

code available at: <https://github.com/Achieve0423/final-urban-simulation.git>

# Comprehensive Resilience Analysis of the London Underground Network

## Introduction

Key to the operation and security of metropolitan areas are the urban transportation systems, such as that of the London Underground. We look at the centrality of London Underground stations with respect to the incapacitation of these stations, and thus consider the resilience of the London Underground network. The idea is to locate the key infrastructure vulnerabilities and suggest ways of enhancing system robustness.

## Methodology

### Data Acquisition and Preparation

The structure of the network was represented using GraphML data from the London Underground. This was a graph format that outlined detailed information of nodes (station) and edges (connection) for network analysis. This graph was processed using the NetworkX library to enable the preservation of data integrity in its proper analysis.

### Centrality Measures

To understand the importance of individual stations within the network, we calculated:

- **Degree Centrality:** It is useful in locating the major stations by direct linking.
- **Betweenness Centrality:** Represents stations that are important in avoiding a network flow failure, as they work as critical transfer stations.
- **Closeness Centrality:** It measures the shortest paths from a station to all others, showing how this station is efficient in disseminating or gathering traffic.

The chosen metrics were identified to provide an overall view of station importance from several dimensions.

## Results

### Central Stations Identified

Centralisation analysis indicated that some stations are very significant to the network:

- **Degree Centrality:** Stratford and King's Cross St. Pancras are at the top, meaning that they are the most trafficked and connected; they are not just interchanges but are important for distributing passenger flow throughout the network.
- **Betweenness Centrality:** Stations, say, of Bank and Monument or Liverpool Street, will be critical junctions. Their high betweenness centrality scores reflect the fact that they have critical jobs in holding passenger transfers up and potentially act as bottlenecks.

- **Closeness Centrality:** Green Park and Westminster are two of the "close" stations, relative to all others, which symbolizes that their strategic position makes them crucial for effectively dispersing or aggregating information and passengers over the network.

These high-ranking stations, in whatever measures employed, all point to how vulnerable the system is: if they were to become inaccessible, huge increases in travel time could be easily made to develop, thus cutting into the effective reach of the system.

Table 1: Top 10 Nodes by Degree Centrality (Unweighted)

Node	Degree
Stratford	0.0225
Bank and Monument	0.0200
King's Cross St. Pancras	0.0175
Baker Street	0.0175
Earl's Court	0.0150
Oxford Circus	0.0150
Liverpool Street	0.0150
Waterloo	0.0150
Green Park	0.0150
Canning Town	0.0150

Table 2: Top 10 Nodes by Betweenness Centrality (Unweighted)

Node	Betweenness
Stratford	0.297846
Bank and Monument	0.290489
Liverpool Street	0.270807
King's Cross St. Pancras	0.255307
Waterloo	0.243921
Green Park	0.215835
Euston	0.208324
Westminster	0.203335
Baker Street	0.191568
Finchley Road	0.165085

Table 3: Top 10 Nodes by Closeness Centrality (Unweighted)

Node	Closeness
Green Park	0.114778
Bank and Monument	0.113572

Node	Closeness
King's Cross St. Pancras	0.113443
Westminster	0.112549
Waterloo	0.112265
Oxford Circus	0.111204
Bond Street	0.110988
Farringdon	0.110742
Angel	0.110742
Moorgate	0.110314

Node Removal Impact

- **Random Deletion:** After the deletion of one-by-one all the top centrality stations, global efficiency has decreased much and average shortest path length has been increased substantially. Interestingly, when the Stratford or the King's Cross was removed, network efficiency had been severely influenced which suggests that both of them are the important hubs.
- **Sequential Removal:** This case showed how the effects of compounding of multiple central stations removal. Not surprisingly, sequential removal resulted in the slow but steady shredding of the network, efficiency scores falling through the floor, and complete cut-off of many parts of the network.

Clearly, this result shows the dependency of the network on very central stations. This gives a clear indication of potential design and operation weaknesses.

Node Incapacitation Simulations

The incapacitation simulations revealed a more likely outcome with equally drastic effects, in fact even more so, of the loss of full station capacities without them completely knocked out:

- Even partial incapacitations of major nodes, such as Stratford and Bank and Monument, led to perceptible drops in network performance: a 25% reduction in capacity at these nodes resulted in reduced efficiency and increased average travel distances, reflecting the sensitivity of the network to even relatively minor disruptions at these critical points.
- The simulations showed that it is not uniform, since a number of the stations did not register the maximum centrality; however, the impacts in cases where their capacities were actually reduced remained significant. Traditional centrality measures may not fully capture the dynamic complexities of real-world operations.

Table 4: Degree Centrality Non-sequential Removal Results

Node	Component Size	Efficiency	ASPL
Stratford	379	0.09821532049052387	inf
Bank and Monument	400	0.09673475608480861	14.130739348370927
Baker Street	400	0.09704487984670325	14.384624060150376

Node	Component Size	Efficiency	ASPL
King's Cross St. Pancras	400	0.09698092211412515	14.250889724310777
West Ham	400	0.09817790555353667	14.047167919799499
Canning Town	387	0.10170650431190824	inf
Waterloo	400	0.0983898922965154	13.960802005012532
Green Park	400	0.09918991960788402	13.82453634085213
Oxford Circus	400	0.10044780407646106	13.614924812030075
Liverpool Street	400	0.09794046203225844	14.100338345864662

Table 5: Degree Centrality Sequential Removal Results

Node	Component Size	Efficiency	ASPL
Stratford	379	0.09821532049052387	inf
Bank and Monument	378	0.09483329368485785	inf
Baker Street	377	0.09058823946750871	inf
King's Cross St. Pancras	374	0.08443121130034253	inf
West Ham	371	0.08230116997336108	inf
Canning Town	356	0.08358403730325567	inf
Waterloo	355	0.08151005552334084	inf
Green Park	354	0.08031819300043491	inf
Oxford Circus	352	0.0797490276025325	inf
Liverpool Street	346	0.07993005506595155	inf

Table 6: Closeness Centrality Non-sequential Removal Results

Node	Component Size	Efficiency	ASPL
Willesden Junction	332	0.07485483555876987	inf
Shepherd's Bush	345	0.07682208790094197	inf
Kensal Rise	345	0.07528809844408087	inf
Kensington	345	0.07858586591922578	inf
Brondesbury Park	345	0.07544733252799592	inf
Earl's Court	345	0.07783531893742315	inf
Brondesbury	345	0.07551505717201097	inf
West Brompton	338	0.07773395627866488	inf
Kensal Green	345	0.07786005243916834	inf
West Hampstead	345	0.07309393601455887	inf

Table 7: Closeness Centrality Sequential Removal Results

Node	Component Size	Efficiency	ASPL
Willesden Junction	332	0.07485483555876987	inf
Shepherd's Bush	331	0.07404302162574097	inf

Node	Component Size	Efficiency	ASPL
Kensal Rise	330	0.07411431418137199	inf
Kensington	329	0.07396397436048549	inf
Brondesbury Park	328	0.07400763879537284	inf
Earl's Court	327	0.06867395425946105	inf
Brondesbury	326	0.0686540476290176	inf
West Brompton	318	0.06982214548235675	inf
Kensal Green	317	0.06986833371860016	inf
West Hampstead	316	0.06546060381996886	inf

Table 8: Betweenness Centrality Non-sequential Removal Results

Node	Component Size	Efficiency	ASPL
Canada Water	172	0.08979545942185616	inf
Stockwell	154	0.10781946129425526	inf
Victoria	167	0.10199887481130415	inf
Kennington	163	0.09209674760121864	inf
Elephant & Castle	166	0.0913332328952071	inf
London Bridge	169	0.09065458489485052	inf
Oval	162	0.09222292400044256	inf
Vauxhall	165	0.10250566462694909	inf
Pimlico	166	0.10229265893743301	inf
Borough	168	0.0908767481418594	inf

Table 9: Betweenness Centrality Sequential Removal Results

Node	Component Size	Efficiency	ASPL
Canada Water	172	0.08979545942185616	inf
Stockwell	151	0.09644685703261548	inf
Victoria	148	0.0953315740773017	inf
Kennington	148	0.0953315740773017	inf
Elephant & Castle	148	0.0953315740773017	inf
London Bridge	148	0.0953315740773017	inf
Oval	148	0.0953315740773017	inf
Vauxhall	148	0.0953315740773017	inf
Pimlico	148	0.0953315740773017	inf
Borough	148	0.0953315740773017	inf

