

COMS3008A Assignment – Report

Claudio Da Mata - 2128358

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1 Problem 1: Parallel Scan

- Given a set of elements, $[a_0, a_1, \dots, a_{n-1}]$, the scan operation associated with addition operator for this input is the output set $[a_0, (a_0 + a_1), \dots, (a_0 + a_1 + \dots + a_{n-1})]$.
- For example, the input set is [2, 1, 4, 0, 3, 7, 6, 3], then the scan with addition operator of this input is [2, 3, 7, 7, 10, 17, 23, 26].

1.1 Serial Implementation:

Firstly I started off with the baseline implementation of serial scan operation given in Listing 1

```
void scan(int out[], int in[], int N){
  out[0] = in[0];

for(int i=1; i<N; i++) {
  out[i] = in[i] + out[i-1];
}
}
</pre>
```

Listing 1: Sequential algorithm for computing scan operation with '+' operator 1.

This got me a baseline average time to measure and compare parallel implementations. I ran the operation on arrays ranging in sizes from 1000 to 50,000 with intervals of 1000 given in Figure 1

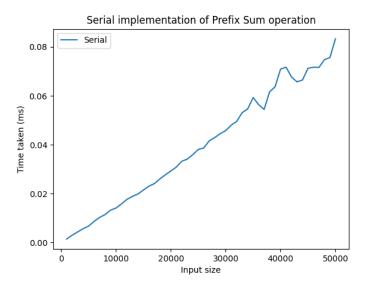


Figure 1: Serial scan operation average times

1.2 OpenMP Parallel Implementation:

Next I implented the scan operation within OpenMP's interface. The algorithm I used is based off the Blelloch² work-effecient algorithm given in Listing 2

```
void scan(int out[], int in[], int N){
 int nthr, *z, *x = out;
 #pragma omp parallel num_threads(4)
   int i;
   #pragma omp single
      nthr = omp_get_num_threads();
      z = malloc(sizeof(int)*nthr+1);
      z[0] = 0;
   }
   int tid = omp_get_thread_num();
   int sum = 0;
   #pragma omp for schedule(static)
   for(i=0; i<N; i++) {
      sum += in[i];
      x[i] = sum;
   z[tid+1] = sum;
   #pragma omp barrier
```

```
int offset = 0;
for(i=0; i<(tid+1); i++) {
    offset += z[i];
}

# pragma omp for schedule(static)
for(i=0; i<N; i++) {
    x[i] += offset;
}

free(z);
}</pre>
```

Listing 2: OpenMP Parallel algorithm for computing scan operation³.

The algorithm works as follows:

- Start omp parallel
- Initiate a 'single' construct which allows only one thread to run the code
- Inside single should declare the size of the temp array and set *element* [0] = 0
- After the single construct, get current threadID and initialize sum = 0
- Begin an omp for contruct with schedule(static)
- Inside the for loop (from 0 to N-1), sum+= the input array at i, and set the output array at i equal to the new sum
- After the for loop, set temp array at [threadID + 1] equal to sum
- · Declare a Barrier construct which forces all threads to wait until other threads finish computation
- Set offset = 0
- Begin a regular for loop that sums all elements of the temp array to *offset*, only adding elements that each specific thread has computed itself
- Begin an omp for construct with schedule(static) again, from i = 0 to N 1
- sum output array element i with offset
- Finish off pragma omp and then free the temp array from memory

I experimented with different number of threads running and managed to narrow it down to thread counts of 2,4,6 given in Figure 2

With 2 threads running there is no noticeable speedup compared to serial implementation. With 4 and 6 threads running there is significant speedup compared to serial implementation. While input size n increases, 4 threads performs slightly better than 6 threads. Thus I choose 4 threads as my optimal implementation of OpenMP parallelization.

