

Name:

ID (Personal Code):

Please answer **thoughtfully, pertinently** and **briefly**.

Q1. [9] We want to encode a speech signal using Linear Predictive Coding (LPC).

- a) Describe the main core idea of LPC and how you can implement LPC solution as a Wiener filter. To do so, provide the data model, draw the block diagram, and briefly explain the overall idea.
(Suggestion: call $\hat{s}(n)$ the estimated signal)
- b) What is the whitening filter?
- c) Provide the definition of the objective function to be minimized.
- d) Define the Prediction Gain of LPC and comments its behavior.
- e) Using Linear Predictive Coding, we want to estimate the coefficients of an auto regressive model of order 2 that approximates the audio signal $s(n)$ as

$$s(n) = \sum_{k=1}^2 a_k s(n-k) + u(n)$$

The estimated values of the auto-correlation function of the signal $s(n)$ are $r(0)=0.5$, $r(1)=0.2$, $r(2)=0.1$. Estimate the optimum (in the MSE sense) coefficient set a_k .

- f) Comment on the results obtained in the previous point.

Q2. [4] Consider the problem of implementing audio effects using delay lines.

- a) Define what is a delay line, clearly explaining the relation between the input and the output.
- b) Explain the main differences among: i) an integer delay line; ii) a fractional delay line; iii) a time-variant fractional delay line.
- c) Which one (or ones) may need the use of an interpolator? Why?
- d) Report the main effect of linear interpolation on a delayed signal.

Q3. [3] Consider the problem of time and pitch scaling.

- a) Describe in your own words what does it mean to apply time scaling to an audio signal.
- b) Describe in your own words what does it mean to apply pitch scaling to an audio signal.
- c) Explain what the duality principle is in the time/pitch scaling context.

Q4. [7] Each answer can be either TRUE or FALSE. Incorrect answers give you -1 points, unanswered 0 points, correct answers +1 point. Provide a brief optional comment when in doubt.

- a) [T] [F] Consider a system implementing audio filtering through overlap and add (OLA). It is possible to use triangular windows still honouring the constant overlap and add (COLA) condition.
- b) [T] [F] In order to apply reverberation to an audio recording, a room impulse response (RIR) is always necessary.
- c) [T] [F] Two tones with different frequency and the same Sound Pressure Level (SPL) provide the same impression of loudness.
- d) [T] [F] A median filter of 5 samples can be used to recover up to 3 corrupted samples in a row.
- e) [T] [F] The just noticeable difference (JND) describes the ability of distinguishing different tones played together.
- f) [T] [F] Consider the problem of resolving sinusoidal peaks in the frequency domain. Given a window with factor $L=2$ and two peaks at 100 and 300 Hz, we need at least 160 window samples if we work at 8 kHz.
- g) [T] [F] In a perfectly anechoic environment (i.e., without reverberation), it is not possible to measure a room impulse response (RIR).

Q5. MATLAB [8]

Implement the following steps.

Define some signals:

- a) [1] Consider a sampling frequency of 8 kHz, generate a 2-second-long cosine function with frequency 250 Hz and amplitude equal to 1. This is your signal y_1 .
- b) [1] Generate the signal y_2 as a 1-second-long sine function with frequency 100 Hz and amplitude equal to 2. This is your signal y_2 .
- c) [0.5] Obtain the signal y as the sum of y_1 and y_2 taking care of the length difference.
- d) [1] Plot y in the time domain correctly expressing the time axis in seconds.

Do some processing:

- e) [0.5] Define a Hann window w of 200 ms.
- f) [0.5] Apply the window w to the signal y to extract the first 200 ms of it.
- g) [1] Compute the zero-crossing rate (ZCR) of the windowed signal.
- h) [1] Filter the windowed signal using the filter $h = [-0.5, 0, 0.5]$ directly in the time domain.
- i) [1.5] Plot the magnitude and phase of the Discrete Fourier Transform of the filtered signal correctly expressing the frequency axis in Hz.