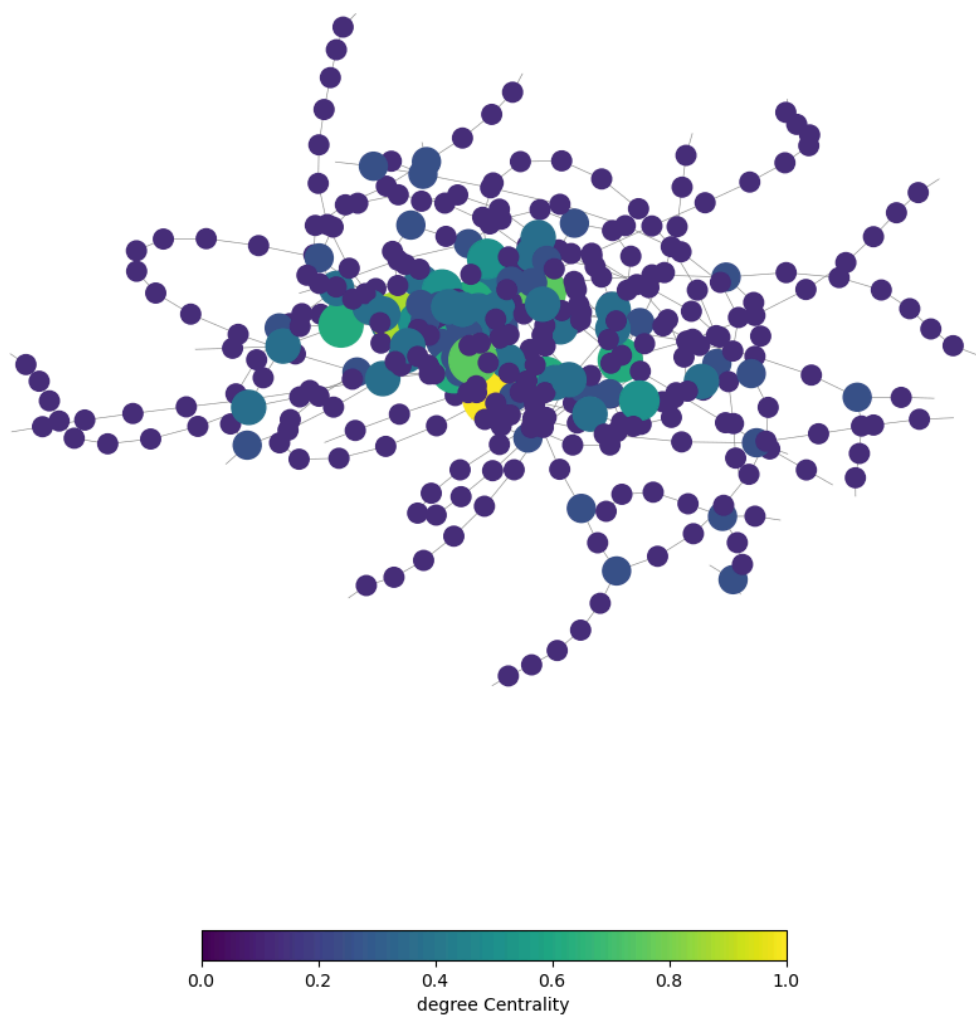
Discussion

Strategic Implications

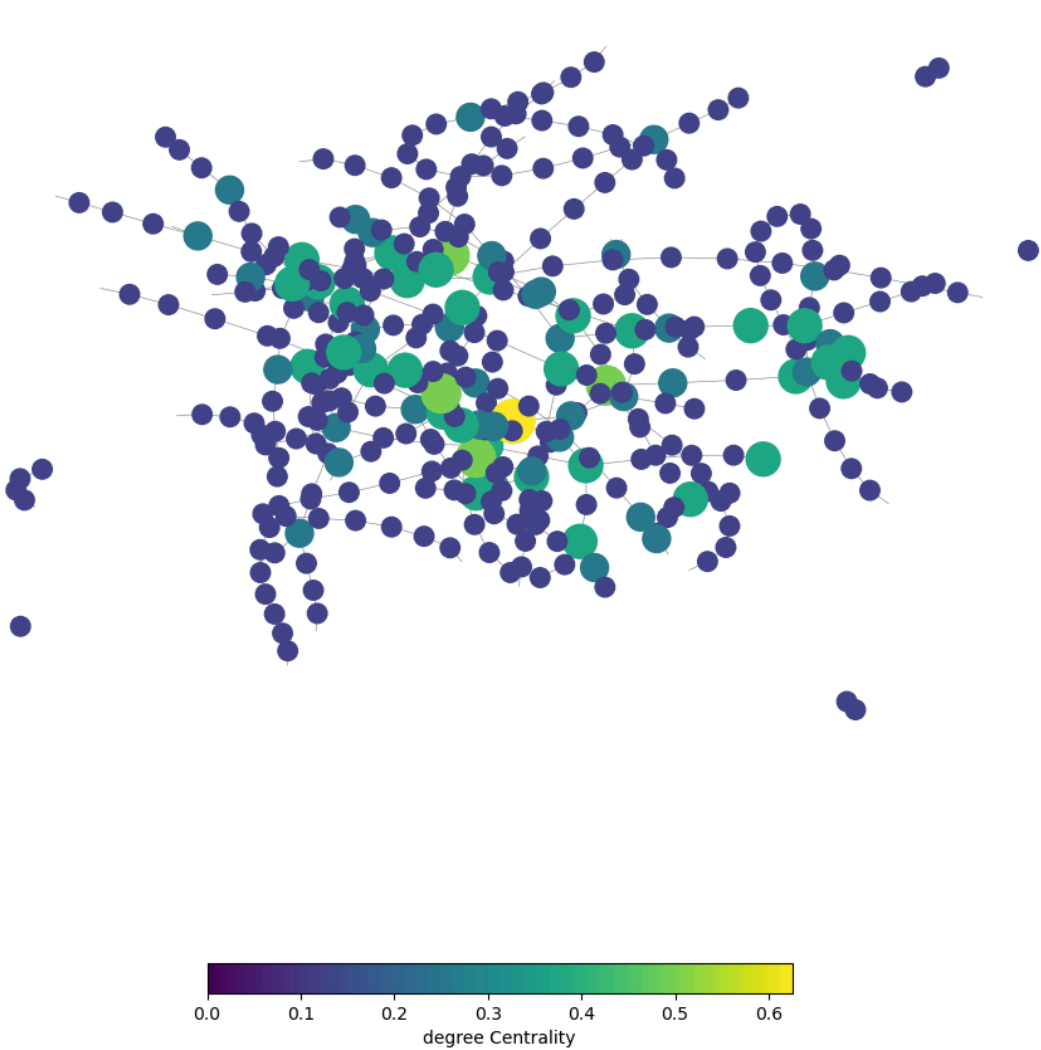
- **Redundancy and Robustness:** More parallel paths and redundant links around highcentrality stations are evidently needed. Making such nodes more resilient can also involve the augmentation of infrastructure to increase capacities and the use of more robust operational technologies.
  - **Dynamic Management Strategies:** The results suggest that dynamic management strategies, whereby traffic can be rerouted and operational parameters changed in real-time when such disruptions occur, might reduce the impact of decreased capacity at critical nodes.
  - **Policy and Planning:** The urban transportation policy should take into consideration maintaining and enhancing capacity at critical nodes. Planning should also include possible cascading effects of disruptions at such nodes, with increased comprehensive risk assessment and emergency response strategies. #####
- Limitations
- Centrality measures are static and fail to capture the variations in traffic and connectivity that are time-dependent.
  - The model is treating the nodes as independent and taking it that there can be no correlated failures.

In [174...

