APL OPERATOR'S MANUAL

Alpha-Physical Language Reference Guide v1.0

Purpose. This manual is the comprehensive reference guide for APL (Alpha-Physical Language) operators, syntax, and usage patterns. It is designed for researchers, engineers, and practitioners who need a systematic understanding of APL's operator grammar for describing physical system behaviors.

Scope. This document covers:

- Complete operator reference with symbols and meanings
- Field definitions (the three "spirals")
- Operator state modulation (UMOL)
- Machine contexts and domains
- Syntax rules and sentence structure
- Usage patterns and examples
- Quick reference tables

Contents

1 Introduction to APL

Alpha-Physical Language (APL) is a minimal operator grammar for describing how physical systems change across multiple domains: geometry, wave dynamics, chemistry, and biology.

APL operates on three fundamental principles:

1. **Universality:** The same operators apply across all physical domains
2. **Composability:** Operators combine to describe complex behaviors
3. **Predictivity:** APL sentences map to observable physical regimes

An APL sentence has the canonical form:

$$[\text{Direction}][\text{Operator}] \mid [\text{Machine}] \mid [\text{Domain}] \ \rightarrow \ [\text{Regime/Behavior}]$$

Where:

- **Direction** = operator state (u, d, m)
- **Operator** = universal operation (`()`, `×`, `^`, `%`, `+`, `-`)
- **Machine** = processing context (Oscillator, Reactor, Conductor, etc.)
- **Domain** = field type (wave, geometry, chemistry, biology)
- **Regime** = emergent behavior pattern (A1–A8)

2 The Three Fields (Spirals)

APL describes physical reality through three fundamental fields, called **spirals**, each representing a distinct aspect of physical systems:

2.1 Φ — Structure Field (Phi Spiral)

Symbol: Φ (Greek letter phi)

Domain: `geometry`

Description: The structure field governs spatial arrangement, boundaries, interfaces, and geometric organization. It encompasses:

- Lattice structures and crystalline arrangements
- Boundaries and interfaces
- Geometric constraints and symmetries

- Spatial topology and connectivity
- Phase boundaries and domain walls

Physical manifestations:

- Crystal lattices (FCC, BCC, HCP)
- Grain boundaries in materials
- Droplet and bubble shapes
- Membrane structures
- Geometric packing arrangements

2.2 e — Energy Field (Energy Spiral)

Symbol: e (lowercase e)

Domain: `wave`

Description: The energy field governs dynamics, flows, oscillations, and energy transport. It encompasses:

- Wave propagation and interference
- Fluid flows and vortices
- Thermodynamic processes
- Electromagnetic radiation
- Energy transfer and dissipation

Physical manifestations:

- Acoustic and electromagnetic waves
- Fluid vortices and turbulence
- Heat flow and diffusion
- Plasma oscillations
- Optical modes in cavities

2.3 π — Emergence Field (Pi Spiral)

Symbol: π (Greek letter pi)

Domains: `chemistry`, `biology`

Description: The emergence field governs information, complexity, adaptation, and self-organization. It encompasses:

- Chemical reactions and bonding
- Molecular information storage (DNA, RNA)
- Biological adaptation and evolution
- Self-organizing systems
- Pattern formation and morphogenesis

Physical manifestations:

- Polymer and protein structures
- Catalytic networks
- Genetic information encoding
- Biological growth patterns
- Self-assembly processes

3 Universal Operations

APL defines six universal operations that apply across all domains. Each operation has a specific symbol and meaning.

