

Prediction of Splicing Sites by BN

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Among the various tools in computational genetic research, gene prediction remains one of the most prominent tasks. Accurate gene prediction is of prime importance for the creation and improvement of annotations of sequenced genomes. In this paper, I have developed a model combined WAM and Bayesian Network. Compared with the existing model like Weight Array Model and Support Vector Machine, WAM+BN show great performance with excellent predicting accuracy and acceptable balanced time and space expenses.

Key Words: Bayesian Network, Machine Learning, Gene Finding, Splice Sites.

Availability: <https://github.com/Achuan-2/Splicing-Sites-Predictor>

1 INTRODUCTION

A gene is a basic unit of heredity and a sequence of nucleotides in DNA or RNA that encodes the synthesis of a gene product, either RNA or protein. Gene prediction or gene finding refers to the process of identifying the regions of genomic DNA that encode genes. This includes protein-coding genes as well as RNA genes, but may also include prediction of other functional elements such as regulatory regions. Gene finding is one of the first and most important steps in understanding the genome of a species once it has been sequenced.

In its earliest days, "gene finding" was based on painstaking experimentation on living cells and organisms. Statistical analysis of the rates of homologous recombination of several different genes could determine their order on a certain chromosome, and information from many such experiments could be combined to create a genetic map specifying the rough location of known genes relative to each other. Today, with comprehensive genome sequence and powerful computational resources at the disposal of the research community, gene finding has been redefined as a largely computational problem.

Ab Initio gene prediction is an intrinsic method based on **signal detection** and **gene content**. These signs can be broadly categorized as either signals, specific sequences that indicate the presence of a gene nearby, or content, statistical properties of the protein-coding sequence itself. Ab initio gene finding might be more accurately characterized as gene prediction, since extrinsic evidence is generally required to conclusively establish that a putative gene is functional.

In the genomes of prokaryotes, genes have specific and relatively well-understood promoter sequences (signals), such as the Pribnow box and transcription factor binding sites, which are easy to systematically identify. Also, the sequence coding for a protein occurs as one contiguous open reading frame (ORF), which is typically many hundred or thousands of base pairs long. Furthermore, protein-coding DNA has certain periodicities and other statistical properties that are easy to detect in a sequence of this length. These characteristics make prokaryotic gene finding relatively straightforward, and well-designed systems are able to achieve high levels of accuracy.

Ab initio gene finding in eukaryotes, especially complex organisms like humans, is considerably more challenging for several reasons. First, the promoter and other regulatory signals in these genomes are more complex and less well-understood than

in prokaryotes, making them more difficult to reliably recognize. Second, splicing mechanisms employed by eukaryotic cells mean that a particular protein-coding sequence in the genome is divided into several parts (exons), separated by non-coding sequences (introns). A typical protein-coding gene in humans might be divided into a dozen exons, each less than two hundred base pairs in length, and some as short as twenty to thirty. It is therefore much more difficult to detect periodicities and other known content properties of protein-coding DNA in eukaryotes.

In eukaryotic genes, splice sites mark the boundaries between exons and introns. Within introns, a donor site (5' end of the intron), a branch site (near the 3' end of the intron) and an acceptor site (3' end of the intron) are required for splicing. The splice donor site includes an almost invariant sequence GU at the 5' end of the intron, within a larger, less highly conserved region. The splice acceptor site at the 3' end of the intron terminates the intron with an almost invariant AG sequence. Upstream (5'-ward) from the AG there is a region high in pyrimidines (C and U), or polypyrimidine tract. Further upstream from the polypyrimidine tract is the branchpoint, which includes an adenine nucleotide involved in lariat formation.

In this paper, I focus on the signal related to pre-mRNA splicing, i.e. the splice sites that include donor and acceptor sites. However the occurrence of the dimer in splicing sites is not sufficient for the splice site. Indeed, it occurs very frequently at non splice site positions. So we need to construct a model that can analyze the correlation of the bases upstream and downstream of the splicing sites to identify splicing sites. I will try to use Bayesian network to predict splicing sites, compared with other models such as WAM, SVM.