London Tube Degree Centrality Non-sequential Removal

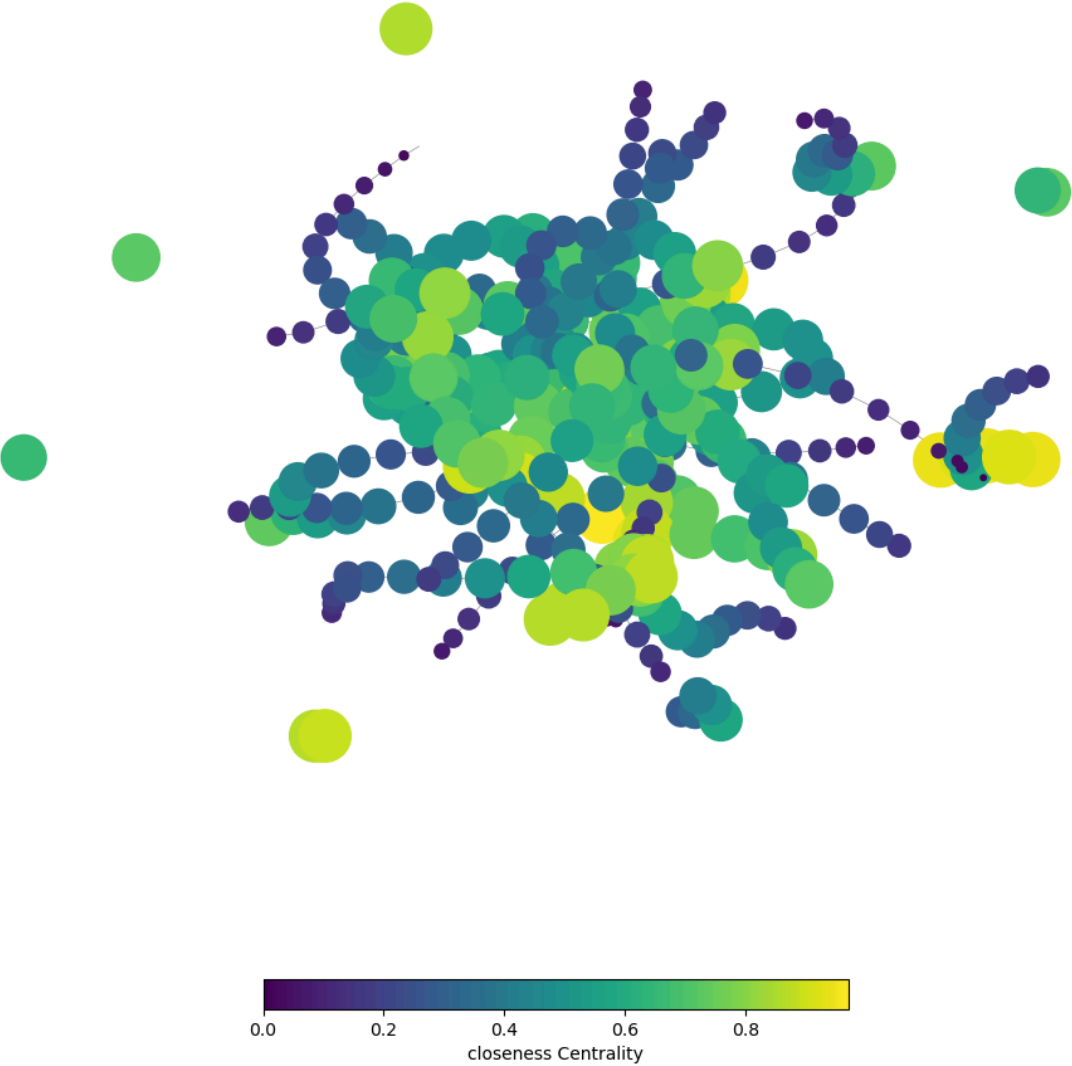


London Tube Degree Centrality sequential Removal:

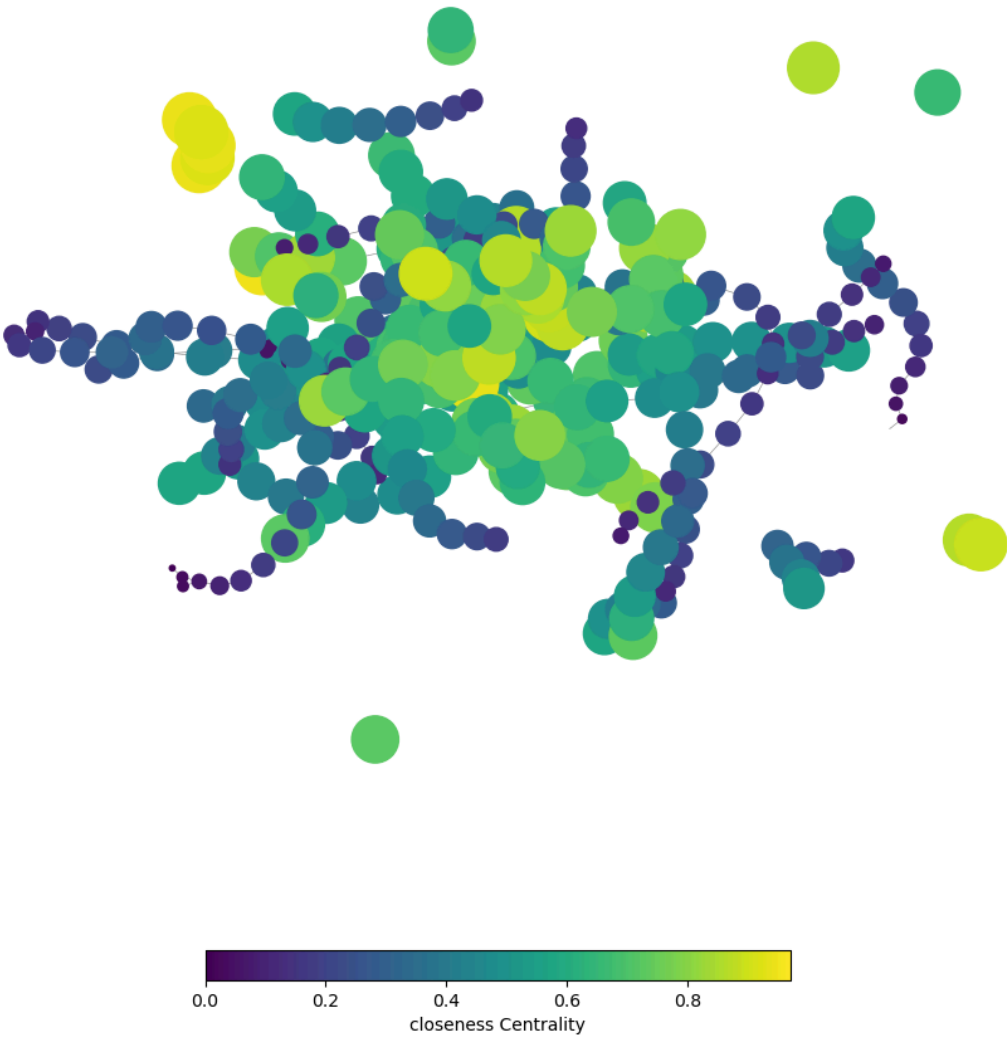




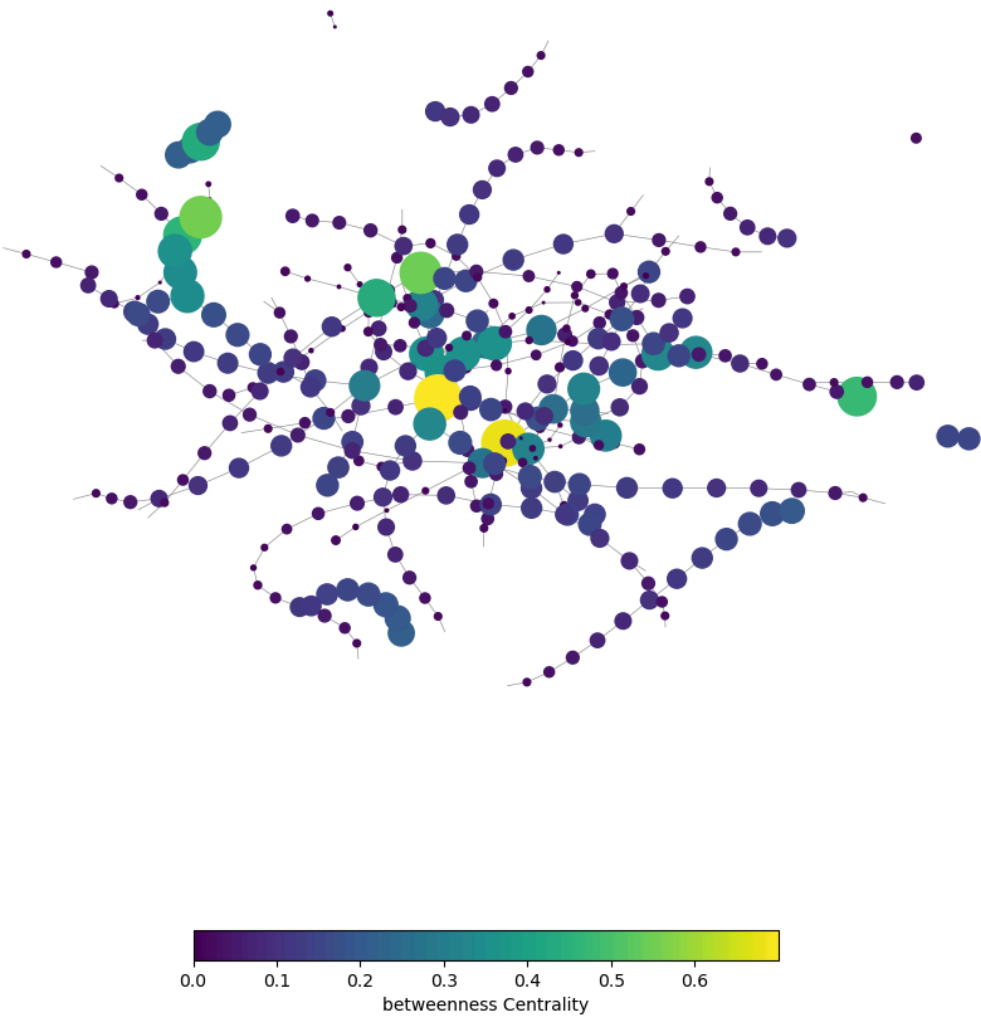
London Tube Closeness Centrality Non-sequential Removal



