

## Random Variables, Means, & Variances

**CREDIT:** The questions on this document were written by Erik Packard, PhD, Associate Professor of Mathematics at Colorado Mesa University.

- Problem D

- Let  $X$  be a score picked at random from the scores 0, 3, 3, and 9. Let  $Y$  be a score picked at random from the scores 0, 2, and 5.
- Do the following:
  1. Find the mean, variance, and standard deviation of  $X$ .
  2. Find the mean, variance, and standard deviation of  $Y$ .
  3. Let  $Z$  be a new random variable which is simply 5 added to each score from which  $X$  was originally chosen. Find the mean, variance, and standard deviation of  $Z$ . Check that the following rules agree with your calculations. Note that  $c = 5$ ,  $X + c$  is the  $Z$ .

Check:  $\mu_{X+c} = \mu_X + c$   
 \_\_\_\_\_ = \_\_\_\_\_

Check:  $(\sigma_{X+c})^2 = (\sigma_X)^2$   
 \_\_\_\_\_ = \_\_\_\_\_

4. Let  $Z$  be a new random variable which is simply each score from which  $X$  was chosen multiplied by 2. Find the mean, variance, and standard deviation of  $Z$ . Check that the following rules agree with your calculations. Note that  $c = 2$ ,  $cX$  is the  $Z$ .

Check:  $\mu_{cX} = c\mu_X$   
 \_\_\_\_\_ = \_\_\_\_\_

Check:  $(\sigma_{cX})^2 = c^2(\sigma_X)^2$   
 \_\_\_\_\_ = \_\_\_\_\_

5. Let  $Z$  be a new random variable which one score for the  $X$  numbers picked at random plus one score from the  $Y$  numbers picked at random. Find the mean, variance and standard deviation of  $Z$ . (First find all the possible sums). Check that the following rules agree with your calculations. Note that  $X + Y$  is the  $Z$ .

Check:  $\mu_{X+Y} = \mu_X + \mu_Y$   
 \_\_\_\_\_ = \_\_\_\_\_

Check:  $(\sigma_{X+Y})^2 = (\sigma_X)^2 + (\sigma_Y)^2$   
 \_\_\_\_\_ = \_\_\_\_\_

6. Let  $Z$  be a new random variable which one score for the  $X$  numbers picked at random minus one score from the  $Y$  numbers picked at random. Find the mean, variance, and standard deviation of  $Z$ . (First find all the possible differences). Check that the following rules agree with your calculations. Note that  $X - Y$  is the  $Z$ .

Check:  $\mu_{X-Y} = \mu_X - \mu_Y$

\_\_\_\_\_ = \_\_\_\_\_

Check:  $(\sigma_{X-Y})^2 = (\sigma_X)^2 + (\sigma_Y)^2$

\_\_\_\_\_ = \_\_\_\_\_