

# MATLAB

## Lecture 2

# Making Folders

- Use folders to keep your programs organized
- To make a new folder, click the 'Browse' button next to 'Current Directory'
- Click the 'Make New Folder' button, and change the name of the folder. Do NOT use spaces in folder names.
- Highlight the folder you just made and click 'OK'
- The current directory is now the folder you just created
- To see programs outside the current directory, they should be in the Path. Use File-> Set Path to add folders to the path

# MATLAB Basics

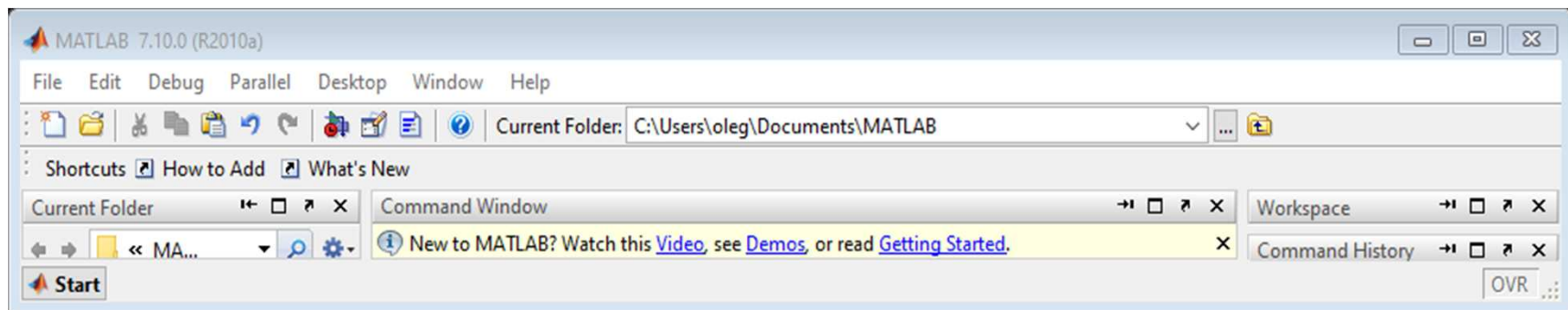
- MATLAB can be thought of as a super-powerful graphing calculator
- In addition it is a programming language
  - MATLAB is an interpreted language, like Java
  - Commands executed line by line

# Help/Docs

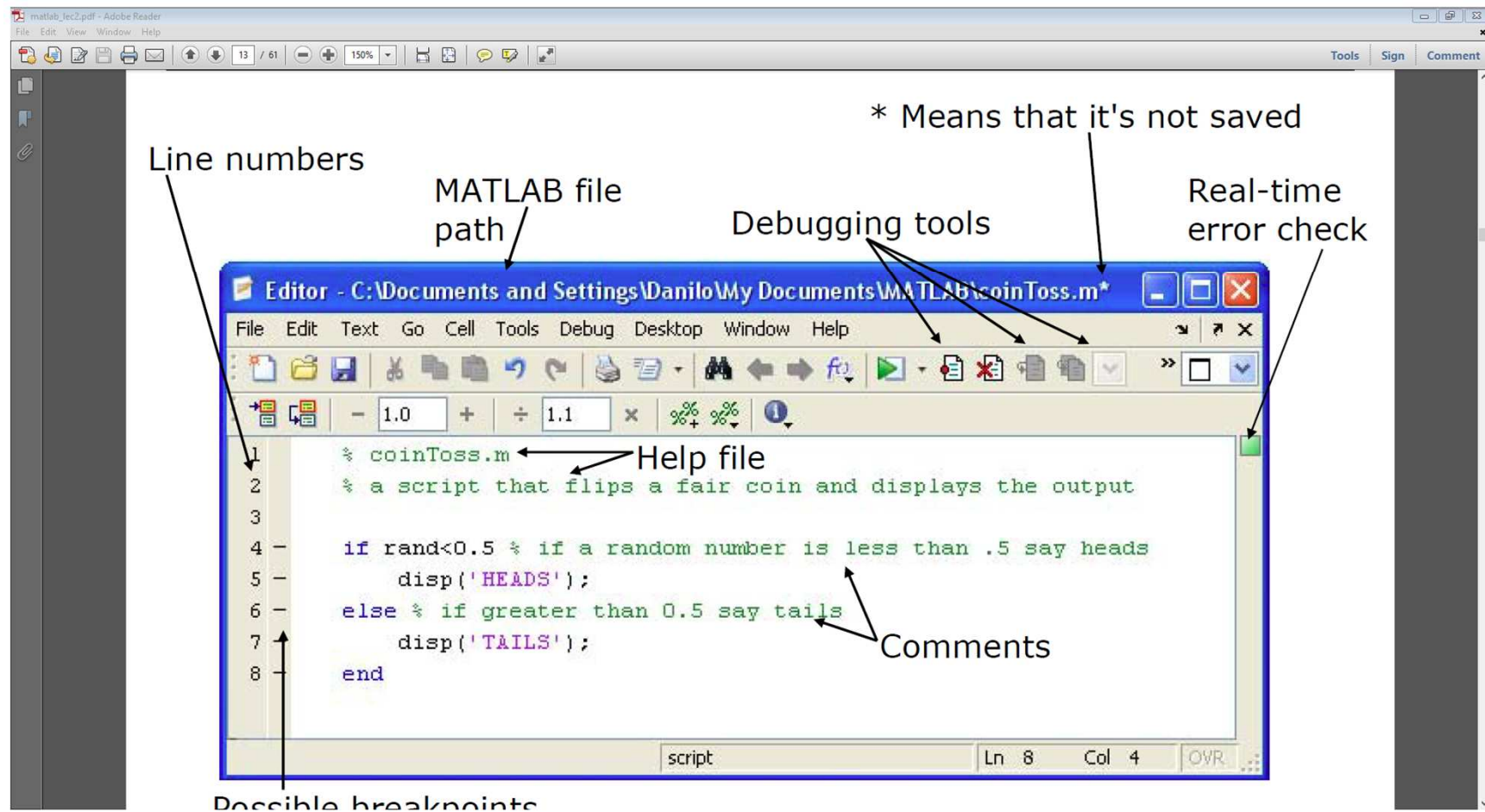
- help
  - The most important function for learning MATLAB on your own
- To get info on how to use a function:
  - »help sin
  - Help lists related functions at the bottom and links to the doc
- To get a nicer version of help with examples and easy-to read descriptions:
  - »doc sin