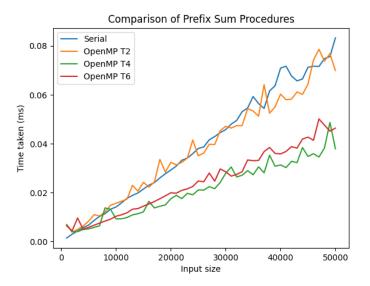


Figure 2: OpenMP Parallel scan operation average times for different thread counts

1.3 MPI Parallel Implementation:

Next I implented the scan operation within MPI's interface. The algorithm I used is based off the Blelloch² prescan algorithm given in Listing 3

```
MPI_Init(&argc, &argv); //Initialize MPI

MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);
MPI_Comm_size(MPI_COMM_WORLD, &comm_size);

MPI_Barrier(MPI_COMM_WORLD);

size_t num_per_proc = n / comm_size;
int sum;

start_find_sum(my_rank, comm_size, data, num_per_proc, &sum);
start_find_psum(my_rank, comm_size, data, num_per_proc, sum);

MPI_Barrier(MPI_COMM_WORLD);

MPI_Barrier(MPI_COMM_WORLD);

MPI_Finalize(); //Close MPI
Listing 3: MPI Parallel algorithm for computing scan operation4.
```

The essence of the algorith comes from the start_find_sum() and start_find_psum() functions.

The algorithm works as follows:

- · Start MPI
- · Get comm rank and size
- · Barrier that forces all threads to wait
- Set num per proc equal to array size *n*/*commsize*. This dictates how many numbers each thread will compute the sums of
- Call start find sum() function
 - The algoritem works like a binary tree with levels
 - Gets MPI_Status
 - Sums input array elements from 0 to numPerProc
 - Begin for loop from level = 0 to $log_2(commsize)$
 - Inside the loop set $position = rank/level^2$
 - If position is even, receives the sendersSum (with senderRank = $rank + level^2$) and adds to total sum
 - If position is odd, sends total sum to receiver with senderRank = $rank level^2$, then kills current thread
 - Before for loop ends, calls Barrier so all threads wait
- Call start_find_psum() function
 - The algorithm works like a binary tree with levels
 - Gets MPI_Status
 - If rank == 0, sets psum = sum
 - Begin for loop from $level = log_2(commsize) 1$ down to 0
 - If process is on current level:
 - Set $position = rank/level^2$
 - If position is even this means this process was the parent of sendingRank, and so first sets senderRank = $rank + level^2$, then sends psum, then receives the senderSum and finally subtracts psum by senderSum
 - If position is odd, sets $receivingRank = rank level^2$, then receives psum from parent, and then sends sum with receivingRank
 - Before for loop ends, calls Barrier so all threads wait
 - After the loop ends, put the *prefixSums* associated with this process in the input array
- Calls Barrier so all threads wait
- Ends MPI

With start_find_sum() and start_find_psum() functions given respectively by Listing 4 and Listing 5

```
void start_find_sum(int rank, int mysize, int* in,
                size_t num_per_proc, int* overall_sum){
        MPI_Status status;
        int sum = find_sum(in, num_per_proc);
        int still_alive = 1;
        int level;
        for (level = 0; level < (int)log2(mysize); level++) {</pre>
          if (still_alive) {
11
            int position = rank / (int)pow(2, level);
            if (position % 2 == 0) {
              // I am a receiver
              int sender_sum;
              int sending_rank = rank + (int)pow(2, level);
              MPI_Recv(&sender_sum, 1, MPI_INT, sending_rank,
19
              0, MPI_COMM_WORLD, &status);
              sum += sender_sum;
            }else {
              // I am a sender
              int receiving_rank = rank - (int)pow(2, level);
              MPI_Send(&sum, 1, MPI_INT, receiving_rank, 0,
27
              MPI_COMM_WORLD);
              still_alive = 0;
            }
          }
31
          MPI_Barrier(MPI_COMM_WORLD);
        }
33
        *overall_sum = sum;
34
                                Listing 4: start_find_sum()
      void start_find_psum(int rank, int mysize, int* in,
                size_t num_per_proc, int sum){
        int psum;
        int level;
        MPI_Status status;
        if (rank == 0) {
          psum = sum;
       for (level = (int)log2(mysize) - 1; level >= 0; level--) {
          // only trigger the processes on the current level
```

```
if (level == 0 || rank % (int)pow(2, level) == 0) {
            int position = rank / (int)pow(2, level);
            if (position % 2 == 0) {
              int sender_sum;
              int sending_rank = rank + (int)pow(2, level);
              MPI_Send(&psum, 1, MPI_INT,
19
              sending_rank, // RIGHT CHILD
              O, MPI_COMM_WORLD);
              MPI_Recv(&sender_sum, 1, MPI_INT,
              sending_rank, 0, MPI_COMM_WORLD, &status);
              // psum <- (prefix sum of parent) - (sum of sibling)
              psum -= sender_sum;
            }else{
              int receiving_rank = rank - (int)pow(2, level);
              MPI_Recv(&psum, 1, MPI_INT,
31
              receiving_rank, // PARENT
              0, MPI_COMM_WORLD, &status);
              // send sum to receiving_rank so it can fix its sum
              MPI_Send(&sum, 1, MPI_INT,
              receiving_rank, 0, MPI_COMM_WORLD);
          }
          MPI_Barrier(MPI_COMM_WORLD);
        }
        // put the prefix sums associated with this node in input array
        int next_sum = in[num_per_proc-1];
        in[num_per_proc-1] = psum;
       for (int j = num_per_proc - 2; j >= 0; j--) {
          int next_sum_tmp = in[j];
          in[j] = in[j+1] - next_sum;
          next_sum = next_sum_tmp;
        }
      }
53
```

