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%DualSimplex
clc
clear all
format short
% To solve the LPP by Simplex Method
% Maximize  $z = -2x_1 - x_3$ 
% Subject to  $x_1 + x_2 - x_3 \geq 5$ 
%  $x_1 - 2x_2 + 4x_3 \geq 0$ 
Variables = {'x_1', 'x_2', 'x_3', 's_1', 's_2', 'sol'}
Cost = [-2, 0, -1, 0, 0, 0]
Info = [-1, -1, 1; -1, 2, -4]
b = [-5; -8]
s = eye(size(Info, 1))
A = [Info s b]
%% To find the starting BFS
BV = []
for j = 1:size(s, 2)
    for i = 1:size(A, 2)
        if A(:, i) == s(:, j)
            BV = [BV i]
        end
    end
end
fprintf('The Basic Variables (BV) ')
disp(Variables(BV))
%% To compute Z-Row ( $z_j - c_j$ )
ZjCj = Cost(BV) * A - Cost
%% To print the table
ZCj = [ZjCj; A]
SimpTable = array2table(ZCj)
SimpTable.Properties.VariableNames(1:size(ZCj, 2)) = Variables
%% Dual Simplex Starts
Run = true
while Run
    sol = A(:, end)
    if any(sol < 0)
        fprintf('The current BFS is not Feasible \n')
        %% Finding the leaving Variable
        [Leaving_Value Pvt_Row] = min(sol)
        fprintf('Leaving Row=%d \n', Pvt_Row)
        %% Finding the Entering Variable
        Row = A(Pvt_Row, 1:end-1)
        ZRow = ZjCj(:, 1:end-1)
        for i = 1:size(Row, 2)
            if Row(i) < 0
                ratio(i) = abs(ZRow(i) ./ Row(i))
            else
                ratio(i) = inf
            end
        end
        %% to Find the Min ratio
        [MinRatio, Pvt_Col] = min(ratio)
        fprintf('Entering Variables in %d \n', Pvt_Col)

        %% UPDATE THE BASIC VARIABLES
        BV(Pvt_Row) = Pvt_Col
        fprintf('Basic Variable=')
        disp(Variables(BV))
    end
end

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%pivot key
Pvt_Key=A(Pvt_Row,Pvt_Col)
%Update the Table for the next Iteration
A(Pvt_Row,:)=A(Pvt_Row,:)./Pvt_Key
for i=1:size(A,1)
    if i~=Pvt_Row
        A(i,:)=A(i,:)- A(i,Pvt_Col).*A(Pvt_Row,:);
    end
ZjCj=ZjCj-ZjCj(Pvt_Col).*A(Pvt_Row,:);
%To print the table
ZCj=[ZjCj;A];
SimpTable=array2table(ZCj);
SimpTable.Properties.VariableNames(1:size(ZCj,2))=Variables
end
else
    Run=false
    fprintf('The current BS is Feasible and Optimal sol \n')
end
end
%Final Optimal Sol
Final_BFS=zeros(1,size(A,2))
Final_BFS(BV)=A(:,end)
Final_BFS(end)=sum(Final_BFS.*Cost)
OptimalBFS=array2table(Final_BFS)
OptimalBFS.Properties.VariableNames(1:size(OptimalBFS,2))=Variables

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