

(1) SIMPLEX CODE :-

```
clc
clear all
%% defining parameters
c = [4 6 3 1];
a = [1 4 8 6; 4 1 2 1; 2 3 1 2];
b = [11; 7; 2]
s = eye(size(a, 1))
variables = size(a, 2)
%% creating table
var = {'x1', 'x2', 'x3', 'x4', 's1', 's2', 's3', 'sol'}
A = [a s b]
cost = zeros(1, size(A,2))
cost(1: variables) = c
bv = variables+1: size(A, 2)-1
zjcj = cost(bv)*A - cost
zcj = [zjcj; A]
ST = array2table(zcj, VariableNames=var)
%% finding solution
RUN = true
while RUN
    if any(zjcj(1:end-1) < 0)
        fprintf('Not optimal solution')
        zc = zjcj(1:end-1)
        [enter_val, pvt_col] = min(zc)
        if all(zcj(:, pvt_col)) <= 0
            fprintf('LPP is unbounded')
        else
            sol = A(:, end)
            column = A(:, pvt_col)
            for i=1:size(A, 1)
                if column(i) > 0
                    ratio(i) = sol(i)./column(i)
                else
                    ratio(i) = inf
                end
            end
            [leaving_val, pvt_row] = min(ratio)
            bv(pvt_row) = pvt_col
            pvt_key = A(pvt_row, pvt_col)
            A(pvt_row, :) = A(pvt_row, :)./pvt_key
            for i=1: size(A, 1)
                if i ~= pvt_row
                    A(i, :) = A(i, :) - A(i, pvt_col).*A(pvt_row, :)
                end
            end
            zjcj = cost(bv)*A - cost
            next_table = [zjcj; A]
            ST = array2table(next_table, VariableNames=var)
        else
            RUN = false
            fprintf('The final optimal value is ')
            zjcj(end)
        end
    end
end
```

(2) Big M :-

```
(3) % Big M method
(4) clc
(5) clear all
(6) M=1000;
(7) %---1---
(8) cost=[-3 -5 0 0 -M -M 0];
(9) a=[1 3 -1 0 1 0; 1 1 0 -1 0 1];
(10) b=[3;2];
(11) A=[a b];
(12) bv=[5 6];
(13) Var={'x1','x2','x3','s1','s2','s3','A1','A2','sol'};
(14) %cost=[20 10 0 0 0 -M -M 0];
(15) %a=[1 2 1 0 0 0 0;3 1 0 -1 0 1 0;4 3 0 0 -1 0 1];
(16) %b=[40;30;60];
(17) artifical_var=[7 8];
(18) % bv=[3 6 7];
(19) % cost=[1 1 0 0 -M 0];
(20) % a=[2 1 -1 0 1;1 7 0 1 0];
(21) % b=[4;7];
(22) % artifical_var=[5];
(23) % bv=[4 5];
(24) %cost=[5 3 0 0 0 -M 0];
(25) %a=[1 1 1 0 0 0;5 2 0 1 0 0;2 8 0 0 -1 1];
(26) %b=[2;10;12];
(27) %artifical_var=[6];
(28) %bv=[3 4 6];
(29) %---3---
(30) % cost=[3 2 0 0 -M 0];
(31) % artifical_var=5
(32) % bv=[3 5];
(33) % a=[2 1 1 0 0; 3 4 0 -1 1];
(34) % b=[2;12];
(35) A=[a b];
(36) Var={'x1','x2','s1','s2','s3','A1','sol'};
(37) % %---2---
(38) % cost=[4 -3 0 0 -M -M 0];
(39) % a=[2 1 -1 0 1 0; 2 -1 0 -1 0 1];
(40) % b=[0;2];
(41) % artifical_var=[5 6]
(42) % A=[a,b];
(43) % Var={'x1','x2','s1','s2','A1','A2','sol'};
(44) % bv=[5 6];
(45) zjcj=cost(bv)*A-cost
(46) % Display initial simplex table
(47) simplex_table=[zjcj; A];
(48) array2table(simplex_table,'VariableNames',Var)
(49) RUN=true;
(50) while RUN
(51) if any(zjcj(1:end-1)<0) % check for negative value
(52) fprintf(' The current BFS is not optimal \n');
(53) zc=zjcj(1:end-1);
(54) [Enter_val, pvt_col]= min(zc) ;
(55) if all(A(:,pvt_col)<=0)
(56) error('LPP is Unbounded');
(57) else
(58) sol=A(:,end);
(59) column=A(:,pvt_col);
```

```

(60)     for i=1:size(A,1)
(61)     if column(i)>0
(62)     ratio(i)= sol (i)./column(i);
(63)     else
(64)     ratio(i)=inf;
(65)     end
(66)     end
(67)     [leaving_value,pvt_row]=min(ratio);
(68)     end
(69)     bv(pvt_row)=pvt_col;
(70)     pvt_key=A(pvt_row, pvt_col);
(71)     A(pvt_row,:)=A (pvt_row,:)./pvt_key;
(72)     % row operation
(73)     for i=1:size(A,1)
(74)     if i~=pvt_row
(75)     A(i,:)=A(i,:)-A (i, pvt_col).*A(pvt_row,:);
(76)     end
(77)     end
(78)     zjcj=cost(bv)*A-cost;
(79)     next_table=[zjcj; A]
(80)     array2table(next_table,'VariableNames',Var)
(81)
(82)     else
(83)         RUN=false;
(84)         if any(bv==artifical_var(1))
(85)             error('Infeasible solution');
(86)         else
(87)             fprintf('The table is optimal \n');
(88)             end
(89)             z=input(' Enter 0 for minimization and 1 for max \n');
(90)
(91)             if z==0
(92)                 Obj_value=-zjcj(end);
(93)             else
(94)                 Obj_value=zjcj(end);
(95)             end
(96)             fprintf('The final optimal value is % f \n',Obj_value);
(97)         end
(98)     end