# Scripts: Overview

- Scripts are
  - collection of commands executed in sequence
  - written in the MATLAB editor
  - saved as MATLAB files (.m extension)
- To create an MATLAB file from command-line
  - »edit helloWorld.m
  - or click “page” button under “File”



# Scripts: the Editor



# Scripts: Some Notes

- COMMENT!
  - Anything following a % is seen as a comment
  - The first contiguous comment becomes the script's help file
  - Comment thoroughly to avoid wasting time later
- Note that scripts are somewhat static, since there is no input and no explicit output
- All variables created and modified in a script exist in the workspace even after it has stopped running

# Scripts

- Make a helloWorld script
- Open the editor and save a script as helloWorld.m. This is an easy script, containing two lines of code:
  - % helloWorld.m
  - % my first hello world program in MATLAB
  - disp('Hello World!');
  - disp('I am going to learn MATLAB!');
- Command **disp** displays strings. Strings are written between single quotes, like 'This is a string'



# Variables

- No need to initialize variables!
- MATLAB supports various types, the most often used are
  - »3.84 64-bit double (default)
  - »'a' 16-bit char
- Most variables you'll deal with will be vectors or matrices of doubles or chars
- Other types are also supported: complex, symbolic, 16-bit and 8 bit integers, etc. You will be exposed to all these types through the homework

# Naming variables

- **To create a variable, simply assign a value to a name:**
  - »`var1=3.14`
  - »`myString='hello world'`
- **Variable names**
  - first character must be a LETTER
  - after that, any combination of letters, numbers and \_
  - CASE SENSITIVE! (`var1` is different from `Var1`)
- **Built-in variables. Don't use these names!**
  - `i` and `j` can be used to indicate complex numbers
  - `pi` has the value 3.1415926...
  - `Ans` stores the last unassigned value (like on a calculator)
  - `Inf` and `-Inf` are positive and negative infinity
  - `NaN` represents 'Not a Number'

# Variables

- A variable can be given a value explicitly
  - `»a = 10`
  - shows up in workspace!
- Or as a function of explicit values and existing variables
  - `»c = 1.3*45-2*a`
- To suppress output, end the line with a semicolon
  - `»cooldude = 13/3;`

# Arrays

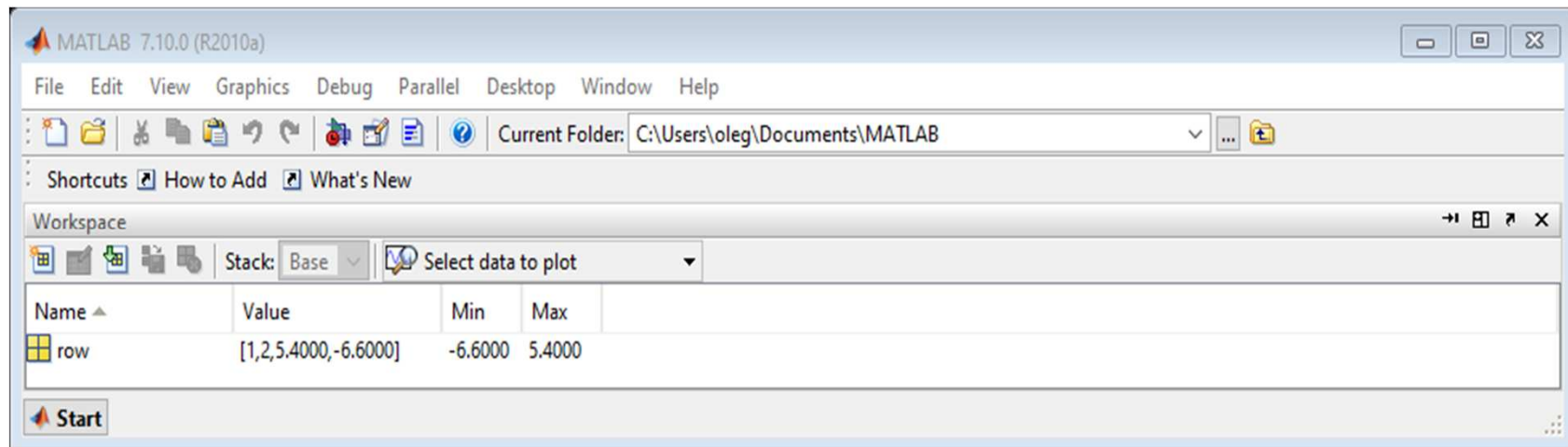
- Like other programming languages, arrays are an important part of MATLAB
- Two types of arrays
  - (1) matrix of numbers (either double or complex)
  - (2) cell array of objects (more advanced data structure)



