightarrow \mathrm{H2O}+\mathrm{M}$  | 2.200000E+16          | -2.000000E+00 | 0.0000000E+00   |
|     | C2H6:3.00E+00 CH4:2.00E+00 H2:7.30E-01 H2O:3.65E+00  |                       |               |                 |
| 39  | $H + HO2 \longleftrightarrow H2O + O$  | 3.970000E+09          | 0.000000E+00  | 2.807464E + 06  |
| 40  | $H + HO2 \longleftrightarrow H2 + O2$  | 4.480000E+10          | 0.0000000E+00 | 4.468512E + 06  |
| 41  | $\mathrm{H} + \mathrm{HO2} \longleftrightarrow 2~\mathrm{OH}$  | 8.400000E+10          | 0.000000E+00  | 2.656840E + 06  |
| 42  | $H + H2O2 \longleftrightarrow H2 + HO2$  | 1.210000E+04          | 2.000000E+00  | 2.175680E + 07  |
| 43  | $H + H202 \longleftrightarrow H20 + OH$  | 1.000000E+10          | 0.000000E+00  | 1.506240E + 07  |
| 44  | $CH2 + H (+M) \longleftrightarrow CH3 (+M)$  | 1.040000E+20          | -2.760000E+00 | 6.694400E + 06  |
|     | $5.62E-01\ 9.10E+01\ 5.84E+03\ 8.55E+03$   | 6.000000E+11          | 0.0000000E+00 | 0.0000000E+00   |
|     | C2H6:3.0E+00 CH4:2.0E+00 CO:1.5E+00 CO2:2.0E+00 H2:2.0E+00 H2O:6.0E+00   |                       |               |                 |
| 45  | $CH2(S) + H \longleftrightarrow CH + H2$   | 3.000000E + 10        | 0.0000000E+00 | 0.0000000E+00   |
| 46  | $CH3 + H (+M) \longleftrightarrow CH4 (+M)$  | 2.620000E+27          | -4.760000E+00 | 1.020896E + 07  |
|     | 7.83E-01 7.40E+01 2.94E+03 6.96E+03  | $\mid 1.390000E + 13$ | -5.340000E-01 | 2.242624E + 06  |
| 7   | CZH6:3.UE+UU   | 8 600000E+05          | 1 690000E±00  | 7 535756F±07    |
| ; × |  | 7.340000E±10          | 0.00000E+00   | 0.000000E+00    |
| 64  | $CH_{1} = CH_{1} = CH_{2} = C$ | 1.93000E-10           | -4 820000E+00 | 9.739159E±07    |
| 2   | _  | 5.210000E 1.28        | 4:020001   00 | 1 506940F±07    |
|     | 7.13E-01 1.03E+02 1.23E+03 4.10E+03<br>C2H6:3 0E+00 CH4:2 0E+00 CO:1 5E+00 CO:2 0E+00 H2:2 0E+00 H2O:6 0E+00   | 9.400000T-00          | 4.04000012-01 | 1.30024011      |
| 0   |  | 9 200000E±27          | -/ SOOOOFT    | 9 39630/E±07    |
| 3   | 7.58E-01.9.40E+01.1.56E+03.4.20E+03  | 5.400000E+08          | 4.540000F-01  | 1.087840E+07    |
|     | C2H6:3.0E+00 CH4:2.0E+00 CO:1.5E+00 CO:2.0E+00 H2:2.0E+00 H2O:6.0E+00  |                       |               |                 |
| 51  | $CH2O + H \longleftrightarrow H2 + HCO$  | 5.740000E+04          | 1.900000E+00  | 1.147253E+07    |
| 52  | $CH2OH + H \longleftrightarrow CH2O + H2$  | 2.000000E+10          | 0.0000000E+00 | 0.0000000E+00   |
| 53  |  | 1.650000E + 08        | 6.500000E-01  | -1.188256E+06   |
| 54  | $CH2OH + H \longleftrightarrow CH2(S) + H2O$   | 3.280000E+10          | -9.000000E-02 | 2.552240E+06    |
| 55  | $CH3O + H (+M) \longleftrightarrow CH3OH (+M)$   | 4.660000E+35          | -7.440000E+00 | 5.891072E + 07  |
|     | $7.00E-01\ 1.00E+02\ 9.00E+04\ 1.00E+04$   | 2.430000E+09          | 5.150000E-01  | 2.092000E + 05  |
|     |  |                       |               |                 |
| 26  |  | 4.150000E+04          | 1.630000E+00  | 8.050016E + 06  |
| 57  |  | 2.000000E+10          | 0.000000E+00  | 0.000000E+00    |
| 28  |  | 1.500000E+09          | 5.000000E-01  | -4.602400E+05   |
| 59  |  | 2.620000E + 11        | -2.300000E-01 | 4.476880E+06    |
| 0.9 |  | 1.700000E+04          | 2.100000E+00  | 2.037608E+07    |
| 61  | 7  | 4.200000E+03          | 2.100000E+00  | 2.037608E+07    |
| 62  | $C2H2 + H (+M) \longleftrightarrow C2H3 (+M)$  | 3.800000E + 34        | -7.270000E+00 | 3.020848E + 07  |
|     | $7.51E-01\ 9.85E+01\ 1.30E+03\ 4.17E+03$   | $\mid 5.600000E{+}09$ | 0.000000E+00  | 1.004160E + 07  |
|     | C2H6:3.0E+00 CH4:2.0E+00 CO:1.5E+00 CO2:2.0E+00 H2:2.0E+00 H2O:6.0E+00   |                       |               |                 |
| 63  | $C2H3 + H \longleftrightarrow C2H2 + H2$   | 3.000000E + 10        | 0.0000000E+00 | 0.0000000E + 00 |
| 64  | $\operatorname{C2H4} + \operatorname{H} (+\operatorname{M}) \longleftrightarrow \operatorname{C2H5} (+\operatorname{M})$   | 6.000000E+35          | -7.620000E+00 | 2.916248E+07    |
|     | 9.75E-01 2.10E+02 9.84E+02 4.37E+03<br>Caite: 9 0F 1 00 Cit4: 9 0E 1 00 CO:1 EE 1 00 CO9: 9 0E 1 00 II3-3 0E 1 00 II3-3 0E 1 00  | 5.400000E+08          | 4.540000E-01  | 7.614880E+06    |
|     | CZH0:3.0E+00 CH4:Z.0E+00 CO:1.3E+00 COZ:Z.0E+00 HZ:Z.0E+00 HZO:0.0E+00   |                       |               |                 |