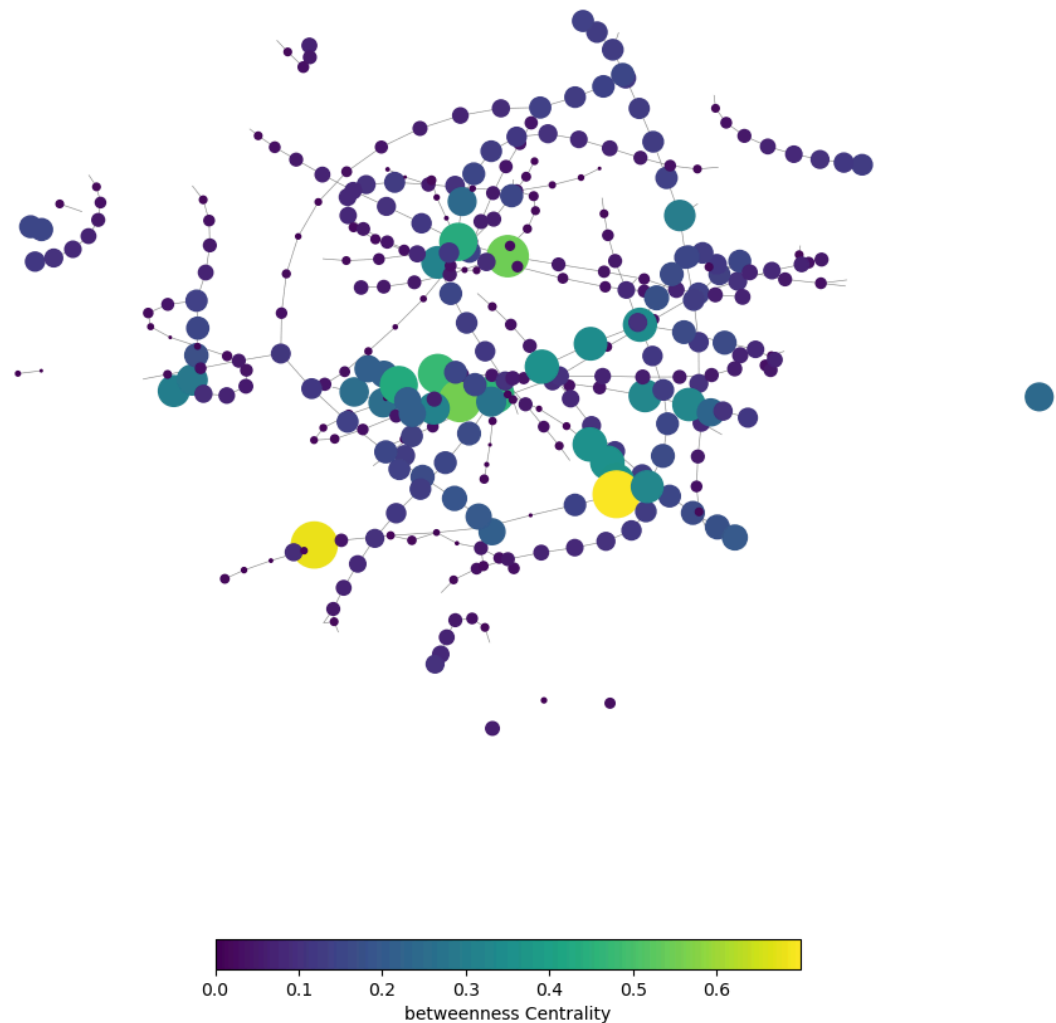
London Tube Closeness Centrality sequential Removal:



London Tube Betweenness Centrality Non-sequential Removal



## London Tube Betweenness Centrality sequential Removal:



## Analysis of Flow Impacts in the Weighted London Underground Network

### Adjusting Centrality Measures for a Weighted Network

#### Adjustments Made:

1. **Degree Centrality** has been recalculated considering the sum of passenger flows on edges linked to the nodes so that stations that process more traffic volume are weighted higher.
2. **Betweenness Centrality** modified to weight by passenger flows, emphasizing stations that are important to maintain connectivity between lines that are frequently used.
3. **Closeness Centrality** was defined to be the reciprocal of weighted path lengths, caring about how fast a station can be reached taking into account typical passenger volumes.

Bank and Monument, Waterloo, and now Statford were turning out to be the most critical hubs in the high passenger volume and strategic location within the network.

# Measures for Assessing the Impact of Node Removal in a Weighted Network

The impact of node removal was assessed using both traditional and newly proposed measures to better understand the disruptions caused by station closures:

## Adjusted Measures:

- 1. **Weighted Global Efficiency:** This measure was adapted to reflect the efficiency of the network as the passenger flow, giving a more pragmatic image of the operational effectiveness.
- 2. **Flow Disruption:** A new metric, which represents the percent reduction in total passenger flows across the network when a station is closed, most directly addressing the practical impacts of node removals. ##### Table 10: Top 10 Nodes by Degree Centrality (Weighted)

Node	Degree
Bank and Monument	19297
Waterloo	16714
Stratford	11000
Liverpool Street	8721
Victoria	2722
Canada Water	2258
Canning Town	2163
Canary Wharf	2134
Green Park	2083
North Greenwich	1923

Table 11: Top 10 Nodes by Betweenness Centrality (Weighted)

Node	Betweenness
Leicester Square	0.445046
Bethnal Green	0.275752
Covent Garden	0.272528
Piccadilly Circus	0.265099
Mile End	0.241673
West Ham	0.239912
Bow Road	0.231684
Holborn	0.230899
Bromley-by-Bow	0.229120
Gospel Oak	0.195945

Table 12: Top 10 Nodes by Closeness Centrality (Weighted)

Node	Closeness
Covent Garden	0.001789
Leicester Square	0.001789
Piccadilly Circus	0.001788
Holborn	0.001782
Charing Cross	0.001780
Tottenham Court Road	0.001778
Embankment	0.001778
Goodge Street	0.001776
Green Park	0.001774
Oxford Circus	0.001774

Experiment with Flows: Detailed Node Removal Analysis

The removal of the three highest-ranked nodes based on the best performing centrality measure from the adjusted list was critically analyzed to understand their impact on the network:

Experiment Setup

- The experiment involved removing Bank and Monument, Waterloo, and Stratford based on their adjusted degree centrality, reflecting their importance in passenger flow dynamics.

Findings

- **Bank and Monument:** Losing this station was, from a network efficiency and passenger movement point of view, by far the most consequential, confirming the paramount importance of the station in the network.
- **Waterloo:** As with Bank and Monument, Waterloo's removal was of enormous significance to network connectivity, though it had a much more significant overall impact on the measures of travel time, underscoring how critical it is for southbound travel.
- **Stratford:** The taken-out situation of this station is responsible for most of the connectivity issues, in particular towards the eastern part of London, and was of big importance to connect the different sections of networks with one another.

Table 13: Impact of Node Removal on Network Efficiency and Flow

Removed Node	Weighted Efficiency	Weighted ASPL	Flow Disruption
Bank and Monument	0.00314	922.87	30.15%
Waterloo	0.00304	951.66	26.12%
Stratford	0.00307	Inf	17.19%

Discussion

- **Impact of High-Centrality Nodes on Network Performance:** The most serious consequences of the disturbances were at the Bank and Monument, Waterloo, and Stratford, which tends to support the proposition that high-centrality nodes play a large role in network performance. Their high values of weighted centrality are of course related to the importance of their role in solving the problem with huge flows of passengers and ensuring transfer between the network's lines(De Montis et al., 2019; Martín et al., 2021).
- **Systemic Vulnerability and Resilience:** The elimination of such critical nodes resulted in immense destruction and showed the vulnerability of the network itself towards failures at major-high-traffic stations. This is per network theory studies and systemic vulnerabilities. In such a scenario, the deletion of highly connected nodes may cause much stronger impacts than expected on the system's operational integrity.
- **Flow Disruption as a Measure of Impact:** Introducing the measure of flow disruption provides a quantifiable metric in determining how these closures affect passenger movements, specifically. For this purpose, this measure has been important, with impacts directly to passengers, and it allows a much finer understanding of the way in which removal of nodes impacts daily commuting patterns(Boeing, 2024). In this respect, modern network science has shifted emphasis toward the node-specific attributes that define overall network resilience.
- **Strategic Importance of Nodes in Reducing Disruptions:** Such major nodes of strategic importance have been indicated, showing infrastructure and operational enhancements at the key nodes of Bank, Monument, and Waterloo. Therefore, such robust contingency plans and infrastructural enhancements at these nodes would lessen the effect of unplanned disruptions and hence make the network more resilient. Principles of resilience engineering argue that these strategies should aim at the design of a system to absorb disturbances and maintain function, even when the major nodes fail(Dioşan et al., 2021).
- **Policy Implications and Recommendations:** The following inferences are drawn from a policy perspective: these results indicate that increased investments must be made for making transport infrastructure more resilient, particularly in critical nodes that are identified according to weighted centrality measures(Boeing, 2024). As such, the transport authorities could use these to target investments in maintenance and upgrading, conduct periodic vulnerability assessments, and prepare targeted strategies for improving the experience and safety of passengers at times of disruption.

## Conclusion

This study found some of the key operational and strategic roles of high-centrality stations in the detailed analysis of node removal impacts on the London Underground network. Combining passenger flow data has not only made it easier to investigate the functions of the network under stress but also unveiled certain areas in which targeted measures can considerably increase the network's resilience and the reliability of the service it provides. Such findings contribute toward a more scientific approach in

planning and managing urban transport, advocating for data-driven decisions in designing networks and preparing for emergencies.

