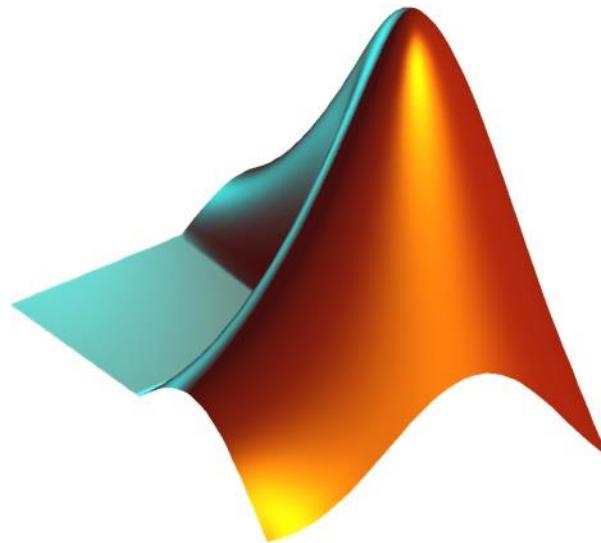


# MATLAB / Simulink Lab Course

## Simulink Fundamentals



UPDATED TO  
**R2019A**

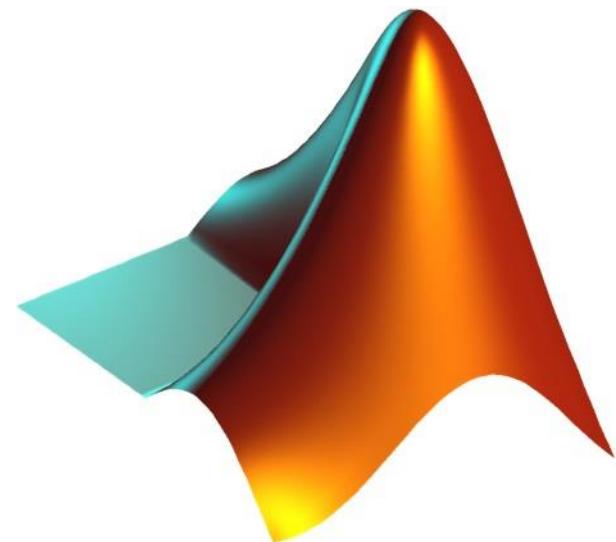
# Objectives & Preparation “Simulink Fundamentals”

- Which MathWorks products are covered?
  - ⇒ Simulink
- What skills are learnt?
  - ⇒ Basic Introduction to Simulink
  - ⇒ Modelling Simple Systems with Simulink
    - (i.e. translate a set of (ordinary differential) equations into a simulation model)
  - ⇒ Derive the Governing Equations from a Given Model
  - ⇒ Basic Visualization of Simulation Results
- How to prepare for the session?

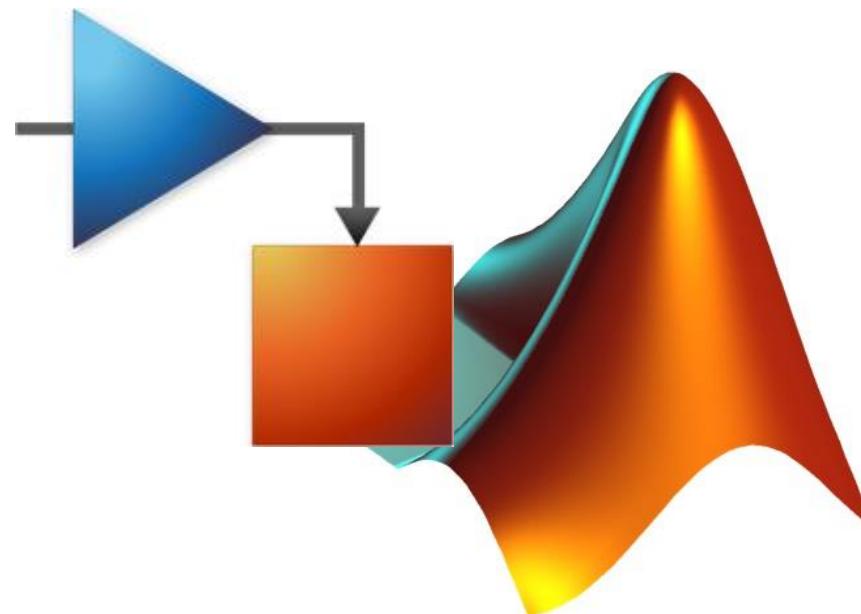
Videos	Tutorials
<b>Getting Started With Simulink</b> <a href="https://de.mathworks.com/videos/getting-started-with-simulink-69027.html">https://de.mathworks.com/videos/getting-started-with-simulink-69027.html</a> 	<b>Create a simple model</b> <a href="https://de.mathworks.com/help/simulink/gs/create-a-simple-model.html">https://de.mathworks.com/help/simulink/gs/create-a-simple-model.html</a> 
<b>Visualizing Simulation Results</b> <a href="https://de.mathworks.com/videos/visualizing-simulation-results-102160.html">https://de.mathworks.com/videos/visualizing-simulation-results-102160.html</a> 	<b>Model a Dynamic System</b> <a href="https://de.mathworks.com/help/simulink/gs/define-system.html">https://de.mathworks.com/help/simulink/gs/define-system.html</a> 

# Outline

1. Introduction
2. A Simple Example System
3. Start-up Simulink
4. The Simulink Editor
5. The Block Library
6. Modelling in Simulink
  1. The Working Principle of Simulink
  2. Blocks
  3. Signals
  4. Subsystems
  5. Parameters
  6. Model Configuration Parameters
7. Simulation
8. List of Useful Blocks & Descriptions

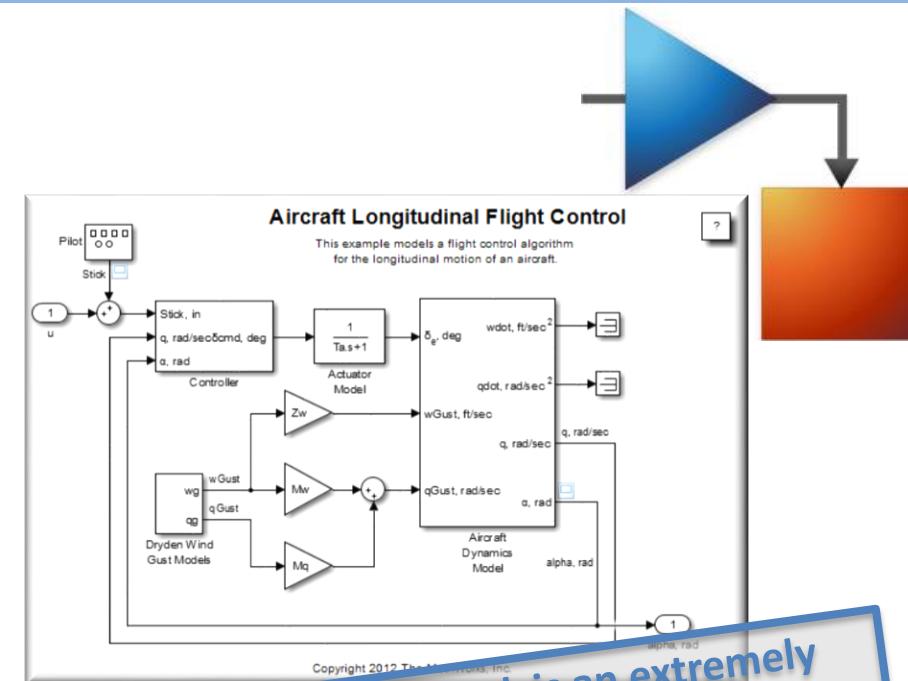


# 1. Introduction



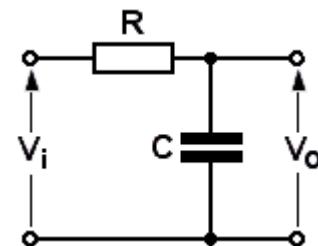
# Introduction

- Simulink 1 available in 1990
- Shipped with MATLAB starting from 1992
- Multi-domain **dynamic systems** can be
  - modelled
  - simulated
  - analyzed
- Interface: graphical **block diagramming**
- Uses compiled code + \*.mex (Matlab DLL)
- Tightly integrated with MATLAB
- Add-ons expand capabilities
  - Stateflow
  - Embedded Coder
  - Simulink Real-Time
  - Simulink Verification and Validation
  - ...
- **Automatic C-Code Generation**
- Most widely used in automatic control / digital signal processing



Simulink is an extremely powerful and large program!  
Here only the necessary things for basic modelling tasks are introduced!

## 2. A Simple Example System

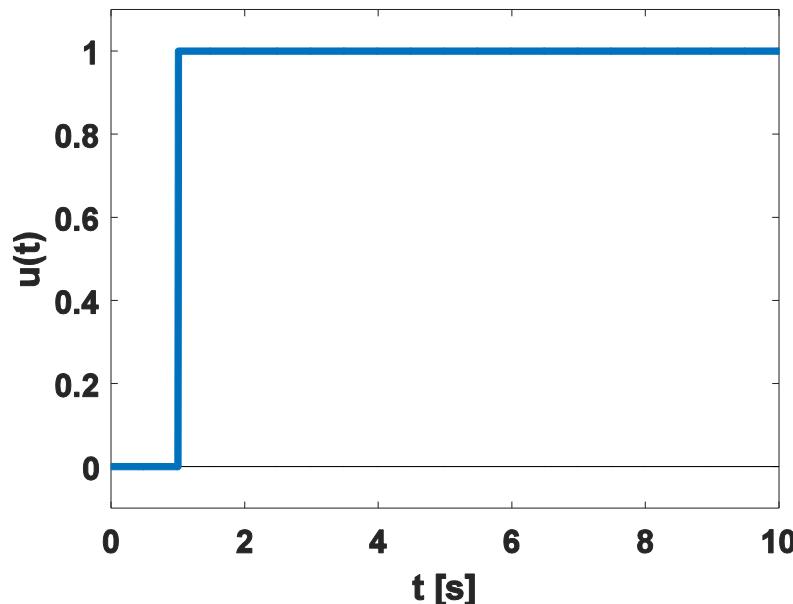


## A Simple Example System

Consider the reaction of the following first order dynamic system to a unit step input

$$\dot{x}(t) = -\frac{1}{T}x(t) + \frac{K}{T}u(t)$$
$$y(t) = Cx(t)$$

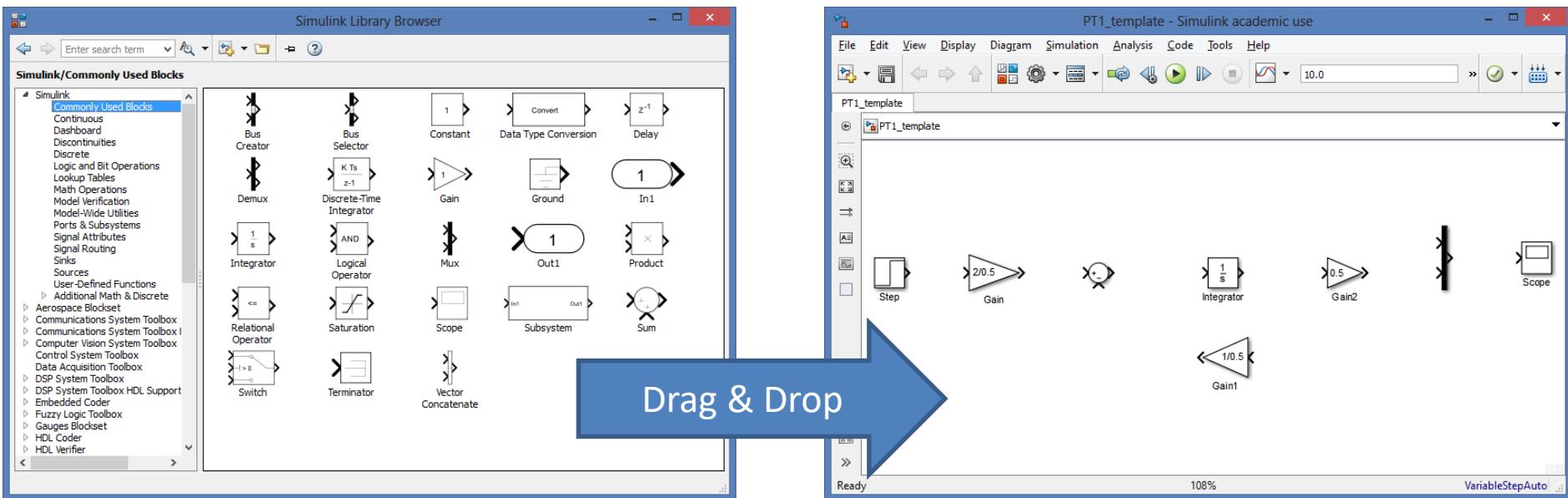
with  $T = 0.5$ ,  $K = 2$ ,  $C = 0.5$



# A Simple Example System

## Simulink Solution

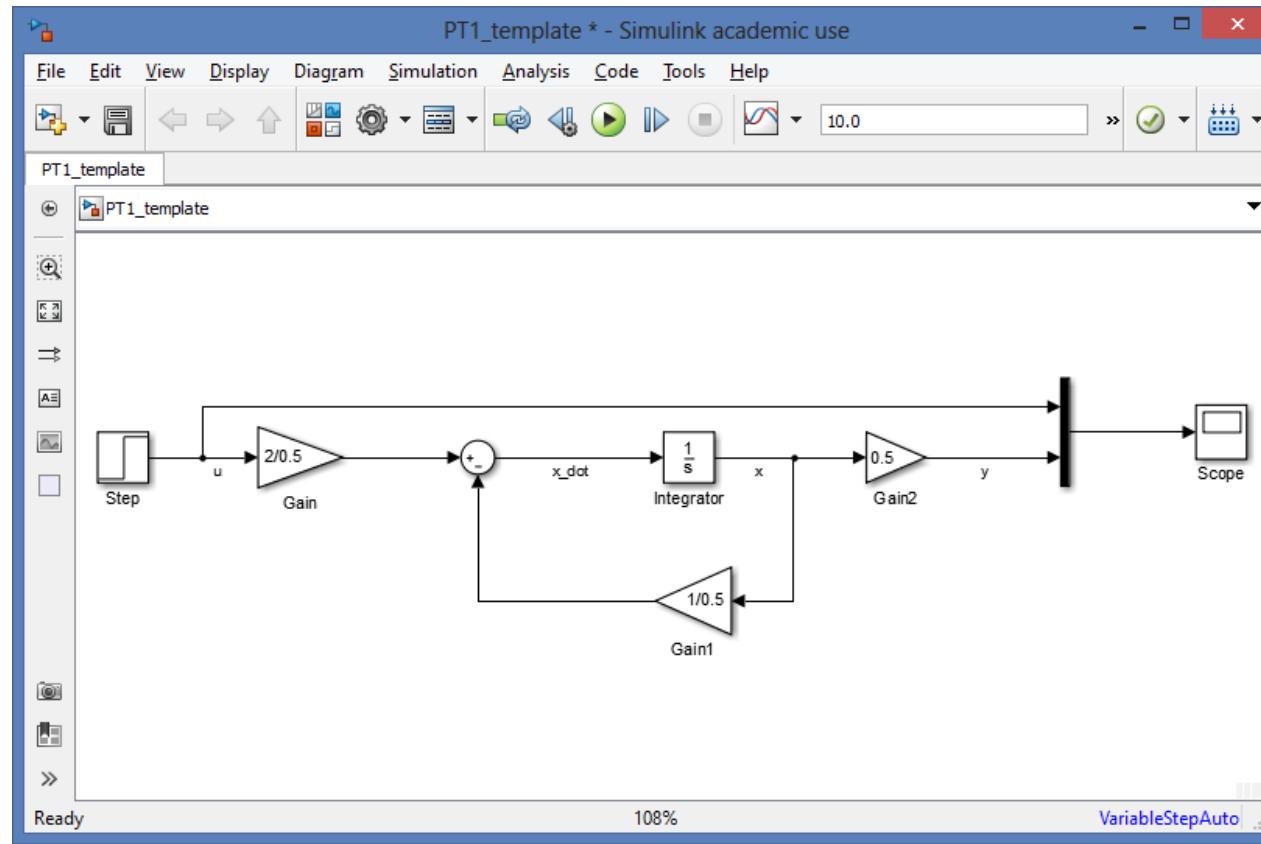
1. Assemble blocks
2. Adjust Parameters



# A Simple Example System

## Simulink Solution

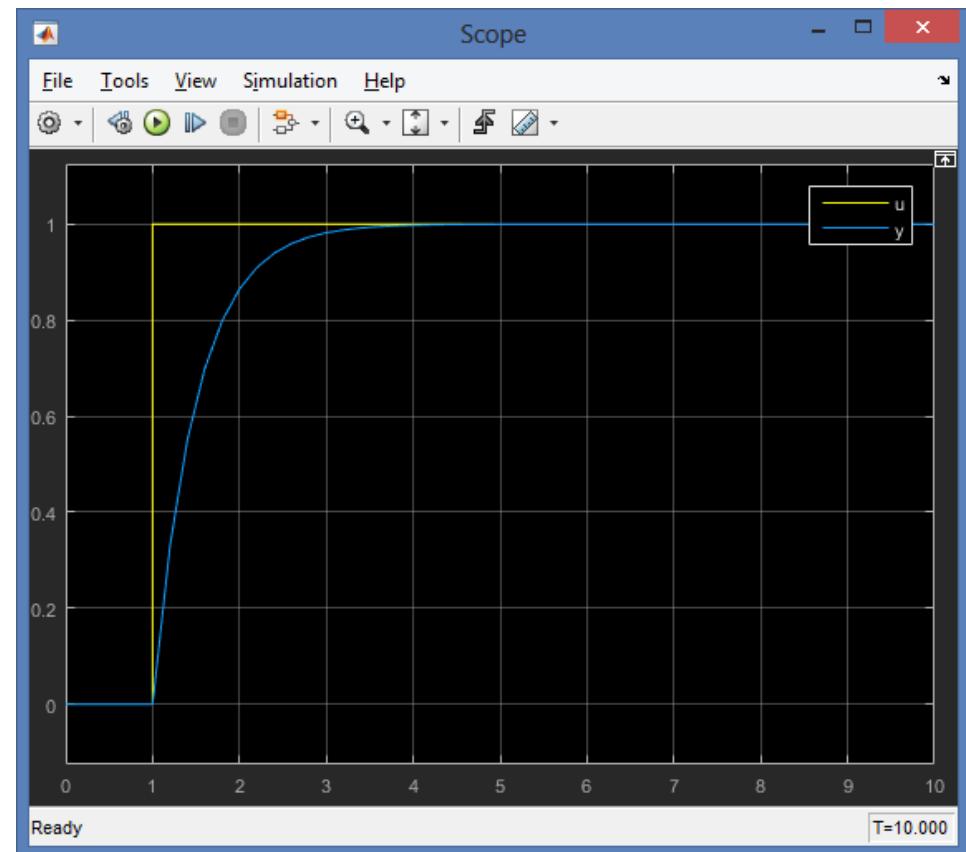
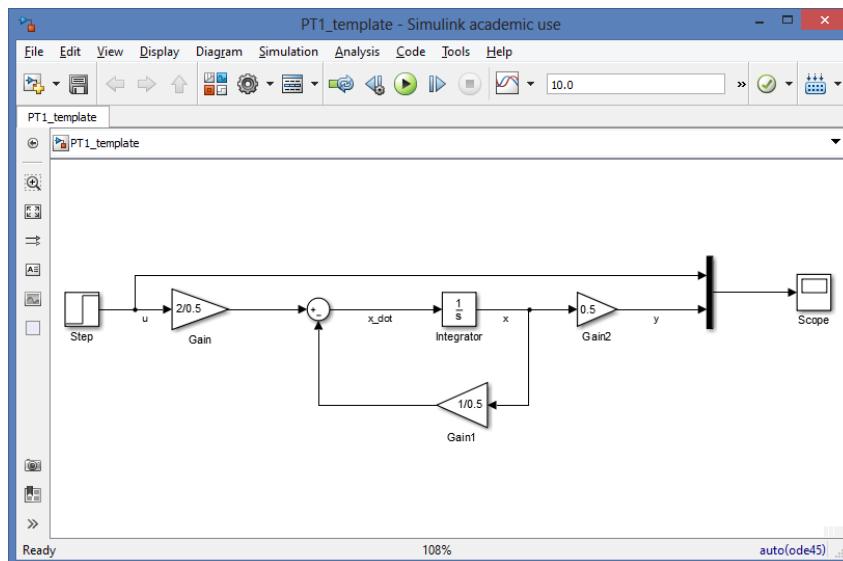
### 3. Connect Blocks