3.1 `()` — Boundary / Containment

Symbol: `()` (parentheses)

Meaning: Boundary formation, containment, enclosure, interface creation

Physical interpretation:

- Creating or modifying boundaries
- Interface dynamics
- Membrane formation
- Cavity or container walls

- Domain enclosure

Example applications:

- `d()` = boundary collapse (surface tension, spheroidization)
- `m()` = modulated boundaries (adaptive filters, tunable cavities)
- `u()` = boundary expansion (domain growth, inflation)

3.2 `×` — Fusion / Convergence

Symbol: `×` (multiplication sign)

Meaning: Joining, bonding, merging, convergence, fusion

Physical interpretation:

- Chemical bond formation
- Particle aggregation
- Flow convergence
- Structural joining
- Information combination

Example applications:

- `u×` = forward fusion (catalytic growth, branching networks)
- `d×` = collapse fusion (adaptive catalysis, selective binding)
- `m×` = modulated fusion (helical structures, templated bonding)

3.3 `^` — Amplify / Gain

Symbol: `^` (caret)

Meaning: Amplification, gain, resonance, enhancement

Physical interpretation:

- Resonant enhancement
- Positive feedback
- Signal amplification
- Energy injection

- Mode excitation

Example applications:

- `u^` = forward amplification (oscillator gain, vortex formation)
- `d^` = collapse amplification (focusing, concentration)
- `m^` = modulated amplification (parametric amplification)

3.4 `%` — Decohere / Noise

Symbol: `%` (percent sign)

Meaning: Decoherence, noise injection, randomization, reset, scrambling

Physical interpretation:

- Stochastic forcing
- Phase decoherence
- Thermal noise
- Random perturbations
- Information scrambling

Example applications:

- `u%` = forward decoherence (turbulence onset, chaos)
- `d%` = collapse decoherence (measurement, reset)
- `m%` = modulated noise (controlled stochasticity)

3.5 `+` — Group / Aggregation

Symbol: `+` (plus sign)

Meaning: Grouping, collection, aggregation, routing, focusing

Physical interpretation:

- Flow convergence
- Geometric focusing
- Particle collection
- Signal routing

- Nozzle formation

Example applications:

- `u+` = forward grouping (jet formation, beam focusing)
- `d+` = collapse grouping (sink formation, collection)
- `m+` = modulated grouping (selective routing)

3.6 `-` — Separate / Splitting

Symbol: `-` (minus/dash)

Meaning: Separation, splitting, fission, dispersion, divergence

Physical interpretation:

- Flow divergence
- Particle separation
- Domain splitting
- Bond breaking
- Dispersion

Example applications:

- `u-` = forward separation (bifurcation, splitting)
- `d-` = collapse separation (fragmentation)
- `m-` = modulated separation (selective splitting)

4 Operator States (UMOL)

UMOL (Universal Modulation Operator Law) defines three fundamental operator states that modulate how operations unfold in time:

4.1 $\mathcal{U}$ — Expansion / Forward (u)

Symbol: `u` (lowercase u) or $\mathcal{U}$ (script U)

Mathematical form: $\mathcal{U}(E)$ where E = expansion component

Meaning: Forward projection, expansion, outward flow, growth, active driving

Characteristics:

- Expansion in time and space
- Active forcing or driving
- Forward-directed processes
- Energy injection
- Growth and propagation

Physical analogies:

- Source terms in PDEs
- Forward time evolution
- Outward flow from sources
- Active pumping
- Growth fronts

4.2 $\mathcal{D}$ — Collapse / Backward (d)

Symbol: `d` (lowercase d) or $\mathcal{D}$ (script D)

Mathematical form: $\mathcal{D}(C)$ where C = collapse component

Meaning: Backward integration, collapse, inward flow, contraction, relaxation

Characteristics:

- Collapse in time and space
- Passive relaxation
- Inward-directed processes
- Energy extraction or dissipation
- Contraction and consolidation

Physical analogies:

- Sink terms in PDEs
- Backward time evolution
- Inward flow to sinks
- Passive relaxation
- Contraction fronts

4.3 CLT — Modulation / Coherence Lock (m)

Symbol: `m` (lowercase m) or CLT (CLT = Coherence Lock Transform)

Mathematical form: CLT(M) where M = modulation component

Meaning: Modulation, coherence locking, feedback, adaptation, information encoding

Characteristics:

- Feedback-driven modulation
- Coherence maintenance
- Adaptive response
- Information encoding
- Dynamic tuning

