

انهارده هنقل كلام علي الباك بروب وهنخش في الديب ليرننج .. لما بنتكلم علي الديب ليرننج هنتكلم علي حاجتين CNNs and RNNs واللي محتاجين نعرفو هو ازاي ال 2 دول بيعملولهم تمرين .. فعلياً هو الباك بروب يعني .. المهم الدكتور مسميهم هم الاتنين decision functions ... المهم HW4 هخلص انهارده ان شاء الله .. ربنا يعين ويوفق ... الدكتور مش بيطلع الامتحانات برا .. فينزلو paper versions بس ... في سؤال الدكتور اتسألو ...

Q&A

Q: Do I need to know Matrix Calculus to derive the backprop algorithms used in this class?

A: No. We've carefully constructed our assignments so that you do **not** need to know Matrix Calculus.

That said, it's kind of handy.

الدكتور بيقلك ان ده يعني بيحي في الإيدن كسكيلل يعني . بس اشطأ ..

Let $y, x \in \mathbb{R}$ be scalars, $\mathbf{y} \in \mathbb{R}^M$ and $\mathbf{x} \in \mathbb{R}^P$ be vectors, and $\mathbf{Y} \in \mathbb{R}^{M \times N}$ and $\mathbf{X} \in \mathbb{R}^{P \times Q}$ be matrices

| Matrix Calculus | | Numerator | | |
|----------------------|-------------|--|---|---|
| Types of Derivatives | Denominator | scalar | vector | matrix |
| | scalar | $\frac{\partial y}{\partial x}$ | $\frac{\partial \mathbf{y}}{\partial x}$ | $\frac{\partial \mathbf{Y}}{\partial x}$ |
| | vector | $\frac{\partial y}{\partial \mathbf{x}}$ | $\frac{\partial \mathbf{y}}{\partial \mathbf{x}}$ | $\frac{\partial \mathbf{Y}}{\partial \mathbf{x}}$ |
| | matrix | $\frac{\partial y}{\partial \mathbf{X}}$ | $\frac{\partial \mathbf{y}}{\partial \mathbf{X}}$ | $\frac{\partial \mathbf{Y}}{\partial \mathbf{X}}$ |

Matrix Calculus

| Types of Derivatives | scalar |
|----------------------|--|
| scalar | $\frac{\partial y}{\partial x} = \left[\frac{\partial y}{\partial x} \right]$ 1×1 matrix |
| vector | $\frac{\partial y}{\partial \mathbf{x}} = \begin{bmatrix} \frac{\partial y}{\partial x_1} \\ \frac{\partial y}{\partial x_2} \\ \vdots \\ \frac{\partial y}{\partial x_P} \end{bmatrix}$ List of deriv |
| matrix | $\frac{\partial y}{\partial \mathbf{X}} = \begin{bmatrix} \frac{\partial y}{\partial X_{11}} & \frac{\partial y}{\partial X_{12}} & \dots & \frac{\partial y}{\partial X_{1Q}} \\ \frac{\partial y}{\partial X_{21}} & \frac{\partial y}{\partial X_{22}} & \dots & \frac{\partial y}{\partial X_{2Q}} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial y}{\partial X_{P1}} & \frac{\partial y}{\partial X_{P2}} & \dots & \frac{\partial y}{\partial X_{PQ}} \end{bmatrix}$ |

Matrix Calculus

| Types of Derivatives | scalar | vector |
|----------------------|--|--|
| scalar | $\frac{\partial y}{\partial x} = \left[\frac{\partial y}{\partial x} \right]$ | $\frac{\partial \mathbf{y}}{\partial x} = \begin{bmatrix} \frac{\partial y_1}{\partial x} & \frac{\partial y_2}{\partial x} & \dots & \frac{\partial y_N}{\partial x} \end{bmatrix}$ <i>with respect to scalar</i> |
| vector | $\frac{\partial y}{\partial \mathbf{x}} = \begin{bmatrix} \frac{\partial y}{\partial x_1} \\ \frac{\partial y}{\partial x_2} \\ \vdots \\ \frac{\partial y}{\partial x_P} \end{bmatrix}$ | $\frac{\partial \mathbf{y}}{\partial \mathbf{x}} = \begin{bmatrix} \frac{\partial y_1}{\partial x_1} & \frac{\partial y_1}{\partial x_2} & \dots & \frac{\partial y_1}{\partial x_P} \\ \frac{\partial y_2}{\partial x_1} & \frac{\partial y_2}{\partial x_2} & \dots & \frac{\partial y_2}{\partial x_P} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial y_N}{\partial x_1} & \frac{\partial y_N}{\partial x_2} & \dots & \frac{\partial y_N}{\partial x_P} \end{bmatrix}$ <i>N entries</i> <i>P entries</i> |