# A Simple Example System

## Simulink Solution

### 4. Simulate



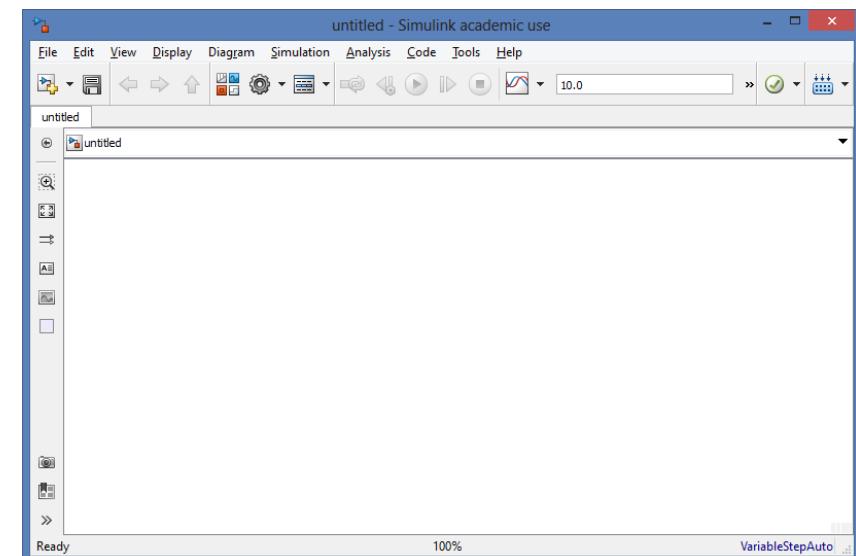
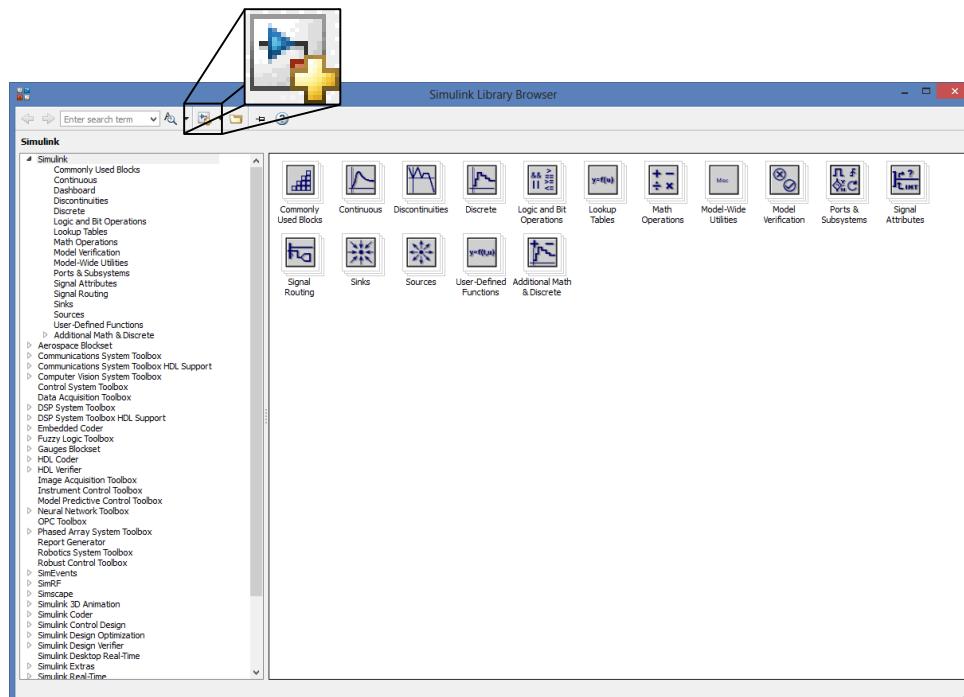
# 3. Start-Up Simulink

*fx* >> simulink

# Simulink Startup

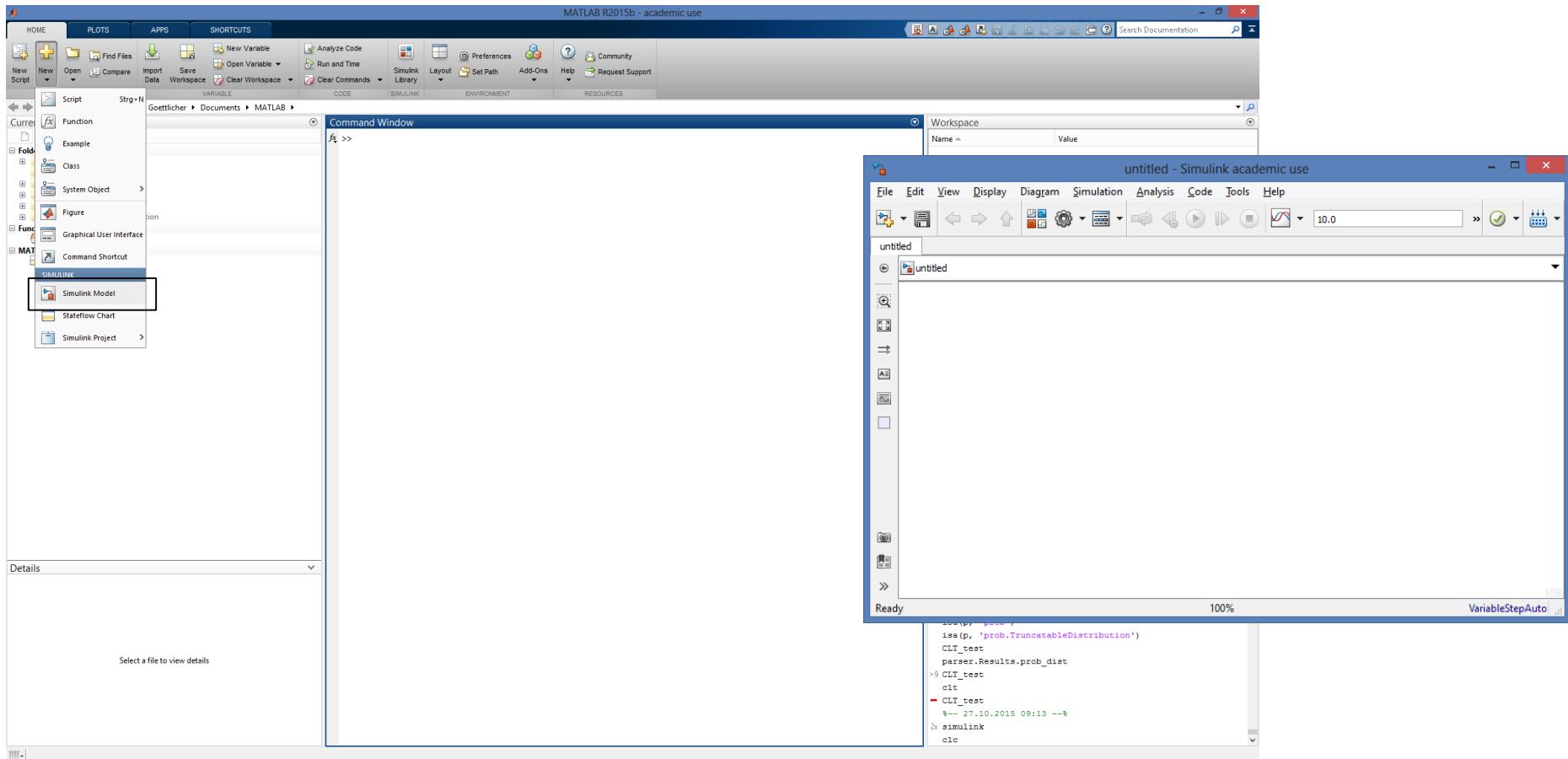
Command line:

```
>>simulink
```



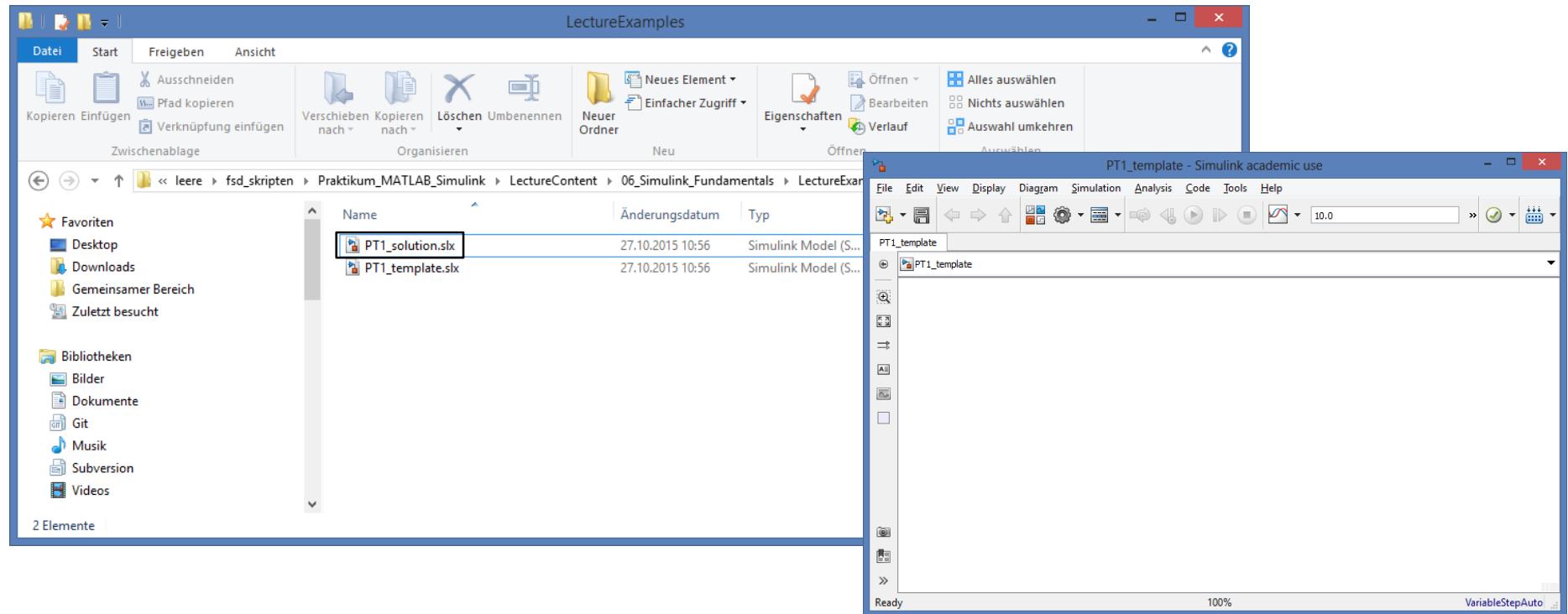
# Simulink Startup

New -> Simulink Model

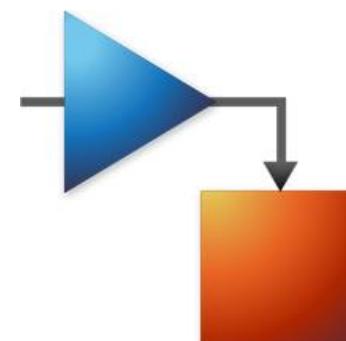


# Simulink Startup

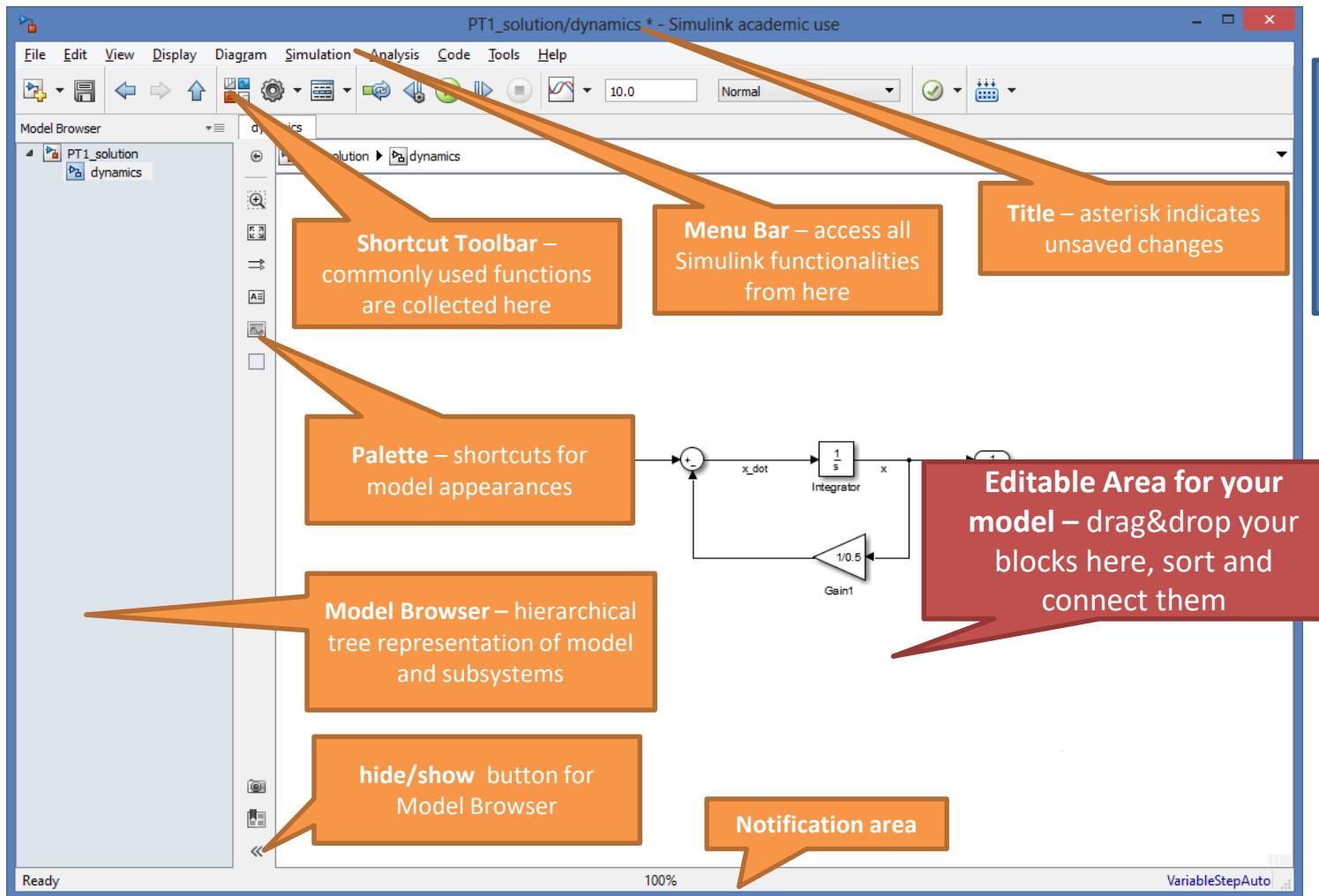
## Existing model via Windows Explorer



# 4. The Simulink Editor

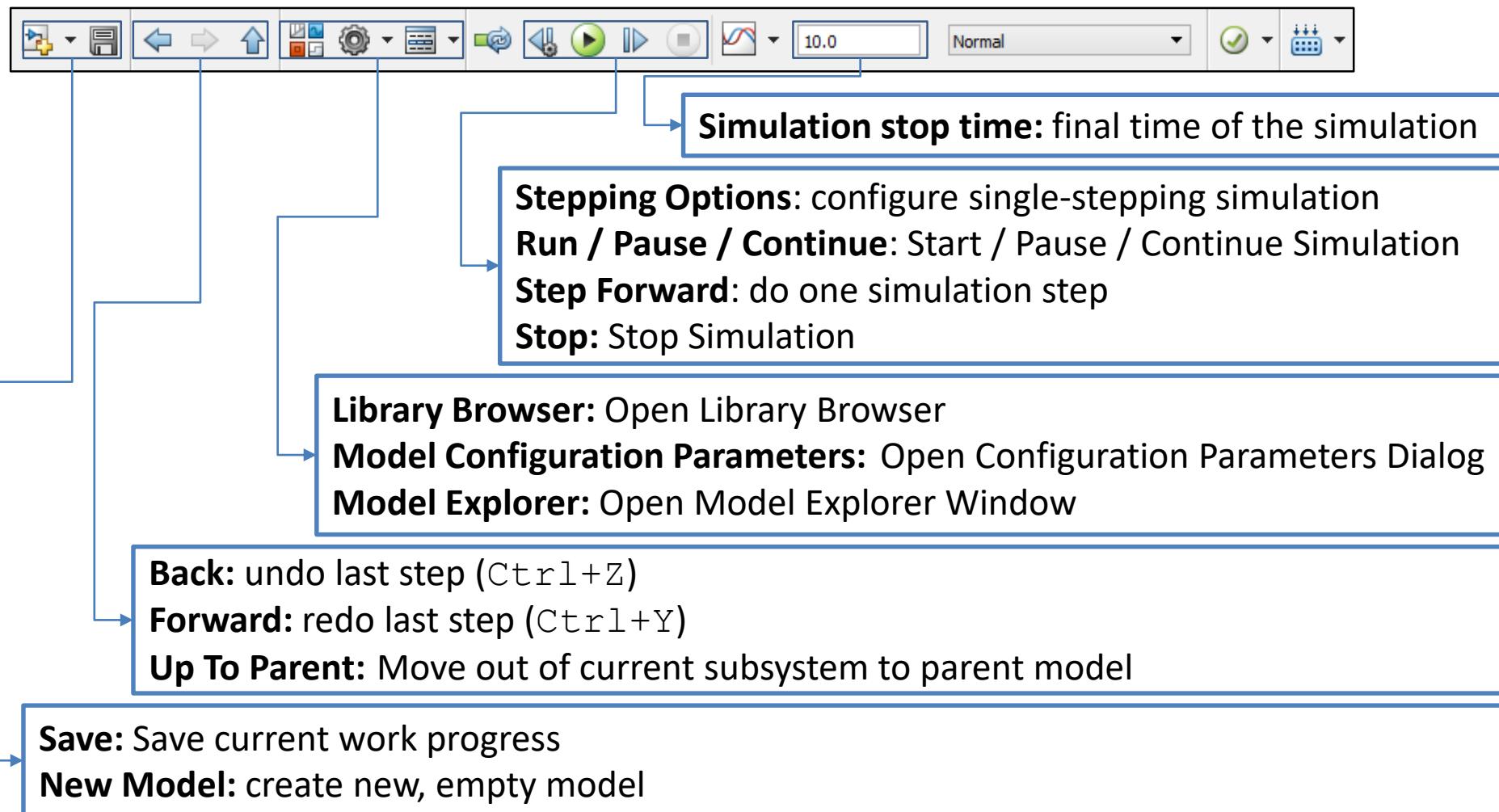


# The Simulink Editor

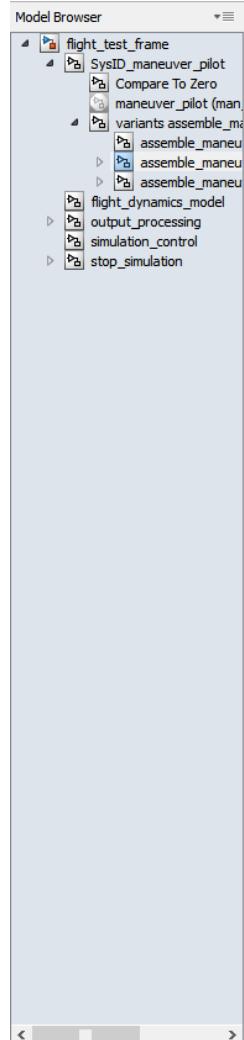


- Main modeling interface for Simulink!
- User oriented at other vector graphics programs