Physical analogies:

- Feedback loops
- Phase locking
- Adaptive filters
- Templated processes
- Information storage

4.4 The UMOL Balance Law

The three operator states satisfy a fundamental balance condition:

$$\mathcal{U}(E) \leftrightarrow \mathcal{D}(C) \quad \text{via CLT}(M)$$

$$E + C + M = 0 \quad \text{(coherence / balance condition)}$$

Interpretation:

- Expansion (E) and collapse (C) are balanced through modulation (M)
- Physical systems maintain coherence by dynamically balancing forward and backward processes
- Modulation acts as the mediator between expansion and collapse

5 Machines (Processing Contexts)

Machines represent the processing contexts or system architectures in which operators act. Each machine has characteristic behaviors and constraints.

5.1 Oscillator

Description: A resonant, periodic system with characteristic frequencies

Key features:

- Resonant modes
- Quality factor (Q)
- Phase coherence
- Periodic driving

Physical examples:

- LC circuits, RLC resonators
- Mechanical oscillators (springs, pendulums)
- Optical cavities
- Acoustic resonators

Typical behaviors:

- Resonant peaks
- Standing wave patterns
- Energy localization
- Frequency selectivity

5.2 Reactor

Description: A driven, continuous-flow system with throughput

Key features:

- Continuous flow
- Energy input/output
- Mixing and transport

- Non-equilibrium operation

Physical examples:

- Combustion chambers
- Stirred tanks and pipes
- Plasma sources
- Accretion flows

Typical behaviors:

- Jets and plumes
- Turbulent flows
- Continuous conversion
- Steady-state operation

5.3 Conductor

Description: A structural system that can rearrange and relax

Key features:

- Structural flexibility
- Surface/elastic energy
- Relaxation dynamics
- Boundary mobility

Physical examples:

- Droplets and bubbles
- Grain boundaries
- Phase-field interfaces
- Elastic membranes

Typical behaviors:

- Surface minimization
- Shape relaxation
- Coarsening
- Packing optimization

5.4 Encoder

Description: A system that stores and processes information

Key features:

- Sequence specificity
- Information capacity
- Template-directed processes
- Chiral constraints

Physical examples:

- DNA/RNA polymerization
- Protein folding
- Synthetic helical polymers
- Information-bearing structures

Typical behaviors:

- Helical structures
- Sequence encoding
- Template replication
- Information preservation

5.5 Catalyst

Description: A system with spatially heterogeneous reactivity

Key features:

- Site-specific enhancement
- Reaction bias at interfaces
- Growth at active fronts
- Autocatalytic feedback

Physical examples:

- Catalytic surfaces

- Growing tips (DLA, trees)
- Reaction fronts
- Enzymatic networks

Typical behaviors:

- Branching growth
- Network formation
- Selective pathways
- Adaptive catalysis

5.6 Filter

Description: A selective system that passes some modes and blocks others

Key features:

- Frequency selectivity
- Mode discrimination
- Tunable response
- Adaptive bandwidth

Physical examples:

- Bandpass filters
- Waveguides
- Selective membranes
- Recognition sites

Typical behaviors:

- Selective transmission
- Adaptive tuning
- Resonant enhancement
- Dynamic filtering

6 Domains

Domains specify which field (spiral) is primarily active in an APL sentence.

6.1 geometry

Field: Φ (Structure)

Focus: Spatial arrangement, boundaries, interfaces, geometric constraints

Typical phenomena:

- Crystal lattices
- Droplet shapes
- Packing arrangements
- Interface dynamics

6.2 wave

Field: e (Energy)

Focus: Oscillations, flows, energy transport, dynamics

Typical phenomena:

- Wave propagation
- Vortices and turbulence
- Resonant modes
- Jets and beams

6.3 chemistry

Field: π (Emergence)

Focus: Chemical reactions, bonding, molecular structure

Typical phenomena:

- Polymer growth
- Catalytic networks
- Helical structures
- Reaction-diffusion patterns