```

(3) Two Phase :-

```
% Two phase method
clc
clear all
%-----Problem 1-----
Variables={'x1','x2','s1','s2','A1','A2','sol'};
OVariables={'x_1','x_2','s_1','s_2','sol'}; % original variables
OrigC=[-3 -5 0 0 -1 -1 0];
a=[1 3 -1 0 1 0; 1 1 0 -1 0 1];
b=[3;2];
A=[a b];

%-----Problem 2-----
% Variables={'x1','x2','s1','s2','A1','A2','sol'};
% OVariables={'x_1','x_2','s_1','s_2','sol'};
% OrigC=[-3 4 0 0 -1 -1 0];
% a=[1 -1 -1 0 1 0; 2 -1 0 -1 0 1];
% b=[0;2];
% A=[a b];
% PHASE-1
fprintf('***** PHASE-1 ***** \n')
%-----Problem 1-----
cost=[0 0 0 0 -1 -1 0]
Artifical_var=[5 6]
bv=[5 6];

%-----Problem 2-----
% cost=[ 0 0 0 0 -1 -1 0];
% Artifical_var=[5 6];
% bv=[5 6];

zjcj=cost(bv)*A-cost
simplex_table=[zjcj;A]
array2table(simplex_table,'VariableNames',Variables)
RUN=true;
while RUN
if any(zjcj(1:end-1)<0) % check for negative value
    fprintf(' the current BFS is not optimal \n')
    zc=zjcj(1:end-1);
    [Enter_val, pvt_col]= min(zc);
    if all(A(:,pvt_col)<=0)
        error('LPP is Unbounded all enteries are <=0 in column % d',pvt_col);
    else
        sol=A(:,end);
        column=A(:,pvt_col);
        for i=1:size(A,1)
            if column(i)>0
                ratio(i)= sol (i)./column(i);
            else
                ratio(i)=Inf;
            end
        end
        [leaving_val, pvt_row]=min(ratio);
        end
        bv(pvt_row)=pvt_col;
        pvt_key=A(pvt_row, pvt_col);
        A(pvt_row,:)=A (pvt_row,:)./pvt_key;
```

```

for i=1:size(A,1)
    if i~=pvt_row
        A(i,:)=A(i,:)-A (i, pvt_col).*A(pvt_row,:);
    end
end
% zjcj=zjcj-zjcj (pvt_col).*A(pvt_row,:);
zjcj=cost(bv)*A-cost;
next_table=[zjcj;A];
table=array2table(next_table,'VariableNames',Variables)
else
    RUN=false;
    if any(bv==Artifical_var(1)) || any(bv==Artifical_var(2))
        error('Infeasible solution');
    else
        fprintf('optimal table of phase-1 is achieved \n');
    end
end
end

% PHASE-2
fprintf('***** PHASE-2 ***** \n')
A(:,Artifical_var)=[]; % Removing Artificial var by giving them empty value
OrigC(:,Artifical_var)=[]; % Removing Artificial var cost by giving them empty
value
cost=OrigC;
zjcj=cost(bv)*A-cost;
simplex_table=[zjcj;A];
array2table(simplex_table,'VariableNames',OVariables)

RUN=true;
while RUN
    if any (zjcj(1:end-1)<0) % check for negative value
        fprintf('The current BFS is not optimal \n')
        zc=zjcj(1:end-1);
        [Enter_val, pvt_col]= min(zc);
        if all(A(:,pvt_col)<=0)
            error('LPP is Unbounded, all entries are <=0 in column %d',pvt_col);
        else
            sol=A(:,end);
            column=A(:,pvt_col);
            for i=1:size(A,1)
                if column(i)>0
                    ratio(i)= sol (i)./column(i);
                else
                    ratio(i)=inf;
                end
            end
            [leaving_val, pvt_row]=min(ratio);
        end
        bv(pvt_row)=pvt_col;
        pvt_key=A(pvt_row, pvt_col);
        A(pvt_row,:)=A (pvt_row,:)./pvt_key;
        for i=1:size(A,1)
            if i~=pvt_row
                A(i,:)=A(i,:)-A (i, pvt_col).*A(pvt_row,:);
            end
        end
        % zjcj=zjcj-zjcj (pvt_col).*A(pvt_row,:);
        zjcj=cost(bv)*A-cost;