## The Simulink Editor



# The Simulink Editor



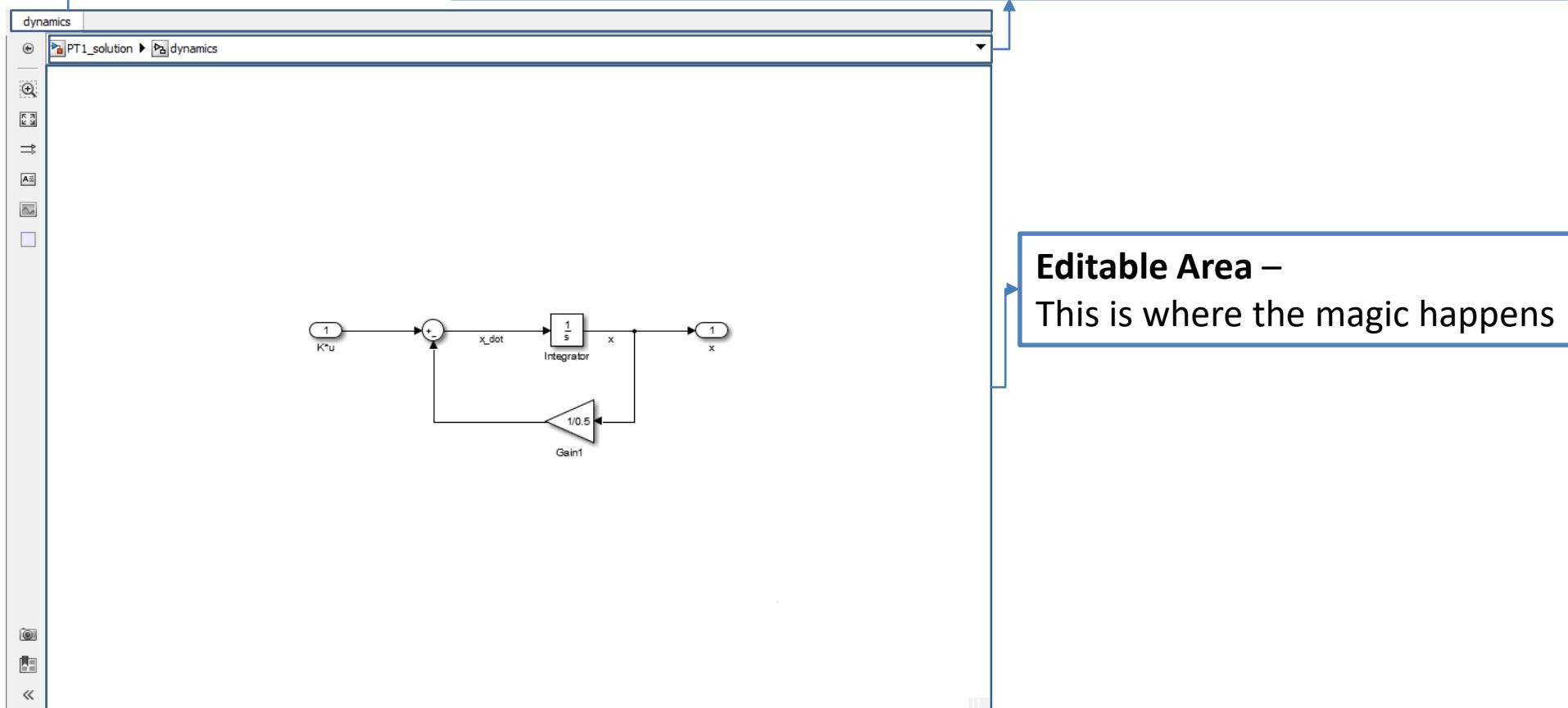
## Model Browser

Hierarchical tree structure of the model;  
Use this to quickly navigate between subsystems

## The Simulink Editor

**Tab Bar** – different model views can be opened in different tabs

**Address Bar** – address (all parent subsystems) of current subsystem



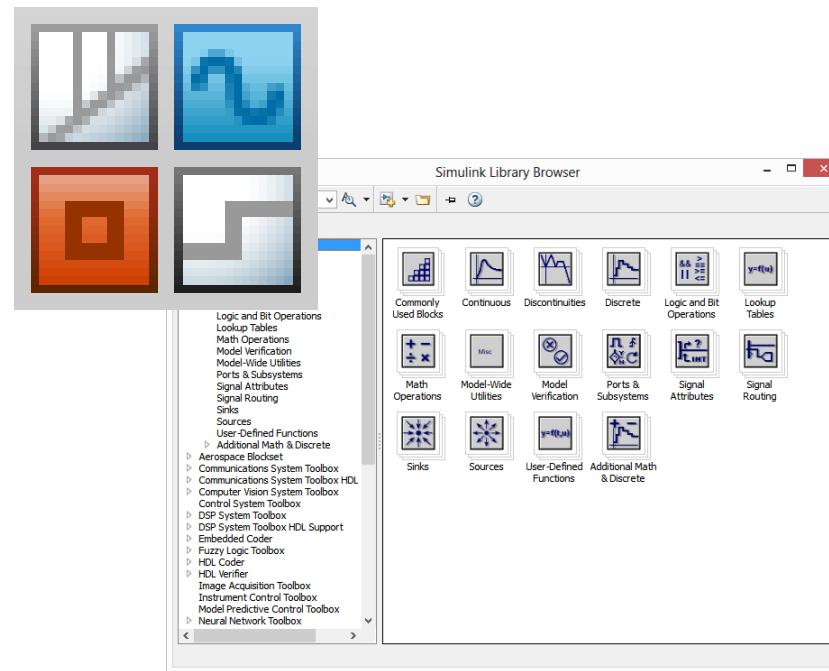
**Editable Area** –  
This is where the magic happens

## The Simulink Editor

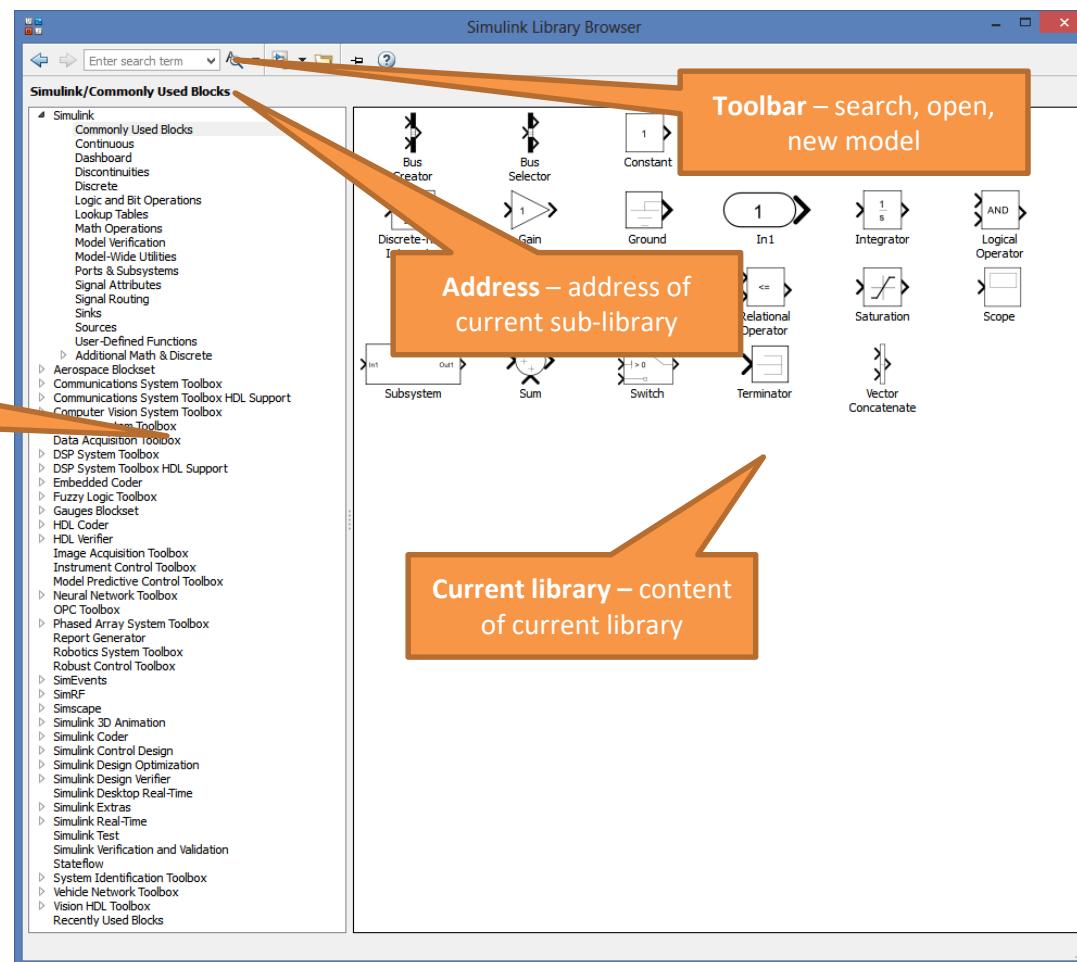
Navigating a model - Shortcuts:

<b>double-click on subsystem</b>	enter subsystem
<b>mouse-wheel</b>	zoom in / out
<b>push &amp; hold mouse-wheel</b>	pan diagram
<b>space</b>	fit diagram to window
<b>Alt + 1</b>	center view and zoom 100%

# 5. The Library Browser

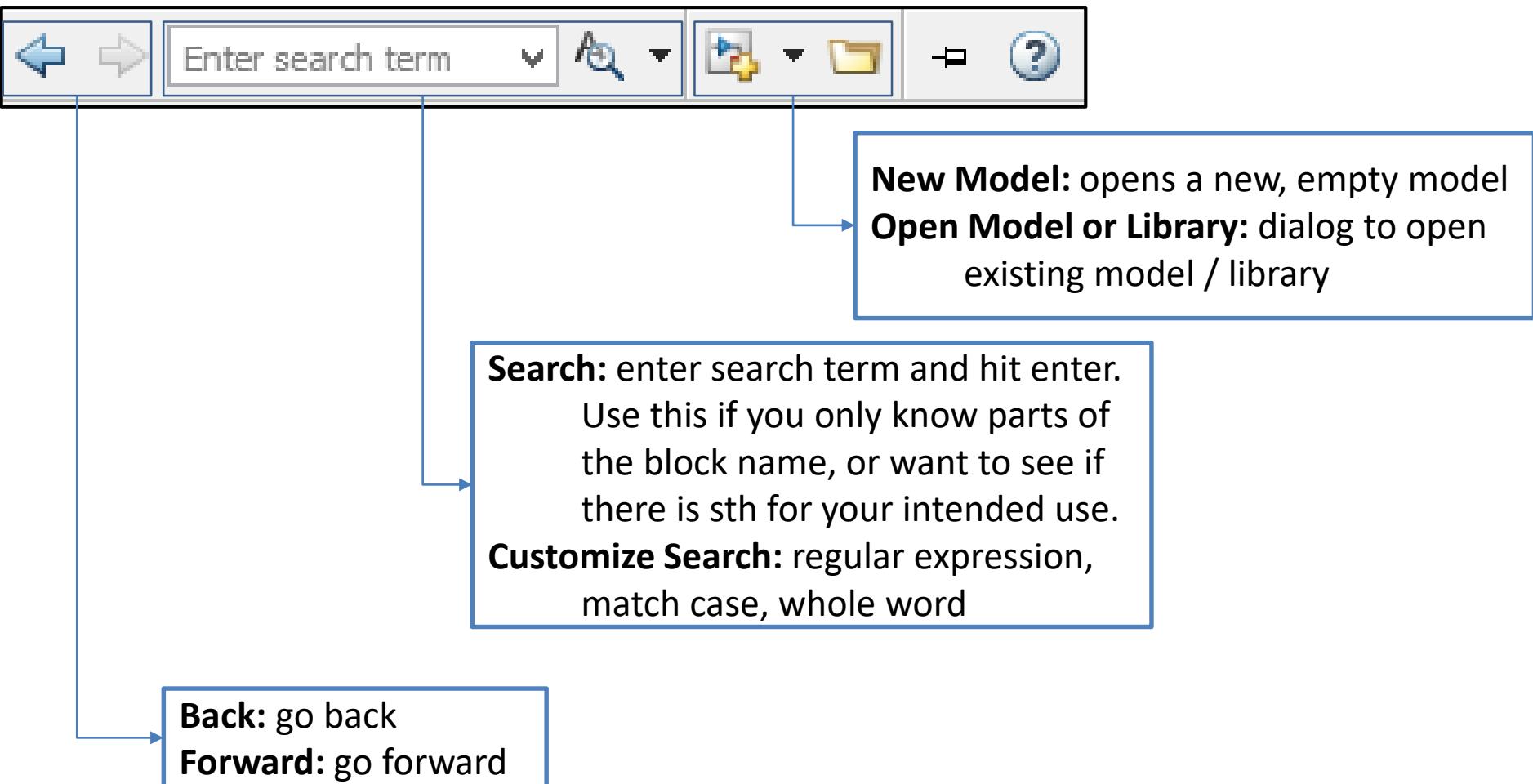


# The Library Browser

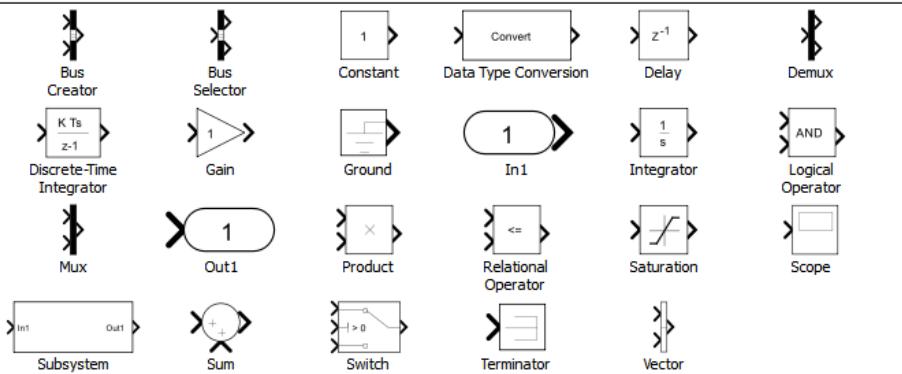


Central source for blocks

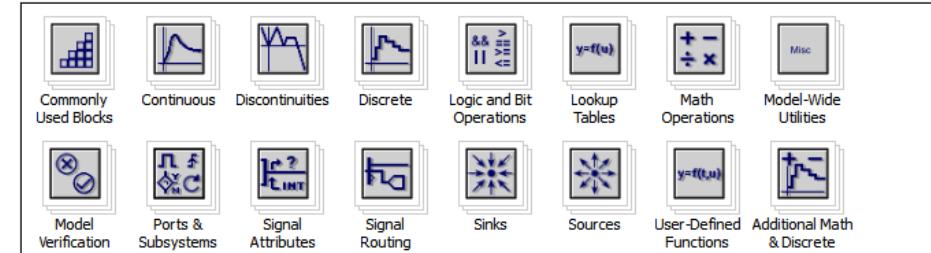
## The Library Browser



# The Library Browser



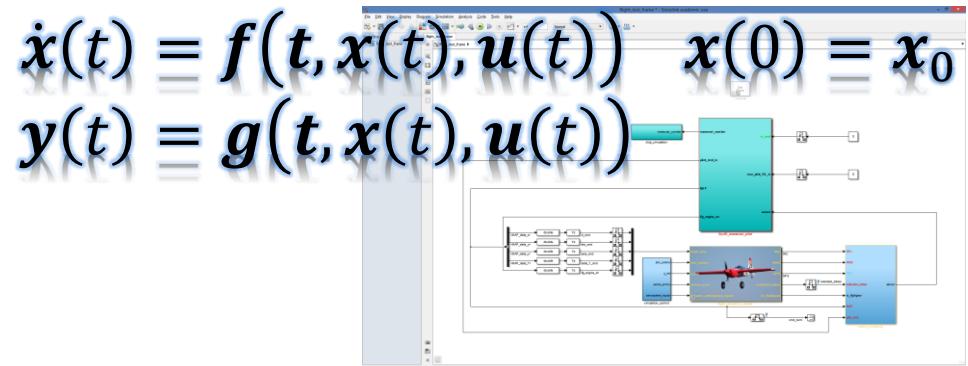
**Library can contain usable blocks:**  
→ drag-& drop blocks to simulink editor



**Library can contain sub-libraries:**  
→ navigate further down tree-structure

# 6. Modeling in Simulink

- **the Working Principle of Simulink**
  - Blocks
  - Signals
  - Subsystems
  - Parameters
  - Model Configuration Parameters



# Modeling in Simulink

## the Working Principle of Simulink

Simulink solves systems of **non-linear, first order, ordinary differential equations (ODE)**

$$\begin{aligned}\dot{x}(t) &= f(t, x(t), u(t)) \\ x(t = 0) &= x_0\end{aligned}$$

using numerical integration schemes.