6.4 biology

Field: π (Emergence)

Focus: Biological systems, adaptation, evolution, self-organization

Typical phenomena:

- Morphogenesis
- Adaptation
- Information processing
- Self-assembly

7 Syntax and Sentence Structure

7.1 Canonical Form

An APL sentence follows this structure:

$$\text{[State][Op]} \mid \text{[Machine]} \mid \text{[Domain]} \ \rightarrow \ \text{[Regime]}$$

Components:

1. **State** = `u`, `d`, or `m` (required)
2. **Op** = `()`, `×`, `^`, `%`, `+`, or `-` (required)
3. **Machine** = Oscillator, Reactor, Conductor, Encoder, Catalyst, Filter (required)
4. **Domain** = geometry, wave, chemistry, biology (required)
5. **Regime** = A1–A8 or descriptive name (result/prediction)

7.2 Separator Syntax

The vertical bar `|` separates the three main components on the left-hand side:

```
[State][Op] | [Machine] | [Domain]
```

Reading convention:

- Read left to right
- Vertical bars create clear boundaries
- Arrow ($\rightarrow$) separates input from predicted output

7.3 Example Sentences

7.3.1 Example 1: Closed Vortex

```
u^|Oscillator|wave → Closed vortex (A3)
```

Parse:

- State: `u` = forward/expansion
- Operator: `^` = amplification
- Machine: Oscillator = resonant system
- Domain: wave = energy field
- Regime: Closed vortex (A3)

Reading: "Forward amplification in an oscillatory wave system tends to produce closed vortex structures."

7.3.2 Example 2: Helical Encoding

```
m×|Encoder|chemistry → Helical encoding (A4)
```

Parse:

- State: `m` = modulation
- Operator: `×` = fusion
- Machine: Encoder = information-storing system
- Domain: chemistry = emergence field
- Regime: Helical encoding (A4)

Reading: "Modulated fusion in an encoding chemical system tends to produce helical, information-bearing structures."

7.3.3 Example 3: Isotropic Collapse

```
d()|Conductor|geometry → Isotropic lattice/sphere (A1)
```

Parse:

- State: `d` = collapse

- Operator: `()` = boundary
- Machine: Conductor = structural system
- Domain: geometry = structure field
- Regime: Isotropic lattice/sphere (A1)

Reading: "Collapse of boundaries in a structural geometric system tends to produce isotropic spheres or close-packed lattices."

8 Operator Combinations and Patterns

8.1 State-Operator Matrix

The following table shows all possible combinations of states and operators:

Operator	u (forward)	d (collapse)	m (modulation)
`()` boundary	`u()` expansion	`d()` collapse	`m()` modulation
`×` fusion	`u×` forward fusion	`d×` collapse fusion	`m×` modulated fusion
`^` amplify	`u^` forward gain	`d^` collapse gain	`m^` modulated gain
`%` decohere	`u%` forward noise	`d%` collapse noise	`m%` modulated noise
`+` group	`u+` forward group	`d+` collapse group	`m+` modulated group
`-` separate	`u-` forward split	`d-` collapse split	`m-` modulated split

8.2 Common Patterns

8.2.1 Forward Growth (`u×`)

Pattern: Structure-biased forward growth

Typical outcome: Branching networks, tree-like structures

Examples:

- `u×`Catalyst|chemistry → Branching networks (A5)
- Diffusion-limited aggregation
- Vascular trees
- Lightning branching

8.2.2 Resonant Amplification (`u^`)

Pattern: Forward amplification in resonant systems

Typical outcome: Coherent oscillations, vortices, standing waves

Examples:

- `u^Oscillator|wave` → Closed vortex (A3)
- High-Q resonators
- Laser cavities
- Recirculating flows