| ,   | 1  | •               | •             | t               |
|-----|--|-----------------|---------------|-----------------|
| No. |  | A               | q             | $E_a$           |
| 65  | $C2H4 + H \longleftrightarrow C2H3 + H2$                               | 1.325000E+03    | 2.530000E+00  | 5.121216E+07    |
| 99  | $C2H5 + H (+M) \longleftrightarrow C2H6 (+M)$                          | 1.990000E + 35  | -7.080000E+00 | 2.797004E+07    |
|     | 6.4  | 5.2100000E + 14 | -9.900000E-01 | 6.610720E + 06  |
|     | C2H6:3.0E+00 CH4:2.0E+00 CO:1.5E+00 CO2:2.0E+00 H2:2.0E+00 H2O:6.0E+00 |                 |               |                 |
| 29  | $C2H5 + H \longleftrightarrow C2H4 + H2$                               | 2.0000000E + 09 | 0.0000000E+00 | 0.000000E+00    |
| 89  | $C2H6 + H \longleftrightarrow C2H5 + H2$                               | 1.150000E + 05  | 1.900000E+00  | 3.150552E + 07  |
| 69  | $H + HCCO \longleftrightarrow CH2(S) + CO$                             | 1.000000E+11    | 0.0000000E+00 | 0.0000000E+00   |
| 20  | $CH2CO + H \longleftrightarrow H2 + HCCO$                              | 5.0000000E + 10 | 0.0000000E+00 | 3.347200E+07    |
| 71  | $CH2CO + H \longleftrightarrow CH3 + CO$                               | 1.130000E + 10  | 0.0000000E+00 | 1.434275E+07    |
| 7.5 | $CO + H2 (+M) \longleftrightarrow CH2O (+M)$                           | 5.070000E + 21  | -3.420000E+00 | 3.529204E+08    |
|     | $9.32E-01\ 1.97E+02\ 1.54E+03\ 1.03E+04$                               | 4.300000E+04    | 1.500000E+00  | 3.330464E + 08  |
|     | C2H6:3.0E+00 CH4:2.0E+00 CO:1.5E+00 CO2:2.0E+00 H2:2.0E+00 H2O:6.0E+00 |                 |               |                 |
| 73  | $H2 + OH \longleftrightarrow H + H2O$                                  | 2.1600000E + 05 | 1.510000E+00  | 1.435112E + 07  |
| 74  | $2 \text{ OH } (+M) \longleftrightarrow H2O2 (+M)$                     | 2.300000E+12    | -9.000000E-01 | -7.112800E+06   |
|     | $7.35E-01\ 9.40E+01\ 1.76E+03\ 5.18E+03$                               | 7.400000E+10    | -3.700000E-01 | 0.0000000E + 00 |
|     | $^{\circ}$   |                 |               |                 |
| 75  | $2 \text{ OH} \longleftrightarrow \text{H2O} + \text{O}$               | 3.570000E+01    | 2.400000E+00  | -8.828240E+06   |
| 92  | $HO2 + OH \longleftrightarrow H2O + O2$                                | 1.450000E + 10  | 0.0000000E+00 | -2.092000E+06   |
| 22  | $H2O2 + OH \longleftrightarrow H2O + HO2$                              | 2.000000E+09    | 0.0000000E+00 | 1.786568E+06    |