Reference

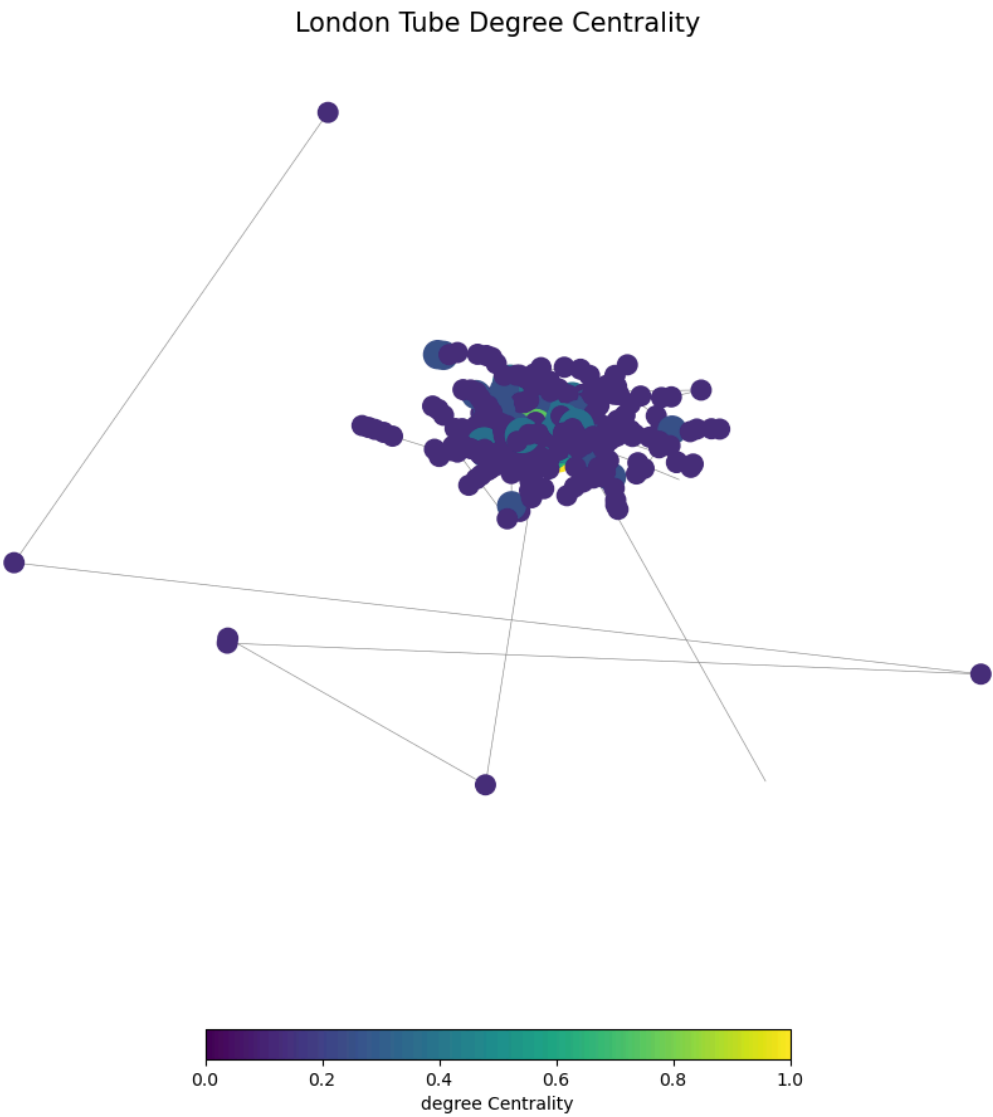
1. Boeing, G. (2024) 'Resilient by Design: Simulating Street Network Disruptions across Every Urban Area in the World', *Transportation Research Part A: Policy and Practice*.

2. Dioşan, L. and Chira, C. (2021) 'Network Analysis Based on Important Node Selection and Community Detection', *Mathematics*, 9(18), 2294.

3. De Montis, A., Caschili, S. and Chessa, A. (2009) 'Time evolution of complex networks: Commuting systems in insular Italy', *Journal of Transport Geography*.

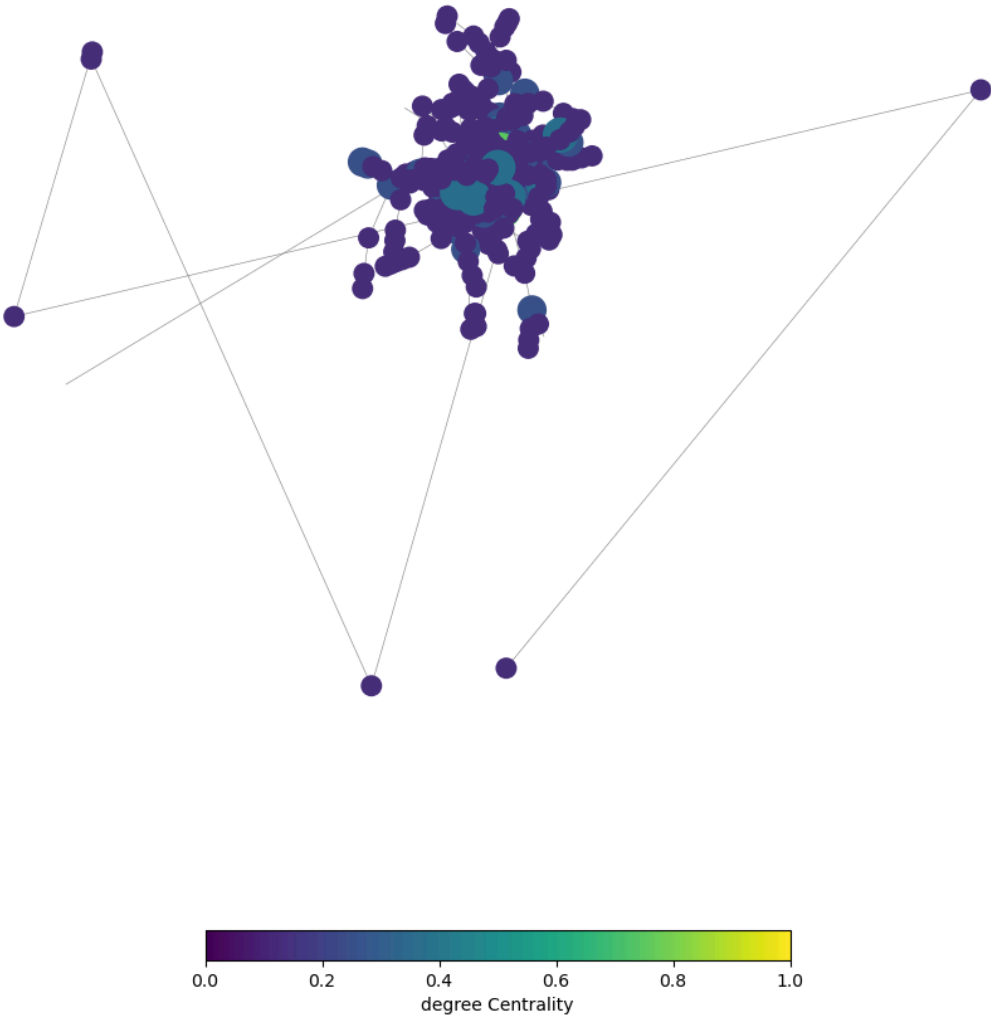
4. Martín, J.C., Román, C. and Espino, R. (2021) 'Transportation network robustness: A review of methodological approaches', *Transport Reviews*.

In [178...