Consider a linear Taylor approximation of  $x(t)$  at time  $t_i$

$$\begin{aligned}x(t) &= x(t_i) + \frac{dx(t)}{dt} \Big|_{t=t_i} (t - t_i) + h.o.t. \\ &\approx x(t_i) + f(t_i, x(t_i), u(t_i)) \cdot (t - t_i)\end{aligned}$$

Then  $x(t)$  at the next time instant  $t_{i+1}$  can be approximated by  
(using the **integration time step**  $\Delta t = t_{i+1} - t_i$ ):

$$x(t_{i+1}) = x(t_i) + f(t_i, x(t_i), u(t_i)) \cdot \Delta t_i$$

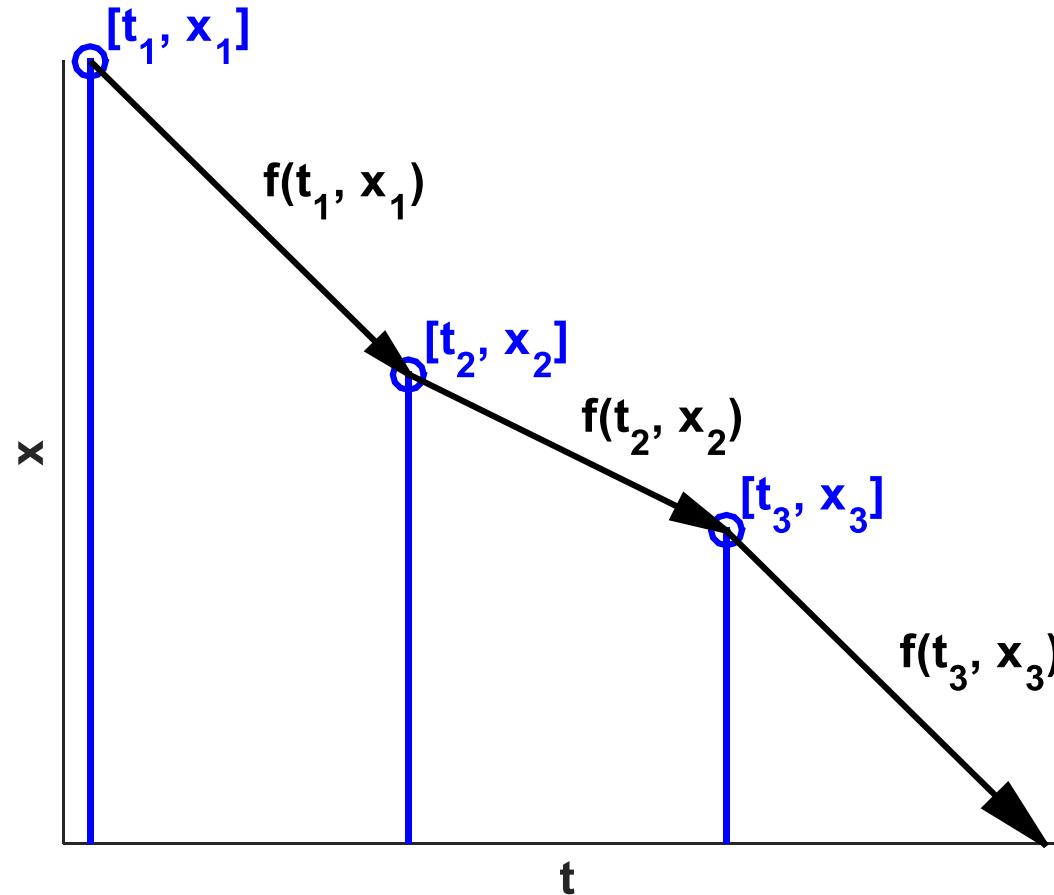
**This results in the so called „Euler Integration Scheme“**

sometimes referred to as first order integration, since the overall approximation error is  
of order  $\mathcal{O}(\Delta t)$

# Modeling in Simulink

## the Working Principle of Simulink

Euler's Method results in a linear, one-step approximation of the ode's solution:



# Modeling in Simulink

## the Working Principle of Simulink

If more evaluations of the ode's right hand side at intermediate points are considered, **multi-step** methods arise:

*Instead of one evaluation of  $f(t, x, u)$ , (as in the case of the Euler method) a weighted sum of intermediate evaluations of  $f(t, x, u)$  is used to compute the next step.*

One example is the “classic” Runge-Kutta method (4<sup>th</sup> order):

with  $\mathbf{k}_1 = f(t_i, x_i, \mathbf{u}(t_i))$

$$\mathbf{k}_2 = f\left(t_i + \frac{\Delta t}{2}, x_i + \frac{\Delta t}{2} \mathbf{k}_1, \mathbf{u}\left(t_i + \frac{\Delta t}{2}\right)\right)$$

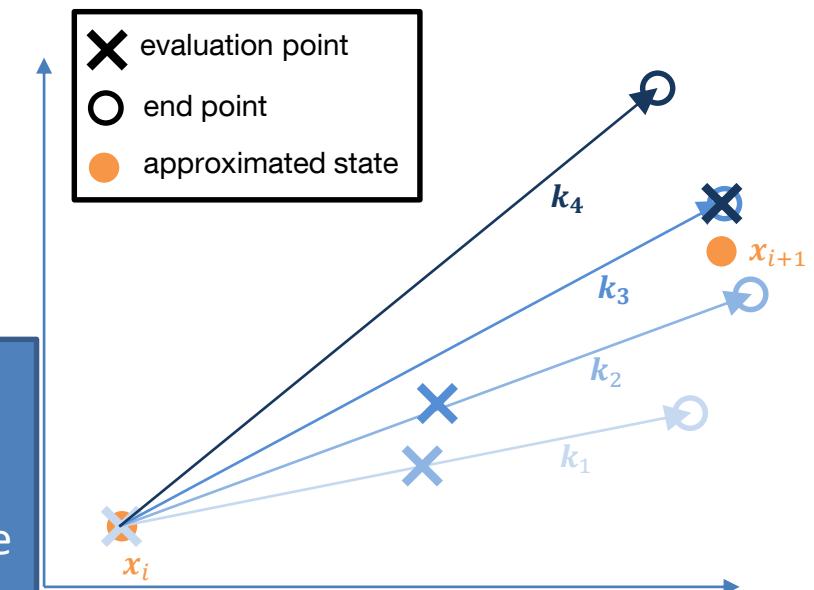
$$\mathbf{k}_3 = f\left(t_i + \frac{\Delta t}{2}, x_i + \frac{\Delta t}{2} \mathbf{k}_2, \mathbf{u}\left(t_i + \frac{\Delta t}{2}\right)\right)$$

$$\mathbf{k}_4 = f(t_{i+1}, x_i + \Delta t \mathbf{k}_3, \mathbf{u}(t_{i+1}))$$

$$x_{i+1} = x_i + \frac{\Delta t}{6} (\mathbf{k}_1 + 2\mathbf{k}_2 + 2\mathbf{k}_3 + \mathbf{k}_4)$$

This results in the “classic” Runge-Kutta Integration Scheme

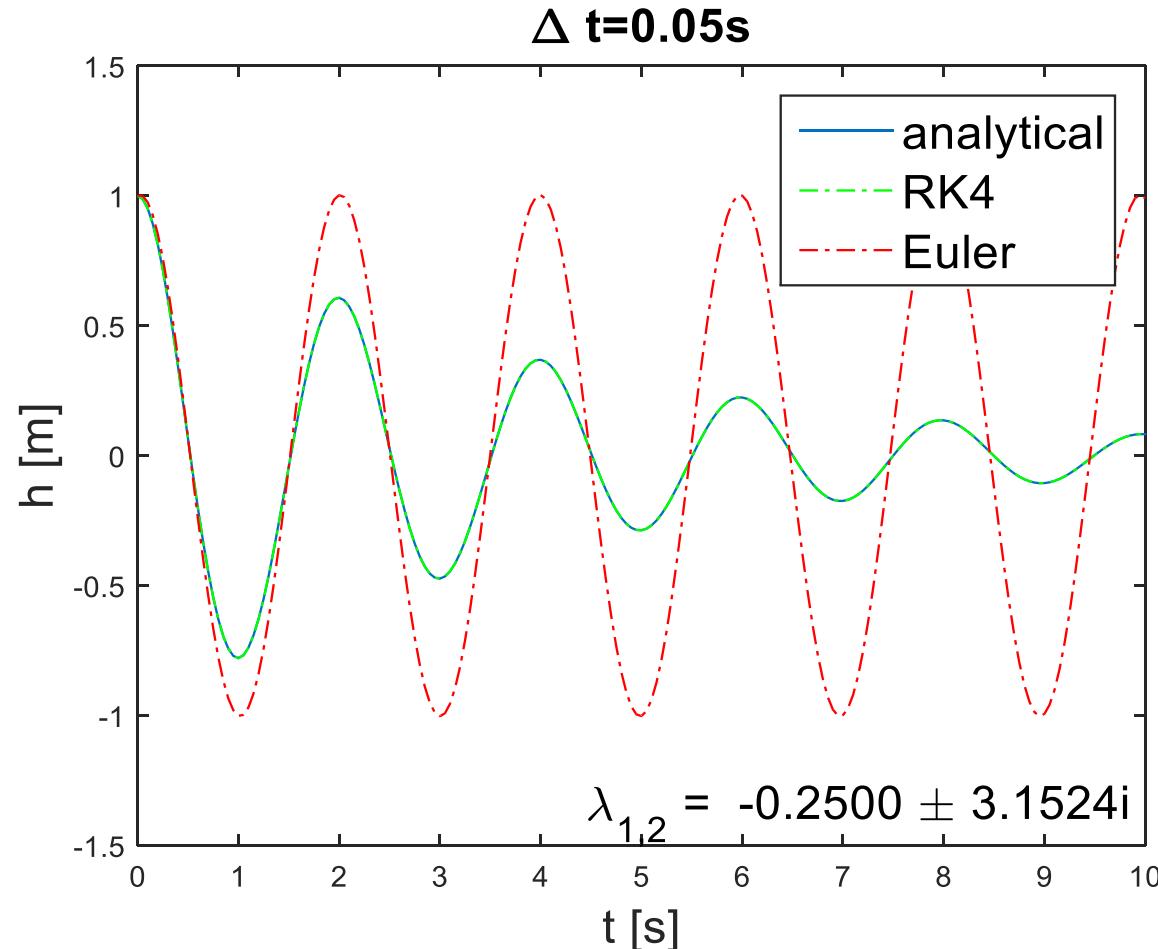
sometimes referred to as 4<sup>th</sup> order integration, since the overall approximation error is of order  $\mathcal{O}(\Delta t^4)$



# Modeling in Simulink

## the Working Principle of Simulink

Compare integration methods (simple oscillator) :



# Modeling in Simulink

## the Working Principle of Simulink

### Variable Step-Size Algorithms

- For many multi-step methods, the result of the method with one less error order can be obtained without additional evaluations of  $f(t, x, u)$   
→ i.e. 5<sup>th</sup> order integration yields result for 4<sup>th</sup> order integration as by-product
- Variable step size algorithms adjust  $\Delta t$  based on the difference of two consecutive methods:

$$\begin{aligned} |x_{i+1,RK5} - x_{i+1,RK4}| &\geq \epsilon_{upp} & \Rightarrow \text{decrease } \Delta t \\ |x_{i+1,RK5} - x_{i+1,RK4}| &\leq \epsilon_{low} & \Rightarrow \text{increase } \Delta t \end{aligned}$$

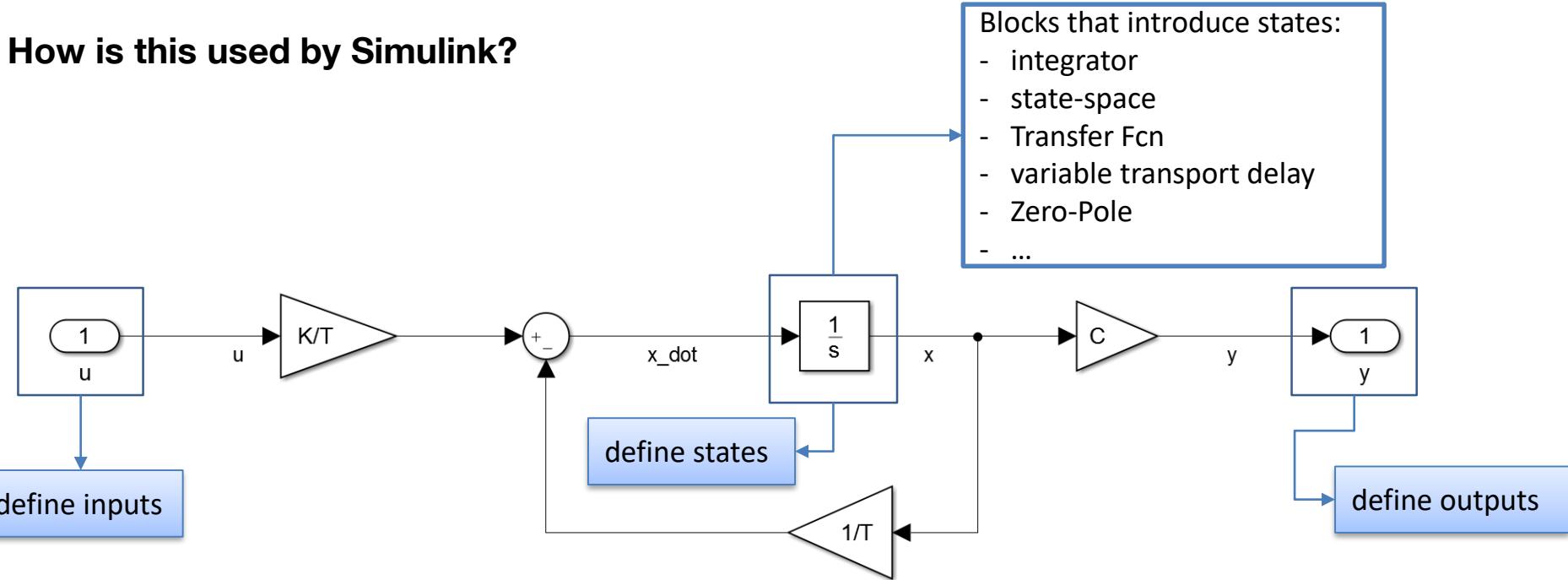
- This yields `ode45` (Dormand-Prince)

- Thus the step-size is adapted to the system's dynamics  
(fast-changing → small step size; slow-changing → large step size)
- Results in comparatively fast **AND** accurate results
- However, **NO** a priori knowledge of evaluation times  $t_i$ ! They are adapted online.

# Modeling in Simulink

## the Working Principle of Simulink

### How is this used by Simulink?

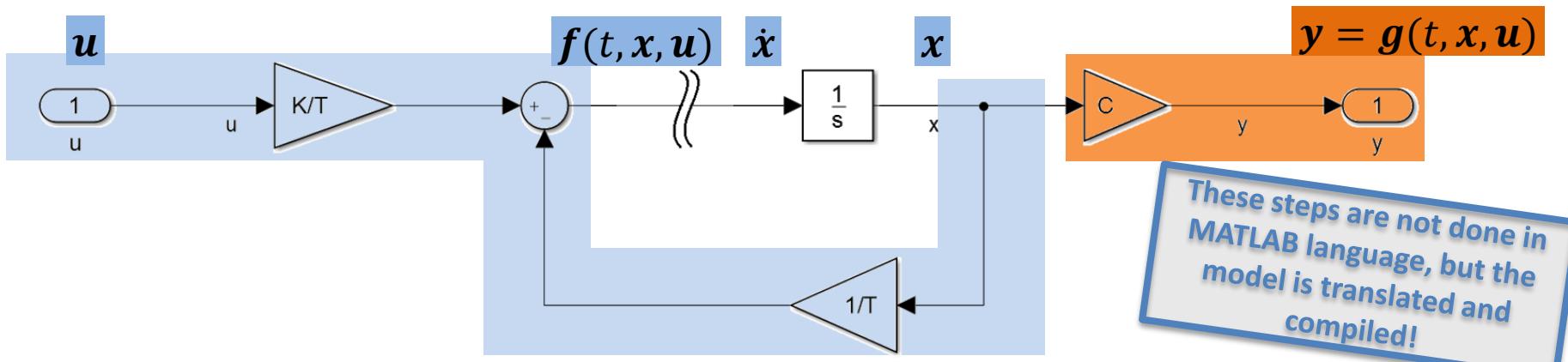


# Modeling in Simulink

## the Working Principle of Simulink

### How is this used by Simulink?

- I. translate block diagram to system of first order ordinary differential equations
  1. define states, state derivatives, outputs and inputs
  2. ,cut' in front of integrators
  3. from integrator: go backwards through model until an input  $u$  or state  $x$  is reached  $\rightarrow f(t, x, u)$
  4. from output: go backwards until an input  $u$  or state  $x$  is reached  $\rightarrow g(t, x, u)$
- II. solve system using above mentioned integration schemes

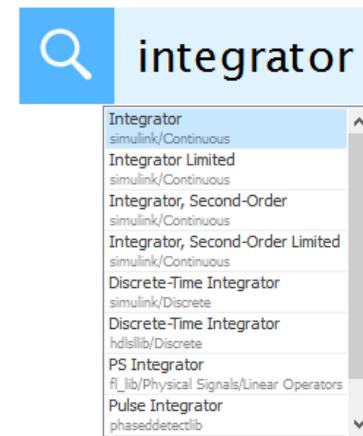
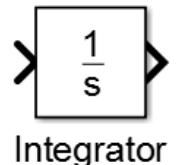


example system:

$$\begin{aligned}\dot{x} &= f(t, x, u) = -\frac{1}{T}x + \frac{K}{T}u \\ y &= g(t, x, u) = Cx\end{aligned}$$

# 6. Modeling in Simulink

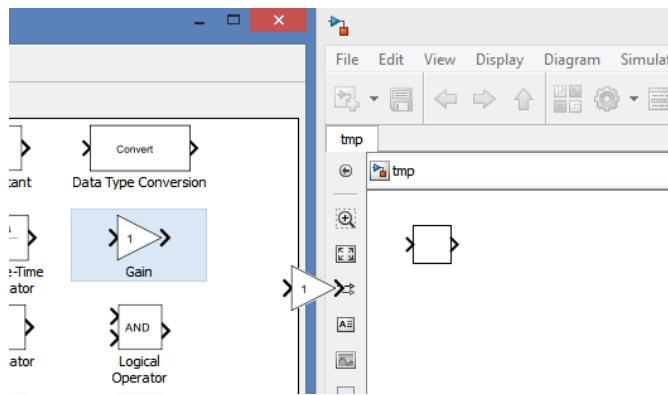
- the Working Principle of Simulink
- **Blocks**
- Signals
- Subsystems
- Parameters
- Model Configuration Parameters



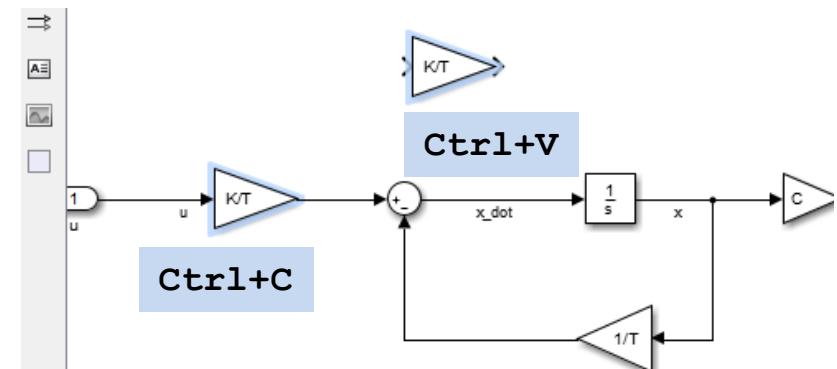
# Modeling in Simulink Blocks

add a block to a Simulink model:

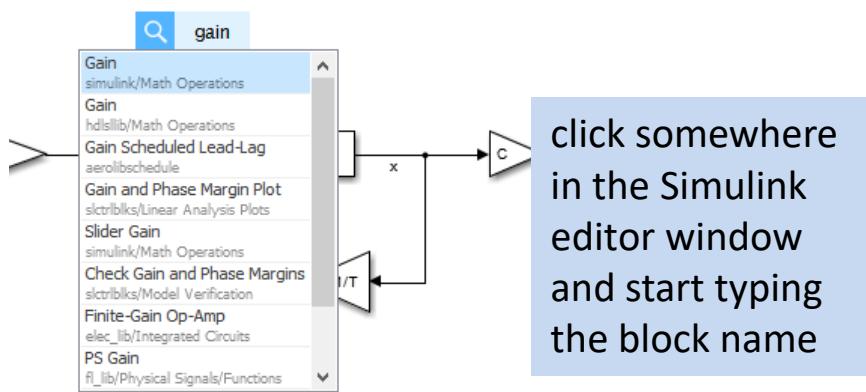
drag & drop from Library Browser



copy & paste another block

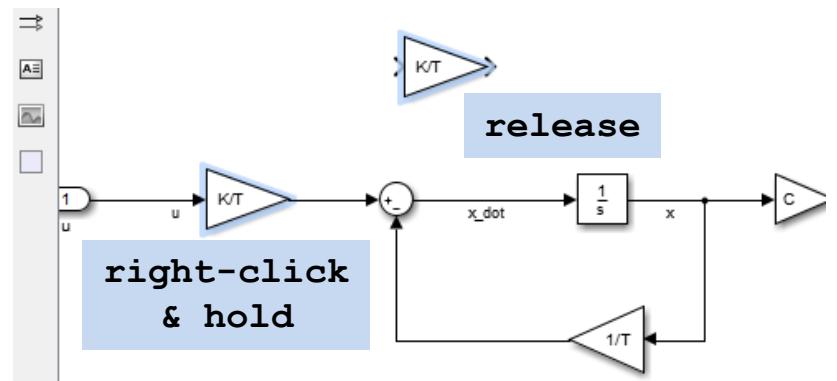


use intelligent search



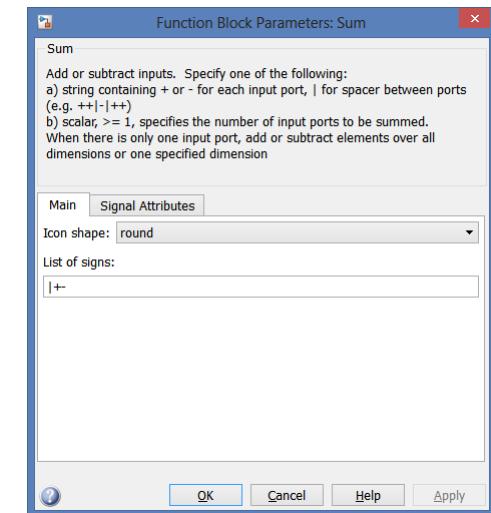
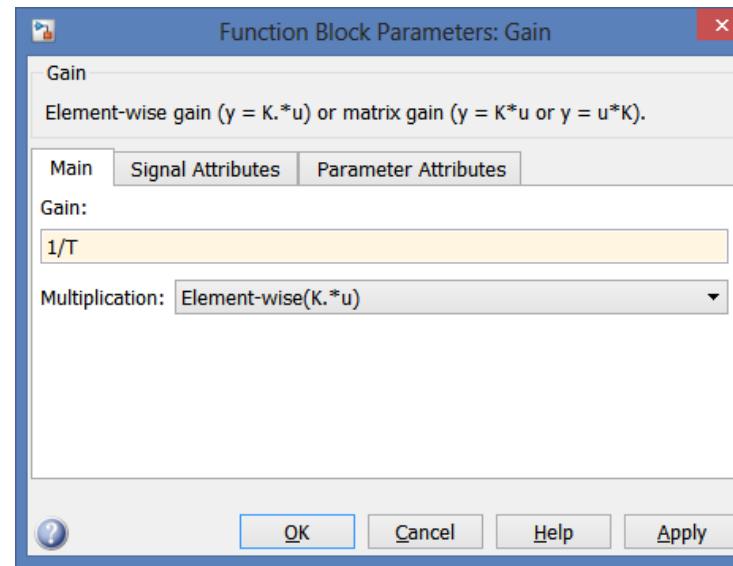
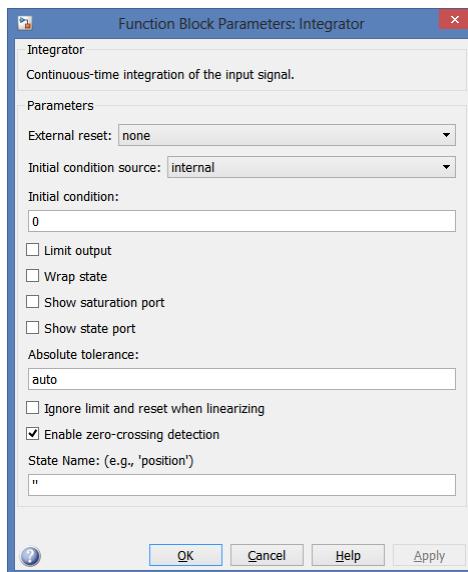
click somewhere  
in the Simulink  
editor window  
and start typing  
the block name

drag & drop with right mouse button



# Modeling in Simulink Blocks

- a double click on a block opens a specific configuration window.
- Here the block's properties can be adjusted



**instead of numerical values, variable names can be used as well.**

As long as those variables are defined in the workspace (or somewhere else). For example the Gain here is  $1/T$ , where  $T$  is defined in the base workspace.