Matrix Calculus

Common Vector Derivatives

Let $\frac{\partial f(\vec{x})}{\partial \vec{x}} = \nabla_{\vec{x}} f(\vec{x})$ be the vector derivative of f , $B \in \mathbb{R}^{m \times n}$, $\vec{x} \in \mathbb{R}^n$

Scalar Derivative

$$f(x) \rightarrow \frac{\partial f}{\partial x}$$

$$bx \rightarrow b$$

$$xb \rightarrow b$$

$$x^2 \rightarrow 2x$$

$$bx^2 \rightarrow 2bx$$

Vector Derivative

$$f(\mathbf{x}) \rightarrow \frac{\partial f}{\partial \mathbf{x}}$$

~~$$x^T b \rightarrow b$$~~

$$x^T b \rightarrow b$$

$$x^T x \rightarrow 2x$$

$$x^T B x \rightarrow 2Bx$$

\leftarrow symmetric

vector x

Vector Chain Rule

$\vec{x} \in \mathbb{R}^P$ $y \in \mathbb{R}$ $\vec{u} \in \mathbb{R}^N$

$$\frac{\partial y}{\partial \vec{x}} = \left(\left(\frac{\partial y}{\partial \vec{u}} \right)^T \left(\frac{\partial \vec{u}}{\partial \vec{x}} \right)^T \right)^T$$

$P \times 1$ $\begin{bmatrix} N \times 1 & P \times N \\ 1 \times N & N \times P \end{bmatrix}$ $P \times 1$

$$\begin{bmatrix} \frac{\partial y}{\partial \vec{x}} \end{bmatrix}_{P \times 1} \quad \begin{bmatrix} \frac{\partial y}{\partial \vec{u}} \end{bmatrix}_{N \times 1} \quad \begin{bmatrix} \frac{\partial \vec{u}}{\partial \vec{x}} \end{bmatrix}_{P \times N}$$

طيب هنا احنا بنبص علي الصورة بتاعت الباك بروب ألجورزم في الجينيرال فيرجن .. عندك كمان الفورود بروب .. بتقول ان عندك فانكشن f .. اللي انت عاوز تحسبها فانت عاوز تكتب الجورزم يحسبها .. الأالجورزم هيعرف directed acyclic graph .. ده اللي هو ال computational graph .. ال forward computational هيقك visit each node in topological order اللي هو معناها visit all the children of a node before visiting the node itself .. فلغارييل اسمو u_i .. عندو انبوتس اسمها $v_1 \dots v_N$.. هتجيب ال u_i كإنها intermediate function و تخزن النواتج في النود اللي عندك . عشان هتحتاجها في الباك بروب ... في الباك بروب انت بت initialize dy/dy ل 1 .. و بعدين تبدأ ت visit each node in reverse topological order

الدكتور رسم الصورة وقال ان كل ال u_i فانكشن في كل ال V_s ... انت هنا في الباك بروب دايماً هت visit the parent before the children

Training

Backpropagation

Automatic Differentiation – Reverse Mode (aka. Backpropagation)

Forward Computation

1. Write an **algorithm** for evaluating the function $y = f(x)$. The algorithm defines a **directed acyclic graph**, where each variable is a node (i.e. the “**computation graph**”)
2. Visit each node in **topological order**.
For variable u_i with inputs v_1, \dots, v_N
 - a. Compute $u_i = g_i(v_1, \dots, v_N)$
 - b. Store the result at the node

Backward Computation (Version A)