# Row Vectors

- Row vector: comma or space separated values between brackets
  - `»row = [1 2 5.4 -6.6]`
  - `»row = [1, 2, 5.4, -6.6];`
- Command window:
  - `row =`  
1.0000 2.0000 5.4000 -6.6000

Workspace:



# Column Vectors

- Column vector: semicolon separated values between brackets

- »column = [4;2;7;4]

- Command window

```
» column =
```

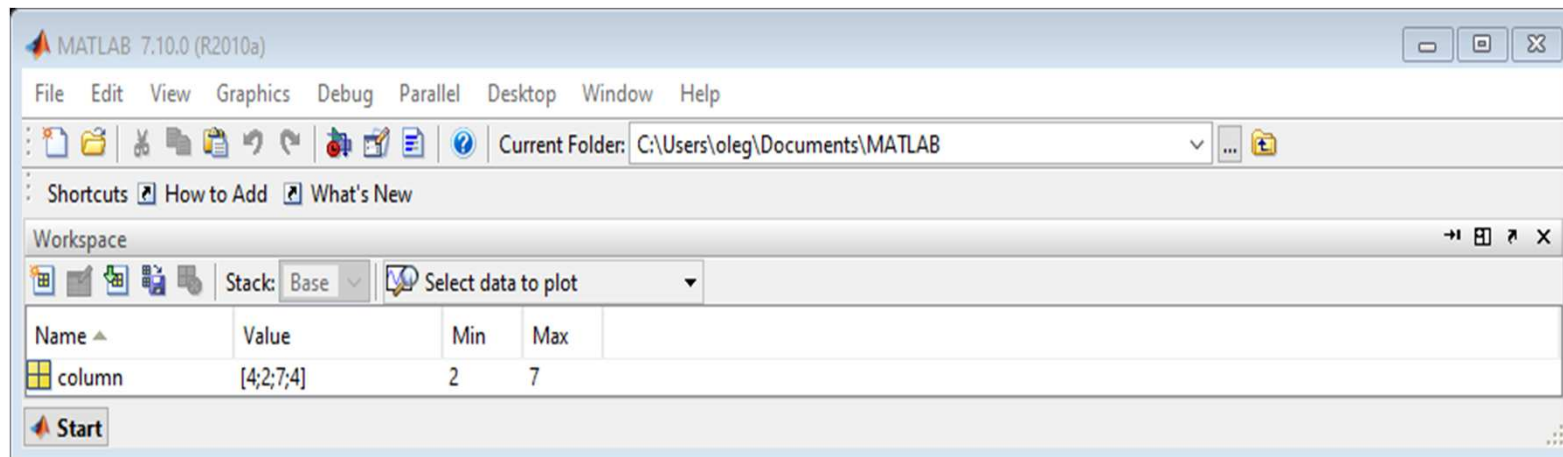
```
» 4
```

```
» 2
```

```
» 7
```

```
» 4
```

- Workspace



# size & length

- You can tell the difference between a row and a column vector by:
  - Looking in the workspace
  - Displaying the variable in the command window
  - Using the size function

```
size(row)
```

```
ans =
```

```
1 4
```

```
size(column)
```

```
ans =
```

```
1 4
```

To get a vector's length, use the length function

```
length(row)
```

```
ans =
```

```
4
```

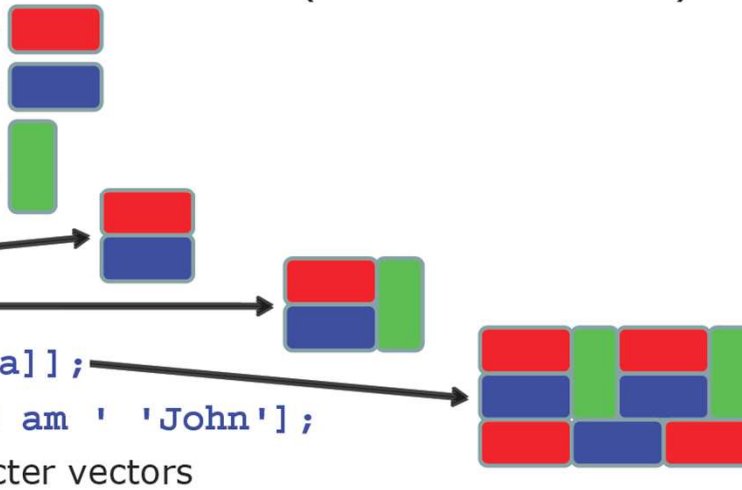
# Matrices

- Make matrices like vectors

- Element by element  
» `a = [1 2; 3 4];` →  $a = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$