# Modeling in Simulink Blocks

**most important block context menu entries**  
*(right-click on any block to obtain this menu)*

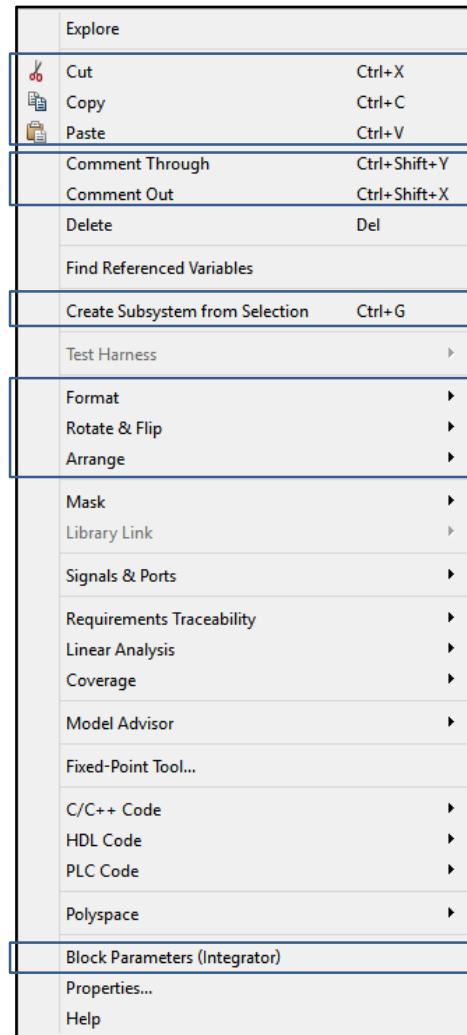
same as any other program...

„comment out“ block, i.e. make it  
inoperative

„take all marked blocks, and put them in  
one common subsystem“

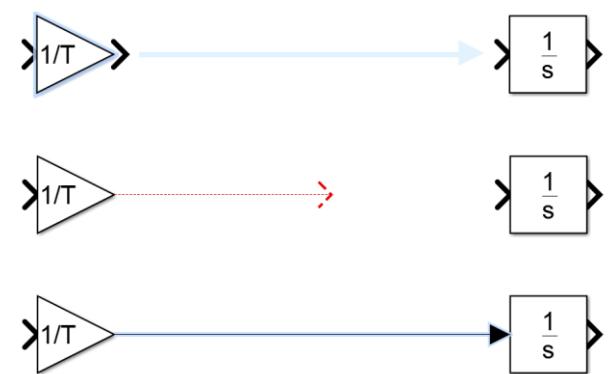
change appearance of block (color, font  
color, font size, shadows, block  
orientation, ...)

same as double-clicking on a block:  
change its characteristic behaviour



# 6. Modeling in Simulink

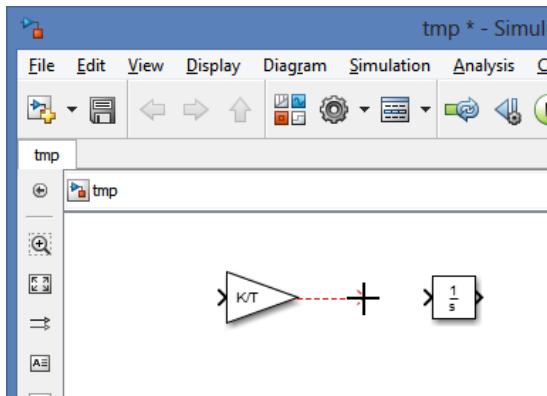
- the Working Principle of Simulink
- Blocks
- **Signals**
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- Model Configuration Parameters



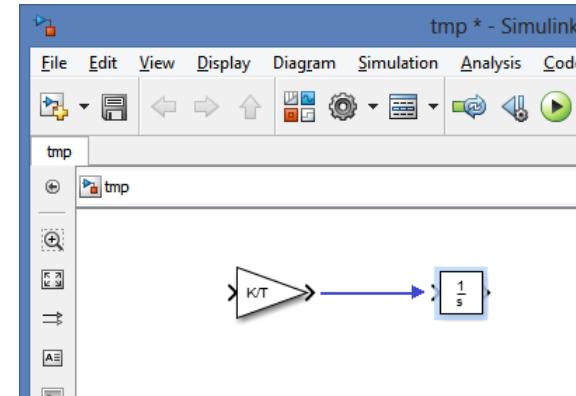
# Modeling in Simulink

## Signals

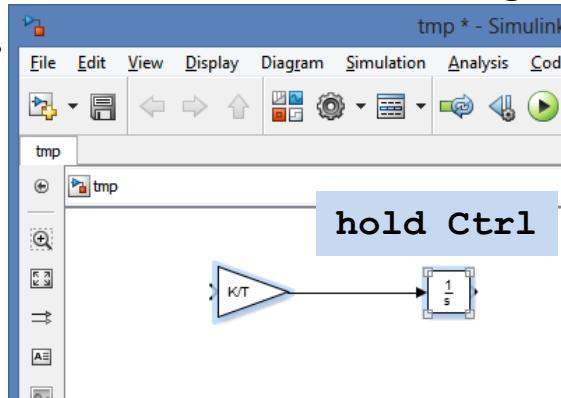
click on outport, hold to connect to import  
(or vice versa)



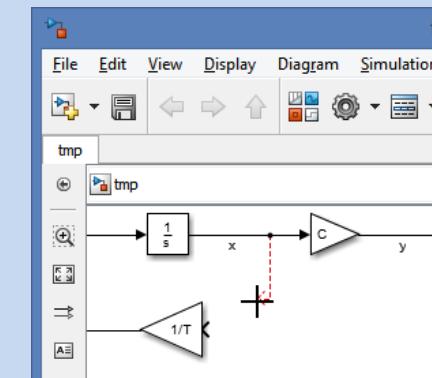
when blocks are aligned, click on blue arrow



mark first block; hold  $\text{Ctrl}$  while clicking  
on the second.  
*(useful for  
connecting  
multiple outputs  
to multiple  
inputs)*



to branch signals: right click and hold on  
existing signal

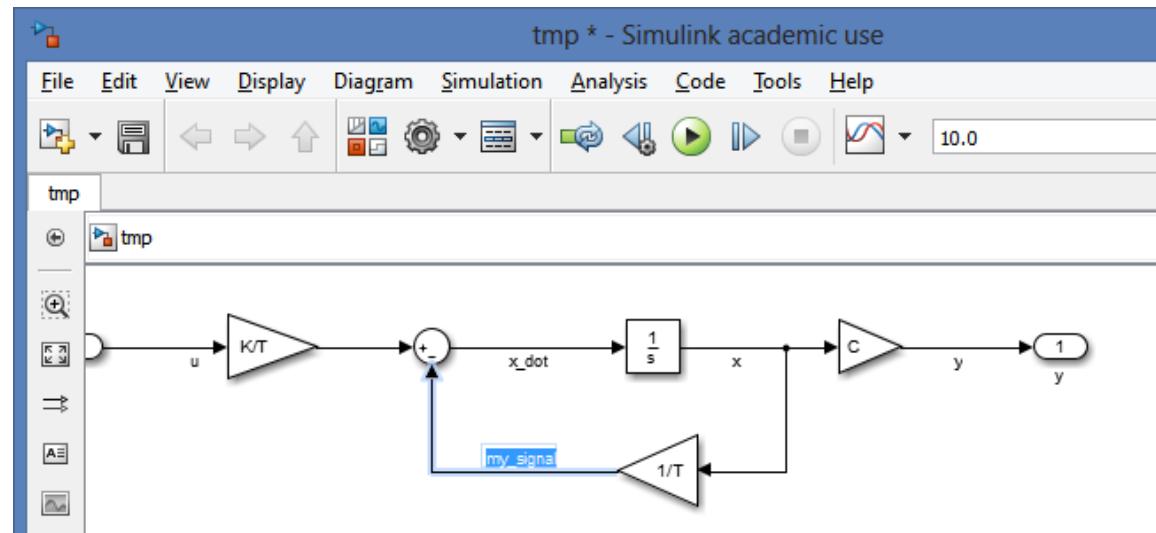


# Modeling in Simulink

## Signals

**to name a signal, double click on it and type name:**

(make sure to really click **on the signal**. Double-clicking somewhere and typing adds an annotation, which is **not** associated with a signal!)



- signal names allow the unique identification of a signal
- signal names make your model more readable
- signal names can be used for logging a signal (see later slides)
- signal names allow unique mapping in a Bus signal (see later slides)

# Modeling in Simulink

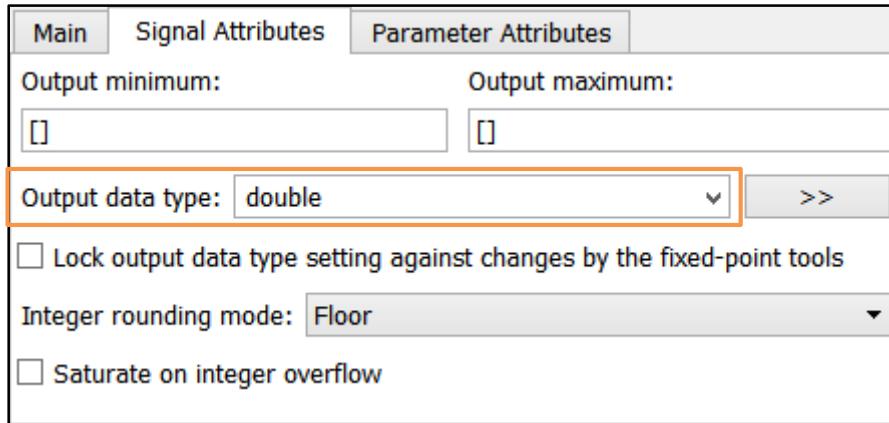
## Signals

**Signals always have a designated data type. (Default is ‘double’)**

(activate display of signal data type: Menubar -> Display -> Signals & Ports -> Port Data Types)

common data types are: double, single, int32, uint32, int16, uint16, int8, uint8, bool

### set via Block Properties



- many blocks have a ‘Signal Attributes’ tab in their block properties menu.
- here the output data type can be set

### set via ‘Data Type Conversion’ Block



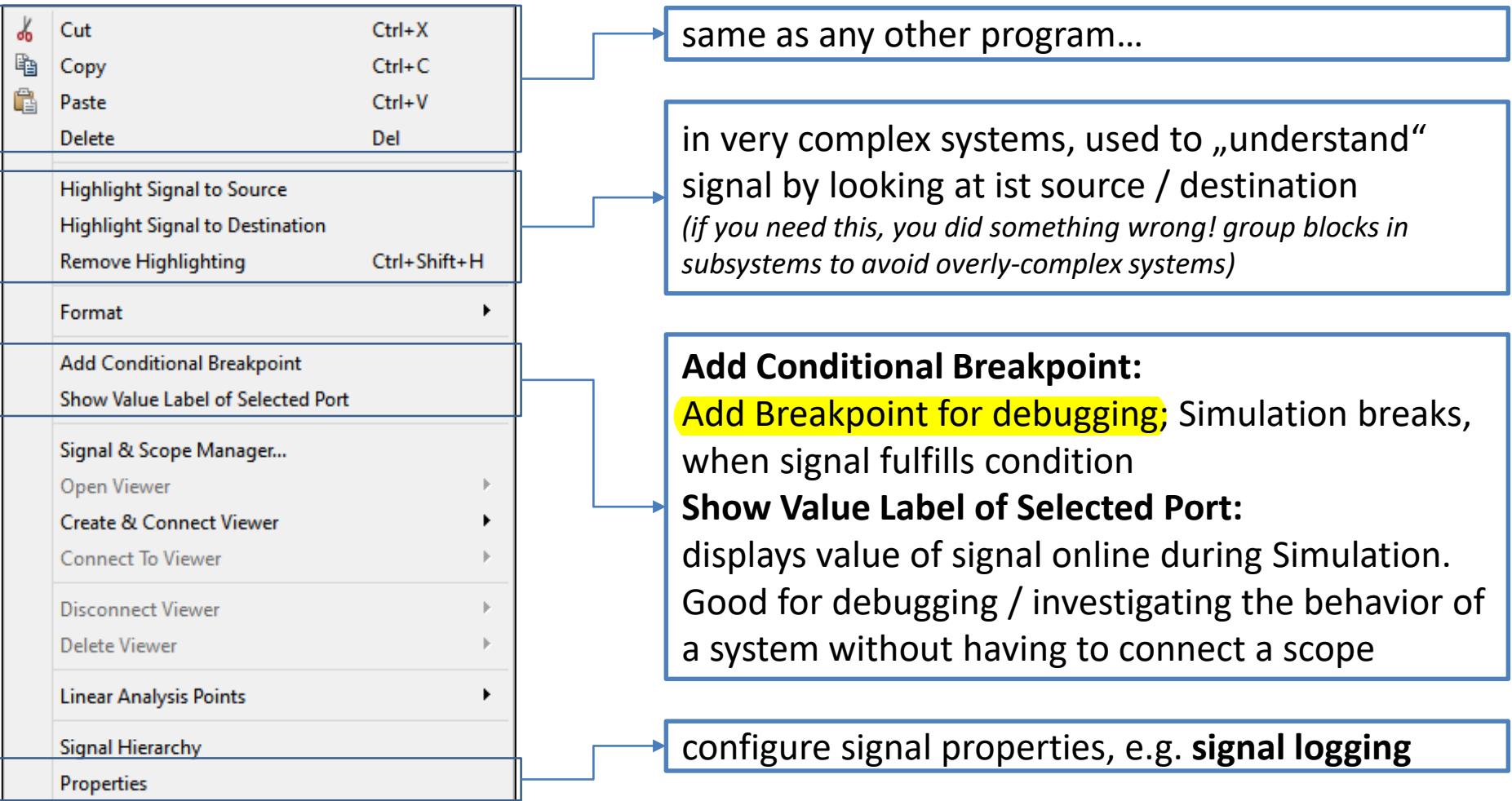
Data Type Conversion

- block to explicitly change signal data type
- equivalent to ‘casting’ in C / C++

the data type can be set to “Inherit via...” then Simulink applies internal rules to determine it

# Modeling in Simulink

## Signals



# Modeling in Simulink

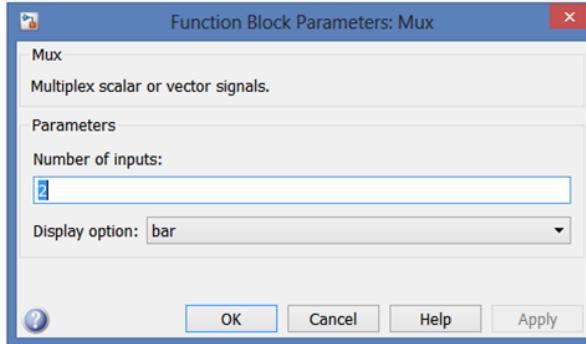
## Signals

having only scalar signals can make model „messy“

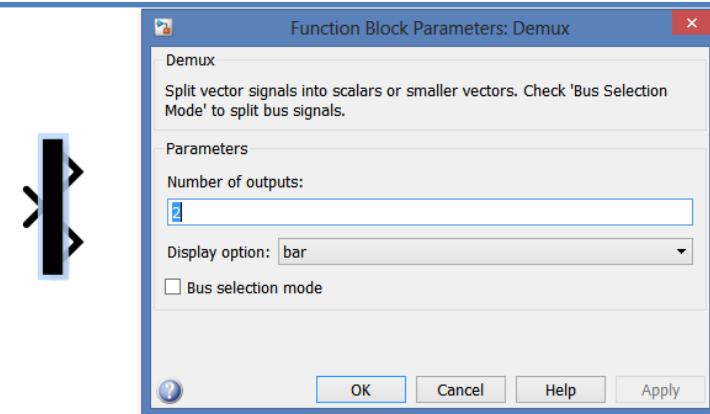
→ use **Mux blocks** to group signals.

*This is equivalent to ‚arrays‘ in other programming languages (C/C++, Matlab)*

→ use **Demux blocks** to ungroup signals



- number of inputs can be configured in Block parameters
- the block changes its appearance accordingly
- **only signals of same datatype / sample time can be ‚muxed‘ together!**
- muxed signals can be inputs to a Mux block, too.



