Research

Austin Castelo April 21, 2018

```
Initialize Data
```

```
Market Data <- read excel("C:/Users/caste/Desktop/PSTAT199/Market Data.xlsx")
MD <- Market Data
MD = MD[-1,]
MD$ Price Earnings Ratio One-Year Earnings [143:146] = c(17.03, 18.15, 20.02, 22.18)
MD$ Price Earnings Ratio Ten-Year Earnings [144:146] = c(24.86, 26.49, 24.21)
GDP <- data.matrix(MD[2:2])</pre>
S_P <- read_excel("C:/Users/caste/Desktop/PSTAT199/Market Data.xlsx",
                        sheet = "S&P Daily")
SPY <- data.matrix(S P[8])
Adjusting for Inflation and finding D(t)
Adj_inf <- MD$CPI[80:147]/MD$CPI[80]## Adjusted inflation relataive 1950
SPY = SPY[1:68,]/Adj_inf
D_t \leftarrow matrix(nrow = 66, ncol = 1)
for(i in 2:66){D_t[i-1] = (SPY[i]/SPY[i-1])-1}
D_t = D_t[-66,]
PE1_lm = lm(D_t~MD$`Price Earnings Ratio One-Year Earnings`[80:144])
CPI_{lm} = lm(D_t \sim MD\$CPI[80:144])
GDP_lm = lm(D_t[11:65] \sim MD_s^GDP (current US_s)^[90:144])
PE10_lm = lm(D_t~MD$`Price Earnings Ratio Ten-Year Earnings`[80:144])
LongBond_lm = lm(D_t~MD$`Long Government Bond Yield 10yrpost53`[80:144])
RD_{lm} = lm(D_t[1:63] \sim MD_{RD}  RealD S&P Dividend [80:142])
Consump_lm = lm(D_t[1:60] \sim MD Real Per Capita Consumption (in 2005 dollars) [80:139])
GDPDEfl_lm = lm(D_t[12:65]~MD$`Inflation, GDP deflator (annual %)`[91:144])
Earning_lm = lm(D_t[1:62]~MD$`RealE Earnings`[80:141])
IntRate_lm = lm(D_t[1:62]~MD$`One-Year Interest Rate`[80:141])
SPComp_lm = lm(D_t~MD$`S&P Composite Stock Price Index`[80:144])
DivIn_lm = lm(D_t[1:64]~MD$`Dividends Accuring to Index`[80:143])
Full = lm(D_t[12:60]~ MD$`Price Earnings Ratio One-Year Earnings`[91:139] + MD$`Price Earnings Ratio Te
```

GDP

```
summary(GDP_lm)

##

## Call:
## lm(formula = D_t[11:65] ~ MD$`GDP (current US$)`[90:144])
##
```

```
## Residuals:
                 1Q Median
##
       Min
                                  3Q
## -0.36105 -0.05412 0.01063 0.08729 0.27104
## Coefficients:
                                 Estimate Std. Error t value Pr(>|t|)
##
                                 1.610e-02 2.815e-02
                                                       0.572
## (Intercept)
## MD$`GDP (current US$)`[90:144] 3.225e-15 3.414e-15
                                                                0.349
                                                       0.945
## Residual standard error: 0.1331 on 53 degrees of freedom
## Multiple R-squared: 0.01656, Adjusted R-squared: -0.001994
## F-statistic: 0.8926 on 1 and 53 DF, p-value: 0.3491
```

Price Earning ratio 1 year

```
summary(PE10_lm)
##
## lm(formula = D_t ~ MD$`Price Earnings Ratio Ten-Year Earnings`[80:144])
##
## Residuals:
       \mathtt{Min}
                  1Q
                     Median
                                    ЗQ
## -0.33291 -0.07531 0.00455 0.08894 0.31118
## Coefficients:
##
                                                        Estimate Std. Error
## (Intercept)
                                                        0.086385
                                                                   0.045427
## MD$`Price Earnings Ratio Ten-Year Earnings`[80:144] -0.002131
##
                                                       t value Pr(>|t|)
## (Intercept)
                                                         1.902
                                                                 0.0618 .
## MD$`Price Earnings Ratio Ten-Year Earnings`[80:144] -0.944
                                                                 0.3487
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.135 on 63 degrees of freedom
## Multiple R-squared: 0.01395, Adjusted R-squared: -0.001702
## F-statistic: 0.8913 on 1 and 63 DF, p-value: 0.3487
```