- By concatenating vectors or matrices (dimension matters)

```
» a = [1 2];  
» b = [3 4];  
» c = [5;6];  
  
» d = [a;b];  
» e = [d c];  
» f = [[e e];[a b a]];  
» str = ['Hello, I am ' 'John'];  
➤ Strings are character vectors
```





# save/clear/load

- Use `save` to save variables to a file
  - `»save myFile a b`
    - saves variables a and b to the file `myfile.mat`
    - `myfile.mat` file is saved in the current directory
- Use `clear` to remove variables from environment
  - `»clear a b`
    - look at workspace, the variables a and b are gone
- Use `load` to load variable bindings into the environment
  - `»load myFile`
    - look at workspace, the variables a and b are back
- Can do the same for entire environment
  - `»save myenv; clear all; load myenv;`

## Exercise: Variables

- Get and save the current date and time
  - Create a variable `start` using the function `clock`
  - What is the size of `start`? Is it a row or column?
  - What does `start` contain? See help `clock`
  - Convert the vector `start` to a string. Use the function `datestr` and name the new variable `startString`
  - Save `start` and `startString` into a mat file named `startTime`

# Basic Scalar Operations

- Arithmetic operations (+, -, \*, /)
  - »7/45
  - »(1+i)\*(2+i)
  - »1 / 0
  - »0 / 0
- •Exponentiation ( ^)
  - »4^2
  - »(3+4\*j)^2
- •Complicated expressions, use parentheses
  - »((2+3)\*3)^0.1
- •Multiplication is NOT implicit given parentheses
  - »3(1+0.7) gives an error
- •To clear command window
  - »clc

# Built-in Functions

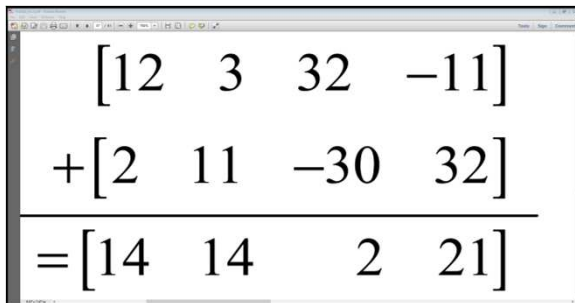
- MATLAB has an enormous library of built-in functions
- Call using parentheses –passing parameter to function
  - »sqrt(2)
  - »log(2), log10(0.23)
  - »cos(1.2), atan(-.8)
  - »exp(2+4\*i)
  - »round(1.4), floor(3.3), ceil(4.23)
  - »angle(i); abs(1+i);

# Transpose

- The transpose operators turns a column vector into a row vector and vice versa
  - `»a = [1 2 3 4+i]`
  - `»transpose(a)`
  - `»a'`
  - `»a.'`
- The `'` gives the Hermitian-transpose, i.e. transposes and conjugates all complex numbers
- For vectors of real numbers `.'` and `'` give same result

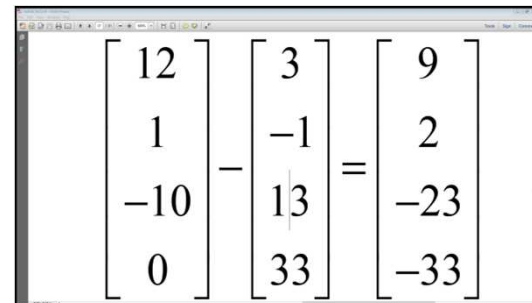
# Addition and Subtraction

- Addition and subtraction are element-wise; sizes must match (unless one is a scalar):



A hand-drawn diagram showing the addition of two 1x4 vectors. The first vector is  $[12 \ 3 \ 32 \ -11]$  and the second vector is  $[2 \ 11 \ -30 \ 32]$ . They are added element-wise to produce a result vector  $[14 \ 14 \ 2 \ 21]$ . The diagram uses a horizontal line to separate the inputs from the result.

$$\begin{array}{r} [12 \ 3 \ 32 \ -11] \\ + [2 \ 11 \ -30 \ 32] \\ \hline = [14 \ 14 \ 2 \ 21] \end{array}$$



A hand-drawn diagram showing the subtraction of two 4x1 vectors. The first vector is  $\begin{bmatrix} 12 \\ 1 \\ -10 \\ 0 \end{bmatrix}$  and the second vector is  $\begin{bmatrix} 3 \\ -1 \\ 13 \\ 33 \end{bmatrix}$ . They are subtracted element-wise to produce a result vector  $\begin{bmatrix} 9 \\ 2 \\ -23 \\ -33 \end{bmatrix}$ . The diagram uses vertical bars to represent the vectors and a horizontal line to separate the inputs from the result.