2 METHODS

2.1 Bayesian Network

A Bayesian network, Bayes network, belief network, Bayes(ian) model or probabilistic directed acyclic graphical model is a probabilistic graphical model (a type of statistical model) that represents a set of random variables and their conditional dependencies via a directed acyclic graph (DAG). Bayesian networks are mostly used when we want to represent causal relationship between the random variables. Bayesian Networks are parameterized using Conditional Probability Distributions (CPD). Each node in the network is parameterized using $P(\text{node} | Pa(\text{node}))$ where $Pa(\text{node})$ represents the parents of node in the network.

From the Bayesian rule, the global joint distribution function $P(x_1, x_2, \dots, x_n)$ of variables X_1, X_2, \dots, X_n can be represented as a product of local conditional distribution functions. That is,

$$P(x_1, x_2, \dots, x_n) = P(x_1) P(x_2 | x_1) \cdots P(x_n | x_1, \dots, x_{n-1})$$

A Bayesian network for a collection $\{X_1, X_2, \dots, X_n\}$ of random variables represents the joint probability distribution of these variables. The joint probability distribution, which is associated with a set of assertions of conditional independence among the variables, can be written as:

$$P(x_1, x_2, \dots, x_n) = \prod_{i=1}^n P(x_i | E_{x_i})$$

where E_{x_i} is a subset of variables x_1, \dots, x_{i-1} on which x_i is dependent. Hence, a Bayesian network can be described as a directed acyclic graph consisting of a set of n nodes and a set of directed edges between nodes. Each node in the graph corresponds to a variable x_i and each directed edge is constructed from a variable in E_{x_i} to the variable x_i . If each variable has a finite set of values, to each variable x_i with parents in E_{x_i} , there is an attached table of conditional probabilities $P(x_i | E_{x_i})$.

2.2 Program Design

Step 1: Feature Extraction and Encoding Extract sequences from training set and test set and then extract windows with fixed length that contains a donor splice site, excluding the windows that contained base positions not labeled with A, T, C, G but with other symbols. Finally encode sequences with the rule that **A is encoded for 0, G for 1, C for 2, T for 3**.

Step 2: Define the network structure I use **pgmpy** for model architecture. **pgmpy** is a python library for working with Probabilistic Graphical Models. In **pgmpy** we define the network structure and the CPDs separately and then associate them with the structure. And I use the **HillClimbSearch** function to estimate the structure, which performs local hill climb search to estimates the DAG structure that has optimal score, according to the scoring method supplied. Starts at model start.dag and proceeds by step-by-step network modifications until a local maximum is reached.

Step 3: Model architecture and Parameter Learning According to a DAG and features from training set (label positive samples as 1 and negative as 0), build a Bayesian model and estimate the (conditional) probability distributions of the individual variables.

For model architecture, the network have **two kinds of nodes**: the feature nodes N_i and label node N_{Label} . In the Bayesian network, each feature node has state $Base \in \{a, c, g, t\}$ and label node has state $Label \in \{0, 1\}$. To enable Bayesian network to learn conditional probability for all nodes, both donor sites and pseudo sites are fitted in a Bayesian network.

For parameter learning, I use **Bayesian Parameter Estimation**. The Bayesian Parameter Estimator starts with already existing prior CPDs, that express our beliefs about the variables *before* the data was observed. Those "priors" are then updated, using the state counts from the observed data. A sensible choice of prior is *BDeu* (Bayesian Dirichlet equivalent uniform prior). For *BDeu* we need to specify an equivalent sample size N and then the pseudo-counts are the equivalent of having observed N uniform samples of each variable (and each parent configuration).

Step 4: Prediction and score Input all samples from test set with missing label, predict probabilities of label 1 and label 0.

The score, $Score(S)$, of a tested potential splice site S under the two labels is the log-odds ratio defined as follows:

$$Score(S) = \log \left[\frac{P(S | Label_1)}{P(S | Label_0)} \right]$$

With an empirically determined threshold score T , the tested potential splice site S will be claimed real if the log-odds score is no less than T ; otherwise, it will be claimed pseudo signal.

Step 5: Evaluation Compare the performance of Bayesian Network with other models such as WAM and SVM by ROC curve and PR curve.