| 28  | $H2O2 + OH \longleftrightarrow H2O + HO2$                              | 1.700000E+15    | 0.0000000E+00 | 1.230514E + 08  |
| 79  | $CH + OH \longleftrightarrow H + HCO$                                  | 3.000000E + 10  | 0.0000000E+00 | 0.0000000E + 00 |
| 80  | $CH2 + OH \longleftrightarrow CH2O + H$                                | 2.0000000E + 10 | 0.0000000E+00 | 0.000000E+00    |
| 81  | $CH2 + OH \longleftrightarrow CH + H2O$                                | 1.130000E+04    | 2.0000000E+00 | 1.255200E + 07  |
| 85  | $CH2(S) + OH \longleftrightarrow CH2O + H$                             | 3.000000E + 10  | 0.0000000E+00 | 0.000000E+00    |
| 83  | $CH3 + OH(+M) \longleftrightarrow CH3OH(+M)$                           | 4.000000E + 30  | -5.920000E+00 | 1.313776E + 07  |
|     | $4.12E-01\ 1.95E+02\ 5.90E+03\ 6.39E+03$                               | 2.790000E+15    | -1.430000E+00 | 5.564720E + 06  |
|     | C2H6:3.0E+00 CH4:2.0E+00 CO:1.5E+00 CO2:2.0E+00 H2:2.0E+00 H2O:6.0E+00 |                 |               |                 |
| 84  | $CH3 + OH \longleftrightarrow CH2 + H2O$                               | 5.6000000E + 04 | 1.600000E+00  | 2.267728E+07    |
| 85  | $CH3 + OH \longleftrightarrow CH2(S) + H2O$                            | 6.440000E+14    | -1.340000E+00 | 5.928728E + 06  |
| 98  | $CH4 + OH \longleftrightarrow CH3 + H2O$                               | 1.0000000E + 05 | 1.6000000E+00 | 1.305408E+07    |
| 87  | ⋆  | 4.760000E+04    | 1.228000E+00  | 2.928800E + 05  |
| 88  | $\wedge$   | 5.0000000E + 10 | 0.0000000E+00 | 0.0000000E+00   |
| 86  | $CH2O + OH \longleftrightarrow H2O + HCO$                              | 3.430000E + 06  | 1.180000E+00  | -1.870248E+06   |
| 06  | $CH2OH + OH \longleftrightarrow CH2O + H2O$                            | 5.0000000E + 09 | 0.0000000E+00 | 0.0000000E+00   |
| 91  | $\wedge$   | 5.0000000E + 09 | 0.0000000E+00 | 0.0000000E+00   |
| 95  | -  | 1.440000E+03    | 2.000000E+00  | -3.514560E + 06 |
| 93  | _  | 6.3000000E+03   | 2.0000000E+00 | 6.276000E+06    |
| 94  | $\downarrow \hspace{0.25cm}$   | 2.180000E-07    | 4.500000E+00  | -4.184000E+06   |
| 95  | $\uparrow$   | 4.830000E-07    | 4.000000E+00  | -8.368000E+06   |
| 96  | $\uparrow$   | 5.0000000E + 09 | 0.0000000E+00 | 0.0000000E + 00 |
| 97  | $\uparrow$   | 3.6000000E + 03 | 2.0000000E+00 | 1.046000E + 07  |
| 86  | → C2H5 →   | 3.540000E+03    | 2.120000E+00  | 3.640080E + 06  |
| 96  | $\rightarrow$ HO + C   | 7.500000E+09    | 0.000000E+00  | 8.368000E+06    |
| 100 | $2 \text{ HO2} \longleftrightarrow \text{H2O2} + \text{O2}$            | 1.300000E+08    | 0.000000E+00  | -6.819920E+06   |