$$\begin{bmatrix} 12 \\ 1 \\ -10 \\ 0 \end{bmatrix} - \begin{bmatrix} 3 \\ -1 \\ 13 \\ 33 \end{bmatrix} = \begin{bmatrix} 9 \\ 2 \\ -23 \\ -33 \end{bmatrix}$$

- •The following would give an error
  - $c = \text{row} + \text{column}$
- Use the transpose to make sizes compatible
  - $c = \text{row}' + \text{column}$
  - $c = \text{row} + \text{column}'$
- Can sum up or multiply elements of vector
  - $s = \text{sum}(\text{row});$
  - $p = \text{prod}(\text{row});$

# Element-Wise Functions

- All the functions that work on scalars also work on vectors
  - `t = [1 2 3];`
  - `f = exp(t);`
- is the same as
  - `f = [exp(1) exp(2) exp(3)];`
- If in doubt, check a function's help file to see if it handles vectors elementwise
- Operators (`*` / `^`) have two modes of operation
  - element-wise
  - standard

# Operators: element-wise

- To do element-wise operations, use the dot:  $.(.* , ./, .^)$ . BOTH dimensions must match (unless one is scalar)!
  - $a=[1\ 2\ 3];b=[4;2;1];$
  - $a.*b, a./b, a.^b$  all errors
  - $a.*b', a./b', a.^(b')$  all valid

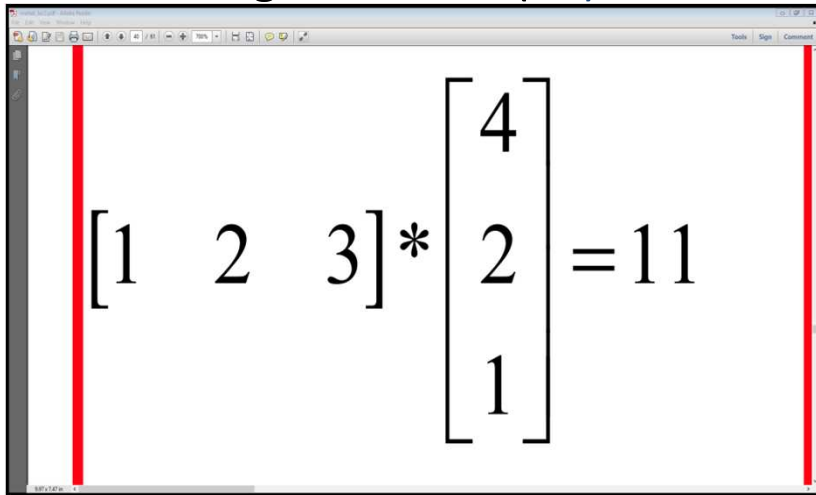
The screenshot shows a presentation slide with three boxes illustrating element-wise operations and their dimensions:

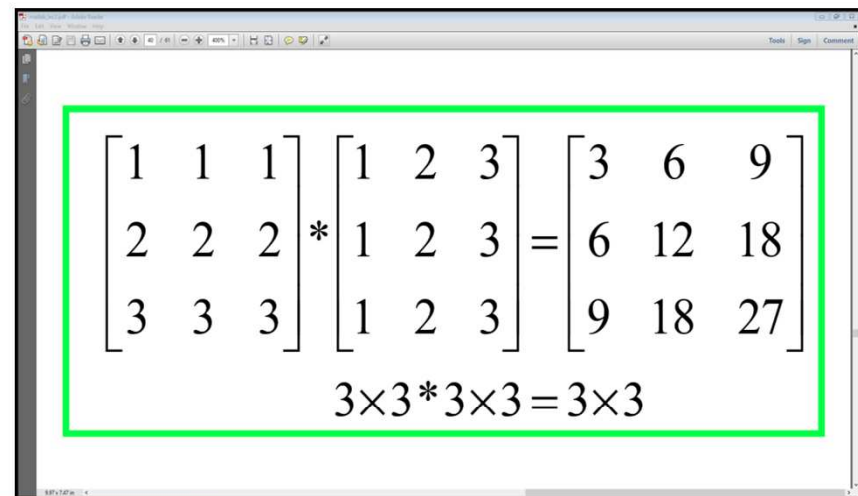
- Red box (top left):** Shows an invalid operation  $\begin{bmatrix} 1 & 2 & 3 \end{bmatrix} .* \begin{bmatrix} 4 \\ 2 \\ 1 \end{bmatrix} = \text{ERROR}$  and a valid operation  $\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} .* \begin{bmatrix} 4 \\ 2 \\ 1 \end{bmatrix} = \begin{bmatrix} 4 \\ 4 \\ 3 \end{bmatrix}$  with dimensions  $3 \times 1 .* 3 \times 1 = 3 \times 1$ .
- Green box (top right):** Shows a valid operation  $\begin{bmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 3 & 3 \end{bmatrix} .* \begin{bmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \\ 1 & 2 & 3 \end{bmatrix} = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 6 \\ 3 & 6 & 9 \end{bmatrix}$  with dimensions  $3 \times 3 .* 3 \times 3 = 3 \times 3$ .
- Blue box (bottom right):** Shows a valid operation  $\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} .^2 = \begin{bmatrix} 1^2 & 2^2 \\ 3^2 & 4^2 \end{bmatrix}$  with the note "Can be any dimension".