```

```

next_table=[zjcj;A];
table=array2table(next_table,'VariableNames',0Variables)
else
    RUN=false;
    fprintf('The current BFS is optimal \n');
    z=input(' Enter 0 for minimization and 1 for max \n');
    if z==0
        Obj_value=-zjcj(end);
    else
        Obj_value=zjcj(end);
    end
    fprintf('The final optimal value is %f \n',Obj_value);
end
end

```

(4) Dual Simplex :-

```

clc
clear all
format short

cost = [-2 0 -1 0 0 0];
A = [-1 -1 1 1 0 -5; -1 2 -4 0 1 -8];
bv = [4 5]
%S = eye(size(A1,1))

%cost = zeros(1,size(A,2))
%variables = size(A1,1)
%cost(1:variables)= C

%bv = variables+1:size(A,2)-1

zjcj = cost(bv)*A - cost
zc = [zjcj;A]
simplex_table = array2table(zc,'VariableNames',{'x1','x2','x3','s1','s2','sol'})

run = true
while(run)
    sol = A(:,end)
    if any(sol <0)
        fprintf('table is not faesible')
        fprintf('\n')
        %fprintf('old basic variables %d \n',bv)
        z = zjcj(1:end-1)
        [leaving_val pvt_row]= min(sol)
        fprintf('leaving variable is %d',pvt_row)

        solu =A(:,end)
        row = A(:,pvt_row)
        if(row<=0)
            fprintf('problem is unbounded')
        else
            for i=1:size(A,2)-1
                if A(pvt_row , i)<0
                    ratio(i) = abs(zjcj(i) /A(pvt_row , i));
                else

```

```

        ratio(i)= inf
    end
end
end
[entering_val pvt_col]=min(ratio)
fprintf('entering variable %d',pvt_col)
bv(pvt_row) = pvt_col
fprintf('new basic variables are ')
display(bv)
pvt_key=A(pvt_row,pvt_col)

A(pvt_row,:)=A(pvt_row,+)/pvt_key
for i=1:size(A,1)
    if i~=pvt_row
A(i,:)=A(i,)-A(i,pvt_col)*A(pvt_row,:)
    end
end
zjcj=zjcj-zjcj(pvt_col)*A(pvt_row,:);
zcyj = [zjcj ; A]
simplest = array2table(zcyj,'VariableNames',{'x1','x2','x3','s1','s2','sol'})
bfs = zeros(1,size(A,2))
bfs(bv)= A(:,end)
bfs(end) = sum(bfs .* cost);
currentbfs = array2table(bfs,'VariableNames',{'x1','x2','x3','s1','s2','sol'})
else
    run = false
    fprintf('table is feasible')
end
end
end

```