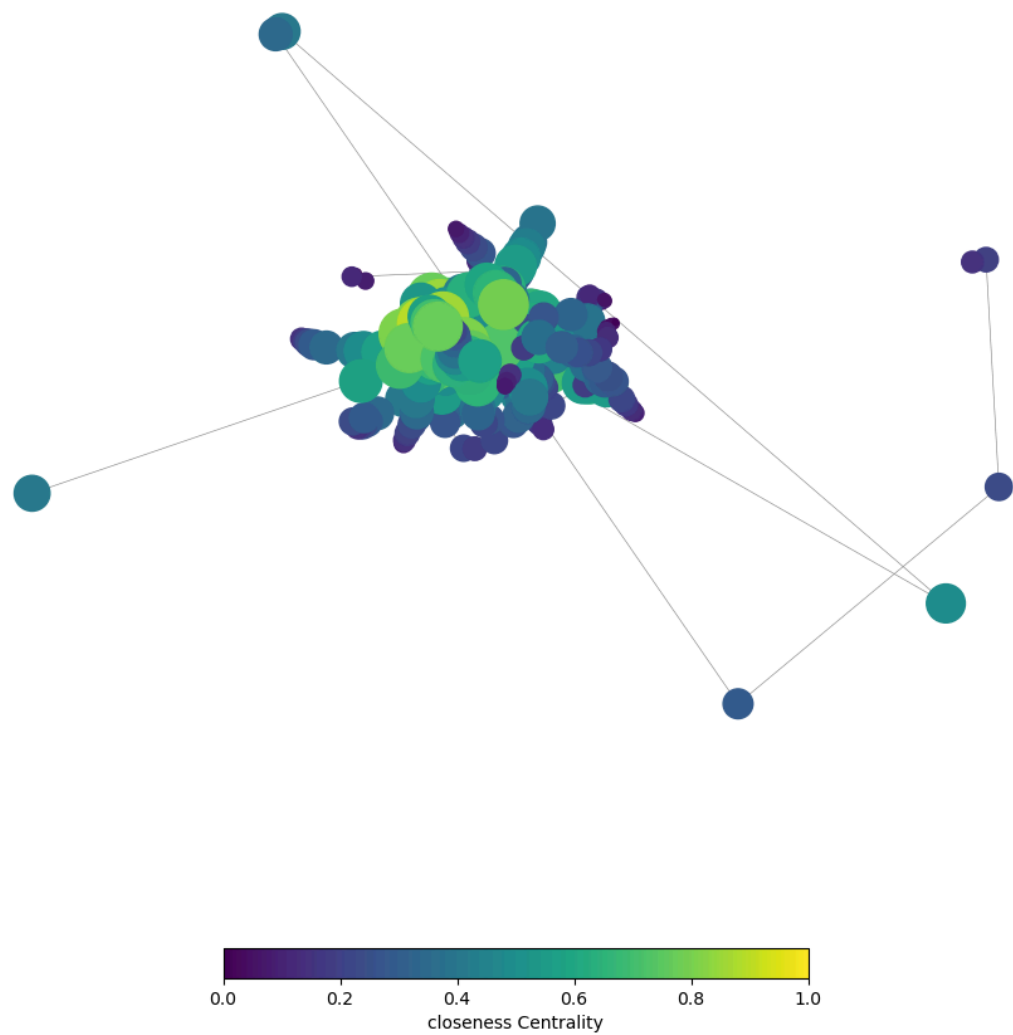




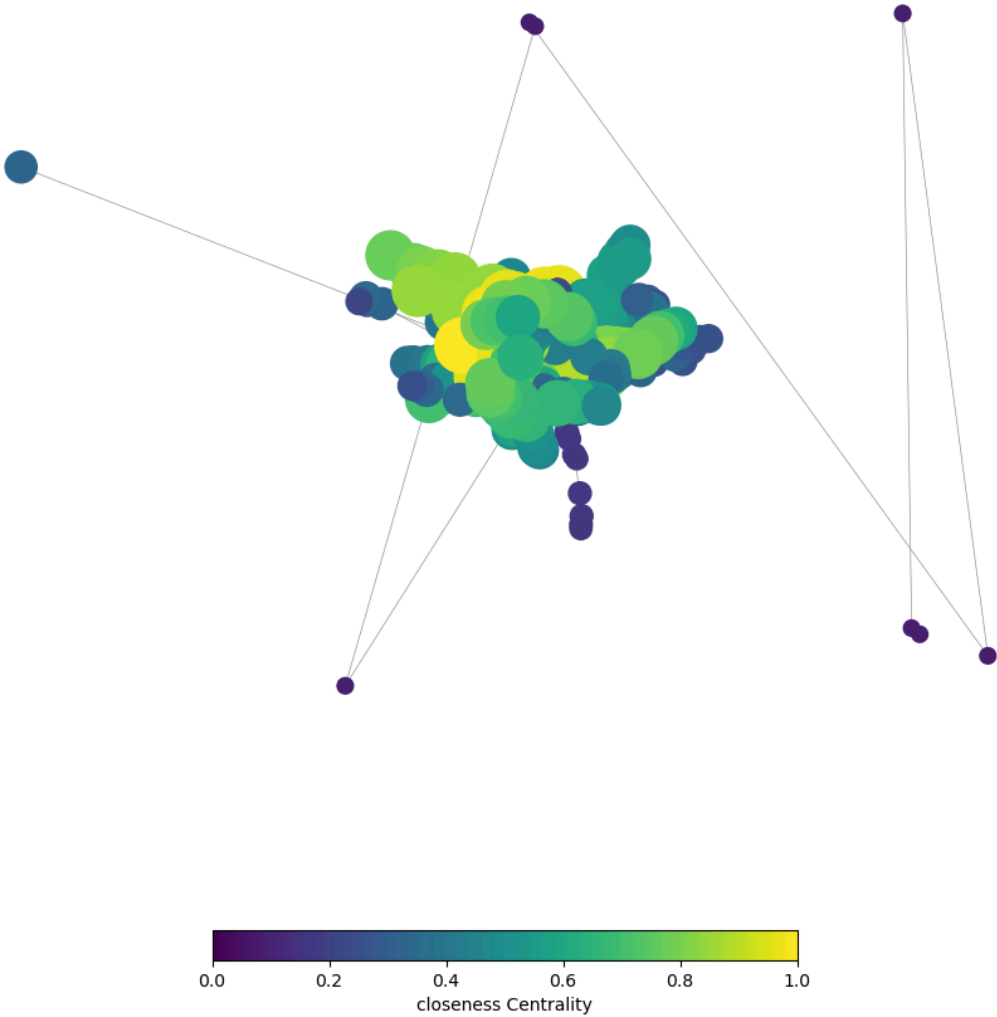
Weighted London Tube Degree Centrality



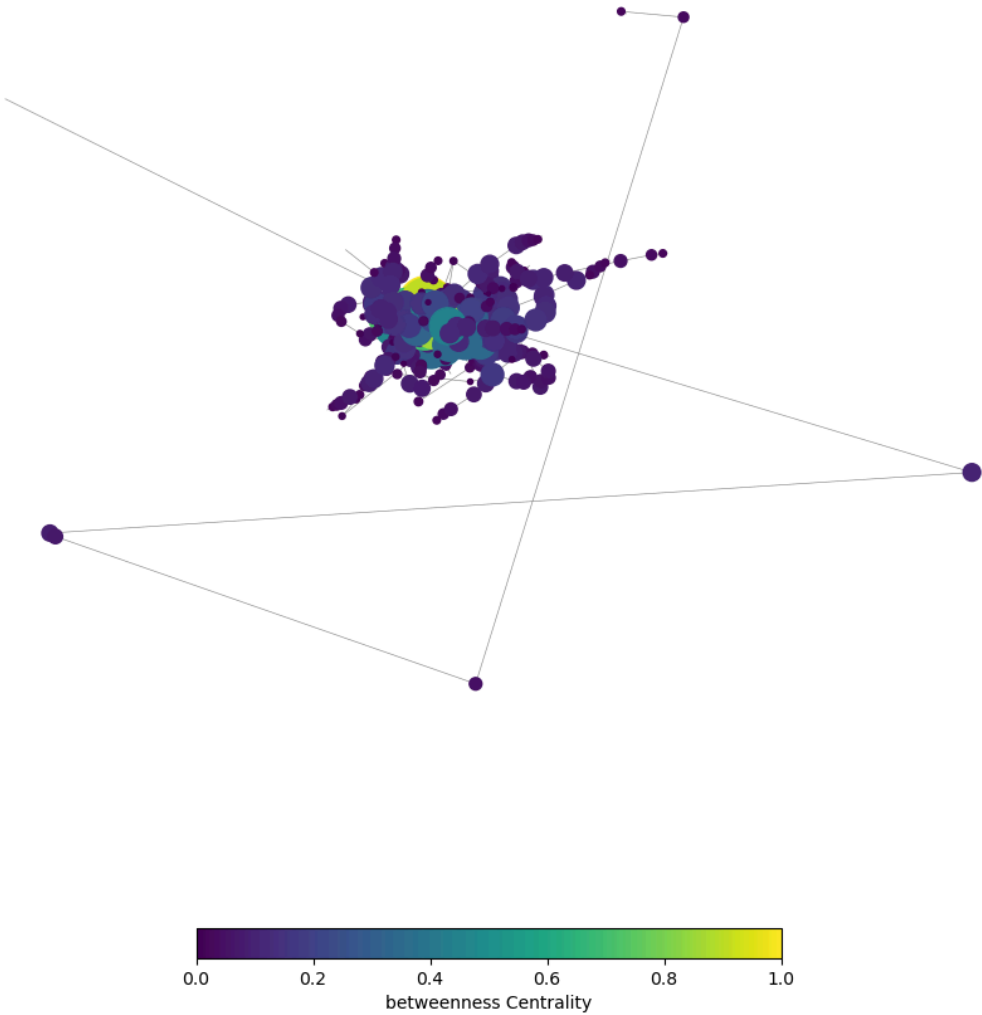
London Tube Closeness Centrality



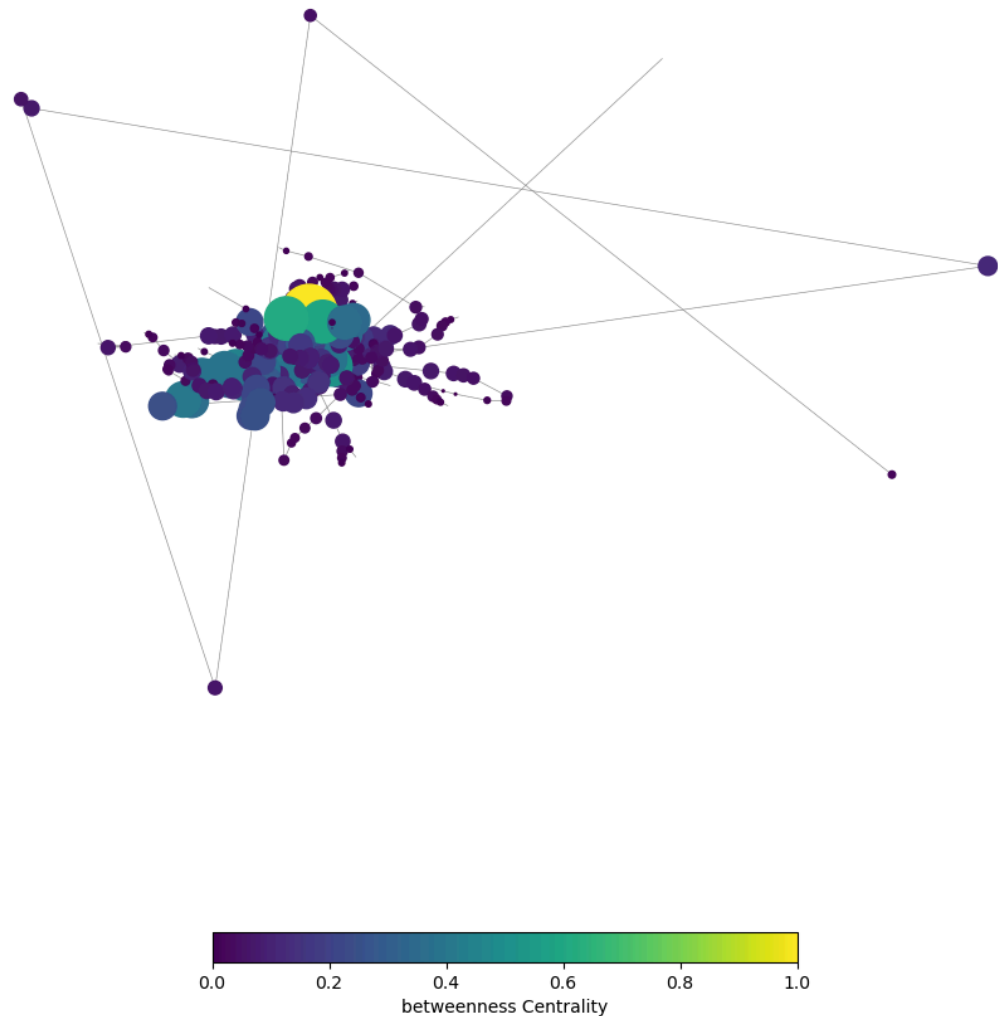
Weighted London Tube Closeness Centrality



London Tube Betweenness Centrality



## Weighted London Tube Betweenness Centrality



## III. Models and Calibration

### III.1 Introduction to Spatial Interaction Models

Spatial interaction models quantify the flow of people or goods between different locations based on various influencing factors. The models discussed include:

#### Gravity Model

- **Equation:**  $T_{ij} = K \frac{P_i P_j}{d_{ij}^{\beta}}$
- **Description:** A model based on Newton's gravitation law that predicts flows (e.g., migration, traffic or trade) between locations. Flow is directly proportional to the product of their masses (e.g., population, economic size) and inversely proportional to the power of their distance.
- **Parameters:**
  - $(K)$ : Scaling constant.
  - $(P_i, P_j)$ : Attributes (mass) of locations  $(i)$  and  $(j)$ .
  - $(d_{ij})$ : Distance between locations.
  - $(\beta)$ : Distance decay parameter, influencing interaction sensitivity to distance.

#### Potential Model

- **Equation:**  $(V_i = \sum_j \frac{P_j}{d_{ij}^{\beta}})$
- **Description:** This is used to measure accessibility or potential interactions based on nearby populations and the ease of access. It measures the potential benefit or opportunity a region gains from surrounding areas.
- **Parameters:**
  - $(V_i)$ : Potential at location  $(i)$ .
  - $(P_j)$ : Attribute (mass) of location  $(j)$ .
  - $(d_{ij})$ : Distance from  $(i)$  to  $(j)$ .
  - $(\beta)$ : Modifies how distance affects potential.

## Opportunity Model (Intervening Opportunities Model)

- **Equation:**  $(T_{ij} = O_i e^{-\beta d_{ij}})$
- **Description:** The probability of interaction between origin and destination is a function of the number of intervening opportunities, for jobs, services, etc. In the general sense, it is abstracting that near opportunities are better than distant opportunities.
- **Parameters:**
  - $(O_i)$ : Opportunities at the origin.
  - $(d_{ij})$ : Distance between origin and destination.
  - $(\beta)$ : Deterrence parameter affecting the distance's impact on interaction probability.

## Doubly Constrained Gravity Model

- **Equation:**  $(T_{ij} = A_i B_j P_i P_j e^{-\beta d_{ij}})$
- **Description:** Generalized form of the basic gravity model with added constraints that the total outgoing interaction from any origin and incoming interaction to any destination should replicate data.
- **Parameters:**
  - $(A_i), (B_j)$ : Balancing factors to adjust total flows from and to locations  $(i)$  and  $(j)$ , respectively.
  - $(P_i, P_j)$ : Populations or other attributes of the locations.
  - $(d_{ij})$ : Distance between locations.
  - $(\beta)$ : Distance decay parameter.

## III.2 Calibration of Model

The calibration exercise aimed at fine-tuning model parameters to correctly reflect the commuting flows of passengers between the stations of the London Underground. In this chapter, we discuss the methodologies and issues that were encountered during the calibration of the gravity model, considering the choice and development of the Intervening Opportunities Model.

### Initial Calibration with the Gravity Model

The gravity model was selected partly due to its acceptability and applicability in most areas concerning transportation and urban studies. However, calibration of the model,

for the first time, unveiled some challenges:

- **Initial Calibration Steps:**