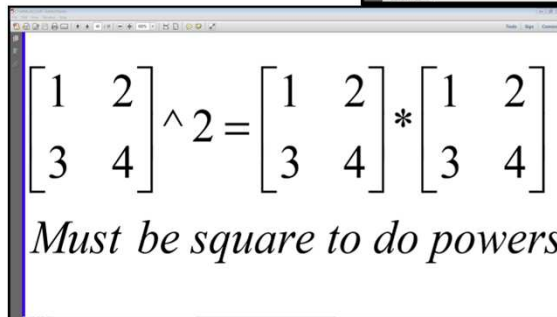
# Operators: standard

- Multiplication can be done in a standard way or element-wise
- Standard multiplication (\*) is either a dot-product or an outer product
- ¾Remember from linear algebra: inner dimensions must MATCH!!
- Standard exponentiation (^) can only be done on square matrices or scalars
- Left and right division (/ \) is same as multiplying by inverse


$$\begin{bmatrix} 1 & 2 & 3 \end{bmatrix} * \begin{bmatrix} 4 \\ 2 \\ 1 \end{bmatrix} = 11$$


$$\begin{bmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 3 & 3 \end{bmatrix} * \begin{bmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \\ 1 & 2 & 3 \end{bmatrix} = \begin{bmatrix} 3 & 6 & 9 \\ 6 & 12 & 18 \\ 9 & 18 & 27 \end{bmatrix}$$

$3 \times 3 * 3 \times 3 = 3 \times 3$


$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} ^2 = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} * \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

*Must be square to do powers*

# Automatic Initialization

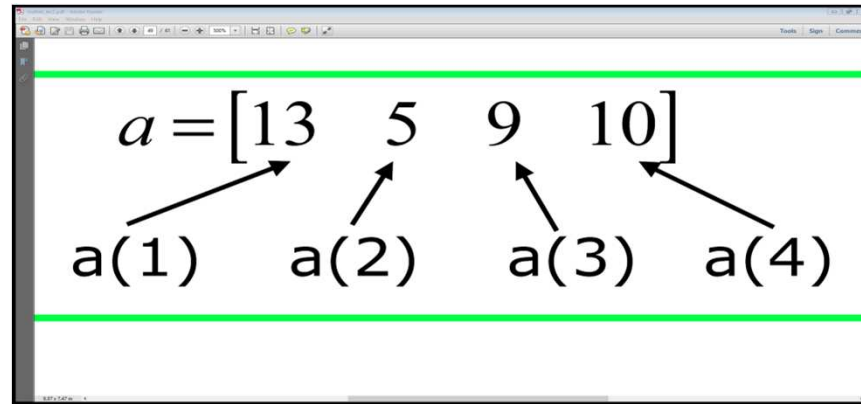
- Initialize a vector of ones, zeros, or random numbers
  - `o=ones(1,10)`
- row vector with 10 elements, all 1
  - `z=zeros(23,1)`
- column vector with 23 elements, all 0
  - `r=rand(1,45)`
  - row vector with 45 elements (uniform [0,1])
  - `n=nan(1,69)`
- row vector of NaNs (useful for representing uninitialized variables)
- `var=zeros(M,N);`
  - Number of rows      Number of columns

# Automatic Initialization

- To initialize a linear vector of values use `linspace`
- `a=linspace(0,10,5)`
  - starts at 0, ends at 10 (inclusive), 5 values
- Can also use colon operator (`:`)
- `b=0:2:10`
  - starts at 0, increments by 2, and ends at or before 10
  - increment can be decimal or negative
- `c=1:5`
  - if increment isn't specified, default is 1
- To initialize logarithmically spaced values use `logspace` similar to `linspace`, but see `help`