Receiver operating characteristic Curve (ROC Curve for short) is a curve reflecting the relationship between sensitivity and specificity. The closer the ROC curve is to the upper left corner, the higher the accuracy of the test. The point closest to the top left corner of the ROC curve is the best threshold. AUC is the area under the ROC curve. The meaning of AUC value is to randomly take a pair of positive and negative samples, and the probability that the score of positive samples is greater than that of negative samples. AUC is robust to the unbalanced distribution of positive and negative samples, and it is a very common measure of classifier.

Precision-Recall Curve is a useful measure of success of prediction when the classes are very imbalanced (PR curve for short). In information retrieval, precision is a measure of result relevancy, while recall is a measure of how many truly relevant results are returned. When the distribution of positive and negative samples is unbalanced, the ROC curve remains unchanged, while the PR curve changes greatly. Compared with the ROC curve, the PR curve can reflect the ability of the model to identify positive samples. AUROC is always going to be 0.5 — a random classifier, or a coin toss, will get you an AUROC of 0.5. But with AUPRC, the baseline is equal to the fraction of positives.

Other measures of predictive accuracy are as follows:

$$\begin{aligned} Sn/Recall &= \frac{TP}{TP + FN} \\ Precision &= \frac{TP}{TP + FP} \\ F1-score &= 2 * \frac{Precision * Recall}{Precision + Recall} \end{aligned}$$

3 RESULTS

3.1 Splice Site Datasets

The Kulp-Reese dataset is used as a training set, which consists of 462 non-redundant multi-exon genes, is a benchmark data set and has been widely used to train many powerful gene prediction algorithms.

The Test set is Burset & Guigo set. The dataset assembled by Burset and Guigo(1996) consists of 570 vertebrate genomic sequences containing exactly multi-exon gene. There are 2079 exons and introns in the whole dataset, with more than 140000 pseudo exons and introns in the dataset. (the testing dataset can be found at <https://genome.crg.cat/datasets/genomics96/>)

3.2 Bayesian Network Results

Choose a window that contains 3 consecutive bases upstream from the exon/intron boundary and 9 consecutive bases down-

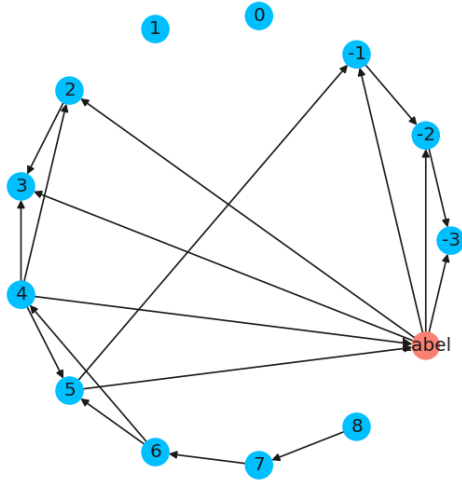


Figure 1. The Bayesian Network Structure

stream to the exon/intron boundary. Build a model by pgmpy. The network obtained is shown in Figure1.

Using the Bayesian network to train model, ROC and PR curves and confusion matrixes are shown in Figure2 and Figure5. It can be seen from ROC and PR curves that the performance of this model is ordinary. Although we consider the correlation of all bases, the performance of the model is not significantly improved compared with WAM.

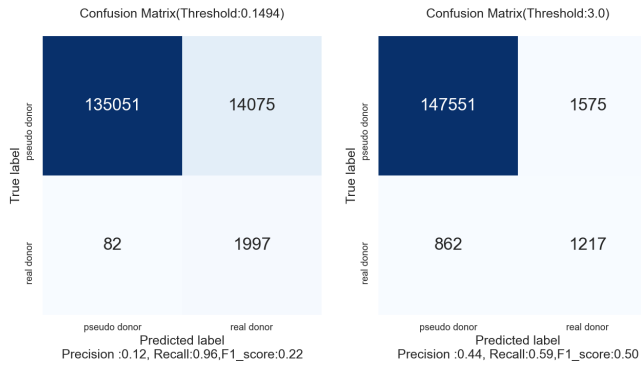


Figure 2. Confusion Matrix for Bayesian Network: The left is under the threshold is the best parameter of ROC curve. The right is under the threshold when F1-score is highest.