Dividends

```
##
## Call:
## lm(formula = D_t[1:63] ~ MD$`RealD S&P Dividend`[80:142])
##
## Residuals:
## Min 1Q Median 3Q Max
## -0.32904 -0.08228 0.00912 0.08453 0.30993
```

```
##
## Coefficients:
##
                                    Estimate Std. Error t value Pr(>|t|)
                                               0.075375
                                                          1.454
## (Intercept)
                                    0.109629
                                                                    0.151
## MD$`RealD S&P Dividend`[80:142] -0.003545
                                               0.003878 -0.914
                                                                    0.364
## Residual standard error: 0.1352 on 61 degrees of freedom
## Multiple R-squared: 0.01351,
                                    Adjusted R-squared:
## F-statistic: 0.8353 on 1 and 61 DF, p-value: 0.3643
```

Bond Yield 10yr

```
summary(LongBond_lm)
##
## Call:
## lm(formula = D_t ~ MD$`Long Government Bond Yield 10yrpost53`[80:144])
## Residuals:
       Min
                  1Q
                     Median
                                    3Q
## -0.34840 -0.07517 -0.00140 0.08502 0.31887
##
## Coefficients:
##
                                                       Estimate Std. Error
## (Intercept)
                                                       0.058897
                                                                  0.039087
## MD$`Long Government Bond Yield 10yrpost53`[80:144] -0.002131
                                                                   0.006073
                                                      t value Pr(>|t|)
                                                        1.507
## (Intercept)
                                                                 0.137
## MD$`Long Government Bond Yield 10yrpost53`[80:144] -0.351
                                                                  0.727
##
## Residual standard error: 0.1358 on 63 degrees of freedom
## Multiple R-squared: 0.001951,
                                    Adjusted R-squared:
## F-statistic: 0.1232 on 1 and 63 DF, p-value: 0.7268
```

Consumption Per Capita

```
summary(Consump_lm)
##
## lm(formula = D_t[1:60] ~ MD$`Real Per Capita Consumption (in 2005 dollars)`[80:139])
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    3Q
                                             Max
## -0.32509 -0.07974 0.00565 0.08220 0.31277
##
## Coefficients:
##
                                                                 Estimate
## (Intercept)
                                                                7.912e-02
## MD$`Real Per Capita Consumption (in 2005 dollars)`[80:139] -2.182e-06
```

```
##
                                                              Std. Error
                                                               4.895e-02
## (Intercept)
## MD$`Real Per Capita Consumption (in 2005 dollars)`[80:139] 2.574e-06
                                                              t value
## (Intercept)
                                                                1.616
## MD$`Real Per Capita Consumption (in 2005 dollars)`[80:139] -0.848
                                                              Pr(>|t|)
## (Intercept)
                                                                 0.111
## MD$`Real Per Capita Consumption (in 2005 dollars)`[80:139]
                                                                 0.400
## Residual standard error: 0.1382 on 58 degrees of freedom
## Multiple R-squared: 0.01224,
                                   Adjusted R-squared:
## F-statistic: 0.7185 on 1 and 58 DF, p-value: 0.4001
```

GDP Deflator

```
summary(GDPDEfl lm)
##
## Call:
## lm(formula = D_t[12:65] \sim MD$`Inflation, GDP deflator (annual %)`[91:144])
## Residuals:
##
       Min
                 1Q
                     Median
                                   3Q
## -0.35755 -0.05464 0.00194 0.07958 0.27878
##
## Coefficients:
                                                   Estimate Std. Error
##
                                                              0.031664
## (Intercept)
                                                   0.094061
## MD$`Inflation, GDP deflator (annual %)`[91:144] -0.017328
                                                              0.007707
                                                  t value Pr(>|t|)
## (Intercept)
                                                    2.971 0.00449 **
## MD$`Inflation, GDP deflator (annual %)`[91:144] -2.248 0.02882 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1287 on 52 degrees of freedom
## Multiple R-squared: 0.0886, Adjusted R-squared: 0.07107
## F-statistic: 5.055 on 1 and 52 DF, p-value: 0.02882
```

Earnings

```
summary(Earning_lm)

##

## Call:
## lm(formula = D_t[1:62] ~ MD$`RealE Earnings`[80:141])
##

## Residuals:
## Min 1Q Median 3Q Max
```