- number of outputs can be configured in Block parameters
- the block changes its appearance accordingly
- **scalar number of outputs  $x$ :** input array is split into  $x$  equally sized signals
- **vector of output sizes  $[x_1, x_2, \dots]$ :** input array is split in signals of sizes  $x_1, x_2, \dots$

*activate display of signal dimensions: Menubar -> Display -> Signals & Ports -> Signal Dimensions*

# Modeling in Simulink

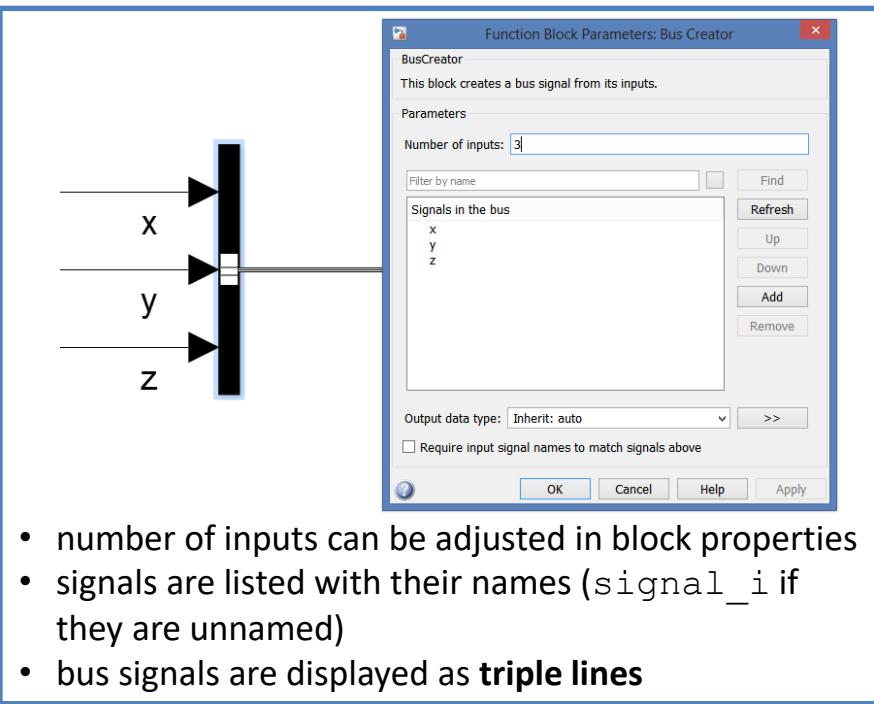
## Signals

**Bus Signals** expand the functionality of muxes by storing signal name information as well

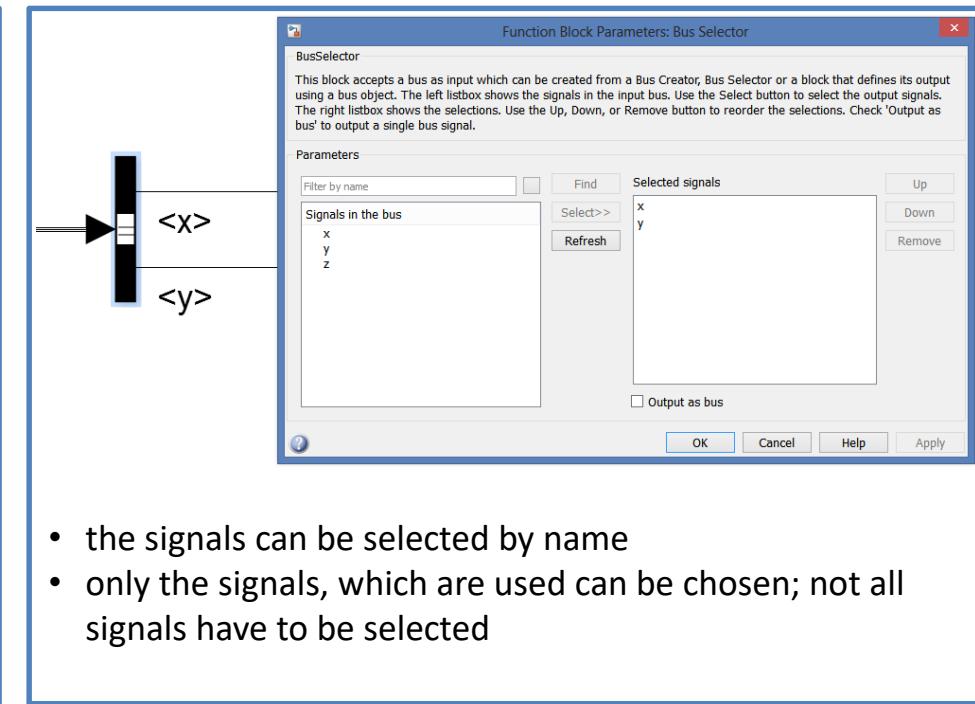
→ **Bus Creator:** create a bus signal from other signals (scalar-, array- or other Bus Signals).

*This is equivalent to ‘structs’ in other programming languages (C/C++, Matlab)*

→ **Bus Selector:** select a signal from a bus.



- number of inputs can be adjusted in block properties
- signals are listed with their names (`signal_i` if they are unnamed)
- bus signals are displayed as **triple lines**



- the signals can be selected by name
- only the signals, which are used can be chosen; not all signals have to be selected

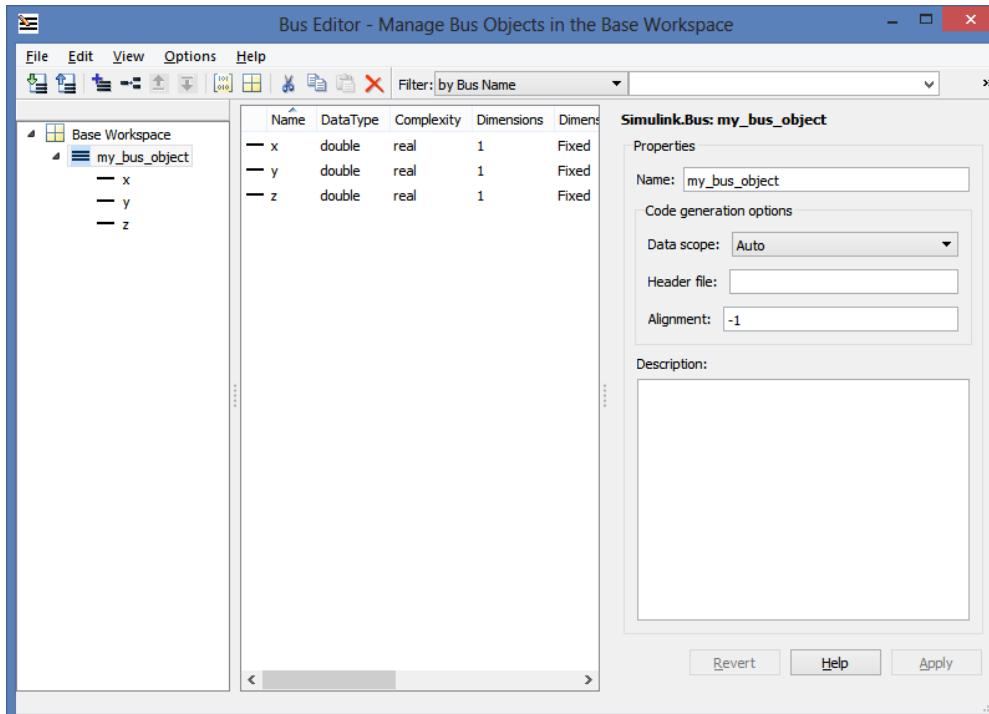
# Modeling in Simulink

## Signals

The structure of Busses can be pre-define via **Bus Objects**.

- type `>> buseditor` in the Matlab command window
- use: *Menubar -> Edit -> Bus Editor*

to open **Bus Editor** window. Here, Bus structure and element properties can be set graphically



### Properties of Bus Objects

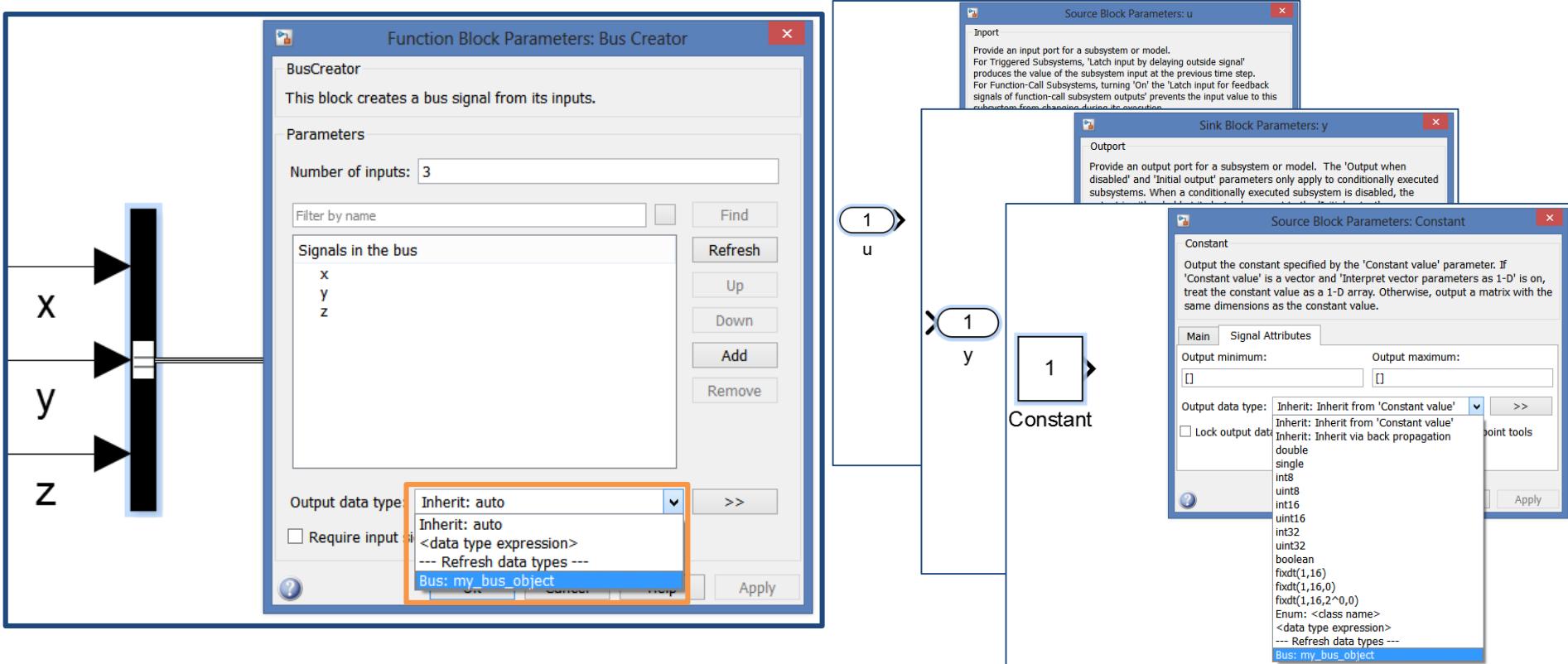
- **use to define interfaces**
- assure that busses in use have pre-defined structure
- assure that bus-elements have defined data-types
- **necessary when using busses in root-level imports / outports**
- similar to `typedef struct {}` in C/C++ → ‘defines new data type’

# Modeling in Simulink

## Signals

The structure of Busses can be pre-define via **Bus Objects**.

These **Bus Object** can then be chosen as **Data Type** in the **Bus Creator Block**, or any other block, where an output data type can be assigned, e.g. **inport / outport, constant, ...**

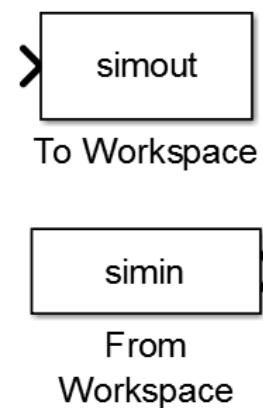


# Modeling in Simulink

## Signals

To analyze simulation data with MATLAB, there are several possibilities to exchange data:

- **From / To Workspace blocks**



- signal is stored in / read from MATLAB variable in base workspace
- the following formats for that variable are possible

1. MATLAB timeseries object

```

1 % timeseries
2 sim_data = timeseries(t, data);
  
```

2. matrix: first **column** has to be time-vector, subsequent columns are data vectors

```

3 % matrix
4 sim_data = [t, data];
  
```

3. structure: the following fields must present

```

var.time=[TimeValues]
var.signals.values=[DataValues]
var.signals.dimensions=[DimValues]
  
```

```

5 % struct
6 sim_data.time = t;
7 sim_data.signals.values = data;
8 sim_data.signals.dimensions = size(data);
  
```

- intermediate values are interpolated
- out of range behavior for *from Workspace* block can be adjusted

- Root-Level input / output ports:



- logging signals directly put input / output port on root level of model
- configure in *Data Import/Export* tab of *Model Configuration Parameters*

- log signals directly

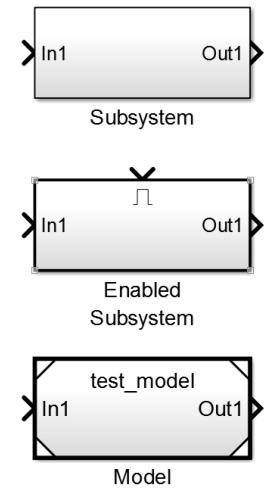


- right-click on signal, activate in *Logging and accessibility* tab in *Signal Properties*
- configure in *Data Import/Export* tab of *Model Configuration Parameters*

**additional possibilities  
for data import / export;  
Not to be used here!**

# 6. Modeling in Simulink

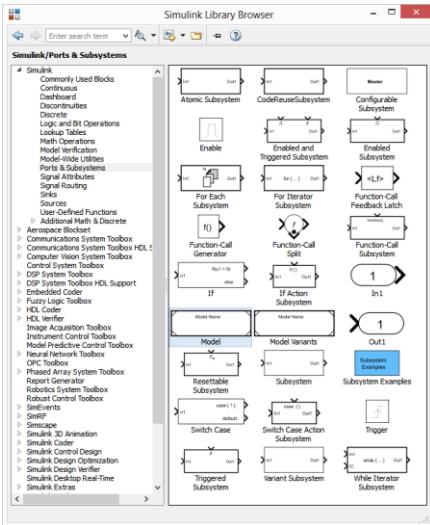
- the Working Principle of Simulink
- Blocks
- Signals
- **Subsystems**
- Parameters
- Model Configuration Parameters



# Modeling in Simulink Subsystems

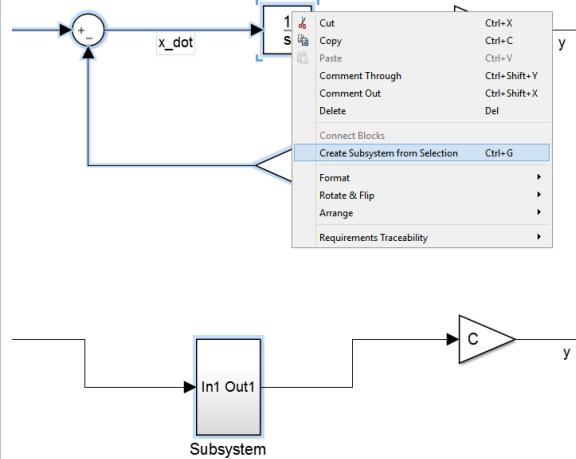
create a **subsystem** in one of the following ways:

## add from Library Browser



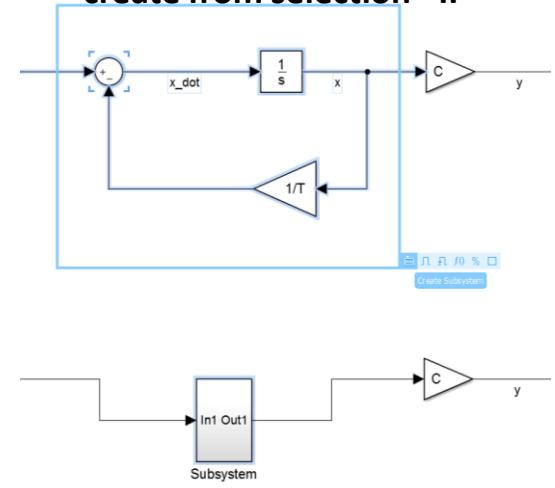
- go to *Simulink->Ports & Subsystems*
- choose the subsystem of your liking
- the subsystem will be empty

## create from selection - I



- mark some existing blocks
- right-click and choose *Create Subsystem from Selection*
- the subsystem will contain the marked blocks

## create from selection - II



- mark some existing blocks
- use menu at bottom right corner of marked area
- the subsystem will contain the marked blocks

- subsystems are used to structure your model
- subsystems can be nested

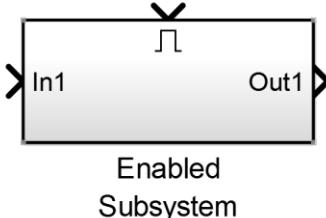
- subsystems are (in general) virtual blocks, they do not perform any action on the signals they merely serve organizational purposes

# Modeling in Simulink

## Subsystems

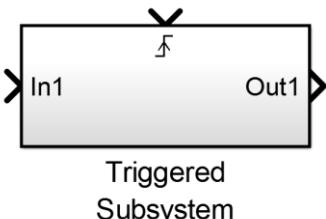
special subsystems:

**enabled subsystem**



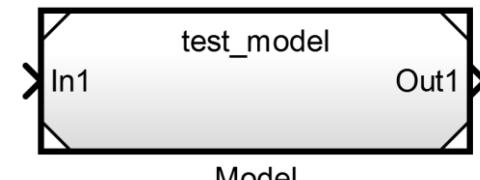
- create from library browser or by adding an *enable* block to an existing subsystem
- only executes when control signal at top is true
- behavior of states within subsystem (i.e. subsystem contains a state-defining block like an integrator) can be configured via block parameters of *enable* block
  - **held**: states are held and continue at last value
  - **reset**: every time the system is enabled, the states assume their initial conditions

**triggered subsystem**



- create from library browser or by adding a *trigger* block to an existing subsystem
- only executes when trigger event occurs, i.e. rising and/or falling edge of the control signal
- triggering event can be configured via block parameters of *trigger* block
- always holds its outputs and states at last value between triggering events

**model reference subsystem**



- create from library browser
- contains reference to a second Simulink model file (here `test_model.slx`)
- inputs and outputs are root-level imports and exports of the referenced system
- double-clicking opens the referenced model
- model reference can be changed by right-clicking -> Block Parameters (ModelReference)
- helps modular design, since models can be quickly interchanged
- for root level **Bus imports / Bus outports** the corresponding **Bus Objects** have to be defined

# Modeling in Simulink

## Subsystems

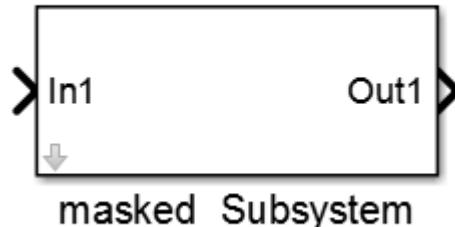
subsystems properties:

linked subsystem



- indicated by **chain symbol** in lower left corner  
*to active display of linked blocks use Menubar -> Display -> Library Links -> All*
- only a **reference** to a block, which is stored within a library file
- link has to be actively broken in order to make changes within the linked subsystem

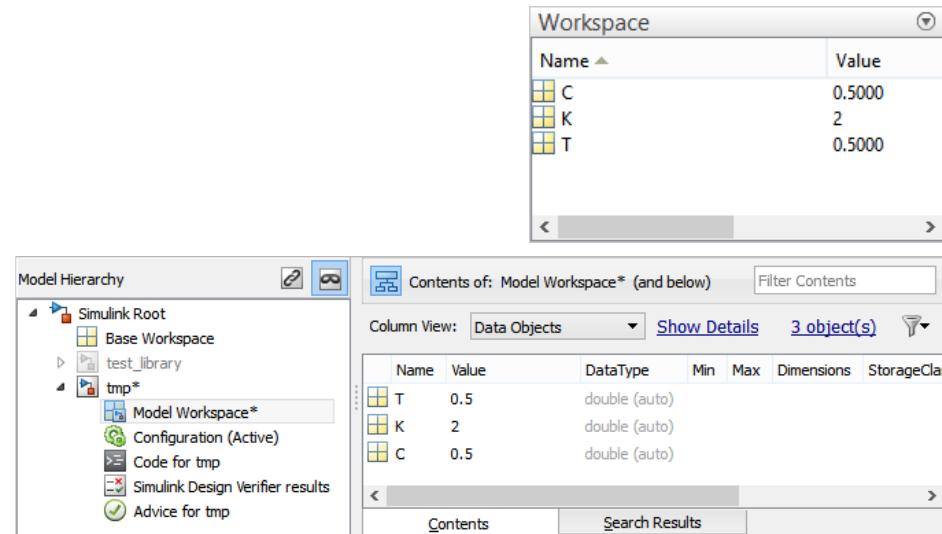
masked subsystem



- implementation details are hidden behind a **mask**
- double-clicking on the subsystems does not open the block parameters dialog, but a user-defined **mask** dialog
- indicated by arrow in lower left corner
- to look under the mask, click on arrow or right click on system and choose *Mask -> Look Under Mask*

# 6. Modeling in Simulink

- the Working Principle of Simulink
- Blocks
- Signals
- Subsystems
- **Parameters**
- Model Configuration Parameters



# Modeling in Simulink

## Parameters

- Block Parameters don't have to be numeric values
- Instead they can be variable names; those variables have to be defined somewhere

### Possibility I: define variables in the base Workspace

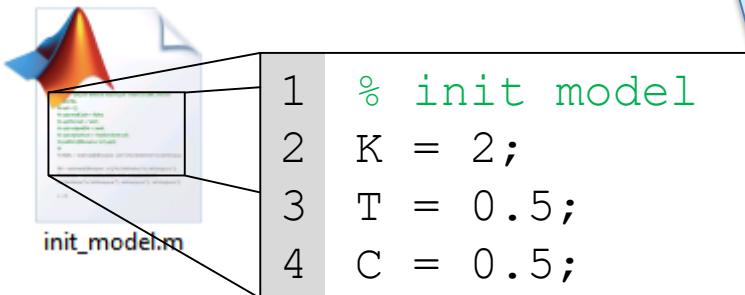
- use command line

```
>> K = 2; T = 0.5; C = 0.5;
```

store data in Matlab  
base Workspace

Name	Value
C	0.5000
K	2
T	0.5000

- or initialization script



store data in Matlab  
base Workspace

#### Pro:

- very flexible, many different Matlab objects can be used (structs, timeseries, matrices, ...)