3.3 WAM+Bayesian Network

In view of the unsatisfactory effect of Bayesian network, I try to use WAM to filter out the samples with large difference between negative samples and positive samples, and then use Bayesian network to train and predict the input positive and negative samples, i.e., I hope Bayesian network can separate the samples with similar scores in positive and negative samples in WAM.

During training, the positive and negative samples in the training set whose score is less than the threshold are filtered out, and then the Bayesian network is used to train with the filtered samples. In the process of prediction, WAM is used to score the samples whose score is less than the threshold value, and

the samples whose score is higher than the threshold value are predicted as negative samples. Finally Bayesian network is used to predict the samples whose score is higher than the threshold value.

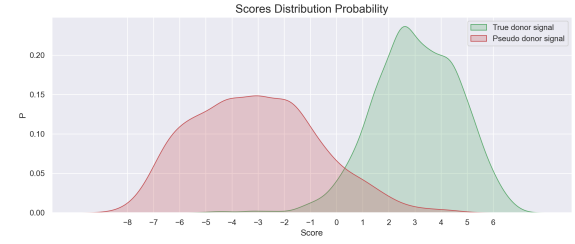


Figure 3. The scoring of positive and negative samples input from the training set by WAM in the first layer.

According to Figure 3, I set the threshold value of the first layer WAM to -3, and the result is excellent. As can be seen from Figure 5 and Figure 6, the AUROC of WAM+BN is 0.988, close to the SVM Poly Kernel performance. Compared with WAM and BN, the PR curve has been greatly improved, although it is worse than SVM Poly Kernel.

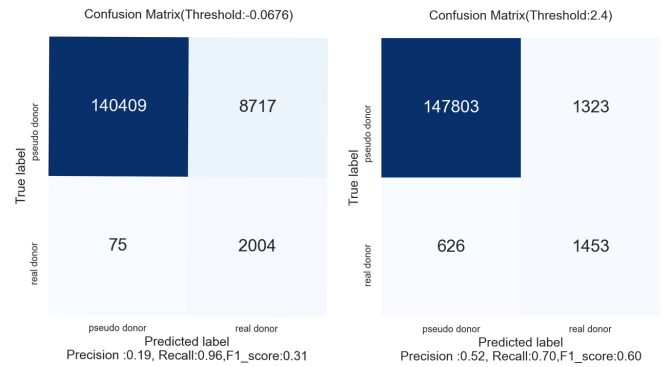


Figure 4. Confusion Matrix for WAM+Bayesian: The left is under the threshold is the best parameter of ROC curve. The right is under the threshold when F1-score is highest.

4 DISCUSSION & CONCLUSION

In this study, I firstly use Bayesian Network to build a model to predict donor sites, in view of the effect compared with WAM, almost no improvement. So I try WAM + BN to build a two-layer model, which can be compared with SVM. At first, the effect of only using Bayesian network is poor, which may be due to the unbalanced number of positive and negative samples. Bayesian Network constructs conditional probability matrix according to the situation of samples and network structure. When the number of samples is too large, the network will be too complex and eventually the discrimination between positive and negative samples is not high. After one-layer filtering by WAM, the number of input Bayesian network samples is reduced, which reduces the time and space cost of training. The samples that the first layer of WAM can not distinguish the samples well, using more complex Bayesian network to train and predict, making the Bayesian network only for the samples that are difficult to distinguish. It has been proved that this method has greatly improved the prediction accuracy of the model.