# Vector Indexing

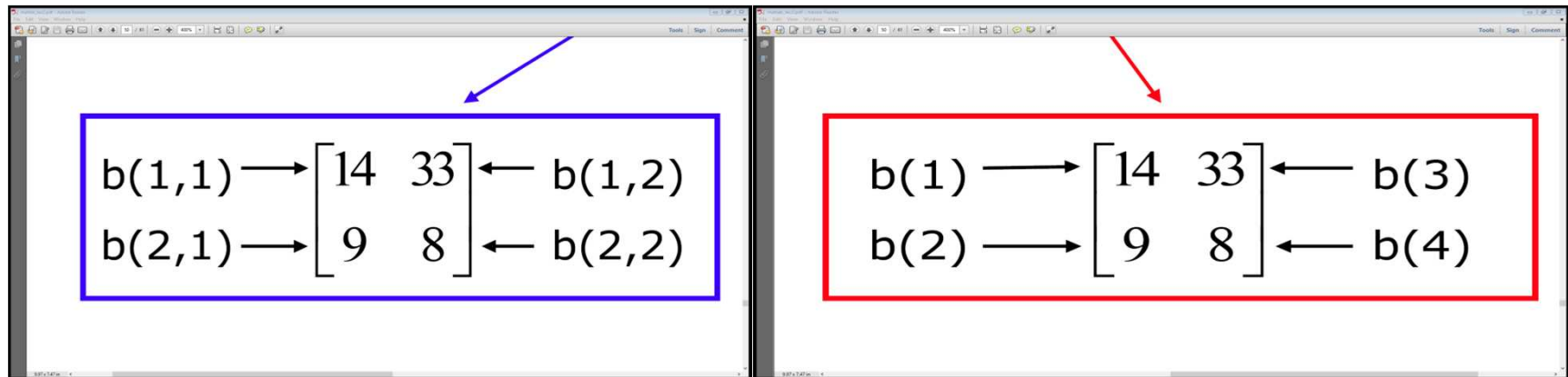
- MATLAB indexing starts with 1, not 0
- $a(n)$  returns the  $n$ (th) element



- The index argument can be a vector. In this case, each element is looked up individually, and returned as a vector of the same size as the index vector.
- $x = [12 \ 13 \ 5 \ 8];$
- $a = x(2:3);$   $\longrightarrow$   $a = [13 \ 5];$
- $b = x(1:end-1);$   $\longrightarrow$   $b = [12 \ 13 \ 5];$

# Matrix Indexing

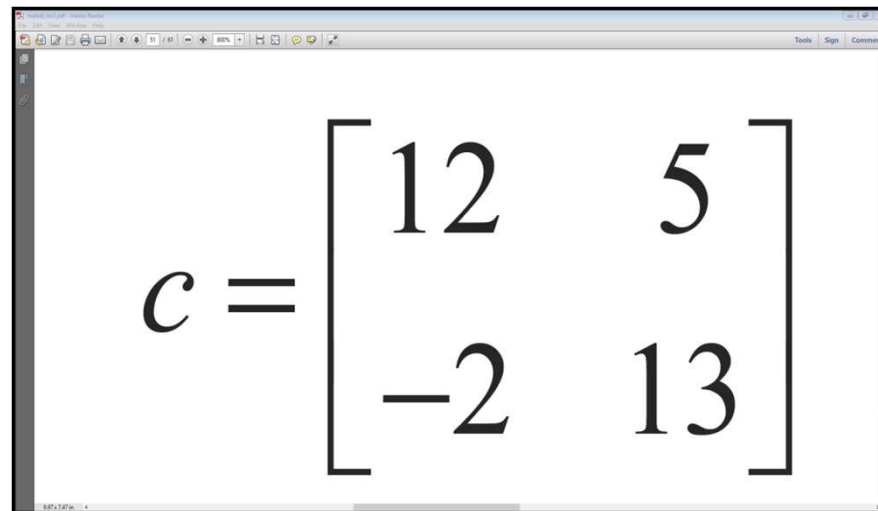
- Matrices can be indexed in two ways
  - using subscripts(row and column)
  - using linear indices(as if matrix is a vector)
- Matrix indexing: **subscripts** or **linear indices**



- Picking submatrices
- `A = rand(5)` % shorthand for 5x5 matrix
- `A(1:3,1:2)` % specify contiguous submatrix
- `A([1 5 3], [1 4])` % specify rows and columns

# Advanced Indexing

- To select rows or columns of a matrix, use the :



A screenshot of a presentation slide showing a 2x2 matrix  $c$ . The matrix is displayed as  $c = \begin{bmatrix} 12 & 5 \\ -2 & 13 \end{bmatrix}$ . The slide has a white background with a black border. The matrix is centered on the slide.

$d=c(1,:); \longrightarrow d=[12 \ 5];$

$e=c(:,2); \longrightarrow e=[5;13];$

$c(2,:)= [3 \ 6];$  %replaces second row of c

# Advanced Indexing

- MATLAB contains functions to help you find desired values within a vector or matrix

```
vec = [5 3 1 9 7]
```

- To get the minimum value and its index:

```
[minVal,minInd] = min(vec);
```

`max` works the same way

- To find any the indices of specific values or ranges

```
ind = find(vec == 9);
```

```
ind = find(vec > 2 & vec < 6);
```

- `find` expressions can be very complex, more on this later

# Plotting

- Example
  - `x=linspace(0,4*pi,10);`
  - `y=sin(x);`
- •Plot values against their index
  - `plot(y);`
- Usually we want to plot y versus x
  - `plot(x,y);`