| 1   |   |                |                 |                |
|-----|---|----------------|-----------------|----------------|
| No. | Reaction  | A              | 9               | $E_a$          |
| 101 | $2 \text{ HO2} \longleftrightarrow \text{H2O2} + \text{O2}$   | 4.200000E+11   | 0.0000000E + 00 | 5.020800E + 07 |
| 102 | $CH2 + HO2 \longleftrightarrow CH2O + OH$   | 2.000000E+10   | 0.0000000E+00   | 0.0000000E+00  |
| 103 | $CH3 + HO2 \longleftrightarrow CH4 + O2$  | 1.000000E+09   | 0.000000E+00    | 0.000000E+00   |
| 104 | - 1   | 3.780000E+10   | 0.000000E+00    | 0.000000E+00   |
| 105 | $\uparrow$  | 1.500000E+11   | 0.000000E+00    | 9.874240E+07   |
| 106 | $CH2O + HO2 \longleftrightarrow H2O2 + HCO$   | 5.600000E+03   | 2.0000000E+00   | 5.020800E+07   |
| 107 |   | 6.710000E+10   | 0.000000E+00    | 0.0000000E+00  |
| 108 | $CH + H2 \longleftrightarrow CH2 + H$   | 1.080000E+11   | 0.000000E+00    | 1.301224E+07   |
| 109 | $\downarrow$  | 5.710000E+09   | 0.0000000E+00   | -3.158920E+06  |
| 110 | 1   | 3.000000E+10   | 0.000000E+00    | 0.000000E+00   |
| 111 | $CH4 \longleftrightarrow$   | 6.000000E+10   | 0.000000E+00    | 0.000000E+00   |
| 112 | $CH + CO (+M) \longleftrightarrow HCCO (+M)$  | 2.690000E+22   | -3.740000E+00   | 8.100224E+06   |
|     | $5.76E-01\ 2.37E+02\ 1.65E+03\ 5.07E+03$  | 5.000000E+10   | 0.000000E+00    | 0.0000000E+00  |
|     | C2H6:3.0E+00 CH4:2.0E+00 CO:1.5E+00 CO2:2.0E+00 H2:2.0E+00 H2O:6.0E+00                                  |                |                 |                |
| 113 | $\wedge$  | 1.900000E+11   | 0.0000000E+00   | 6.607373E+07   |
| 114 | $CH + CH2O \longleftrightarrow CH2CO + H$   | 9.4600000E+10  | 0.0000000E+00   | -2.154760E+06  |
| 115 |   | 5.0000000E+09  | 0.0000000E+00   | 6.276000E + 06 |
| 116 | $\wedge$  | 5.0000000E+02  | 2.0000000E+00   | 3.025032E+07   |
| 117 | $CH2 + CH3 \longleftrightarrow C2H4 + H$  | 4.000000E+10   | 0.0000000E+00   | 0.0000000E+00  |
| 118 | $CH2 + CH4 \longleftrightarrow 2 CH3$   | 2.4600000E+03  | 2.000000E+00    | 3.460168E+07   |
| 119 | $CH2 + CO (+M) \longleftrightarrow CH2CO (+M)$  | 2.690000E + 27 | -5.110000E+00   | 2.968548E+07   |