Table 1. Prediction under different thresholds in Bayesian network

Threshold	TP	FP	TN	FN	Recall	Precision	F1-Score	Sn	Acc
-10	2079	142390	6736	0	1.000	0.014	0.028	0.045	0.058
-9	2079	134157	14969	0	1.000	0.015	0.030	0.100	0.113
-8	2078	124224	24902	1	1.000	0.016	0.032	0.167	0.178
-7	2078	114803	34323	1	1.000	0.018	0.035	0.230	0.241
-6	2078	104199	44927	1	1.000	0.020	0.038	0.301	0.311
-5	2078	90422	58704	1	1.000	0.022	0.044	0.394	0.402
-4	2075	74324	74802	4	0.998	0.027	0.053	0.502	0.508
-3	2070	56339	92787	9	0.996	0.035	0.068	0.622	0.627
-2	2065	41259	107867	14	0.993	0.048	0.091	0.723	0.727
-1	2048	25702	123424	31	0.985	0.074	0.137	0.828	0.830
0	2010	15492	133634	69	0.967	0.115	0.205	0.896	0.897
1	1882	7689	141437	197	0.905	0.197	0.323	0.948	0.948
1.5	1810	5604	143522	269	0.871	0.244	0.381	0.962	0.961
2	1672	3887	145239	407	0.804	0.301	0.438	0.974	0.972
3	1217	1575	147551	862	0.585	0.436	0.500	0.989	0.984
4	684	571	148555	1395	0.329	0.545	0.410	0.996	0.987
4.5	440	266	148860	1639	0.212	0.623	0.316	0.998	0.987
5	267	122	149004	1812	0.128	0.686	0.216	0.999	0.987
5.1	195	82	149044	1884	0.094	0.704	0.166	0.999	0.987
5.5	65	42	149084	2014	0.031	0.607	0.059	1.000	0.986
5.8	27	22	149104	2052	0.013	0.551	0.025	1.000	0.986
5.9	11	14	149112	2068	0.005	0.440	0.010	1.000	0.986
6.2	0	0	149126	2079	0.000			1.000	0.986

Table 2. Prediction under different thresholds in WAM+Bayesian

Threshold	TP	FP	TN	FN	Recall	Precision	F1-Score	Sn	Acc
-7	2077	34920	114206	2	0.999	0.056	0.106	0.766	0.769
-6	2077	34174	114952	2	0.999	0.057	0.108	0.771	0.774
-5	2077	32867	116259	2	0.999	0.059	0.112	0.780	0.783
-4	2076	30756	118370	3	0.999	0.063	0.119	0.794	0.797
-3	2070	26914	122212	9	0.996	0.071	0.133	0.820	0.822
-2	2063	20733	128393	16	0.992	0.090	0.166	0.861	0.863
-1	2052	14321	134805	27	0.987	0.125	0.222	0.904	0.905
0	1993	8345	140781	86	0.959	0.193	0.321	0.944	0.944
1	1880	3874	145252	199	0.904	0.327	0.480	0.974	0.973
1.5	1751	2666	146460	328	0.842	0.396	0.539	0.982	0.980
2	1590	1761	147365	489	0.765	0.474	0.586	0.988	0.985
3	1049	685	148441	1030	0.505	0.605	0.550	0.995	0.989
4	467	200	148926	1612	0.225	0.700	0.340	0.999	0.988
4.5	224	94	149032	1855	0.108	0.704	0.187	0.999	0.987
5	88	40	149086	1991	0.042	0.688	0.080	1.000	0.987
5.5	8	6	149120	2071	0.004	0.571	0.008	1.000	0.986
5.6	3	2	149124	2076	0.001	0.600	0.003	1.000	0.986
5.7	0	0	149126	2079	0.000			1.000	0.986