Listing 5: start_find_psum()

I experimented with different number of threads running and managed to narrow it down to thread counts of 2,4,8 given in Figure 3

With 2 threads running there is noticeably worse running time compared to serial implementation. With 4 and 8 threads running there is significant speedup compared to serial implementation. With smaller input sizes n, 4 threads performs

better than 8 threads, but as n increases, perfermance between 4 threads and 8 threads stays relatively the same. Thus I choose 4 threads as my optimal implementation of MPI parallelization.

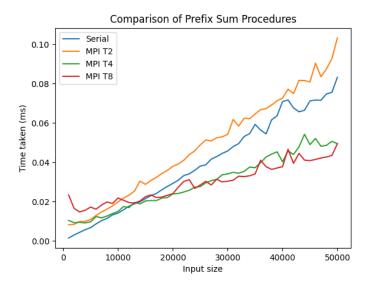


Figure 3: MPI Parallel scan operation average times for different thread counts

1.4 Validation:

Checking if elements are correctly summed, through running run.sh given in Figure 4

```
Validate passed.
-----OpenMP scan is starting-----
Validate passed.
-----OpenMP scan is starting-----
Validate passed.
------MPI scan is starting-----
Validate passed.
------MPI scan is done------
Validate passed.
-------MPI scan is done------
```

Figure 4: Validation of scan operations

1.5 Conclusions:

After comparing the results from serial, optimal OpenMP (with 4 threads) and optimal MPI (with 4 threads), I can make the conclusion that serial performs the best at very small array size n. While at large n, both OpenMP and MPI have significant speedup from serial, OpenMP performs consistently better than MPI. Comparisons given in Figure 5

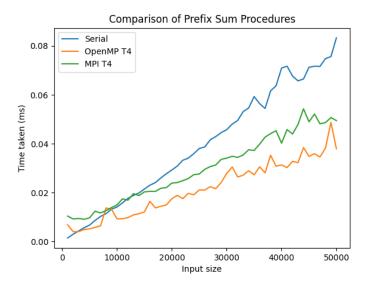


Figure 5: Comparison of all scan operations

2 Problem 2: Parallel Bitonic Sort

The bitonic sort is based on the idea of sorting network. The bitonic sorting algorithm is suitable for parallel processing, especially for GPU sorting. However, in this problem, you are requested to implement parallel bitonic sorting of integers using OpenMP and MPI, respectively.

Another paragraph starts ...

3 Problem 3: Parallel Graph Algorithm

An example figure is given in Figure 6.

An example of table is given Table 1.

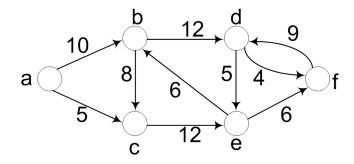


Figure 6: A directed graph

No of vertices	64	128	256	384	512
Serial Parallel	0.1	0.2	0.3	0.4	0.5
Sppedup	2	3	4	5	6

References

- [1] Prefix Sum Array implementation and applications in competitive programming, https://www.geeksforgeeks.org/prefix-sum-array-implementation-applications-competitive-programming/, accessed: 23-10-2022.
- [2] Prefix Sum algorithm 2: Work-efficient, https://en.wikipedia.org/wiki/Prefix_sum, accessed: 23-10-2022.
- [3] CSE 231 Introduction to Parallel and Concurrent Programming at Washington University scan, https://classes.engineering.wustl.edu/cse231/core/index.php/Scan, accessed: 23-10-2022.
- [4] MPI Parallel Prefix Sum (1A), https://upload.wikimedia.org/wikiversity/en/2/2f/ParaPrefix.MPI. 1.A.20140730.pdf, accessed: 23-10-2022.