|     | $5.91E-01\ 2.75E+02\ 1.23E+03\ 5.18E+03$  | 8.100000E+08   | 5.000000E-01    | 1.886984E+07   |
|     | C2H6:3.0E+00 CH4:2.0E+00 CO:1.5E+00 CO2:2.0E+00 H2:2.0E+00 H2O:6.0E+00                                  |                |                 |                |
| 120 |   | 1.500000E+10   | 0.0000000E+00   | 2.510400E+06   |
| 121 | $CH2(S) + O2 \longleftrightarrow CO + H + OH$   | 2.800000E+10   | 0.0000000E+00   | 0.0000000E+00  |
| 122 | $CH2(S) + O2 \longleftrightarrow CO + H2O$  | 1.200000E+10   | 0.0000000E+00   | 0.0000000E+00  |
| 123 | $CH2(S) + H2 \longleftrightarrow CH3 + H$   | 7.000000E+10   | 0.0000000E+00   | 0.0000000E+00  |
| 124 | $CH2(S) + H2O(+M) \longleftrightarrow CH3OH(+M)$  | 1.880000E+32   | -6.360000E+00   | 2.108736E+07   |
|     | $6.03E-01\ 2.08E+02\ 3.92E+03\ 1.02E+04$  | 4.820000E+14   | -1.160000E+00   | 4.790680E+06   |
|     | $\vdash$  |                |                 |                |
| 125 | + H2O ←   | 3.000000E+10   | 0.0000000E+00   | 0.0000000E+00  |
| 126 | $+ \text{CH3} \longleftrightarrow$  | 1.200000E+10   | 0.0000000E+00   | -2.384880E+06  |
| 127 | + CH4 ←   | 1.6000000E+10  | 0.000000E+00    | -2.384880E+06  |
| 128 | + CO +  | 9.0000000E+09  | 0.0000000E+00   | 0.0000000E+00  |
| 129 |   | 7.000000E+09   | 0.000000E+00    | 0.0000000E+00  |
| 130 |   | 1.400000E+10   | 0.0000000E+00   | 0.0000000E+00  |
| 131 | $C2H6 + CH2(S) \longleftrightarrow C2H5 + CH3$  | 4.000000E+10   | 0.0000000E+00   | -2.301200E+06  |
| 132 | $CH3 + O2 \longleftrightarrow CH3O + O$   | 3.560000E+10   | 0.000000E+00    | 1.275283E+08   |
| 133 | $CH3 + 02 \longleftrightarrow CH2O + OH$  | 2.310000E+09   | 0.0000000E+00   | 8.499796E+07   |
| 134 |   | 2.450000E+01   | 2.470000E+00    | 2.167312E+07   |
| 135 | $2 \text{ CH3 (+M)} \longleftrightarrow C2H6 \text{ (+M)}$  | 3.4000000E+35  | -7.030000E+00   | 1.155621E+07   |
|     | 6.19E-01 7.32E+01 1.18E+03 1.00E+04   | 6.770000E+13   | -1.180000E+00   | 2.736336E+06   |
| 136 | CZH6:3.0E+00 CH4:Z.0E+00 CO:1.5E+00 COZ:Z.0E+00 HZ:Z.0E+00 HZ:D.0E+00 $\times$ CZH5:3.0E+00 HZO:0.0E+00 | 6.840000E+09   | 1.000000E-01    | 4.435040E+07   |
|     |   |                |                 |                |