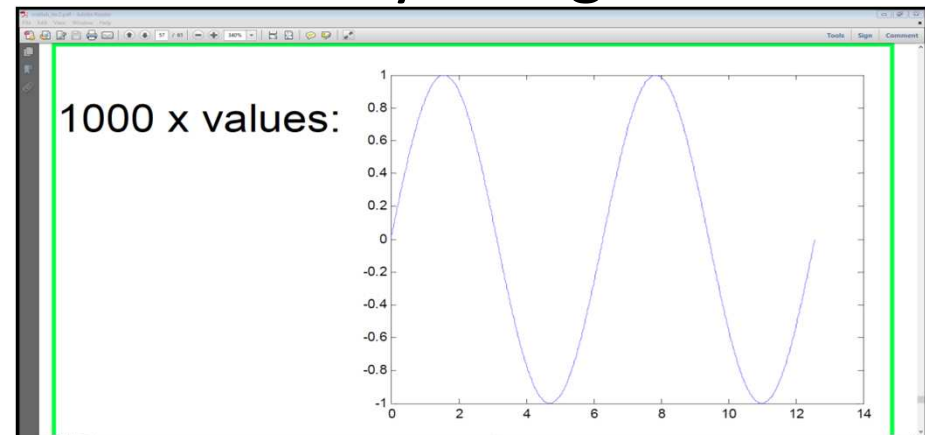
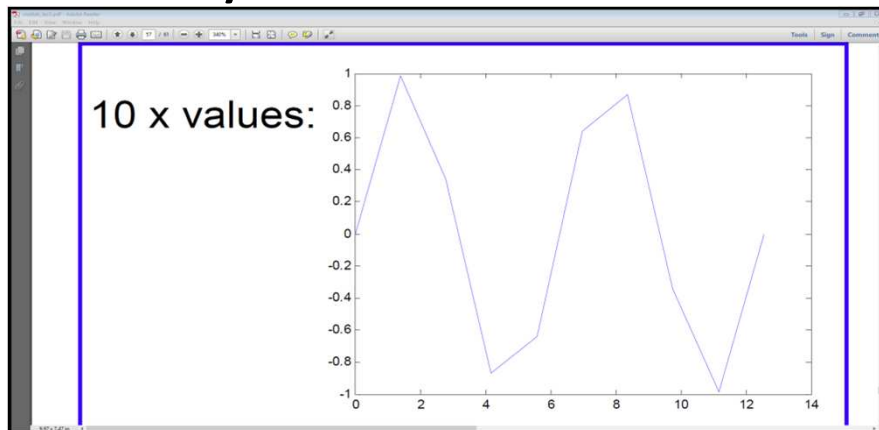


# Plotting

- What does plot do?
- `plot` generates dots at each (x,y) pair and then connects the dots with a line
- To make plot of a function look smoother, evaluate at more points

```
x=linspace(0,4*pi,1000);  
plot(x,sin(x));
```

- x and y vectors must be same size or else you'll get an error



# Functions

- Functions look exactly like scripts, but for ONE difference
  - Functions must have a function declaration
- We are using functions and scripts different way

# Functions

- function declaration

- **function [output1, output2, output3,] = funName(input1, input2)**

Must have the reserved word: function

Outputs arguments

Input arguments

Function name should match MATLAB file name

# Functions

- No need for return: MATLAB 'returns' the variables whose names match those in the function declaration
- Variable scope: Any variables created within the function but not returned disappear from memory after the function stops running

# Functions examples

- Open new script and type :
  - `function [output] = xsq(input)`
  - `output = input.^2;`
- try saving it and the suggested name will be xsq.m. Save it as suggested.
- **We can not run this file as a script!**
- In a command window or in another(script) file type
  - `x = 1:10;`
  - `y = xsq(x)`
- **This is a way how to use functions!**

# Functions examples

- Example with vector output

```
function [output] = func(x,y)
```

```
output = x.^2 + y.^2;
```

- Use it:

```
x= 0.0:pi/10:pi;y = x;
```

```
[X,Y] = meshgrid(x,y);
```

```
f = func(X,Y); contour(X,Y,f);
```

```
axis([0 pi 0 pi]); axis equal;
```

# Functions examples

- Example with two outputs

```
function [sq,cub] = xpowers(input)
sq = input.^2; cub = input.^3;
```

- use

```
x = 1:10; [xsq,xcub] = xpowers(x);
```

- When the function is called we must know what form of output we expect!

# Functions

- MATLAB functions are generally overloaded
- Can take a variable number of inputs
- Can return a variable number of outputs
- What would the following commands return:
  - `a=zeros(2,4,8); %n-dimensional matrices are OK`
  - `D=size(a)`
  - `[m,n]=size(a)`
  - `[x,y,z]=size(a)`
  - `m2=size(a,2)`



# Functions

- All variables are local, unless they are declared global. If you use variable x in the main program, then it is not automatically passed into function

# Functions

- Passing Parameters into Functions as variables
  - `function [output] = myfunc(x,p)`
  - `output = p*x^2;`
- Use it:
  - `X= 0.0:pi/10:pi;P = 2;`
  - `F = myfunc(X,P); plot(X,F);`
- Parameters as global variables
  - `function [output] = myfunc(x)`
  - `global p q;`
  - `output = (x - p)*(x-q);`
- use
  - `global p q;`
  - ...
  - `z = fzero(@myfunc,x0);`