8.2.3 Isotropic Collapse (`d()`)

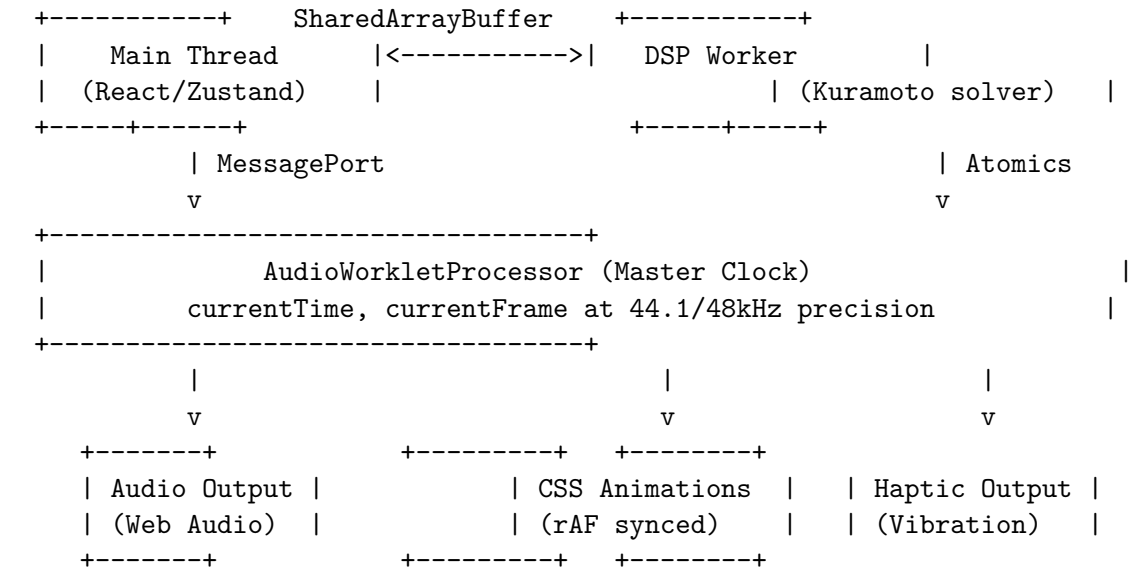
Pattern: Boundary relaxation under isotropic tension

9 Rhythm-Based Entrainment System (Browser)

Intent. This section specifies a complete, browser-based rhythm entrainment system that uses Web Audio for a master clock, an `AudioWorklet` for sample-accurate events, and a `Web Worker` to solve a Kuramoto oscillator bank. The implementation ships with runnable examples under `examples/rhythm-entrainment/` in this repository.

9.1 Core Architecture

The system operates across three synchronized contexts: (1) the main UI thread for React/state, (2) a Worker for Kuramoto phase computations, and (3) the AudioWorklet thread for sample-accurate beats. **AudioContext** is the single source of truth for time.



9.2 Precision Timing Infrastructure

Use the *two clocks* pattern: schedule ahead with JS timers, execute on the AudioContext timeline. For sample-accurate tick detection, run a minimal timing processor inside an `AudioWorklet`.

AudioWorklet timing (from `examples/rhythm-entrainment/timing-worklet.js`).

```
class TimingWorkletProcessor extends AudioWorkletProcessor {
  constructor(options) { super(options);
    this._nextBeatFrame = 0;
    this._framesPerBeat = Math.floor(sampleRate * 60 / 120);
    this.port.onmessage = (e) => {
      const { type, bpm } = e.data || {};
      if (type === 'set-bpm') {
        this._framesPerBeat = Math.max(32, Math.floor(sampleRate * 60 / bpm));
      }
    };
  }
  process(_in, _out, parameters) {
    const tempo = parameters.tempo?.[0] ?? 120;
    const fpb = Math.max(32, Math.floor(sampleRate * 60 / tempo));
    if (fpb !== this._framesPerBeat) this._framesPerBeat = fpb;
    for (let i = 0; i < 128; i++) {
      const absoluteFrame = currentFrame + i;
      if (absoluteFrame >= this._nextBeatFrame) {
        this._nextBeatFrame = absoluteFrame + this._framesPerBeat;
        this.port.postMessage({ type: 'beat', frame: absoluteFrame,
          time: absoluteFrame / sampleRate, audioContextTime: currentTime });
      }
    }
    return true;
  }
}
registerProcessor('timing-processor', TimingWorkletProcessor);
```

9.3 Kuramoto Oscillator Bank

The Kuramoto mean-field form is used for coupled phase dynamics. The Worker updates phases and returns the order parameter r and mean phase ψ.