| No. | Reaction  | A                  | 9             | $E_{a}$         |
|-----|---|--------------------|---------------|-----------------|
| 137 | $CH3 + HCO \longleftrightarrow CH4 + CO$  | 2.648000E+10       | 0.000000E+00  | 0.000000E+00    |
| 138 | $CH2O + CH3 \longleftrightarrow CH4 + HCO$  | 3.320000E+00       | 2.810000E+00  | 2.451824E+07    |
| 139 | $CH3 + CH3OH \longleftrightarrow CH2OH + CH4$   | 3.000000E + 04     | 1.500000E+00  | 4.158896E+07    |
| 140 | $CH3 + CH3OH \longleftrightarrow CH3O + CH4$  | 1.000000E + 04     | 1.500000E+00  | 4.158896E+07    |
| 141 | $C2H4 + CH3 \longleftrightarrow C2H3 + CH4$   | 2.270000E+02       | 2.0000000E+00 | 3.849280E + 07  |
| 142 | $C2H6 + CH3 \longleftrightarrow C2H5 + CH4$   | 6.140000E+03       | 1.740000E+00  | 4.372280E+07    |
| 143 | $H2O + HCO \longleftrightarrow CO + H + H2O$  | 1.500000E + 15     | -1.000000E+00 | 7.112800E+07    |
| 144 | $\mathrm{HCO} + \mathrm{M} \longleftrightarrow \mathrm{CO} + \mathrm{H} + \mathrm{M}$ | 1.870000E+14       | -1.000000E+00 | 7.112800E+07    |
|     | C2H6:3.00E+00 CH4:2.00E+00 CO:1.50E+00 CO2:2.00E+00 H2:2.00E+00 H2O:0.00E+00          |                    |               |                 |
| 145 | $HCO + O2 \longleftrightarrow CO + HO2$   | 1.345000E + 10     | 0.0000000E+00 | 1.673600E + 06  |
| 146 | $CH2OH + O2 \longleftrightarrow CH2O + HO2$   | 1.800000E+10       | 0.0000000E+00 | 3.765600E + 06  |
| 147 | $CH3O + O2 \longleftrightarrow CH2O + HO2$  | 4.280000E-16       | 7.600000E+00  | -1.476952E+07   |
| 148 | $C2H3 + O2 \longleftrightarrow CH2O + HCO$  | 4.580000E+13       | -1.390000E+00 | 4.246760E + 06  |
| 149 | $C2H4 (+M) \longleftrightarrow C2H2 + H2 (+M)$  | 1.580000E + 48     | -9.300000E+00 | 4.091952E + 08  |
|     | $7.35E-01\ 1.80E+02\ 1.04E+03\ 5.42E+03$  | 8.000000E+12       | 4.400000E-01  | 3.630457E + 08  |
|     | C2H6:3.0E+00 CH4:2.0E+00 CO:1.5E+00 CO2:2.0E+00 H2:2.0E+00 H2O:6.0E+00                |                    |               |                 |
| 150 | $C2H5 + O2 \longleftrightarrow C2H4 + HO2$  | 8.400000E + 08     | 0.0000000E+00 | 1.621300E + 07  |
| 151 | $HCCO + O2 \longleftrightarrow 2 CO + OH$   | 3.200000E + 09     | 0.0000000E+00 | 3.573136E + 06  |
| 152 | 4   | 3.370000E+10       | 0.0000000E+00 | 0.0000000E+00   |
| 153 |   | 6.700000E+03       | 1.830000E+00  | 9.204800E + 05  |
| 154 |   | 5.000000E + 12     | 0.0000000E+00 | 7.250872E+07    |
| 155 | $CH3 + OH \longrightarrow CH2O + H2$  | 8.0000000E+06      | 5.000000E-01  | -7.342920E+06   |
| 156 | $CH2 + O2 \longrightarrow CO2 + 2 H$  | 5.800000E + 09     | 0.0000000E+00 | 6.276000E + 06  |
| 157 | $CH2 + 02 \longleftrightarrow CH2O + O$   | 2.400000E+09       | 0.0000000E+00 | 6.276000E + 06  |
| 158 | $CH2(S) + H2O \longrightarrow CH2O + H2$  | 6.820000E+07       | 2.500000E-01  | -3.912040E+06   |
| 159 | $C2H3 + O2 \longleftrightarrow CH2CHO + O$  | 3.030000E + 08     | 2.900000E-01  | 4.602400E+04    |
| 160 | $C2H3 + O2 \longleftrightarrow C2H2 + HO2$  | 1.337000E+03       | 1.610000E+00  | -1.606656E+06   |
| 161 | $CH2CO + H (+M) \longleftrightarrow CH2CHO (+M)$                                      | 1.012000E + 36     | -7.630000E+00 | 1.612514E+07    |
|     | $4.65E-01\ 2.01E+02\ 1.77E+03\ 5.33E+03$  | 4.865000E + 08     | 4.220000E-01  | -7.342920E+06   |
|     | C2H6:3.0E+00 CH4:2.0E+00 CO:1.5E+00 CO2:2.0E+00 H2:2.0E+00 H2O:6.0E+00                |                    |               |                 |
| 162 |   | $ 1.500000E{+}11 $ | 0.0000000E+00 | 0.0000000E + 00 |
| 163 | $\uparrow$  | 1.810000E+07       | 0.0000000E+00 | 0.0000000E+00   |
| 164 |   | 2.350000E+07       | 0.0000000E+00 | 0.0000000E+00   |
| 165 | $CH2CHO + H \longleftrightarrow CH3 + HCO$  | 2.200000E+10       | 0.000000E+00  | 0.0000000E+00   |
| 100 | $\uparrow$  | 1.100000E+10       | 0.000000E+00  | U.UUUUUUUE+UU   |