Intrest Rate

```
summary(IntRate_lm)
##
## Call:
## lm(formula = D_t[1:62] \sim MD$^One-Year Interest Rate^[80:141])
## Residuals:
                 1Q Median
                                           Max
## -0.35011 -0.07165 -0.00804 0.09087 0.31130
##
## Coefficients:
##
                                       Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                                  0.033180
                                                                    0.0373
                                       0.070668
                                                           2.130
## MD$`One-Year Interest Rate`[80:141] -0.005273
                                                 0.005132 -1.027
                                                                     0.3083
##
## (Intercept)
## MD$`One-Year Interest Rate`[80:141]
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1358 on 60 degrees of freedom
## Multiple R-squared: 0.01729, Adjusted R-squared: 0.0009111
## F-statistic: 1.056 on 1 and 60 DF, p-value: 0.3083
```

S&P Price Index

summary(SPComp_lm)

```
##
## Call:
## lm(formula = D_t ~ MD$`S&P Composite Stock Price Index`[80:144])
##
## Residuals:
## Min 1Q Median 3Q Max
## -0.33840 -0.07586 0.00112 0.08750 0.32343
##
## Coefficients:
```

```
##
                                                 Estimate Std. Error t value
                                                4.920e-02 2.237e-02
## (Intercept)
                                                                      2.199
## MD$`S&P Composite Stock Price Index`[80:144] -6.003e-06 3.290e-05 -0.182
                                               Pr(>|t|)
## (Intercept)
                                                 0.0315 *
## MD$`S&P Composite Stock Price Index`[80:144]
                                                 0.8558
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1359 on 63 degrees of freedom
## Multiple R-squared: 0.0005281, Adjusted R-squared:
## F-statistic: 0.03329 on 1 and 63 DF, p-value: 0.8558
```

Dividend Acruing to Index

```
summary(DivIn_lm)
##
## lm(formula = D_t[1:64] \sim MD$`Dividends Accurring to Index`[80:143])
##
## Residuals:
       Min
                  1Q
                      Median
## -0.34886 -0.06976 0.00064 0.08397 0.33042
## Coefficients:
                                             Estimate Std. Error t value
                                                                  1.615
## (Intercept)
                                            0.0415254 0.0257113
## MD$`Dividends Accuring to Index`[80:143] 0.0003474 0.0019657
                                            Pr(>|t|)
##
## (Intercept)
                                               0.111
## MD$`Dividends Accuring to Index`[80:143]
                                               0.860
## Residual standard error: 0.1364 on 62 degrees of freedom
## Multiple R-squared: 0.0005034, Adjusted R-squared:
## F-statistic: 0.03123 on 1 and 62 DF, p-value: 0.8603
```