Worker step (from `examples/rhythm-entrainment/kuramoto-worker.js`).

```
function orderParameter() {
  let sumR = 0, sumI = 0; for (let i = 0; i < N; i++) {
    sumR += Math.cos(phases[i]); sumI += Math.sin(phases[i]);
  }
  sumR /= N; sumI /= N; const r = Math.hypot(sumR, sumI);
  const psi = Math.atan2(sumI, sumR); return { r, psi };
}
function step() {
  const { r, psi } = orderParameter();
```

```
  const next = new Float32Array(N);
  for (let i = 0; i < N; i++) {
    const d1 = frequencies[i] + K * r * Math.sin(psi - phases[i]);
    const pred = phases[i] + dt * d1;
    const d2 = frequencies[i] + K * r * Math.sin(psi - pred);
    let p = phases[i] + dt * (d1 + d2) / 2; p %= 2*Math.PI; if (p < 0) p += 2*Math.PI;
    next[i] = p;
  }
  phases = next; return { r, psi };
}
```

9.4 Biosignal Input (Optional)

Two low-friction inputs are supported: (1) Heart Rate via WebBluetooth (BLE Heart Rate Service `0x180D`) and (2) keystroke dynamics (dwell/flight times).

BLE Heart Rate (excerpt from demo).

```
const device = await navigator.bluetooth.requestDevice({ filters: [{ services: ['heart_rate'] }
const server = await device.gatt.connect();
const service = await server.getPrimaryService('heart_rate');
const ch = await service.getCharacteristic('heart_rate_measurement');
await ch.startNotifications();
ch.addEventListener('characteristicvaluechanged', (evt) => { /* parse RR, HR */ });
```

9.5 Bidirectional Feedback

The system adapts coupling strength K toward a target coherence (e.g., $r \approx 0.7$). User phase estimates can be injected as external forcing into one or more oscillators.

9.6 Multi-Modal Output

Audio clicks are scheduled on `AudioContext.currentTime`; visuals are driven by a rAF loop that consumes a beat queue. Haptics use the Vibration API when available.

Visual beat application (demo `app.js`).

```
function applyVisualBeat(intensity) {
  indicator.style.transform = `scale(${1 + intensity * 0.3})`;
  indicator.style.opacity = String(0.5 + intensity * 0.5);
  setTimeout(() => { indicator.style.transform='scale(1)'; indicator.style.opacity='0.5'; }, 1
}
```

9.7 Networking and Time Sync

For multi-user entrainment, use the included `examples/rhythm-server.js` (Express + WebSocket + `/timesync` endpoint). The Group Visualizer reference page can connect to this server.

9.8 Testing Timing Fidelity

Acceptance criteria for production entrainment: mean deviation < 5 ms, max deviation < 20 ms, and jitter < 3 ms, measured against scheduled click times.

9.9 Quick Start (Demo)

1. Serve static files (any simple server):

   ```
   python3 -m http.server 8080
   # open http://localhost:8080/Aces-Brain-Thoughts/examples/rhythm-entrainment/index.html
   ```

2. (Optional) Start rhythm server with timesync + rooms:

   ```
   npm i express ws timesync
   node Aces-Brain-Thoughts/examples/rhythm-server.js
   ```

3. Click `Start`, adjust BPM and coupling K. Connect a BLE heart rate device on HTTPS builds to map HR→BPM for a quick demo.