## B Transport properties modeling<sup>2</sup>

The simplified transport properties adopted in AVBP consist in a constant mixture Prandtl (Pr) number and a constant Schmidt (Sc) number for each species of the chemical scheme. These values are optimized during the mechanism reduction procedure (see Section A). Pr and Sc numbers for the ARC scheme used in the simulations are summarized in Tab. B.1.

| Property | Specie                | Value |
|----------|-----------------------|-------|
|          | $\mathrm{H}_2$        | 0.207 |
|          | ${ m H}$              | 0.124 |
|          | O                     | 0.484 |
|          | $O_2$                 | 0.751 |
|          | OH                    | 0.493 |
|          | $H_2O$                | 0.558 |
|          | $\mathrm{HO}_2$       | 0.749 |
|          | $H_2O_2$              | 0.754 |
|          | $\mathrm{CH}_3$       | 0.679 |
| Schmidt  | $\mathrm{CH}_4$       | 0.682 |
|          | $^{\rm CO}$           | 0.755 |
|          | $CO_2$                | 0.944 |
|          | $\mathrm{CH_{2}O}$    | 0.868 |
|          | $\mathrm{CH_{3}O}$    | 0.888 |
|          | $\mathrm{CH_{3}OH}$   | 0.889 |
|          | $C_2H_2$              | 0.891 |
|          | $\mathrm{C_{2}H_{4}}$ | 0.900 |
|          | $C_2H_6$              | 0.988 |
|          | $\mathrm{CH_{2}CO}$   | 1.025 |
|          | $N_2$                 | 0.717 |
| Prandlt  | Mixture               | 0.712 |

Table B.1: Constant Schmidt number for each species and mixture Prandtl number used in the simplified transport model.

To take into account the variability of the transport properties when considering a mixture with light molar weight components (e.g.  $H_2$ ), a database of Prandtl number and  $N_2$  Schmidt number as a function of the ternary mixture composition (i.e.  $CH_4$ ,  $H_2$ ,  $N_2$ ) has been computed with the complex-transport module of Cantera. The results of this analysis are showed in Fig. 2(d) of the manuscript. It is then straightforward to compute a polynomial fitting of these two variables and express them as a function of the molar fraction X of  $CH_4$  and  $H_2$  (i.e. the two independent variables), as follows:

<sup>&</sup>lt;sup>2</sup>For additional information on the transport properties modeling please contact P. W. Agostinelli. *E-mail*: agostinelli@cerfacs.fr (personal e-mail: walter-agostinelli@tiscali.it)

$$Prandtl = f(X_{CH_4}, X_{H_2}) = f_{00} + f_{10}X_{CH_4} + f_{01}X_{H_2} + \dots + f_{ab}X_{CH_4}{}^{a}X_{H_2}{}^{b}$$
(1)

$$N_2 \text{ Schmidt} = g(X_{CH_4}, X_{H_2}) = g_{00} + g_{10}X_{CH_4} + g_{01}X_{H_2} + \dots + g_{cd}X_{CH_4}{}^c X_{H_2}{}^d$$
(2)

In particular, the function f in Eq. (1) and the function g in Eq. (2) have been chosen to be a piecewise-defined polynomials with respect to  $X_{CH_4}$  and  $X_{H_2}$  with the coefficients being determined in order to reduce the root mean square errors with respect to the database from Cantera. The resulting polynomial fitting is able to correctly provide the exact Prandtl number and  $N_2$  Schmidt number, with a coefficient of determination  $R^2$  of 0.9996, while not worsening the code performances. Table B.2 and Tab. B.3 report the coefficients used in the piecewise-defined fitting functions and their intervals of validity for the Pr number and the  $N_2$  Sc number expressions, respectively.