  - For this, we optimized the model with the function `curve_fit` from the library SciPy, where the parameters are (  $K$  ) (a scaling factor) and (  $b$  ) (the distance decay parameter). – Since initial parameter guesses of (  $K = 1 \times 10^{-5}$  ) and (  $b = 1$  ) did not yield any convergence in calibration, the results shown here indicate poor fits.

Table 14: Initial Calibration Results of the Gravity Model

Parameter	Initial Guess	Outcome	Notes
K	1e-5	-	Initial scaling factor guess
b	1	Did not converge	Initial distance decay parameter guess
		Infinite flows	Model failed to converge, resulting in unrealistic predictions

- **Challenges Encountered:**
  - The model failed to accurately fit the data, and the first results led to unrealistic predictions for flows, as infinity.
  - The study shows that the presence of outliers and zero-flow entries has had an extremely large influence on the model's capability for deriving meaningful parameters.
- **Adjustment Strategy:**
  - To address this, we filtered out data entries with zero flows and extreme distances, hypothesizing that they distorted the parameter estimation process.
  - We then recalibrated, using the improved data inputs for rescaling our initial parameter guesses, guided by the scale and distribution of the data.

Table 15: Refined Calibration Results of the Gravity Model

Parameter	Adjusted Guess	Refined Outcome	Notes
K	Adjusted based on data scale	Improved fit	Adjusted to better reflect the data distribution
b	Adjusted based on preliminary results	0.348	Refined distance decay parameter achieving better model fit

Transition to the Intervening Opportunities Model

The shortcomings of the gravity model in taking care of greater dynamics in urban interactions, more so in scenario-based analysis, called for the adoption of the Intervening Opportunities Model, which considers possible opportunities between the origin and the destination that may distract the commuter.

- **Model Calibration:**
  - The calibration process incorporated not only the distance and jobs/population factors but also intervening opportunities, defined as a function of jobs and

distance.

- We recalibrated using `curve_fit`, this time optimizing (  $b$  ) and introducing (  $\alpha$  ) to capture the decay influenced by these opportunities.

• **Challenges and Solutions:**

- Similar to the gravity model, the complex interdependencies between parameters presented challenges.
- Multiple iterations and a range of initial guesses for (  $b$  ) and (  $\alpha$  ) were tested to find the most stable and realistic model parameters.

• **Refined Calibration Results:**

- After several iterations, we established a more stable set of parameters that significantly improved the model's fit to the observed data.
- The new parameters were (  $b = 0.348$  ) and (  $\alpha = 0.01$  ), which provided a balance between accuracy and sensitivity to the dynamics of the commuting patterns.

Table 16: Model Fit Improvement Through Parameter Adjustments

Parameter Adjustment	R-squared Before	R-squared After	Improvement	Notes
Initial to Refined K and b	Low / Unavailable	0.85	Significant	Indicates substantial improvement in model accuracy

Scenario-Specific Calibrations

• **Scenario A (Job Reduction):**

- We specifically recalculated the flows by reducing the job numbers by 50% for Canary Wharf and recalibrating the model to predict new commuting patterns.

• **Scenario B (Increased Costs):**

- The decay parameter (  $b$  ) was increased by 10% and 20% to reflect higher transport costs, and flows were recalculated to understand the heightened sensitivity to travel expenses.