#### Con:

- every time the model is opened, the variables have to be initialized

# Modeling in Simulink

## Parameters

- Block Parameters don't have to be numeric values
- Instead they can be variable names; those variables have to be defined somewhere

### Possibility II: define variables in the Model Workspace

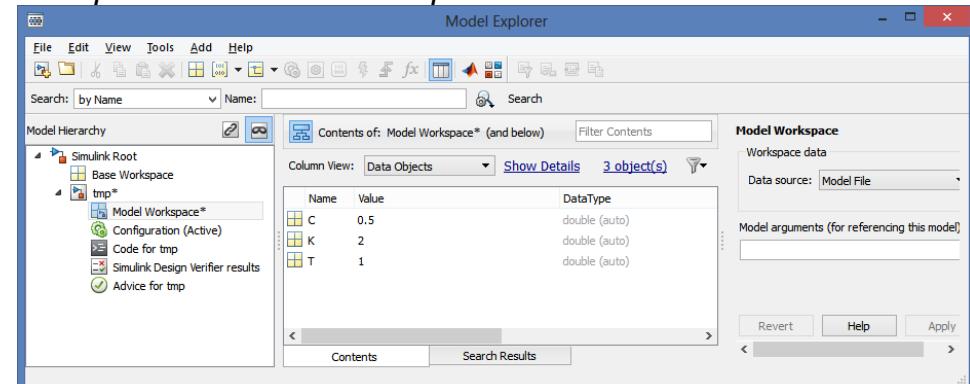
- open base Workspace in Model Explorer via *View -> Model Explorer -> Model Workspace*
- create new variable via *Add -> Matlab Variable*  
Configure name and value
- Alternatively drag&drop existing variables from Base Workspace (higher up in the tree on the left)

#### Pro:

- data is stored directly with model, no external scripts for initialization is necessary

#### Con:

- creating variables in Model Explorer can be tedious
- Advanced data-types (structs, timeseries etc.) are hard to create

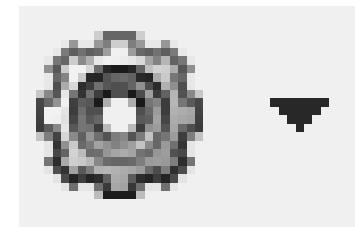
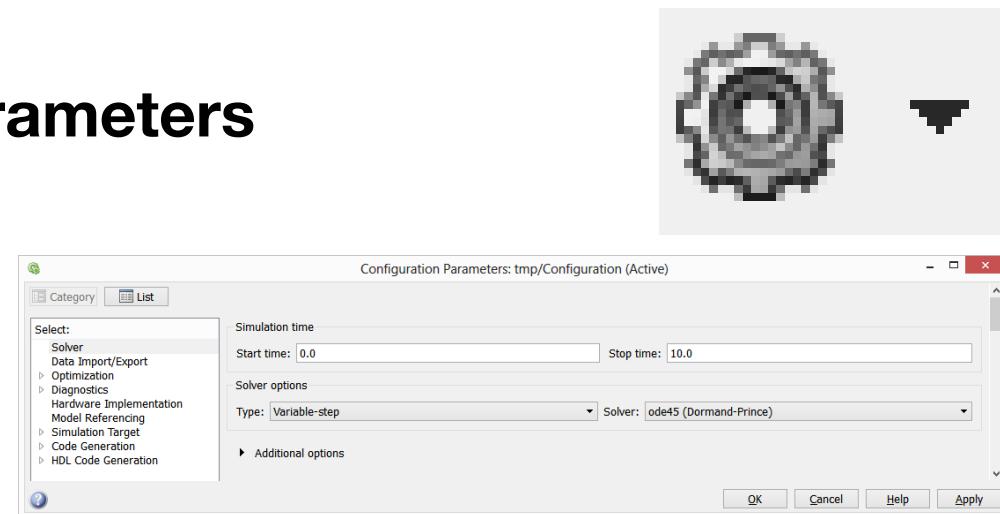


Variables in the **Model Workspace** always are always preferred over Variables in the Base Workspace!

If two variables with the same name exist in Model and Base Workspace, the value of the variable in the Model Workspace will be used during simulation!

# 6. Modeling in Simulink

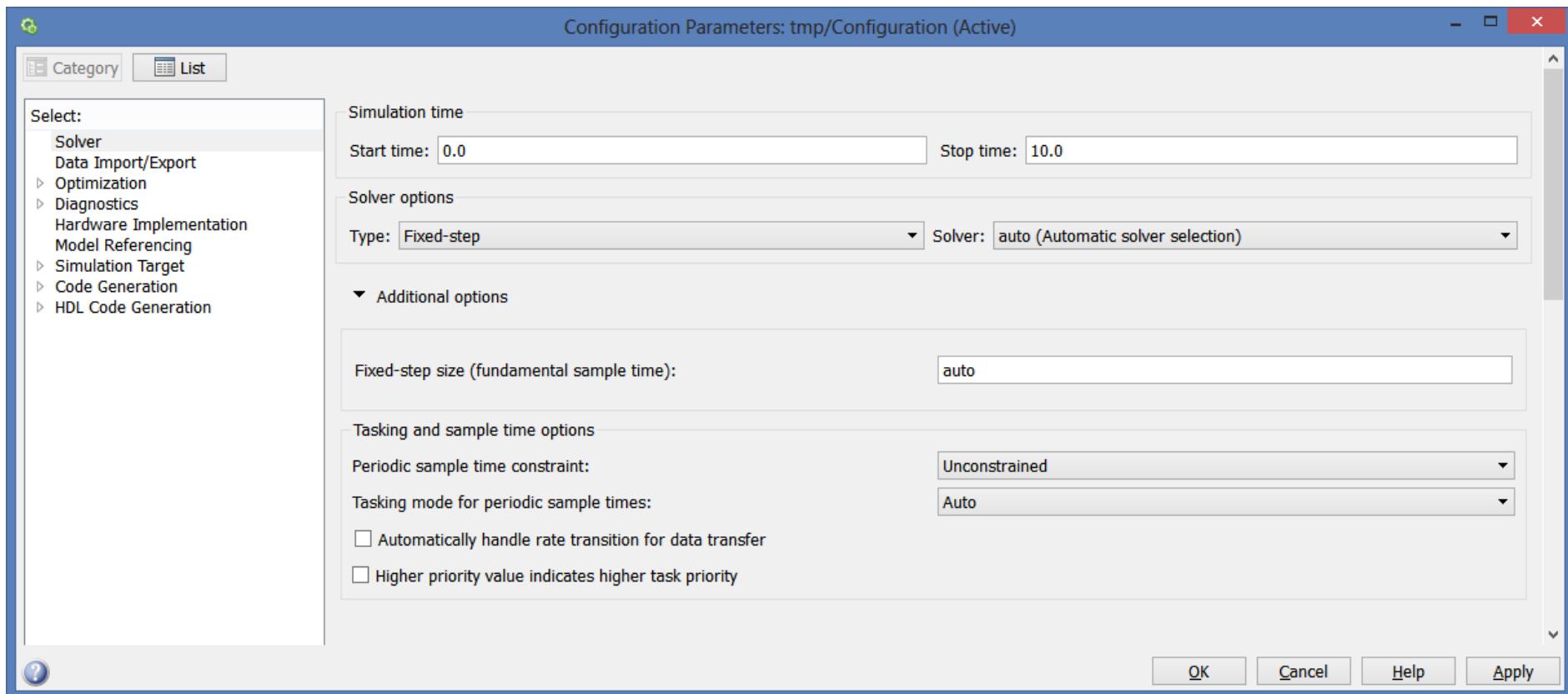
- the Working Principle of Simulink
- Blocks
- Signals
- Subsystems
- Parameters
- **Model Configuration Parameters**



# Modeling in Simulink

## Model Configuration Parameters

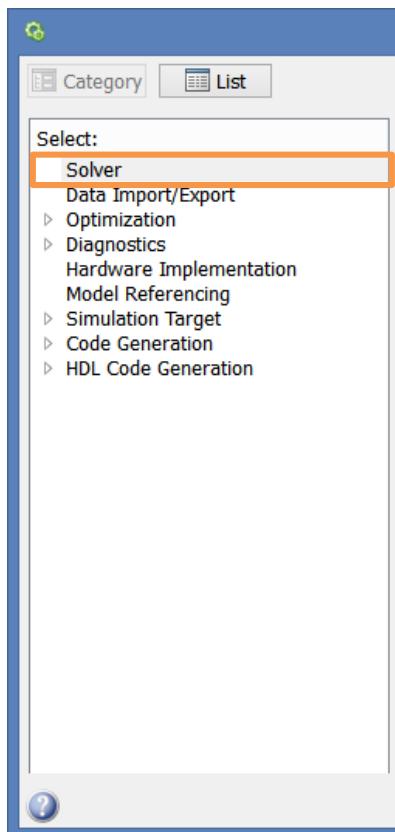
clicking the gear  symbol or choosing *Menu Bar -> Simulation -> Model Configuration Parameters* opens the Configuration Parameters window



# Modeling in Simulink

## Model Configuration Parameters

The **Solver** Pane:



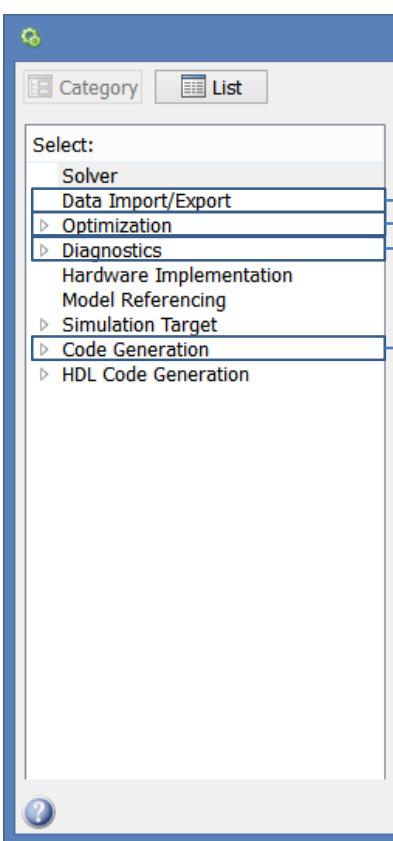
Most important pane in this course:

- choose solver type (variable-step, fixed-step)
- choose solver (ode3, ode4, ode5, ode45, ode23, ...)
- for variable-step solvers
  - set Min / Max step sizes
  - set initial step size
- for fixed-step solvers
  - set fixed step size
- set simulation start / stop time

# Modeling in Simulink

## Model Configuration Parameters

### The other Panes



configure logging of signals (define logging data-type, behavior of root level inputs / outputs, ...)

optimization options for simulation and code generation (focus on faster buils / faster runs,...)

Diagnostic settings; define which event is to be treated as warning, error or ignored;  
*For example: are unconnected signals ignored, is only a warning issued, or is it treated as error*

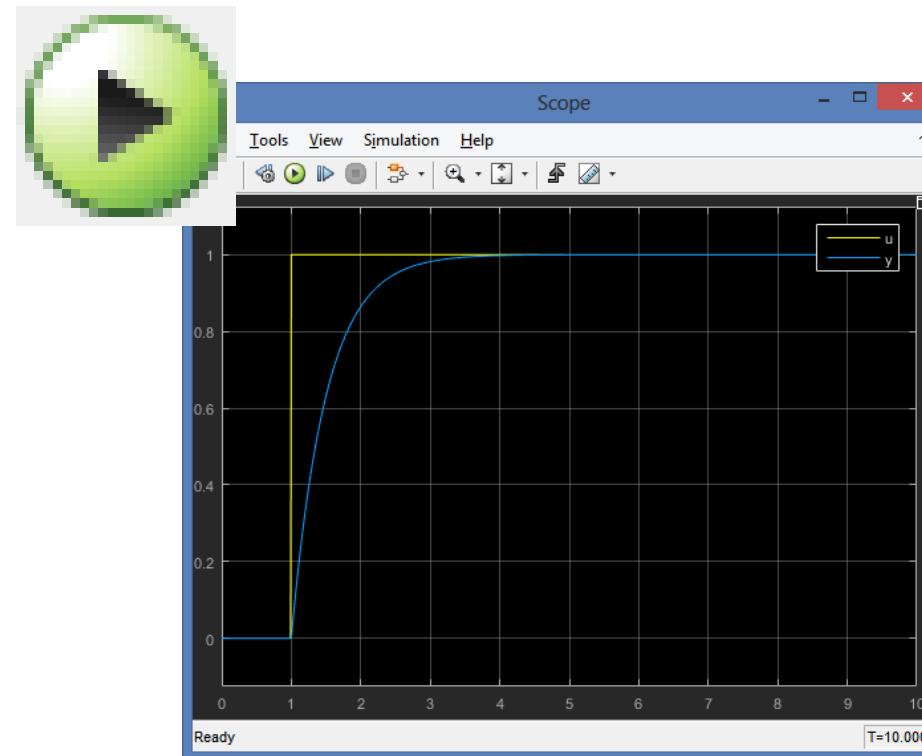
If the model is used for C-Code Generation, this can be configured here (target processor, compiler toolchain, interfaces, custom code inclusion, ...)

# Modeling in Simulink

useful shortcuts:

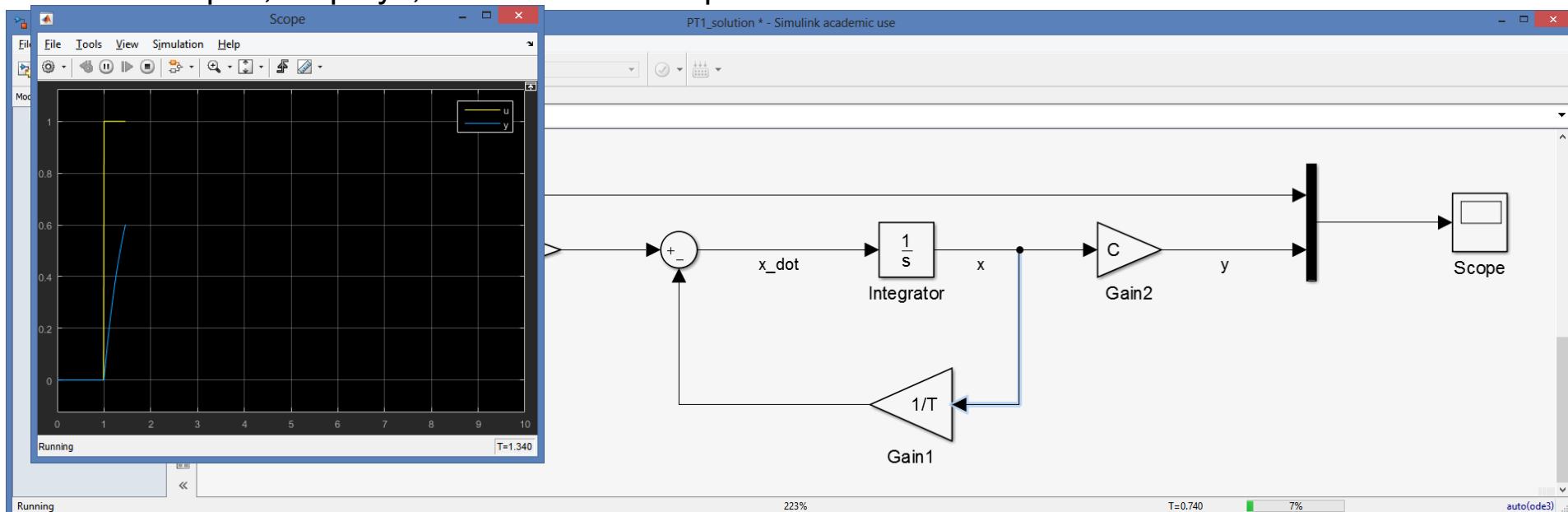
<b>Single click on block / signal</b>	mark block / signal
<b>Click and hold around several elements</b>	mark multiple elements
<b>Shift + single click on block / signal</b>	Add to / remove from selection
<b>Shift + drag marked block</b>	disconnect block from signals; move block only
<b>Drag &amp; drop marked block / signal</b>	move elements around
<b>double-click on subsystem</b>	enter subsystem
<b>Double-click on signal / block name</b>	rename signal / block name
<b>Ctrl + mark second block</b>	quick connect blocks
<b>click and hold right mouse button on signal</b>	branch signal

# 7. Simulation



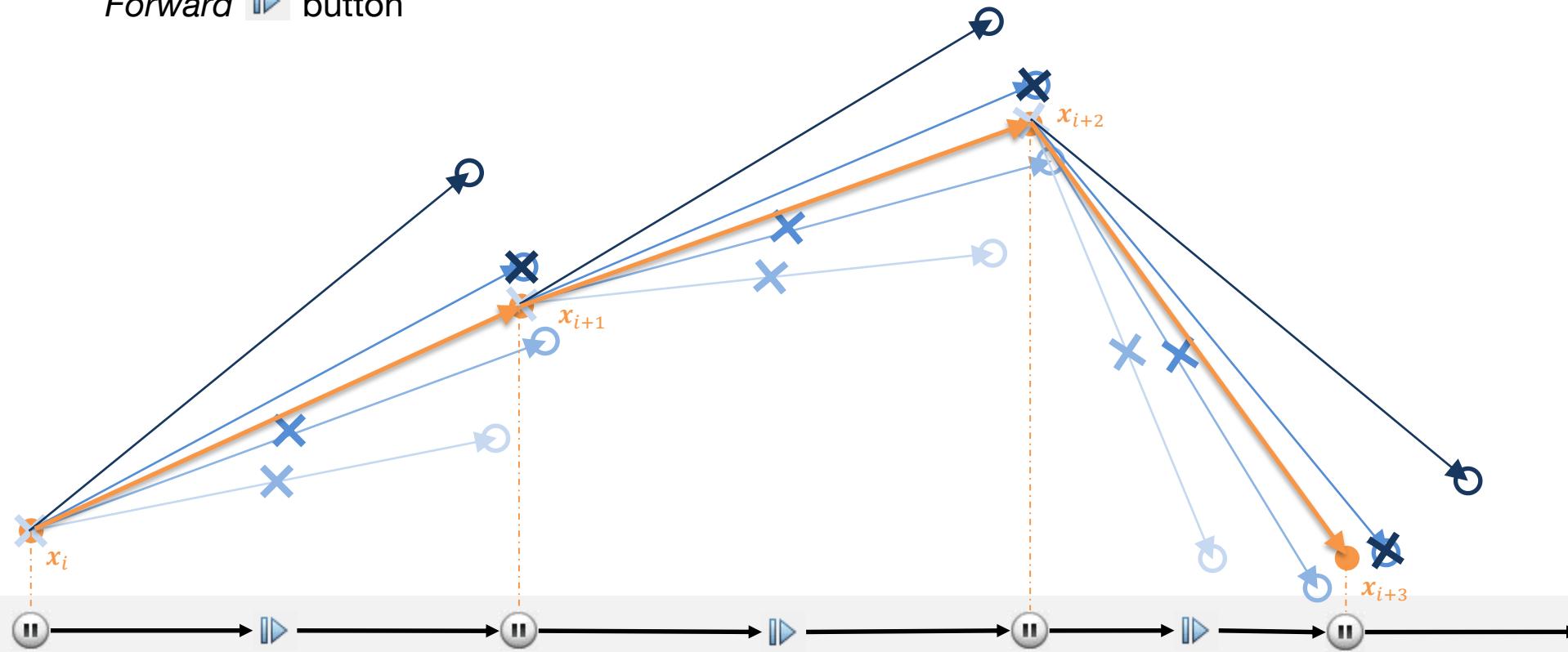
## Simulation

- Once the modeling process is finished, the model can be **simulated**. To start the simulation press the *play*  button, or choose *Menu Bar -> Simulation -> Run*
- The editor will turn gray (no structural model changes are possible during simulation)  
→ some blocks have *tunable* parameters, which can be changed during Simulation (e.g. *Gain*)
- In the notification bar, the message '*Running*' is displayed, along with the current simulation time
- all scopes, displays, value labels are updated online



## Simulation

- Pause the simulation with the *Pause* (II) button, or by setting a *conditional break point* (right-click on signal, set break point and define condition)
- While the simulation is paused, single integration steps can be performed with the *Step Forward* (▶) button



# Simulation

When hitting the *Run* button, the Simulink engine goes through the following phases

**1. Model Compilation:** translate the model to an executable form

- evaluate all block parameters to determine their values (i.e. check if the expressions are valid / the variables exist)
- determine signal attributes (data type, name, dimensionality etc)
- attribute propagation (determine attributes, which are not specified)
- block operations (block reduction, model flattening, ...)
- determine sample times (specified and unspecified)

**2. Link Phase:** link model

- allocate memory (for signals, states, run-time parameters, block data structures)
- create method execution list (block methods to create output)

**3. Simulation Loop Phase:** successively compute states and outputs

- Loop initialization (determine initial states / outputs)
- Loop iteration:
  1. compute outputs
  2. compute states (depending on solver)
  3. check for discontinuities
  4. compute time for next time-step
  5. repeat

Model Compilation can also be initiated by Simulation -> Update Diagram or using Ctrl+D.  
USE THIS FREQUENTLY TO CHECK FOR SYNTACTICAL ERRORS IN YOUR MODEL!!!!