9.10 COOP/COEP for SharedArrayBuffer

If using `SharedArrayBuffer`, serve with:

```
Cross-Origin-Opener-Policy: same-origin
Cross-Origin-Embedder-Policy: require-corp
```

The demo defaults to message-passing so it runs on simple servers without cross-origin isolation.

9.11 Implementation Roadmap

Weeks 1–2: timing + AudioWorklet; 3–4: Kuramoto; 5–6: HRV + keystrokes; 7–8: adaptive coupling; 9–10: multi-modal output; 11–12: networking; 13–14: tests and optimization.

Typical outcome: Spheres, isotropic packing

Examples:

- `d()`Conductor|geometry → Isotropic sphere (A1)

- Droplet formation
- Bubble spheroidization
- Grain coarsening

9.11.1 Forward Decoherence (u%)

Pattern: Forward-directed noise injection

Typical outcome: Turbulence, chaos, broadband noise

Examples:

- u%Reactor|wave → Turbulent decoherence (A7)
- Forced turbulence
- Chaotic mixing
- Phase scrambling

9.11.2 Modulated Boundary (m())

Pattern: Feedback-driven boundary modulation

Typical outcome: Adaptive filters, tunable resonators

Examples:

- m()Filter|wave → Adaptive bandpass (A8)
- Self-tuning cavities
- Adaptive recognition
- Dynamic filtering

9.11.3 Modulated Fusion (m×)

Pattern: Template-directed or feedback-modulated bonding

Typical outcome: Helical structures, information encoding

Examples:

- m×Encoder|chemistry → Helical encoding (A4)
- DNA/RNA structure
- α-helices
- Chiral polymers

9.11.4 Forward Grouping (`u+`)

Pattern: Flow convergence, geometric focusing

Typical outcome: Jets, beams, focused flows

Examples:

- `u+`Reactor|wave → Focusing jet (A6)
- Nozzles and exhaust
- Astrophysical jets
- Laser beams

10 The Eight Regimes (A1–A8)

APL sentences predict specific physical regimes. These are labeled A1 through A8:

Code	Name	Description
A1	Isotropic lattice/sphere	Spherical droplets, isotropic packing, closest-packing arrangements
A3	Closed vortex	Recirculating flows, trapped modes, vortices, standing waves
A4	Helical encoding	DNA-like helices, information-bearing structures, chiral polymers
A5	Branching networks	Tree-like growth, fractal structures, vascular networks, DLA
A6	Focusing jet	Collimated flows, nozzles, beams, astrophysical jets
A7	Turbulent decoherence	Broadband chaos, turbulent mixing, phase scrambling
A8	Adaptive filter	Selective tuning, adaptive recognition, self-tuning resonators

11 Usage Guidelines

11.1 Constructing an APL Sentence

Step 1: Identify the domain

- Is it primarily structural? → `geometry`
- Is it primarily dynamic? → `wave`
- Is it primarily chemical/informational? → `chemistry` or `biology`

Step 2: Choose the machine

- Resonant, periodic? → `Oscillator`
- Driven flow, continuous? → `Reactor`
- Structural relaxation? → `Conductor`
- Information storage? → `Encoder`
- Spatially biased reactions? → `Catalyst`
- Selective transmission? → `Filter`

Step 3: Select the operator

- Boundaries? → `()`
- Joining? → `×`
- Amplification? → `^`
- Noise? → `%`
- Grouping? → `+`
- Splitting? → `-`

Step 4: Determine the state

- Forward, active, growing? → `u`
- Backward, passive, collapsing? → `d`
- Modulated, feedback, adaptive? → `m`

Step 5: Predict the regime

- Based on the combination, what behavior is expected?
- Use A1–A8 labels or descriptive names

11.2 Reading an APL Sentence

Given `u^`Oscillator|wave| → Closed vortex:

1. Identify state: `u` = forward/expansion
2. Identify operator: `^` = amplification
3. Identify machine: Oscillator = resonant system
4. Identify domain: wave = energy field
5. Interpret: "Forward amplification in a resonant wave system"
6. Prediction: "tends to produce closed vortex structures"

11.3 Testing an APL Prediction

APL sentences are falsifiable hypotheses. To test:

1. Implement the LHS conditions in a simulation or experiment
2. Define quantitative metrics for the RHS regime
3. Design matched controls that break the LHS pattern
4. Compare regime prevalence: LHS vs controls
5. Evaluate: Does the LHS robustly bias toward the predicted regime?