1. **Initialize** $dy/dy = 1$.
2. Visit each node v_j in **reverse topological order**.
Let u_1, \dots, u_M denote all the nodes with v_j as an input
Assuming that $y = h(u) = h(u_1, \dots, u_M)$
and $u = g(v)$ or equivalently $u_i = g_i(v_1, \dots, v_j, \dots, v_N)$ for all i
 - a. We already know dy/du_i for all i
 - b. Compute dy/dv_j as below (Choice of algorithm ensures computing (du_i/dv_j) is easy)



$$\frac{dy}{dv_j} = \sum_{i=1}^M \frac{dy}{du_i} \frac{du_i}{dv_j}$$

Return partial derivatives dy/du_i for all variables

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في فيرجن مختلف في الباك بروب .. التعديل بس هيقا في انك هتعامل ال intermediate derivatives كإنهم intermediate variables موجودين عندك من البدايه ... احنا هن initialize them to 0 .. بس الطريقة اللي هنحسب بيها هتبقا مختلفه ... ال computational graph لسه متغيرش ... لما هتخش علي ال u_i انت عارف كل ال children بتوعو اللي هو كل ال V_s اللي عندك ..

Training

Backpropagation

Automatic Differentiation – Reverse Mode (aka. Backpropagation)

Forward Computation

1. Write an **algorithm** for evaluating the function $y = f(\mathbf{x})$. The algorithm defines a **directed acyclic graph**, where each variable is a node (i.e. the “**computation graph**”)
2. Visit each node in **topological order**.
For variable u_i with inputs v_1, \dots, v_N
 - a. Compute $u_i = g_i(v_1, \dots, v_N)$
 - b. Store the result at the node

Backward Computation (Version B)

1. **Initialize** all partial derivatives dy/du_i to \bar{q} and $dy/dy = 1$.
2. Visit each node in **reverse topological order**.
For variable $u_i = g_i(v_1, \dots, v_N)$
 - a. We already know dy/du_i
 - b. Increment dy/dv_j by $(dy/du_i)(du_i/dv_j)$
(Choice of algorithm ensures computing (du_i/dv_j) is easy)



Return partial derivatives dy/du_i for all variables

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Training

Backpropagation

Why is the backpropagation algorithm efficient?

1. Reuses **computation from the forward pass** in the backward pass
2. Reuses **partial derivatives** throughout the backward pass (*but only if the algorithm reuses shared computation in the forward pass*)

(Key idea: partial derivatives in the backward pass should be thought of as variables stored for reuse)

Example: 1-Hidden Layer Neural Network

Algorithm 1 Stochastic Gradient Descent (SGD)

```

1: procedure SGD(Training data  $\mathcal{D}$ , test data  $\mathcal{D}_t$ )
2:   Initialize parameters  $\alpha, \beta$  randomly, zero
3:   for  $e \in \{1, 2, \dots, E\}$  do ← epochs
4:     for  $(x, y) \in \mathcal{D}$  do
5:       Compute neural network layers:
6:        $\mathbf{o} = \text{object}(x, \mathbf{a}, \mathbf{b}, \mathbf{z}, \hat{y}, J) = \text{NNFORWARD}(x, y, \alpha, \beta)$ 
7:       Compute gradients via backprop:
8:        $\left. \begin{array}{l} \mathbf{g}_\alpha = \nabla_\alpha J \\ \mathbf{g}_\beta = \nabla_\beta J \end{array} \right\} = \text{NNBACKWARD}(x, y, \alpha, \beta, \mathbf{o})$ 
9:       Update parameters:
10:       $\alpha \leftarrow \alpha - \gamma \mathbf{g}_\alpha$ 
11:       $\beta \leftarrow \beta - \gamma \mathbf{g}_\beta$ 
12:      Evaluate training mean cross-entropy  $J_{\mathcal{D}}(\alpha, \beta)$ 
13:      Evaluate test val mean cross-entropy  $J_{\mathcal{D}_t}(\alpha, \beta)$ 
14:   return parameters  $\alpha, \beta$ 

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المهم الدكتور حط مثال كذا وقال ان احنا فعلا ممكن نستخدم ال finite difference method عشان نتشيك الحل بتاعنا في الباكروب .. انا بحب الدكتور ده جداً يلا نخش في الديب ليرنينج

اول حاجه هنتكلم علي ال CNN بس الأول هنسال ليه الاهتمام ده ... عشان فيه فلوس كتيره الناس بتستثمر فيها .. بقيت المحاضره جري كثير .. لو مهتم اقراها تاني