

北京航空航天大学

2015—2016 学年 期中考试

Modern Control Engineering

Examination Paper

班 级 _____ 学 号 _____

姓 名 _____ 成 绩 _____

2015 年 11 月 15 日

Class_____ Student number_____ Name_____ Score_____

Examination Questions

1. (15 points) A system consists of the following equations:

$$\dot{x}_1 = r - c$$

$$\dot{x}_2 = \tau \dot{x}_1 + K_1 x_1,$$

$$\dot{x}_3 = K_2 x_2,$$

$$\dot{x}_4 = x_3 - x_5 - K_5 c,$$

$$\dot{x}_5 = K_3 x_4,$$

$$K_4 x_5 = T \dot{c} + c,$$

where τ , K_1 , K_2 , K_3 , K_4 , K_5 and T are positive constants, $r(t)$ is the input signal and $c(t)$ is the output signal. Draw its block diagram and obtain the transfer function $C(s)/R(s)$.

2. (15 points) A block diagram of a system is shown in Figure 2. Obtain the transfer function $C(s)/R(s)$.

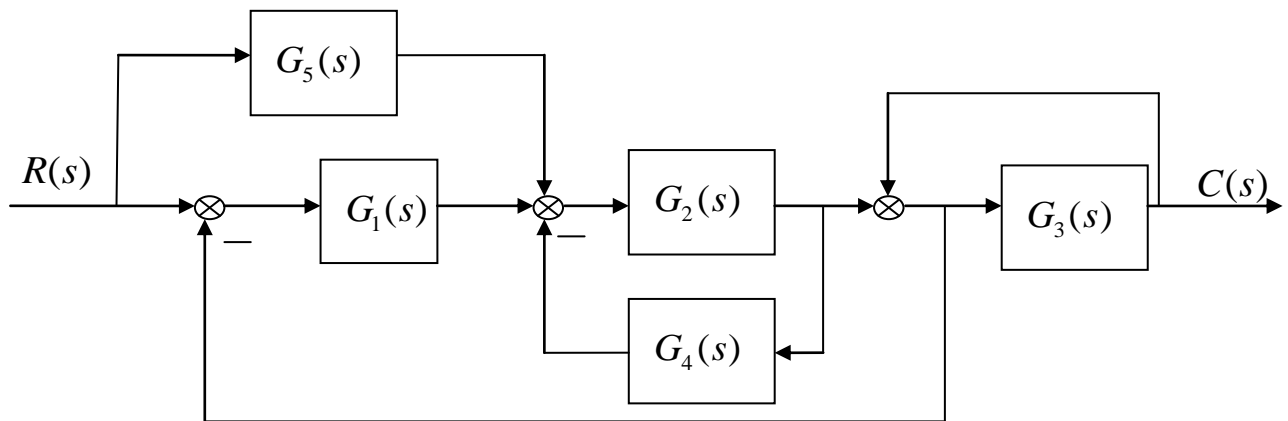


Figure 2

3. (20 points) The block diagram of a system is given by Figure 3. Determine the positive parameter τ such that the damping ratio is $1/\sqrt{2}$. Then, obtain the unit-step response $c(t)$, t_p , M_p and t_s (5%), respectively.

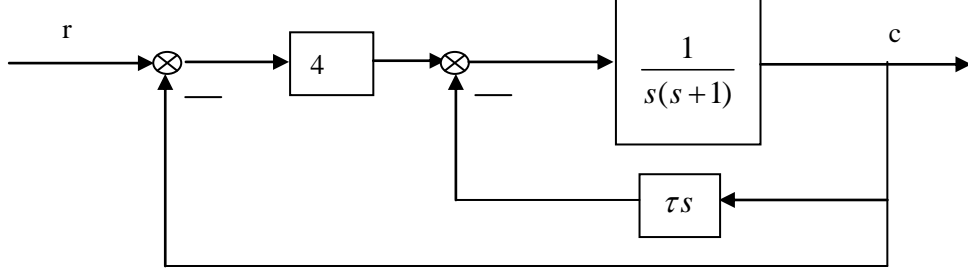


Figure 3

4. (15 points) The block diagram of a system is shown in Figure 4. Determine the system stability. If the system is stable, determine the steady-state errors e_{ssr} and e_{ssn} .

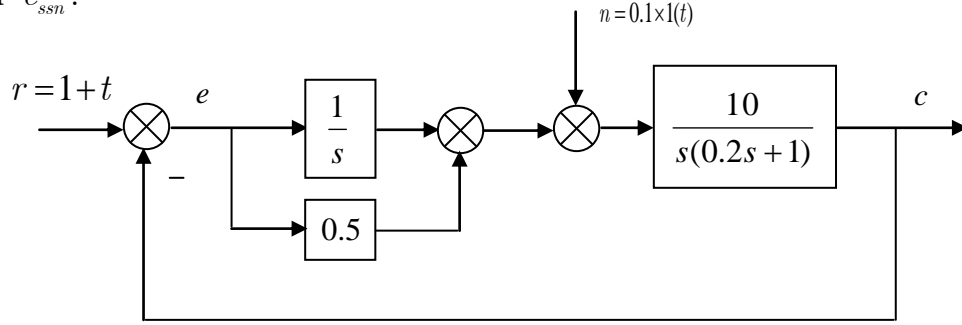


Figure4

5. (15 points) The open loop transfer function of a unity feedback system is

$$G(s) = \frac{3s+2}{s^2(Ts+1)}$$

Sketch, according to the rules, the root loci when T varies from 0 to $+\infty$. Further, determine the range of T for which the system is stable.

6. (20 points) The open loop transfer function of a unity feedback system is

$$G(s) = \frac{K}{s(s+6)(s+8)}$$

Sketch, according to the rules, the root loci when K varies from 0 to $+\infty$. Determine the value of K such that the two closed loop dominant poles have damping ratio $1/\sqrt{2}$. What are the locations of the three closed loop poles for such a damping ratio?