# Simulation

## Algebraic Loops

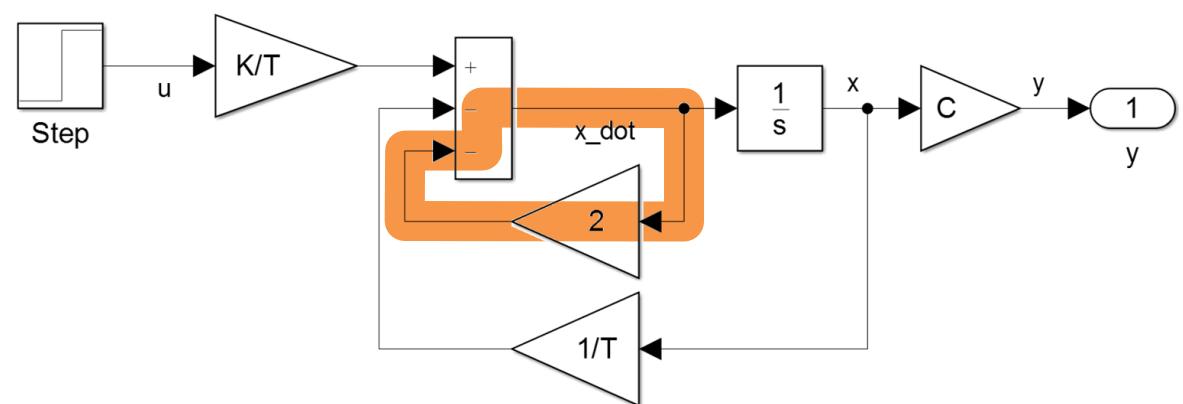
- results if current value of derivative is dependent on derivative itself

$$\begin{aligned}\dot{x}_i &= \tilde{f}_i(x, \dot{x}_i, u) \\ \Leftrightarrow 0 &= f_i(x, \dot{x}_i, u) \quad \text{for some } i\end{aligned}$$

- differential algebraic equation (DAE)
- instead of evaluating  $f(x, u)$  directly, a system of non-linear equations has to be solved to obtain  $\dot{x}_i$  (e.g. for `ode4` this has to be done 4 times!)
- very slow compared to standard ODE
- can be numerically unstable, i.e. no solution is possible
- code generation fails for systems with algebraic loops

Example:

$$\begin{aligned}\dot{x} &= -2\dot{x} - \frac{1}{T}x + \frac{K}{T}u \\ y &= Cx\end{aligned}$$



# Simulation

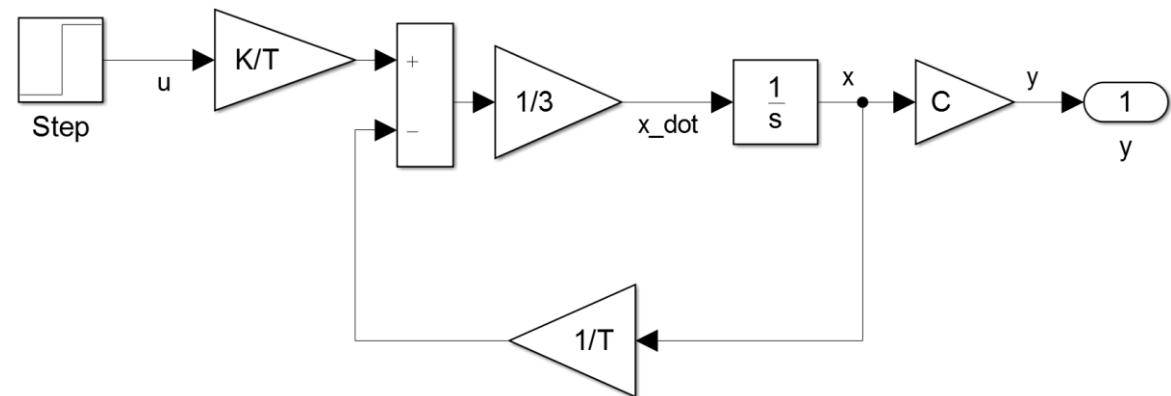
## Algebraic Loops - Remedies

### 1. reformulate system

Example:

$$\dot{x} = \frac{1}{3} \left( -\frac{1}{T}x + \frac{K}{T}u \right)$$

$$y = Cx$$

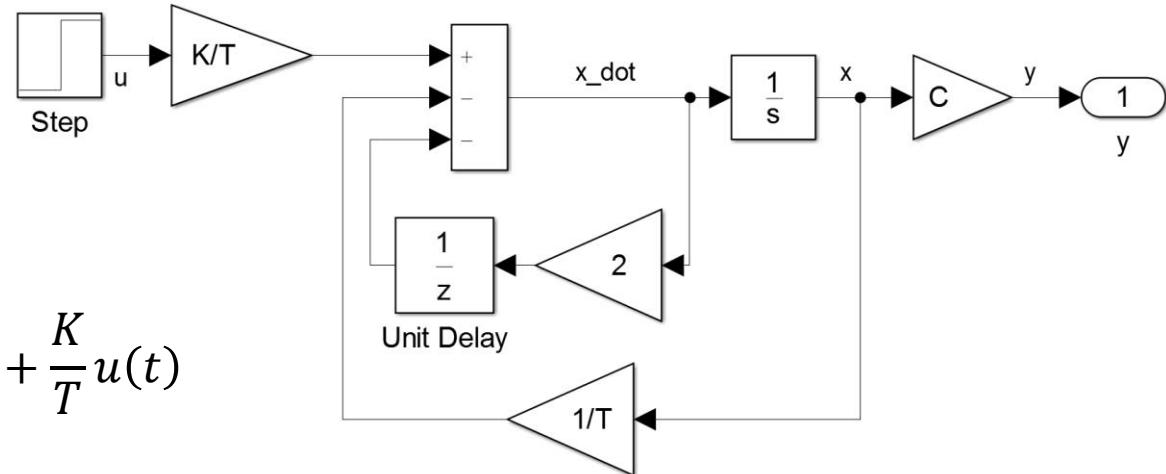


### 2. introduce delay

Example:

$$\dot{x}(t) = -2\dot{x}(t - \Delta t) - \frac{1}{T}x(t) + \frac{K}{T}u(t)$$

$$y(t) = Cx(t)$$



# Simulation

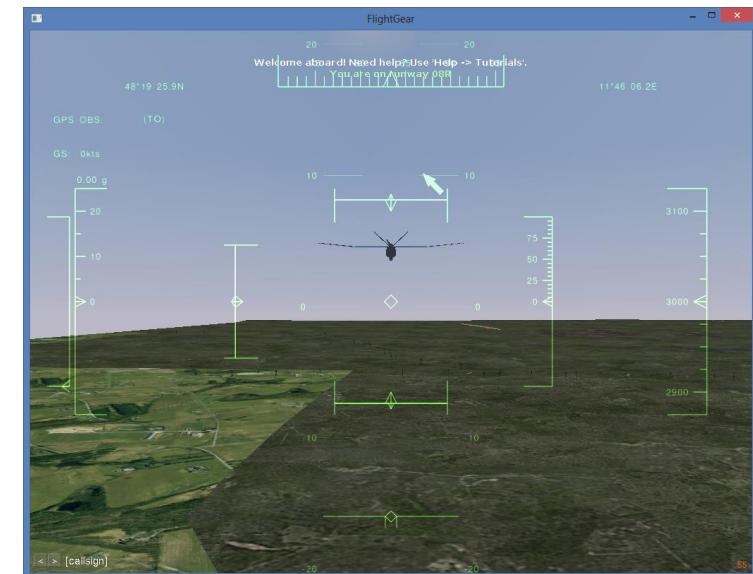
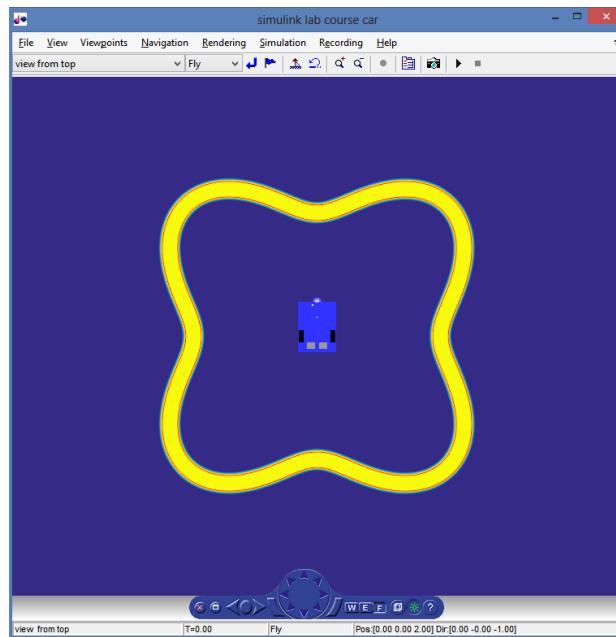
## (pseudo) Real-Time Simulation

Instead of performing a simulation as fast as possible, sometimes it is desirable to see the result in real-time (simulation of real dynamic systems, e.g. line-following robot, flight simulator).

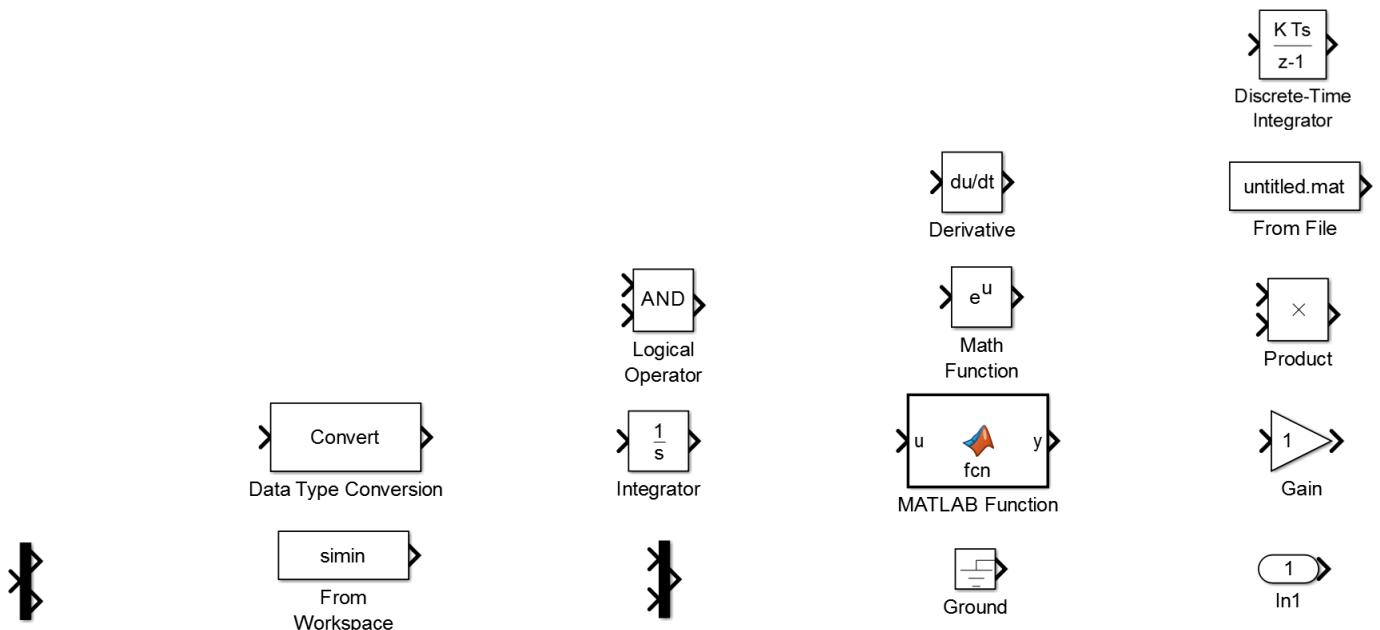
To achieve this, the *Simulation Pace* block can be added anywhere in the model. It slows down the simulation to (pseudo) real-time.



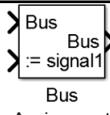
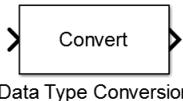
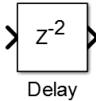
Simulation Pace  
MATLAB Thread  
1 sec/sec



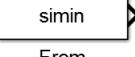
# 8. List of Useful Blocks and Descriptions



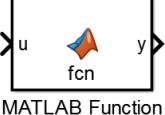
## List of Useful Blocks and Descriptions

 Band-Limited White Noise	<b>Band limited white noise:</b> random number; used to model sensor noise
	<b>Bus Creator:</b> creates signal busses
	<b>Bus Selector:</b> selects signals from busses
 Bus Assignment	<b>Bus Assignment:</b> assigns a new value to one signal in a bus
 Constant	<b>Constant:</b> outputs constant value
 Data Type Conversion	<b>Data Type Conversion:</b> changes data-type of signal
 Delay	<b>Delay:</b> delays signal by one time-step (for discrete time signals only)
	<b>Demux:</b> splits array of signals

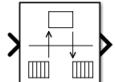
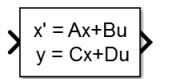
## List of Useful Blocks and Descriptions

	<b>Derivative:</b> approximate derivative of singal; should be avoided, since it can introduce numerical problem!
	<b>Discrete Time Integrator:</b> integrator for controller implementation in discrete time systems
	<b>Display:</b> display value of signal during simulation (scalar, vector, matrix signals)
	<b>From File:</b> load signal from file
	<b>From Workspace:</b> load signal from workspace
	<b>Gain:</b> scales signal with gain value
	<b>Ground:</b> avoid “unconnected input port” warning by using ground block; outputs signal with same data-type as import to which it is connected
	<b>In:</b> input to subsystem / model (on root level)

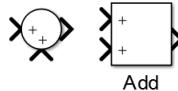
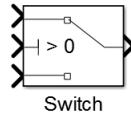
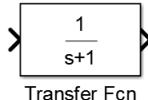
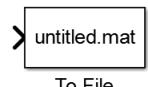
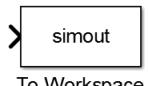
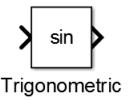
## List of Useful Blocks and Descriptions

 Integrator	<b>Integrator:</b> continuous time integrator for modelling dynamics
 Logical Operator	<b>Logical Operator:</b> perform logical operations on signals
 n-D Lookup Table	<b>n-D Lookup Table:</b> use tabulated data and interpolation algorithms
 Math Function	<b>Math Function:</b> exp(), log, square, pow(), reciprocal, transpose, ...
 MATLAB Function	<b>MATLAB Function:</b> implement custom behavior in MATLAB syntax
	<b>Mux:</b> make array of signals
 Out1	<b>Out:</b> output of subsystem / model (on root level)
	<b>Product:</b> product of signals; can be configured to divide, too.

## List of Useful Blocks and Descriptions

 Rate Transition	<b>Rate Transition:</b> change sample time of signal (up-sampling: zero-order hold; down-sampling: use latest value)
 Relational Operator	<b>Relational Operator:</b> perform relational operations between signals
 Saturation	<b>Saturation:</b> limit signal to defined range
 Scope	<b>Scope:</b> display time-series of data for simulation output
 Signal Builder	<b>Signal Builder:</b> build your own signal patterns via GUI
 Sine Wave	<b>Sine Wave:</b> sine wave input
 Sqrt	<b>Sqrt:</b> compute square root of a signal
 State-Space	<b>State-Space:</b> define linear state space model

## List of Useful Blocks and Descriptions

	<b>Step:</b> step input
	<b>Sum / Add:</b> add signals; can be configured to subtract, too.
	<b>Switch:</b> switch between two signals (of same data type) using a control signal
	<b>Terminator:</b> counterpart of <i>Ground</i> . Use this to terminate unused signals and avoid “unconnected output” warning
	<b>Transfer Fcn:</b> implement transfer function for signal
	<b>To File:</b> write signal data directly to file on harddisc
	<b>To Workspace:</b> write signal data to variable in workspace
	<b>Trigonometric Function:</b> sin, cos, tan, asin, acos, ...

## Further Reading

The following topics might be interesting for further reading (**non**-comprehensive overview):

Topic	Description	Documentation article	Simulink User's Guide
<b>Data-Dictionary</b>	an additional source for simulation parameters, which extends the functionality of base / model workspaces	<b>Simulink Data Dictionary</b>	Chapter 70
<b>Simulation Data Inspector</b>	a tool for quick examination / comparison of logged signals, without having to write plot routines in MATLAB	<b>Inspecting and Comparing Simulation Data</b>	Chapter 30
<b>Model Explorer</b>	manage complete model (configurations, workspaces, signals, etc.)	<b>Exploring, Searching, and Browsing Models</b>	Chapter 13
<b>Masks</b>	creating / working with 'masked' systems; designing your own masks	<b>Working with Block Masks</b>	Chapter 40
<b>Importing / Exporting Data</b>	import / export data for use with MATLAB or other programs	<b>Inspecting and Comparing Simulation Data</b>	Chapter 30
<b>Simulink Debugger</b>	extended Debugging functionalities	<b>Simulink Debugger</b>	Chapter 35

## Excercises

- **Make sure to start Matlab 2019a 64bit!**
- Download the exercise material from moodle
  - Unzip „Templates.zip“ to obtain the templates for the exercises
  - Unzip „Testing\_Students.zip“ to obtain the automatic testing routines for the exercises
  - **Add all folders and subfolders to the Matlab path!**

In order for the automatic checks to work properly:

- whenever naming something (signals, blocks, etc.) make sure to **NOT INCLUDE additional spaces!**
- make sure, that you **DO NOT hit ENTER after entering the name**, this will include a line-break, not confirm your entry!
- When entering variables (Gains, Integrators etc), **do NOT INCLUDE additional spaces and stick to the order** in the booklet!
- Make sure that when naming a signal, you really name the signal, and don't add an annotation by double-clicking next to the signal-line.
- The automatic model checks only work on PCs, i.e. if you work with your own Mac, you will most likely encounter errors.