| Coefficient $(f_{ab})$ | Value      | Interval  |
|------------------------|------------|---|
| $\overline{f_{00}}$    | 0.7076     |   |
| $\mathrm{f}_{10}$      | 0.02157    |   |
| $f_{01}$               | -1.608     |   |
| $f_{20}$               | -0.013     |   |
| $\mathrm{f}_{11}$      | 0.3687     |   |
| $f_{02}$               | 3.643      |   |
| $f_{30}$               | -0.003734  |   |
| $f_{21}$               | 0.04177    |   |
| $\mathrm{f}_{12}$      | -0.5402    |   |
| $f_{03}$               | -3.758     |   |
| $f_{40}$               | -0.0001393 | for $X_{CH_4}$ in $[0,1]$ and $X_{H_2}$ in $[0,1-X_{CH_4}]$ |
| $f_{31}$               | -0.03073   |   |
| $f_{22}$               | -0.3168    |   |
| $f_{13}$               | -0.2286    |   |
| $f_{04}$               | 1.302      |   |
| $ m f_{50}$            | -0.001286  |   |
| $\mathrm{f}_{41}$      | 0.001784   |   |
| $f_{32}$               | 0.09282    |   |
| $f_{23}$               | 0.4952     |   |
| $\mathrm{f}_{14}$      | 0.7872     |   |
| $f_{05}$               | 0.3903     |   |

Table B.2: Coefficient of the piecewise-defined polynomial in Eq. (1) expressing the mixture Prandtl number as a function of  $X_{CH_4}$  and  $X_{H_2}$ .

| Coefficient $(g_{cd})$ | Value    | Interval   |
|------------------------|----------|--|
| g <sub>00</sub>        | 1.295    |  |
| $g_{10}$               | -1.574   |  |
| g <sub>01</sub>        | 4.886    |  |
| $g_{20}$               | 7.229    |  |
| $g_{11}$               | -35.28   |  |
| $g_{02}$               | -7.989   |  |
| $g_{30}$               | -18.36   |  |
| $g_{21}$               | 94.96    |  |
| $g_{12}$               | 56.5     |  |
| $g_{03}$               | 5.543    |  |
| $g_{40}$               | 20.05    | for $X_{CH_4}$ in $[0.05,1]$ and $X_{H_2}$ in $[0.05,1-X_{CH_4}]$    |
| <b>g</b> 31            | -109.1   |  |
| $g_{22}$               | -115.2   |  |
| $g_{13}$               | -39.54   |  |
| $g_{04}$               | -0.1024  |  |
| $g_{50}$               | -7.872   |  |
| $g_{41}$               | 44.01    |  |
| $g_{32}$               | 71.57    |  |
| $g_{23}$               | 39.7     |  |
| $g_{14}$               | 10.76    |  |
| $g_{05}$               | -2.227   |  |
| $g_{00}$               | 2.833    |  |
| $g_{10}$               | -32.13   |  |
| $g_{01}$               | -0.04449 |  |
| $g_{11}$               | 69.78    |  |
| $g_{02}$               | 0.3827   |  |
| $g_{12}$               | -108.3   | for $X_{CH_4}$ in $[0,0.05]$ and $X_{H_2}$ in $[0.05,1-X_{CH_4}]$    |
| $g_{03}$               | -3.604   |  |
| $g_{13}$               | 90.81    |  |
| $g_{04}$               | 6.146    |  |
| $g_{14}$               | -28.94   |  |
| g <sub>05</sub>        | -4.295   |  |
| $g_{00}$               | 0.717    |  |
| $g_{10}$               | 10.05    | for $X_{CH_4}$ in [0,0.05] and $X_{H_2}$ in [0,0.05- $X_{CH_4}$ ]    |
| g <sub>01</sub>        | 42.32    |  |
| $g_{d00}$              | 2.66     |  |
| $g_{d10}$              | -28.82   | for $X_{CH_4}$ in $[0,0.05]$ and $X_{H_2}$ in $[0.05-X_{CH_4},0.05]$ |
| g <sub>d01</sub>       | 3.457    |  |

Table B.3: Coefficient of the piecewise-defined polynomial in Eq. (2) expressing the  $N_2$  Schmidt number as a function of  $X_{\rm CH_4}$  and  $X_{\rm H_2}$ .

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