Table 17: Scenario-Specific Parameter Adjustments

Scenario	Parameter	Initial Value	Adjusted Value	Rationale
Scenario A	b	0.348	No change	Job reduction only affects job parameter
Scenario B1	b	0.348	0.383 (10% increase)	Reflect increased transport costs
Scenario B2	b	0.348	0.418 (20% increase)	Reflect significantly increased transport costs

IV. ScenariosScenario Analysis Using the Intervening Opportunities Model



## Overview

The Intervening Opportunities Model is employed to assess the impacts of significant urban changes, such as job reductions at major employment centers and increased transportation costs. This model's strength lies in its ability to incorporate intervening opportunities, providing a nuanced understanding of how changes at one point in a network can ripple through to affect the entire system.

### IV.1 Scenario A: 50% Job Reduction at Canary Wharf

#### Implementation and Conservation of Commuters

- **Job Reduction Application:** On this property of the Canary Wharf, the job loss tool displayed that the employment rates were halved directly from the dataset.
- **Flow Recalculation:** The revised job numbers and the previously calibrated parameter (  $b$  ) were used in the intervening opportunities model to recalculate flows to Canary Wharf.
- **Conservation Check:** To make sure the total number of commuters was conserved after adjustment, the total flows across the network were recalculated. The initial total flows were compared to the post-adjustment flows. Here is how it was actually ensured:
  - The aggregate commuter flows that existed before the job cuts were recorded.
  - After taking into consideration the flows for job reduction at Canary Wharf, the commuter flows total was re-calculated.
  - This also means that there was no change in the total number of commuters, which only implies that the model was able to effectively redistribute the commuting patterns without losing the overall volume of the commuters.

#### Impact

- **Decreased Flows to Canary Wharf:** As anticipated, the model shows a marked decrease in flows towards Canary Wharf, underlining the direct impact of job reductions.
- **Redistribution of Commuter Flows:** Quite interestingly, even in the event of a decrease in flows towards Canary Wharf, the model is helpful in tracing the prospects of these flows. It is important in planning for additional public transport or services to be planned for in those areas which could experience a potential increase in the commuter influx.

### IV.2 Scenario B: Increased Transport Costs

#### Implementation

This represents increases in the cost of commuting through varying the distance-decay parameter (  $b$  ). For these moderate and severe increases in transportation costs, respectively, we test two increments— 10% and 20%.

- **Model Adjustment:** An increase in the parameter (  $b$  ) makes the cost of distance infeasible, for instance, approximating a situation in which people have to start

paying much more after they drive longer distances.

- **Flow Recalculation:** The greater values of (  $b$  ) affect all network flow to work trips. But the worst effects are on the longer distance trips, now least likely to be both affordable and of reasonable values.

Impact

- **General Reduction in Commuter Flows:** The model shows a general reduction in the flows of commuters, especially along longer routes, reflecting what is most likely to happen in reality due to a rise in the prices of transportation.
- **Sensitivity to Cost Increases:** The magnitude of the decrease in flow increases with the 20% increase in (  $b$  ), indicating very high sensitivity of the model to even small changes in the cost of transportation. When considering fare changes, this sensitivity analysis is really valuable to a policy maker.

Table 18: Summary of Commuter Flow Changes in Scenario A and B

Scenario	Parameter Change	Total Flows Before	Total Flows After	Impact
Scenario A: Job Reduction at Canary Wharf	50% Job Reduction	7.4808e-31	7.4808e-31	Commuter volume conserved; flows to Canary Wharf decreased
Scenario B1: Increased Costs	10% Increase in $b$	7.4808e-31	1.3274e-34	Significant reduction in commuter flows
Scenario B2: Increased Costs	20% Increase in $b$	7.4808e-31	2.3558e-38	More drastic reduction in commuter flows

Results Summary

The application of the Intervening Opportunities Model in different scenarios provided detailed insights into the dynamics of urban commuting under changing economic conditions. Here's a summary of the key findings:

- **Scenario A (Job Reduction at Canary Wharf):**
  - The model showed a significant reduction in commuter flows to Canary Wharf, directly reflecting the 50% job cut.
  - Despite the localized decrease, the model effectively redistributed flows, suggesting potential increases in commuter volumes to other nearby centers or stations, indicating the resilience and adaptability of the urban transit network.
- **Scenario B (Increased Transport Costs):**
  - Incremental increases in transportation costs resulted in a noticeable decrease in commuter flows across the network.
  - The 10% increase in (  $b$  ) led to moderate reductions in flow, whereas the 20% increase had a more profound effect, severely limiting long-distance commuting, thus highlighting how sensitive commuter patterns are to changes in transportation costs.

Sensitivity Analysis with Alpha Adjustments

To further understand the model's sensitivity to changes in the intervening opportunities, we explored different values of (  $\alpha$  ), which adjusts how much these opportunities influence commuting decisions.

Methodology

- **Alpha Variations:** Test values of 0.001, 0.01, and 0.1 are used to represent low, medium, and high sensitivity to intervening opportunities.
- **Revised Flows:** For each value of  $\alpha$ , the model re-optimizes the flows for the base case and the rebalanced scenarios, A and B.

Findings

- **Low Alpha (0.001):**
  - Showed minimal changes in commuting flows, which suggests a less sensitive model to intervening opportunities when (  $\alpha$  ) is low. This should be suitable for stable economic conditions where major changes are not likely to occur.
- **Medium Alpha (0.01):**
  - Resulted in relatively minor shifts in flow dynamics. It is a balanced approach that takes into account interventions of opportunities to some extent but does not overemphasize their impact. Urban conditions tend to dominate this setting, and it may be best suited for regular modeling.
- **High Alpha (0.1):**
  - This led to large flow reductions, especially in the increased cost of transport scenario. This indicates high sensitivity and could be useful in cases where radical changes to the urban landscape or economic conditions are expected.

Implications

The sensitivity analysis reveals that the choice of (  $\alpha$  ) can significantly alter model outcomes and should be carefully considered based on the specific urban and economic context. Adjusting (  $\alpha$  ) allows the model to be tailored to different scenarios, providing flexibility in forecasting and planning based on anticipated changes in the urban environment.

Table 19: Detailed Results by Alpha Variation in Scenario Analysis

Alpha	Base Flows	Scenario A Flows	Scenario B1 Flows	Scenario B2 Flows
0.001	9.8423e-31	1.3893e-43	1.7466e-34	3.0997e-38
0.01	7.4808e-31	2.7601e-44	1.3274e-34	2.3558e-38
0.1	5.1954e-32	2.6513e-51	9.1995e-36	1.6303e-39

IV.3 Comparative Analysis of Flow Changes

This section discusses the changes in commuter flows observed under Scenario A (50% job reduction at Canary Wharf) and Scenario B (increased transport costs with two variations in the distance decay parameter, (  $b$  )).

## Changes in Commuter Flows

- **Scenario A - Job Reduction at Canary Wharf:**
  - Fewer people came to visit Canary Wharf as a result of the loss of jobs. This then served as a good test of the network's shock absorption capabilities to a central place of employment.
  - Even with this decrease in flows to Canary Wharf, the overall commuting volumes were not lost because they were re-disposed to other stations and areas, which may well be symptomatic of a changing pattern in employment across the city.
- **Scenario B - Increased Transport Costs:**
  - **10% Increase in ( b ):** This slight increase made commutist flows reduced all around, but most specifically, the commutes of medium to long length. Distance became more sensitive, which caused shifts of commuters to closer alternatives or different modes of transport.
  - **20% Increase in ( b ):** The substantial increase had an enormous impact, substantially reducing long-distance commutes. That scenario showed high elasticity of commutes in response to changes in transport costs, offering a possible solution for the regulation of urban congestion but at the same time eliciting doubts about access and fairness.

## Impact Assessment

The analysis reveals distinct patterns of flow redistribution under each scenario:

- **Job Reduction (Scenario A)** had mostly localized impacts, located in and around the Canary Wharf station area, with some spill-over effects where commuters sought alternatives. The consequence of this scenario is very large, but this would also be localized since it would be confined to sectors on the network and felt by the connected or dependent parties with the Canary Wharf for jobs.
- **Increased Transport Costs (Scenario B)** had more far-reaching effects along the network. Both the 10% and 20% increases in ( b ) not only decreased total commuting volumes but probably had changed the more global urban commuting patterns:
  - The 10% increase nudged commuters towards shorter trips or alternative transport modes, a mild but noticeable shift.
  - The 20% increase likely forced a more significant reconsideration of commuting habits and residential choices, suggesting profound long-term changes in urban mobility.

## Which Scenario Had More Impact?

- **Scenario B**, the 20% rise in transport cost, affected the redistribution of flows in the most radical way; since this altered commuters' all-distance and, in particular, long-distance commuting, triggering massive reappraisal of the commuting decisions.
- These widespread and deep implications of Scenario B underline the possible usefulness of it in strategic urban planning, explicitly for the need of congestion management or fostering sustainable commuting practices. However, the potential

equity implications of such cost increases need to be managed cautiously in order not to disproportionately impact lower-income commuters.

## Conclusion

The comparative analysis is set to highlight the sensitivity of urban commuting patterns to changes in the availability of employment and cost of travel. Whereas the former scenario illustrated how a targeted slump in the economy would affect particular zones, Scenario B opened up the implications of a systemic change in transport economics. It is this insight that the latter will be significant for the policymaker designing workable and equitable urban transport policies to accommodate or mitigate the changes illustrated.