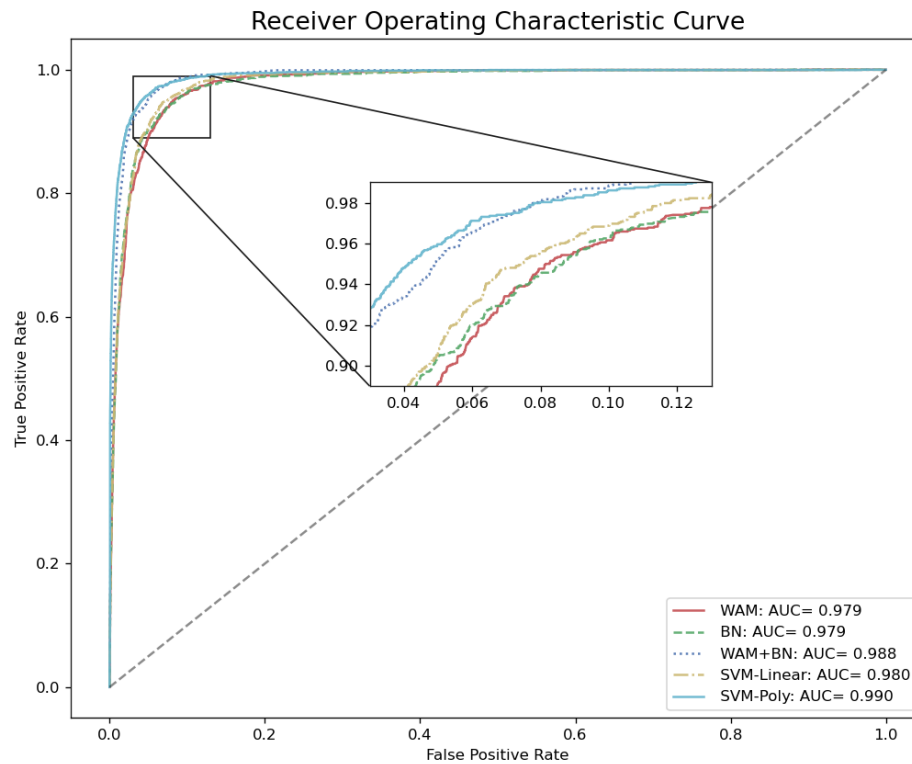


Figure 5. Receiver Operating Characteristic Curve for Bayesian, WAM+Bayesian Network and other models

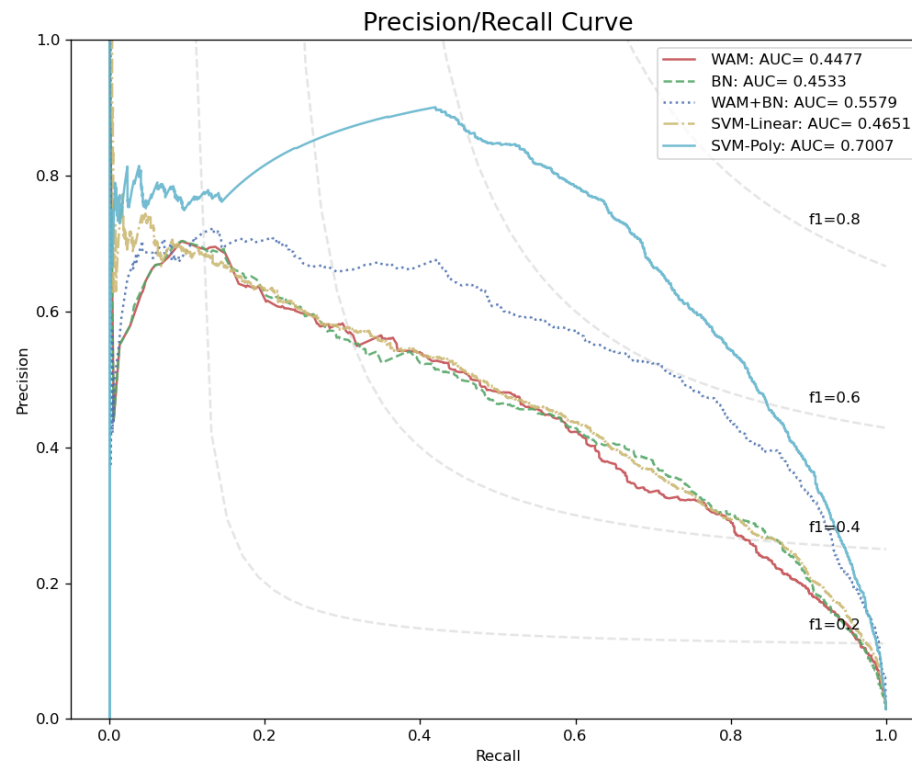


Figure 6. R Precision/Recall Curve for Bayesian, WAM+Bayesian Network and other models

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6 REFERENCES

1. Te-Ming Chen, Chung-Chin Lu, Wen-Hsiung Li, Prediction of splice sites with dependency graphs and their expanded bayesian networks, *Bioinformatics*, Volume 21, Issue 4, 15 February 2005, Pages 471–482,
2. Cai D, Delcher A, Kao B, Kasif S. Modeling splice sites with Bayes networks. *Bioinformatics*. 2000 Feb;16(2):152-8. doi: 10.1093/bioinformatics/16.2.152. PMID: 10842737.