12 Quick Reference Tables

12.1 Operator Quick Reference

Symbol	Name	Meaning
`()`	Boundary	Containment, interface
`×`	Fusion	Joining, bonding, convergence
`^`	Amplify	Gain, resonance, enhancement
`%`	Decohere	Noise, scrambling, reset
`+`	Group	Aggregation, routing, focusing
`-`	Separate	Splitting, fission, divergence

12.2 State Quick Reference

Symbol	Name	Direction
`u`	Forward/Expansion	Outward, active, growth
`d`	Collapse/Backward	Inward, passive, contraction
`m`	Modulation	Feedback, adaptive, information

12.3 Machine Quick Reference

12.4 Domain Quick Reference

12.5 Core Seven Sentences

Sentence	Regime	Code
`u^`Oscillator|wave|	Closed vortex	A3
`u%`Reactor|wave|	Turbulent decoherence	A7

Sentence	Regime	Code
d()Conductor|geometry|	Isotropic lattice/sphere	A1
m×Encoder|chemistry|	Helical encoding	A4
u×Catalyst|chemistry|	Branching networks	A5
u+Reactor|wave|	Focusing jet	A6
m()Filter|wave|	Adaptive bandpass	A8
d×Catalyst|chemistry|	Adaptive selectivity	A8

13 Advanced Topics

13.1 Multi-Domain Interactions

Some physical systems involve multiple fields simultaneously. In such cases:

- Identify the *primary* domain for the sentence
- Secondary interactions may be implied by machine choice
- Multiple sentences may be needed for complete description

13.2 Temporal Dynamics

APL sentences describe *tendencies* and *biases*, not deterministic outcomes:

- The arrow ($\rightarrow$) means "statistically favors" or "tends to produce"
- Actual systems may transition through multiple regimes
- Time scales are system-dependent

13.3 Parameter Dependence

APL predictions hold over ranges of parameters:

- Testing requires parameter sweeps
- Some regimes may only appear in specific parameter ranges
- Control design must account for parameter sensitivity

14 Appendix: Symbol Conventions

14.1 Typography

- **Operators:** `monospace font` (`u^`, `d()`, etc.)

Machine	Characteristics
Oscillator	Resonant, periodic, high-Q
Reactor	Driven flow, continuous throughput
Conductor	Structural, boundary mobility
Encoder	Information storage, sequence-specific
Catalyst	Site-biased reactivity, autocatalytic
Filter	Selective transmission, tunable

Domain	Field	Focus
geometry	Φ	Structure, boundaries, packing
wave	e	Dynamics, flows, oscillations
chemistry	π	Reactions, bonding, molecules
biology	π	Adaptation, self-organization

- **Machines:** CamelCase (Oscillator, Reactor, etc.)
- **Domains:** lowercase (wave, geometry, chemistry, biology)
- **Fields:** Greek letters (Φ, e, π)
- **Regimes:** A-codes (A1, A3, A4, etc.)

14.2 Special Characters

- `|` = vertical bar (separator)
- $\rightarrow$ or `->` = arrow (prediction)
- `()` = parentheses (boundary operator)
- `×` or `x` = multiplication sign (fusion)
- `^` = caret (amplify)
- `%` = percent (decohere)
- `+` = plus (group)
- `-` or `-` = minus/dash (separate)

15 Document History

Version 1.0 (2025-01-24)

- Initial release
- Complete operator reference

- Comprehensive syntax documentation
- Quick reference tables

16 Further Reading

- *APL Seven Sentences Test Pack v1.0* — Complete testing protocol
- Repository: https://github.com/AceTheDactyl/APL