Full Model with all parameters

```
summary(Full)
##
## Call:
## lm(formula = D_t[12:60] ~ MD$`Price Earnings Ratio One-Year Earnings`[91:139] +
##
       MD$`Price Earnings Ratio Ten-Year Earnings`[91:139] + MD$CPI[91:139] +
       MD$`S&P Composite Stock Price Index`[91:139] + MD$`GDP (current US$)`[91:139] +
##
##
      MD$`Long Government Bond Yield 10yrpost53`[91:139] + MD$`RealD S&P Dividend`[91:139] +
##
      MD$`Real Per Capita Consumption (in 2005 dollars)`[91:139] +
##
      MD$ Inflation, GDP deflator (annual %) [91:139] + MD$ RealE Earnings [91:139] +
##
      MD$`One-Year Interest Rate`[91:139] + MD$`S&P Composite Stock Price Index`[91:139] +
```

```
MD$`Dividends Accuring to Index`[91:139])
##
## Residuals:
##
                          Median
         Min
                                         30
                                                  Max
  -0.142627 -0.073871 -0.003367 0.060026 0.215707
##
## Coefficients:
##
                                                                 Estimate
## (Intercept)
                                                                1.456e-01
## MD$`Price Earnings Ratio One-Year Earnings`[91:139]
                                                               -2.917e-03
## MD$`Price Earnings Ratio Ten-Year Earnings`[91:139]
                                                               -9.548e-03
## MD$CPI[91:139]
                                                                8.849e-03
## MD$`S&P Composite Stock Price Index`[91:139]
                                                                2.126e-04
## MD$`GDP (current US$)`[91:139]
                                                               -7.612e-15
## MD$`Long Government Bond Yield 10yrpost53`[91:139]
                                                                3.208e-02
## MD$`RealD S&P Dividend`[91:139]
                                                                2.641e-02
## MD$`Real Per Capita Consumption (in 2005 dollars)`[91:139] -6.492e-05
## MD$`Inflation, GDP deflator (annual %)`[91:139]
                                                               -1.857e-02
## MD$`RealE Earnings`[91:139]
                                                                6.805e-03
## MD$ One-Year Interest Rate [91:139]
                                                               -2.379e-02
## MD$`Dividends Accuring to Index`[91:139]
                                                               -3.970e-02
                                                               Std. Error
## (Intercept)
                                                                3.974e-01
## MD$`Price Earnings Ratio One-Year Earnings`[91:139]
                                                                4.032e-03
## MD$`Price Earnings Ratio Ten-Year Earnings`[91:139]
                                                                1.420e-02
## MD$CPI[91:139]
                                                                5.465e-03
## MD$`S&P Composite Stock Price Index`[91:139]
                                                                4.637e-04
## MD$`GDP (current US$)`[91:139]
                                                                9.279e-14
## MD$`Long Government Bond Yield 10yrpost53`[91:139]
                                                                2.594e-02
## MD$`RealD S&P Dividend`[91:139]
                                                                2.868e-02
## MD$`Real Per Capita Consumption (in 2005 dollars)`[91:139] 2.529e-05
## MD$`Inflation, GDP deflator (annual %)`[91:139]
                                                                1.443e-02
## MD$`RealE Earnings`[91:139]
                                                                1.866e-03
## MD$`One-Year Interest Rate`[91:139]
                                                                1.426e-02
## MD$`Dividends Accuring to Index`[91:139]
                                                                3.985e-02
                                                               t value
## (Intercept)
                                                                 0.366
## MD$`Price Earnings Ratio One-Year Earnings`[91:139]
                                                                -0.723
## MD$`Price Earnings Ratio Ten-Year Earnings`[91:139]
                                                                -0.673
## MD$CPI[91:139]
                                                                 1.619
## MD$`S&P Composite Stock Price Index`[91:139]
                                                                 0.459
## MD$`GDP (current US$)`[91:139]
                                                                -0.082
## MD$`Long Government Bond Yield 10yrpost53`[91:139]
                                                                 1.237
## MD$`RealD S&P Dividend`[91:139]
                                                                 0.921
## MD$`Real Per Capita Consumption (in 2005 dollars)`[91:139]
                                                                -2.567
## MD$`Inflation, GDP deflator (annual %)`[91:139]
                                                                -1.287
## MD$`RealE Earnings`[91:139]
                                                                 3.647
## MD$`One-Year Interest Rate`[91:139]
                                                                -1.669
## MD$`Dividends Accuring to Index`[91:139]
                                                                -0.996
                                                               Pr(>|t|)
## (Intercept)
                                                               0.716263
## MD$`Price Earnings Ratio One-Year Earnings`[91:139]
                                                               0.474109
## MD$`Price Earnings Ratio Ten-Year Earnings`[91:139]
                                                               0.505483
## MD$CPI[91:139]
                                                               0.114131
```

```
## MD$`S&P Composite Stock Price Index`[91:139]
                                                              0.649281
## MD$`GDP (current US$)`[91:139]
                                                              0.935072
## MD$`Long Government Bond Yield 10yrpost53`[91:139]
                                                              0.224273
## MD$`RealD S&P Dividend`[91:139]
                                                              0.363186
## MD$`Real Per Capita Consumption (in 2005 dollars)`[91:139] 0.014552 *
## MD$`Inflation, GDP deflator (annual %)`[91:139]
                                                              0.206367
## MD$`RealE Earnings`[91:139]
                                                              0.000833 ***
## MD$`One-Year Interest Rate`[91:139]
                                                              0.103828
## MD$`Dividends Accuring to Index`[91:139]
                                                              0.325802
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1014 on 36 degrees of freedom
## Multiple R-squared: 0.5852, Adjusted R-squared: 0.447
## F-statistic: 4.233 on 12 and 36 DF, p-value: 0.0003705
```

Plots of PE ratios over years

```
plot(MD$Year, MD$`Price Earnings Ratio Ten-Year Earnings`)
```



