## Homework 1

CS250 Discrete Structures I, Winter 2020

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Due: April 5, 2020

**Problem 1** Figure out how to typeset the following mathematical statements.

- 1.  $f(x) = \mathcal{O}(n \log n)$  (Big 'O' notation)
- 2.  $\neg (A \land B) \leftrightarrow (\neg A \lor \neg B)$  (De Morgan's law in propositional logic notation)
- 3.  $\overline{A \cup B} = \overline{A} \cap \overline{B}$  (De Morgan's law in set theory notation)
- 4.  $f(x) = \log_2 x^2$  (Subscripts and superscripts)
- 5.  $A = \frac{\pi d^2}{4}$  (Fraction and special symbols)
- 6.  $S = \{a, b, c, d\}$  (A set definition)
- 7. (Truth Table)

$$\begin{array}{c|c|c} p & q & p \wedge q \\ \hline T & T & T \\ T & F & F \\ F & T & F \\ F & F & F \\ \end{array}$$

8. (A summation statement)

$$\sum_{k=1}^{n} n$$

**Problem 2** Read chapter 0.1 and 0.2 of the textbook and write up solutions to the following exercises (page 17–23 in the pdf version)

Exercises: 1, 3, 10, 12, 16, and 17.

- 1. For each sentence below, deicide it is an atomic statement, a molecular statement, or not a statement at all.
  - (a) Customers must wear shoes
  - (b) The customers were shoes
  - (c) The customers were shoes and they were socks
- 3. Supposse P and Q are the statements: P: Jack passed math. Q: Jill passed math.
  - (a) Translate "Jack and Jill both passed math" into symbols
  - (b) Translate "If Jack passed math, then Jill did not" into symbols

- (c) Translate " $P \vee Q$ " into English
- (d) Translate " $\neg (P \land Q) \rightarrow Q$ " into English
- (e) Suppose you know that if Jack passed math, then so did Jill. What can you conclude if you know that:
  - i. Jill passed math?
  - ii. JIll did not pass math?
- 10. Write each of the following statements in the form, "if . . . , then . . . ." Careful, some of the statements might be false (which is alright for the purposes of this question).
  - (a) To lose weight, you must exercise.
  - (b) To lose weight, all you need to do is exercise.
  - (c) Every American is patriotic.
  - (d) You are patriotic only if you are American.
  - (e) The set of rational numbers is a subset of the real numbers
  - (f) A number is prime if it is not even.
  - (g) Either the Broncos will win the Super Bowl, or they won't play in the Super Bowl.
- 12. Let P(x) be the predicate, "3x + 1 is even"
  - (a) is P(5) true or false?
  - (b) What, if anything, can you conclude about  $\exists x P(x)$  from the truth value of P(5)?
  - (c) What, if anything, can you conclude about  $\forall x P(x)$  from the truth value of P(5)?
- 16. Translate into symbols. Use E(x) for "x is even" and O(x) for "x is odd."
  - (a) No number is both even and odd.
  - (b) One more than any even number is an odd number.
  - (c) There is prime number that is even.
  - (d) Between any two numbers there is a third number.
  - (e) There is no number between a number and one more than that number.
- 17. Translate into English:
  - (a)  $\forall x(E(x) \to E(x+2))$
  - (b)  $\forall x \exists y (\sin(x) = y)$
  - (c)  $\forall y \exists x (\sin(x) = y)$
  - (d)  $\forall x \forall y (x^3 = y^3 \rightarrow x = y)$